

Spring 2020

SABANCI UNIVERSITY

Faculty of Engineering and Natural Sciences

CS 302 Automata Theory

16.5.2020

Duration: 150 minutes

Final Examination (REMOTE)

Question 1 (25 points)

(a) (15 pts) Construct an NFA or a DFA A that accepts the language L of all strings in $(0+1)^*$ in which : the symbol 0 does **not** occur **consecutively more than two times**.

(b) (10 pts) Compute a minimal state DFA B that accepts the language L described in part (a)

Glossary: consecutively \rightarrow ard arda

Question 2 (25 points)

(a) (10 pts) A gambling machine works as follows: everytime the event ' 1 ' occurs you win 1 TL and every time the event ' 0 ' occurs you lose 1 TL. Can you design a NFA that will automatically ring a bell if and when your net income from gambling exceeds 0 TL? If so design it, if not prove your claim.

(b) (15 pts) Given the gambling machine in part (a) can you design a **PDA** that will automatically ring a bell whenever your income exceeds 0 TL? If so design a deterministic **PDA** (**DPDA**) that will solve the problem.

Question 3 (25 points)

A CFG $G = (\{E, T, F, I\}, \{+, *, (,), x, y, z\}, R, E)$ where the productions R are as follows :

$E \rightarrow E + T \mid T ; T \rightarrow T * F \mid F ; F \rightarrow I \mid (E) \mid I(E) ; I \rightarrow x \mid y \mid z$

(a) (15pts) Compute the **Chomsky Normal Form** (CNF) for G

(b) (10 pts) Compute the **Greibach Normal Form** (GNF) for G

(note that what is required is the precise definition of the **GNF** and **not** necessarily the form used for top down parsing in class in which the first elements of the productions of a non-terminal variable are distinct!)

Question 4 (25 points)

(a) (10 pts) Construct a TM M using graphical or tabular notation that performs the computation $(s, \# w) \vdash^*_M (h, \# u)$ where s is the initial state, h the halt state, $w \in \{0,1\}^*$ and u is obtained from w by interchanging the 0 's and 1 's in w .

(b) (15pts) Construct a 2-tape TM M that **decides** the language L of **palindromes**, i.e.

$L := (\omega \in \Sigma^* \mid \omega = \omega^R)$, where ω^R stands for ω reversed. Assume that the initial configuration of the 2-tape TM M is $(s, \# w, \#)$.