

Homework #8 due December 30, 2016, Friday

Question 1

Give a state-input tabular description of a TM that realizes the following computation :

$(s, \underline{\#u}) \vdash^{*}_M (h, \underline{\#v})$; $u \in (0+1)^*$ and v is obtained from u by interchanging 0s and 1s

Question 2

Describe a $TM M$ in both graphical and compositional tabular forms that *decides* the language

$L = \{u \in \Sigma_0^* \mid u = u^R\}$

(Hint : you may use an extra symbol $\$ \notin \Sigma_0$ and choose as initial $ID : (s, \underline{\#u})$)

Question 3

Describe a $TM M$ in both graphical and compositional tabular forms that performs the following computation :

$(s, \$w\underline{\#}) \vdash^{*}_M (h, \$u\underline{\#})$

where u is obtained from w by compressing all blank ($\#$) symbols in w and $\$$ is a special symbol not used in w .

Question 4

Construct a $TM M$ (*multitape and/or nondeterministic if necessary!*) that decides the language below (*specify the TM in tabular compositional form*).

$L_n = \{w \in (a+b)^* \mid w = u^n, u \in (a+b)^*, n \text{ a fixed positive integer}\}$

(Hint : you may use induction on n)

Question 5

Construct TMs in compositional tabular forms (*multitape and/or nondeterministic if necessary!*) that perform the following computations :

(i) $(s, \underline{\#w}) \vdash^{*}_M (h, \underline{\#w\#w})$

(ii) $(s, \underline{\#w}) \vdash^{*}_M (h, \underline{\#w^R})$

(iii) $(s, \underline{\#w}) \vdash^{*}_M (h, \underline{\#ww})$

(iv) $(s, \underline{\#w}) \vdash^{*}_M (h, \underline{\#w\#w^R})$

(v) $(s, \underline{\#w}) \vdash^{*}_M (h, \underline{\#a^n b^n})$ where the number of a s and b s in w are both equal to n .