

CS 302

REMOTE QUIZ 9

20 May, 2021

ANSWERS

(a) (4 pts) G yields a PDA P as below

$P = (Q = \{q_0, f\}, \Sigma = \{a, b\}, \Gamma = \{S, X, Y, Z_0, a, b\}, \delta, q_0, Z_0, F)$ and δ as :

$(q_0, e, S) \rightarrow \{ (q_0, aXS), (q_0, bYS), (q_0, e) \}$

$(q_0, e, X) \rightarrow \{ (q_0, aXX), (q_0, b) \}; (q_0, e, Y) \rightarrow \{ (q_0, bYY), (q_0, a) \}$ (productions)

$(q_0, a, a) \rightarrow (q_0, e); (q_0, b, b) \rightarrow (q_0, e)$ (input shaving)

$(q_0, e, Z_0) \rightarrow (q_0, SZ_0); (q_0, e, Z_0) \rightarrow (f, Z_0)$ (initial and final)

(b) (6 pts) P' transitions : $(q_0, e, Z_0) \rightarrow (s, SZ_0)$ where s is a new state and :

$(s, a-b, V) \rightarrow (q_a - q_b, V); V = S, X \text{ or } Y; (s, e, S) \rightarrow (f, e)$

$(q_a, e, S) \rightarrow (s, XS); (q_a, e, X) \rightarrow (s, XX); (q_a, e, Y) \rightarrow (s, e)$

$(q_b, e, S) \rightarrow (s, YS); (q_b, e, X) \rightarrow (s, e); (q_b, e, Y) \rightarrow (s, YY)$

$(s, a, a) \rightarrow (s, e); (s, b, b) \rightarrow (s, e)$

$(s, e, Z_0) \rightarrow (f, Z_0)$

Not a DPDA : to fix give **priority** to input presence (see example in slides)

Violates DPDA