

**SABANCI UNIVERSITY**

**Faculty of Engineering and Natural Sciences**  
**CS 302 Automata Theory**  
**Fall 2017**

**Midterm**

*Closed book and notes (of paper and electronic kind)*

*Calculators are not allowed and all phones must be switched off*

*Duration: 60 minutes*

*Name* :

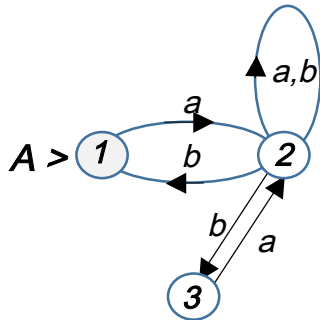
*ID* :

	<i><b>GRADE</b></i>
<i><b>QUESTION 1</b></i>	
<i><b>QUESTION 2</b></i>	
<i><b>QUESTION 3</b></i>	
<i><b>TOTAL</b></i>	

**Question 1** (35 points)

(a) (10 pts) For the regular expression  $E = (1.(0+1)^*.0)^*$  sketch an  $\varepsilon$ -NFA with 3 states that accepts  $E$  interpreted as a language ; and convert this to an *equivalent* NFA again with 3 states but without  $\varepsilon$ -transitions.

(b) (25 pts) Consider the NFA  $A$  below where the input alphabet is  $\Sigma = (a,b)$ .



Compute first an *equivalent* DFA  $B$  to  $A$  above and then an equivalent *minimal state* DFA  $C$  to  $B$ .

**Question 2** (30 points)

**(a)** (15 pts) Consider the language  $L = \{w \in (0+1)^* \mid \#0s \text{ in } w > \#1s \text{ in } w\}$

State whether  $L$  is a *regular* language : if so compute an *NFA* that accepts it ; if not, prove that it is *not regular* using the *pumping lemma*.

**(b)** (15 pts) Repeat part **(a)** for  $L = \{w \in (0+1)^* \mid \#0s \text{ in } w + \#1s \text{ in } w = \text{an even number}\}$

**Question 3** (35 pts)

For the finite state machine below compute the *regular expression* corresponding to the language accepted by it using the state elimination technique.

