Checking the validity of rule-based arguments grounded in cases: a computational approach

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Abstract. Legal justice needs judges' decisions to be rational and reasonable in the sense that arguments are based on rules and grounded in cases. One puzzle studied in AI & Law is how arguments, rules and cases are formally connected. Recently a formal theory was proposed formalizing how the validity of arguments based on rules can be grounded in cases. Three kinds of argument validity were distinguished: coherence, presumptiveness and conclusiveness. In this paper the theory is implemented in a Prolog program. We test the theory using two case studies: the first is a model of Dutch tort law developed earlier; the second is a newly developed model of Chinese copyright infringement law. The case studies illustrate that by the use of the implementation the process of modeling becomes more efficient and less error-prone.

Keywords. Artificial Intelligence and Law, Rule-based Reasoning, Casebased Reasoning, Argumentation Modeling, Prolog

1. Introduction

Legal justice requires judges' to give reasonable decisions. As we know, AI technologies can reduce the number of cases in which people were unjustly charged by verify the rationality and validity of judges' decisions automatically. In the field of AI and law, scholars usually follow three approaches to develop legal reasoning systems, which are case-based reasoning, rule-based reasoning and argument-based reasoning. Verheij's case model formalism [1] is a kind of hybrid theory suitable for legal domain [2] which combines cases, rules and arguments together. This formalism also incorporates ideas from value judgements, it could be used for comparing the arguments implicated in a case model and deciding which argument is more presumptive. However, the models in legal domain based on Verheij's theory often have complex argument structure. For users, it is easy to make mistakes through the original hand-made way during the process of modeling.

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Thus using a program to verify the model and the arguments implicated by it is necessary.

The study of legal reasoning system has been started from 1970s [3]. Scholars developed various systems by following rule-based reasoning, case-based reasoning and argument-based reasoning.

In 1980s, M.J. Sergot[4] implemented British Nationality Act (BNA) by Prolog. This is a successful attempt for applying rule-based reasoning technology in the field of law. K. Ashley [5] developed the first case-based reasoning system HYPO with E. Rissland. Later, K. Ashley designed another case-based system CATO with his student V. Aleven [6], which used factors instead of dimensions in HYPO. HYPO and CATO play important roles in the history of AI and Law, many reasoning systems are influenced by these two systems, including CABARET [7], GREBE [8], BankXX [9] and IBP [10]. Some of these systems are called hybrid reasoning systems, such as CABARET and GREBE. It is because these systems not only use case-based reasoning approaches, but also other kinds of reasoning technologies [11].

Another important approach in the researches of legal reasoning is argumentation. Many scholars who follow this path are inspired by the work form P.M. Dung [12]. He addressed the abstract argumentation framework, and used a scientific method to argue about the acceptability of arguments. The scholars inspired by Dung developed various argument-based reasoning system, such as ASPIC+[13], ABA [14] and DeLP [15].

The theory background of this paper comes from Bart Verheij's research on case model formalism [1]. In this formalism, three kinds of arguments in the case model can be analyzed through a given preferred relation of the cases. Verheij's theory has incorporated the notion of values in argumentation and also combines rules, cases and arguments together which can be applied in the field of law [2] and used for ethical systems design [16].

2. Verheij's case model formalism

Verheij's case model formalism was first introduced in [1]. Verheij uses a classical formal logic language L generated from a set of propositional constants in a standard way. Verheij writes \neg for negation, \land for conjunction, \lor for disjunction, \leftrightarrow for equivalence, \top for a tautology, and \bot for a contradiction. The associated classical, deductive, monotonic consequence relation is denoted \vDash . Verheij assumes a finitely generated language.

Verheij defines case models by the way of formalizing the idea of cases and their preferences. The cases in a case model must be logically consistent, mutually incompatible and different; and the comparison relation must be total and transitive. Here follows the definitions of case models addressed by Verheij.

Definition 2.1: A case model is a pair (C, \geq) with finite $C \in L$, such that the following hold, for all φ , ψ and $\chi \in C$:

- 1. $\not\models \neg \varphi$;
- 2. If $\not\models \varphi \leftrightarrow \psi$, then $\models \neg (\varphi \land \psi)$;
- 3. If $\vDash \varphi \leftrightarrow \psi$, then $\varphi = \psi$;

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4. \varphi \geq \psi or \psi \geq \varphi;
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5. If \varphi \geq \psi and \psi \geq \chi, then \varphi \geq \chi.
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Definition 2.2 (Arguments) An argument is a pair (φ, ψ) with φ and $\psi \in L$. The sentence φ expresses the argument's premises, the sentence ψ its conclusions, and the sentence $\varphi \wedge \psi$ the case made by the arguments. Generalizing, a sentence $\chi \in L$ is a premise of the argument when $\varphi \vDash \chi$, a conclusion when $\psi \vDash \chi$, and a position in the case made by the argument when $\varphi \wedge \psi \vDash \chi$. An argument (φ, ψ) is (properly) presumptive when $\varphi \nvDash \psi$; otherwise not-presumptive. An argument (φ, ψ) is a presumption when $\vDash \varphi$, i.e., when its premises are logically tautologous.

Definition 2.3 (Coherent arguments) Let (C, \geq) be a case model. Then we define, for all φ and $\psi \in L$:

```
(C, \geq) \vDash (\varphi, \psi) if and only if \exists \omega \in C : \omega \in \varphi \land \psi.
```

We then say that the argument from φ to ψ is *coherent* with respect to the case model.

Definition 2.4 (*Conclusive arguments*) Let (C, \geq) be a case model. Then we define, for all φ and $\psi \in L$:

 $(C, \geq) \vDash \varphi \Rightarrow \psi$ if and only if $\exists \omega \in C : \omega \in \varphi \land \psi$ and $\forall \omega \in C$: if $\omega \in \varphi$, then $\omega \in \varphi \land \psi$.

We then say that the argument from φ to ψ is *conclusive* with respect to the case model.

Definition 2.5 (Presumptively valid arguments) Let (C, \geq) be a case model. Then we define, for all φ and $\psi \in L$:

```
(C, \geq) \vDash \varphi \leadsto \psi if and only if \exists \omega \in C:
```

1. $\omega \vDash \varphi \wedge \psi$; and

2. $\forall \omega' \in C$: if $\omega' \models \varphi$, then $\omega \geq \omega'$.

We then say that the argument from φ to ψ is (presumptively) valid with respect to the case model.

Verheij has also defined some kinds of argument attacking in his formalism[2].

Definition 2.6 (Successful attack) Let (C, \geq) be a case model, and (φ, ψ) a presumptively valid argument. Then circumstances χ are defeating or successful attacking the argument when $(\varphi \wedge \chi, \psi)$ is not presumptively valid. We write $(C, \geq) \vDash \varphi \leadsto \psi \times \chi$. Defeating circumstances are excluding when $(\varphi \wedge \chi, \psi)$ is not coherent. A case $\omega \in C$ provides grounding for the attack if $\omega \vDash \varphi \wedge \chi$.

Definition 2.7 (Rebutting attack) When circumstance χ successfully attack presumptively valid argument (φ, ψ) , the circumstances are rebutting when $(\varphi \land \chi, \neg \psi)$ is presumptively valid.

Definition 2.8 (*Undercutting attack*) When circumstances χ successfully attack presumptively valid argument (φ, ψ) , and are not rebutting, the circumstances are *undercutting*.

Definition 2.9 (*Undermining attack*) When circumstances χ successfully attack a presumption (\top, φ) , the circumstances are *undermining*.

3. Implementation in Prolog

The program introduced in this section was written in Prolog. Case models (C, \geq) are used predicate case_model(model_num(N)) to represent. Each model will

be given a number N to distinguish. It is implied by a predicate for cases and a predicate for the preferred relation. In this program, cases in the model are represented in the form of Prolog *list*, as well as the preferred relation. Predicate case(model_num(N), case_num(X), List) is used for describing cases. Similarly, each case in the case model will be given a number X, and List contains all the elementary propositions of the case. Predicate case_order has 2 variables, including model_num(N) and the list Case_order_list shows the preferred relation of cases in the model.

Case_order_list lists cases from strong to weak, if one case is as preferred as another case, then these two cases will be placed in a sublist of Case_order_list. For instance, the preferred relation of a case model with 4 cases is: $case1 > case3 \sim case4 > case2$. This order will be listed as [case_num(1), [case_num(3), case_num(4)], case_num(2)].

The program uses predicate case_model_valid which is implied by a set of predicates to check if the inputted models are consistent, incompatible and different follows the formal definition in Verheij's theory (cf. Definition 2.1).

Predicate case_model_consistent is used for judging the consistency of case models. In this process, we use predicate consistent_case to check if there exists a case in the case list that its negation is still in the list. Predicate consistent_list is implied by consistent_case, which is used for checking whether the whole case list exists the situation that happened in consistent_case. Predicate case_model_incompatible is used to check if the model is incompatible, it is implied by predicate incompatible_case which aims for checking every two cases in one case list is incompatible. Predicate case_model_ different is used for checking the difference of cases in the case model, if there exists two cases the same as each other, the program will return false.

The main function of this program is verifying the validity of the arguments in case models. The program use predicate coherent to examine coherent arguments. This predicate is implied by coherent_casemade, which uses predicate member_list to check if the *case made* by the argument in queries is logically implied by at least one case in the case list.

This program uses predicate conclusive to verify those arguments that considered to be conclusive. According to Verheij's formalism, conclusive arguments must be coherent. In addition, if all cases in the model imply the argument's premises also imply its conclusions. Predicate conclusive_casemade is the basic predicate of the process of verifying conclusive arguments. It is used for checking if a case implies the argument's premises, whether it also implies the case made by the argument. Predicate conclusive_case is implied by conclusive_casemade. In this predicate which is used for analyzing a case, only two situations will be considered as true. Firstly, this case contains both the premises of the argument and the case made by the argument. Secondly, this case does not contain the premises of the argument. The implication of this predicate is conclusive_list, a recursive predicate, which is used to check every case in the case list. If the result of this predicate is true, then we can say all cases in the case model imply the premises of the argument also imply its conclusions.

Presumptively valid arguments will use predicate presumptively_valid to verify, which is implied by a series of predicates. First of all, the program

will use coherent to check if the argument is coherent. Predicate presumptively_valid_casemade_case_basic and its implication presumptively_valid_casemade_case is going to select the strongest case which is implied the *case made* by the argument.

In order to find out the strongest case which implies the premises of an argument, according to the definition of case order, there is a situation must be aware, that is some cases in the model are as preferred as the strongest case. Thus, predicate presumptively_valid_premise_case_basic is used for distinguishing this special situation and its implication presumptively_valid_premise_case is going to find out the most preferred case implies the premises of the argument.

Predicate presumptively_valid will check if the strongest case implied the *case* made by the argument and the strongest case implied the premises of the argument are the same case.

In a query about verifying argument (φ, ψ) in the case model (C, \geq) , we use predicate conclusive and presumptively_valid to verify its properties. There are two Prolog *lists* in these two predicates, the first list contains the premises φ of an argument, the second one is consists of the argument's conclusions ψ . If the argument is conclusive or presumptively valid, the program will return true, else it will return false.

For an argument (φ, ψ) with defeating circumstances χ in the case model (C, \geq) , we use predicate successful_attack to check if it is a successful attack. According to the definition of successful attack, argument (φ, ψ) must be presumptively valid. When the defeating circumstances χ are added, the argument $(\varphi \wedge \chi, \psi)$ will become invalid. We can used predicate presumptively_valid to implement this definition.

Predicate rebutting_attack is used to distinguish rebutting attack, which is implied by successful_attack and presumtively_valid. If circumstances χ successfully attacking the argument (φ, ψ) , and argument $(\varphi \wedge \chi, \psi)$ is also presumptively valid, then we can say this is a rebutting attack. Predicate undercutting_attack is for undercutting attack, which is the negative form of predicate rebutting_attack.

Undermining attack is a special kind of successful attack, which attacks presumption (\top, φ) . In this program, a tautology \top is represented as an empty *list* [], so predicate undermining_attack is not only implied by successful_attack, but also a predicate which is used to check if the list of premises is empty.

4. Case study: Dutch tort law

The case model of Dutch tort law was built by Verheij in 2017[2]. This model applied two articles 6:162 and 6:163 of the Dutch civil code (in the Netherlands referred to as Art. 6:162 and 6:163 BW, BW for 'Burgerlijk Werboek') govern the handling of wrongful acts. Here follows the translation by [17]:

- Art. 6:612 BW. 1. A person who commits an unlawful act toward another which can be imputed to him, must repair the damage which the other person suffers as a consequence thereof.
 - 2. Except where there is a ground of justification, the following acts are deemed to be unlawful: the violation of a right, an act or omission violating

- a statutory duty or a rule of unwritten law pertaining to proper social conduct.
- 3. An unlawful act can be imputed to its author if it results from his fault or from a cause for which he is answerable according to law or common opinion.
- Art. 6:613 BW. There is no obligation to repair damage when the violated norm does not have as its purpose the protection from damage such as that suffered by the victim.

Verheij built a case model for these two articles in his paper presented in ICAIL 2017[2], he gave each elementary proposition in the case model an abbreviation. These propositions will be listed in Table 1.

There are 16 cases in this model which can be found in table 2.

Table 1. The case list of the Dutch tort law model

```
1
        \neg dmg
2
        ¬dut, dmg, ¬unl, ¬vrt, ¬vst, ¬vun
3
        ¬dut, dmg, unl, ¬imp, ¬ift, ¬ila, ¬ico
        ¬dut, dmg, unl, imp, ¬cau
4
        dut, dmg, unl, imp, cau, vrt, ¬vst, ¬vun, ift, ¬ila, ¬ico, ¬jus, prp
6
        dut, dmg, unl, imp, cau, vrt, ¬vst, ¬vun, ¬ift, ila, ¬ico, ¬jus, prp
        dut, dmg, unl, imp, cau, vrt, ¬vst, ¬vun, ¬ift, ¬ila, ico, ¬jus, prp
        dut, dmg, unl, imp, cau, ¬vrt, vst, ¬vun, ift, ¬ila, ¬ico, ¬jus, prp
        dut, dmg, unl, imp, cau, ¬vrt, vst, ¬vun, ¬ift, ila, ¬ico, ¬jus, prp
10
        dut, dmg, unl, imp, cau, \neg vrt, vst, \neg vun, \neg ift, \neg ila, ico, \neg jus, prp
        dut, dmg, unl, imp, cau, ¬vrt, ¬vst, vun, ift, ¬ila, ¬ico, ¬jus, prp
11
12
        dut, dmg, unl, imp, cau, ¬vrt, ¬vst, vun, ¬ift, ila, ¬ico, ¬jus, prp
13
        dut, dmg, unl, imp, cau, \neg vrt, \neg vst, vun, \neg ift, \neg ila, ico, \neg jus, prp
14
        ¬dut, dmg, ¬unl, vrt, ¬vst, jus
        ¬dut, dmg, ¬unl, ¬vrt, vst, jus
15
        ¬dut, dmg, unl, imp, cau, vst, ¬prp
Order case 1 > case 2 > case 3 > case 4 > case 5 \sim case 6 \sim case 7 \sim case 8
        \sim case 9 \sim case 10 \sim case 11 \sim case 12 \sim case 13 > case 14 \sim case 15 \sim
        case 16
```

Figure 1 shows the arguments extracted from this model, according to the formalism's definitions, a series of arguments can be generated:

- $\bullet \ (C, \geq) \vDash dmg \wedge unl \wedge imp \wedge cau \leadsto dut \times vst \wedge \neg prp$
- $(C, \geq) \models vrt \leadsto unl \times jus$
- $\bullet \ (C, \geq) \vDash vst \leadsto unl \times jus$
- $(C, \geq) \models vun \leadsto unl$
- $(C, \geq) \models ift \leadsto imp$
- $\bullet \ (C, \geq) \vDash ila \leadsto imp$
- $\bullet \ (C, \geq) \vDash ico \leadsto imp$

The Dutch tort law model in the Prolog program is represented as model_num(1). Through the verification given by predicate case_model_valid, this model is a valid model, as shown in Figure 2. The queries about the arguments above in this model are shown in Figure 3.

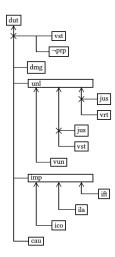


Figure 1. Arguments and their attacks in the case model of Dutch tort law

?- case_model_valid(model_num(1)).

Figure 2. The validity of Dutch tort law model

The first query checks the validity of argument $dmg \wedge unl \wedge imp \wedge cau \leadsto dut \times vst \wedge \neg prp$ in the model. As the second and third queries shows, this attack is a rebutting attack, which means it is not undercutting. This judgement is corresponded to the analysis about the Dutch tort law model above. From the fourth query to the last one, those presumptively valid argument shown above have been verified. According to the results of the program, all of these arguments are presumptively valid.

5. Case study: Copyright infringement in Chinese Criminal Law

The article of Copyright Infringement in Chinese Criminal Law[18] is below:

Article 217 Whoever, for the purpose of making profits, commits any of the following acts of infringement on copyright shall, if the amount of illegal gains is relatively large, or if there are other serious circumstances, be sentenced to fixed-term imprisonment of not more than three years or criminal detention and shall also, or shall only, be fined; if the amount of illegal gains is huge or if there are other especially serious circumstances, he shall be sentenced to fixed-term imprisonment of not less than three years but not more than seven years and shall also be fined:

- (1) copying and publishing a written work, musical work, motion picture, television programme or other visual works, computer software or other works without permission of the copyright owner;
- (2) publishing a book of which another person has the exclusive publishing right;

- ?- successful_attack(argument(model_num(1),argu_num(_),[dmg,unl,imp,cau],[dut]),[vst,not(prp)]). true.

 2- reputting_attack(argument(model_num(1),argu_num(_),[dmg,unl,imp,cau],[dut]) [vst,not(prp)]).
- ?- rebutting_attack(argument(model_num(1),argu_num(_),[dmg,unl,imp,cau],[dut]),[vst,not(prp)]). true.
- ?- undercutting_attack(argument(model_num(1),argu_num(_),[dmg,unl,imp,cau],[dut]),[vst,not(prp)]). false.
- ?- successful_attack(argument(model_num(1),argu_num(_),[vrt],[unl]),[jus]).
- ?- successful_attack(argument(model_num(1),argu_num(_),[vst],[unl]),[jus]). true.
- ?- presumptively_valid(argument(model_num(1),argu_num(_),[vun],[unl])).
- ?- presumptively_valid(argument(model_num(1),argu_num(_),[ift],[imp])). true.
- ?- presumptively_valid(argument(model_num(1),argu_num(_),[ila],[imp])).
- ?- presumptively_valid(argument(model_num(1),argu_num(_),[ico],[imp])).
 true.

Figure 3. The queries in Dutch tort law model

- (3) copying and publishing audio or video recording without permission of the producer; or
- (4) producing or selling an artwork where the signature of the author is forged.

In order to recognize the propositions in the case model easily, each elementary proposition in this model has been given an abbreviation. These abbreviations are shown in table 3.

In Art. 217, there are 4 kinds of situation in copyright infringement, if someone violates other people's copyright for the purpose of making profits, then he will be sentenced to the crime of copyright infringement. The judge will sentenced him to 4 different kinds of punishment according to the degree of severity of his crime. Above all, several rules about copyright infringement can be extracted.

If the defendant has following actions:

- 1. publish or copied something which can be considered as one of the items shown in Art. 217:1 without permission of the copyright owner;
- 2. publish a book of which another person has the exclusive publishing right;
- 3. publish or copied the audio or video resording which the producer is someone else;
- 4. produce or sell an artwork where the signature of the author if forged, Then the defendant will be regarded as violating someone else's copyright.

If the defendant was regarded as violating someone else's copyright for the purpose of making profits, then the defendant will be sentenced to the crime of copyright infringement. This rule can be represented as $ifg \land fpp \Rightarrow crc$.

If the amount of defendant's illegal gains was large or existed other serious circumstances, the defendant shall be sentenced to 3 kinds of punishments, fixed-term imprisonment of not more than 3 years and fined $(crc \land ils \leadsto l3fti \land fin)$;

Table 2. Elementary propositions in the case model of copyright infringement

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criminal detention and fined $(crc \wedge ils \leadsto cdt \wedge fin)$ and only fined $(crc \wedge ils \leadsto fin)$.

If the amount of defendant's illegal gains was huge or existed other especially serious circumstances, then the defendant shall be sentenced to fixed-term imprisonment of not less that three years but not more than seven years and fined, this can be represented as $crc \wedge ihe \Rightarrow m3fti \wedge fin$.

There are two kinds of punishments which are possible to be put on probation, if the defendant satisfied the conditions of probation: 1. fixed-term imprisonment fo not more than 3 years and fined $(crc \wedge l3fti \wedge fin \wedge cpb \Rightarrow pbt)$; 2. criminal detention and fined $(crc \wedge cdt \wedge fin \wedge cpb \Rightarrow pbt)$.

According to Art. 217's relevant judicial explanations, there are 3 defeating circumstance: 1. The action is not belong to "without permission of the copyright owner"; 2. The defendant is sentenced to the crime of copyright infringement, however, he also satisfies with the conditions of being given a heavier punishment; 3. The defendant is sentenced to the crime of copyright infringement, however, he also satisfies with the conditions of being given a lighter punishment.

If we add these defeating circumstance to the rules we listed above, then some of the rules will be changed. For example,

- $pac \wedge ite \wedge pco \leadsto ifg \times pec$
- $crc \wedge ils \rightsquigarrow l3fti \wedge fin \times hps$
- $crc \wedge ihe \Rightarrow m3fti \wedge fin \times lps$

In the light of Art. 217 and the judicial explanations related to it, a case model can be built. The model has 46 cases. Case 1 is built by the principle of "presumption of innocence". Case 2 shows the scenario that although the defendant has published and copied the items shown in Art. 217:1 without the permission of the copyright owner, he still will not be considered as copyright infringement because his action is not belong to "without permission of the copyright owner". Case 3 shows the scenario that the defendant violated someone else's copyright, but he didn't do it for making profits, so he will not be judge through Art. 217.

From Case 4 to Case 13, different punishments for the defendant's action in Art. 217:1 are listed. In the same way, different punishments for the defendant in Art. 217:2, Art. 217:3 and Art. 217:4 will also be listed into the case model. Table 4 lists cases from Case 1 to Case 13. Case 14 to Case 46 have similar components with Case 4 to Case 13, except the situations are different.

Table 3. The case list of the case model

```
1
                   ¬pac, ¬ite, ¬pco, ¬epr, ¬avp, ¬psa, ¬ifg
2
                  pac, ite, pco, pec, ¬ifg
3
                  pac, ite, pco, ¬pec, ¬epr, ¬avp, ¬psa, ifg, ¬fpp
4
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, hps, ¬lps, ¬m3fti,
                  ¬l3fti. ¬cdt. ¬fin
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, ¬hps, lps, ¬m3fti,
                   ¬l3fti, ¬cdt, ¬fin
6
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, ¬hps, ¬lps, m3fti,
                   ¬l3fti, ¬cdt, fin
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, hps, ¬lps, ¬m3fti,
                   ¬l3fti, ¬cdt, ¬fin
8
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, lps, ¬m3fti,
                   ¬l3fti, ¬cdt, ¬fin
9
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti,
                   ¬l3fti, ¬cdt, fin
10
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti,
                  l3fti, ¬cdt, fin, cpb, pbt
11
                  pac, ite, pco, \neg epr, \neg avp, \neg psa, ifg, fpp, \neg ihe, ils, crc, \neg hps, \neg lps, \neg m3fti,
                   ¬l3fti, cdt, fin, cpb, pbt
12
                  pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti,
                  l3fti, ¬cdt, fin, ¬cpb, ¬pbt
13
                  pac, ite, pco, \neg epr, \neg avp, \neg psa, ifg, fpp, \neg ihe, ils, crc, \neg hps, \neg lps, \neg m3fti,
                   ¬l3fti, cdt, fin, ¬cpb, ¬pbt
14
Order case 1 > case 2 = case 3 = case 14 = case 25 = case 36 > case 4 = case
                  5 = \operatorname{case} 7 = \operatorname{case} 8 = \operatorname{case} 15 = \operatorname{case} 16 = \operatorname{case} 18 = \operatorname{case} 19 = \operatorname{case} 26
                  = case 27 = case 29 = case 30 = case 37 = case 38 = case 40 = case 41
                  > case 6 = case 9 = case 10 = case 11 = case 12 = case 13 = case 17 =
                  case 20 = case 21 = case 22 = case 23 = case 24 = case 28 = case 31 =
                  case 32 = case 33 = case 34 = case 35 = case 39 = case 42 = case 43 = case 35 = case 42 = case 43 = case
                  case 44 = case 45 = case 46
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From this copyright infringement model, we can get the argument diagram illustrated in Figure 4. This argument has multi-steps, and it is corresponding to the model we built.



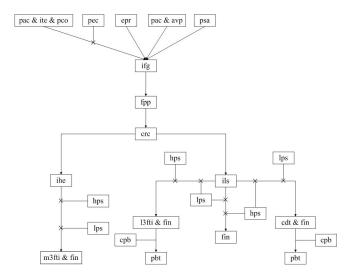


Figure 4. Arguments and their attacks in the case model of Chinese copyright infringement

According to the definitions of Verheij's case model formalism, the rule $epr \Rightarrow ifg$ is valid in this model. As the model shows, case 14 and case 15 implicate sentence $epr \wedge ifg$ which is the case made by the argument (epr, ifg), so this argument is coherent. Besides, all the cases which imply the premise epr, also imply the conclusion ifg. So argument (epr, ifg) is conclusive in the case model. And these arguments are also conclusive in the model:

- $(C, \geq) \models pac \land avp \Rightarrow ifg$
- $(C, \geq) \models ifg \land fpp \Rightarrow crc$
- $(C, \geq) \models crc \wedge l3fti \wedge fin \wedge cpb \Rightarrow pbt$

According to the definitions of Verheij's case model formalism, the rule $pac \land ite \land pco \leadsto ifg \times pec$ is also valid in the copyright infringement model. The attack from pec successfully attacked the presumptively valid argument $(pac \land ite \land pco, ifg)$, and made the argument $(pac \land ite \land pco \land pec, \neg ifg)$ presumptively valid. In the light of the copyright infringement model, Case 2 has implied the case made by the argument $(pac \land ite \land pco \land pec, \neg ifg)$, so this argument is coherent. Furthermore, Case 2 is the strongest case in the cases which implied the premise of this argument. So we say the argument $(pac \land ite \land pco \land pec, \neg ifg)$ is presumptively valid in the case model. The arguments below are also presumptively valid:

- $(C,\subseteq) \models crc \land ils \leadsto l3fti \land fin \times hps$
- $(C, \subseteq) \models crc \land ils \leadsto cdt \land fin \times hps$
- $(C, \subseteq) \models crc \land ihe \leadsto m3fti \land fin \times lps$

The Chinese copyright infringement model is represented as model_num(2) in the program. Figure 5 shows that it is a valid model. The arguments and attacks shown above can be verified by this program.

?- case_model_valid(model_num(2)). true.

Figure 5. The validity of Chinese copyright infringement model

```
?- successful_attack(argument(model_num(2),argu_num(_),[pac,ite,pco],[ifg]),[pec]).
true.
?- rebutting_attack(argument(model_num(2),argu_num(_),[pac,ite,pco],[ifg]),[pec]).
true.
?- undercutting_attack(argument(model_num(2),argu_num(_),[pac,ite,pco],[ifg]),[pec]).
false.
?- successful_attack(argument(model_num(2),argu_num(_),[crc,ils],[l3fti,fin]),[hps]).
true.
?- successful_attack(argument(model_num(2),argu_num(_),[crc,ils],[cdt,fin]),[hps]).
true.
?- successful_attack(argument(model_num(2),argu_num(_),[crc,ihe],[m3fti,fin]),[lps]).
true.
?- conclusive(argument(model_num(2),argu_num(_),[epr],[ifg])).
true.
?- conclusive(argument(model_num(2),argu_num(_),[ifg,fpp],[crc])).
true.
?- conclusive(argument(model_num(2),argu_num(_),[ifg,fpp],[crc])).
true.
?- conclusive(argument(model_num(2),argu_num(_),[crc,l3fti,fin,cpb],[pbt])).
```

Figure 6. The queries in Chinese copyright infringement model

As Figure 6 shows, the program has verified that circumstance pec successfully attack argument $pac \land ite \land pco \leadsto ifg$, and it is a rebutting attack, as well as the other arguments with defeating circumstances above which are also considered to be successful. The program also finds argument $epr \Rightarrow ifg$ and other three arguments to be conclusive. These results are corresponded to the analysis about Chinese copyright infringement model above.

6. Discussion and Conclusion

In this paper, two case models with different backgrounds based on Verheij's case model formalism have been discussed. As the arguments implied in these case models are corresponded to the rules in statutes, Verheij's theory has been proved that it is suitable for Chinese legal system. The preferred relation established by Verheij solves the priority relationship among the cases in case model, so that the presumptive arguments in legal reasoning can be concluded by this theory. In other words, some legal issues can be solved, such as the rules used for legal reasoning, which are beyond the statutes, for instance, "presumption of innocence" in the background of Chinese legal system. Although it is not in any statute, every judge will think about it during the process of making decisions. So we can place this rule as several cases in the preferred relation of a case model properly to solve this issue. Therefore, we believe arguments embedded values are more suitable for dealing with practical issues in legal reasoning.

The program we build in this paper intends to make the modeling process with less mistakes and its main function is automatically verifying the validity of the arguments implicated in a case model and the case model itself. This program has been proved that it is completely suitable for those models based on Verheij's theory, even these models have different backgrounds. Compare with the original hand-made modeling way, it can reduce mistakes during the process of modeling significantly, as this program can verify the model automatically. So, it is a successful attempt as a computational implementation for Verheij's case model formalism which can make Verheij's theory more useable in practical environment.

However, there is still room for improvement. For those people who are unfamiliar with legal statues, an explicit case model can be helpful for them, which means the model needs to contain as much details as possible, such as the official judicial explanations related to Chinese criminal law. But this action can bring a problem cannot be ignored. For instance, there are 8 scenarios about the elementary proposition "amount of illegal gains is huge or other especially serious circumstances" mentioned in the Chinese copyright infringement model in the light of relevant judicial explanations, if all of these specific scenarios are added into the model, the number of cases in this model will become huge. According to the way of building a model completely based on Verheij's formalism, all these scenarios will be treated as elementary propositions and they will replace the position of *ihe*. The number of cases will increase by eight times, if we added these specific scenarios to the model by Verheij's theory directly, which also lets the process of modeling easily to make mistakes. It will be a hard job for the people who wants to build a model. This issue needed to be solved in the future research.

The results of this paper shows that Verheij's case model formalism can be used to model the object with complex argument structure, and the program developed in this paper is feasible for the models based on Verheij's theory. It also proves that the Prolog program we built can well combine cases, rules and arguments. It is not only applicable to the civil law system but also to the Chinese legal system. AI and legal reasoning technology needs to combine rule-based reasoning, case-based reasoning and argumentation together, and argumentation technology can be the bridge of both cases and rules.

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