CS 302 QUIZ 9

5 December, 2017

## ANSWER

 $G = (\{S,A,B\}, \{a,b,c\}, R, S)$  where productions are:

 $R: S \rightarrow SA / a ; A \rightarrow BS / Bb ; B \rightarrow cA$ 

- Eliminate left recursion :  $S \rightarrow aC$ ;  $C \rightarrow AC/e$
- Eliminate common left symbol  $B: A \rightarrow BD; D \rightarrow S \mid b$  and keep on substituting for variables to yield:  $R': S \rightarrow aC; A \rightarrow cAD; C \rightarrow cADC \mid e; D \rightarrow aC \mid b; B \rightarrow cA$ The new grammar is  $G' = (\{S, A, B, C, D\}, \{a, b, c\}, R', S);$  but the variable A is nongenerative; after removing A: D, B, b and c all become nonreachable hence after removing these useless symbols and the productions of the variables the grammar becomes  $G'' = (\{S, C\}, \{a\}, R'', S)$  where  $R'': S \rightarrow aC; C \rightarrow e$

which further simplifies to  $G''' = (\{S\}, \{a\}, R''', S)$  where  $R''' : S \rightarrow a$