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## **ANSWERS**

$$R: E \rightarrow I \mid E+I \mid M ; I \rightarrow \theta \mid IJ ; M \rightarrow M\theta ; J \rightarrow \theta J \mid IJ \mid e$$

(a) After eliminating the null productions

$$R: E \rightarrow I \mid E+I \mid M; I \rightarrow 0 \mid I \mid IJ; M \rightarrow M0; J \rightarrow 0 \mid I \mid 0J \mid IJ$$

After eliminating the unitary productions

$$R: E \rightarrow E+I \mid 0\mid 1\mid 1J\mid M0 ; I \rightarrow 0\mid 1\mid 1J ; M \rightarrow M0 ; J \rightarrow 0\mid 1\mid 0J\mid 1J$$

After eliminating the nongenerating useless symbol M

$$R: E \rightarrow E+I \mid \theta \mid 1 \mid 1J \mid ; I \rightarrow \theta \mid 1 \mid 1J \mid ; J \rightarrow \theta \mid 1 \mid \theta J \mid 1J$$

(b) Chomsky Normal Form

$$E \rightarrow EP |0|1|one J; P \rightarrow plus I; I \rightarrow 0 |1|one J; J \rightarrow 0|1|zero J|one J$$
  
 $one \rightarrow 1; zero \rightarrow 0; plus \rightarrow +$