

*"There is nothing more precious than laughter—it is strength to laugh and lose oneself, to be light."* FRIDA KAHLO

In class work **11** has questions **1** through **4** with a total of **8** points. Turn in your work at the end of class *on paper*. This assignment is due *Thursday February 29 13:20*.

Here are some results that you might like to use

$$\cos(x)^2 \sin(x)^4 = \frac{\cos(6x)}{32} - \frac{\cos(4x)}{16} - \frac{\cos(2x)}{32} + \frac{1}{16},$$

$$\cos(x)^4 \sin(x)^4 = \frac{\cos(8x)}{128} - \frac{\cos(4x)}{32} + \frac{3}{128},$$

$$\cos(\theta)^2 \sin(\theta)^5 = \frac{\sin(7\theta)}{64} - \frac{3\sin(5\theta)}{64} + \frac{\sin(3\theta)}{64} + \frac{5\sin(\theta)}{64},$$

$$\cos(\theta)^5 \sin(\theta)^5 = \frac{\sin(10\theta)}{512} - \frac{5\sin(6\theta)}{512} + \frac{5\sin(2\theta)}{256}$$

- 2 1. Use Desmos to sketch the region  $Q$  defined as  $Q = \{(x, y) \mid 0 \leq y \leq x^4 \sqrt{1-x^2} \text{ and } 0 \leq x \leq 1\}$ . Duplicate the graph here.

- 2 2. Find  $\text{area}(Q)$ . **Suggestion:** Substitute  $x = \sin(\theta)$ . When you change variables, also change the limits of integration; for example, when  $x = 1$ , we have  $\theta = \frac{\pi}{2}$ .

2 3. Using your graph, make a pretty good guess for the x-coordinate to the centroid of  $Q$ .

2 4. Find the x-coordinate of the centroid of  $Q$ .