Checking the validity of rule-based arguments grounded in cases: a computational approach

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Abstract. Legal justice needs judges' decisions to be rational and reasonable in the sense that arguments are based on rules and grounded in cases. One puzzle studied in AI & Law is how arguments, rules and cases are formally connected. Recently a formal theory was proposed formalizing how the validity of arguments based on rules can be grounded in cases. Three kinds of argument validity were distinguished: coherence, presumptive validity and conclusiveness. In this paper the theory is implemented in a Prolog program, used to evaluate a previously developed model of Dutch tort law. We also test the theory and its implementation with a new case study modeling Chinese copyright infringement law. In this way we illustrate that by the use of the implementation the process of modeling becomes more efficient and less error-prone.

Keywords. Artificial Intelligence and Law, Rule-based Reasoning, Case-based Reasoning, Argumentation Modeling, Prolog

1. Introduction

In the field of AI and law—going at least back to the 1970s [1]—, scholars usually follow three approaches to develop legal reasoning systems, which are rule-based reasoning, case-based reasoning and argument-based reasoning. In the 1980s, the British Nationality Act (BNA) was implemented in Prolog [2], in a successful attempt to develop rule-based reasoning systems in the field of law. Case-based reasoning was modeled in the systems HYPO, BankXX, CATO and IBP [3, 4, 5, 6, 7]. CABARET [8] and GREBE [9] are hybrid systems not only use case-based reasoning, but also other kinds of reasoning. Argumentation models of legal rule-based and case-based reasoning [10, 11] are connected to later systems based on abstract argumentation [12], inspiring for instance ASPIC+ [13], ABA [14] and DeLP [15].

The recent case model formalism [16] is a hybrid theory showing connections between cases, rules and arguments [17]. The formalism defines different ways in

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which rule-based arguments can be valid in cases: arguments can be coherent, conclusive or presumptive. The formalism has been applied to model Dutch tort law, showing how a rule-based legal domain can be grounded in legal cases. In this way, a formal connection is established between the civil law tradition focusing on rules and the common law tradition focusing on cases. The formalism has also been applied to the modeling of a series of New York tort cases (as studied by [18, 19]), analyzing value-guided teleological reasoning [20].

The present paper provides a computational version of the case model formalism. A Prolog program is presented that can computationally check whether a case model is correct, whether rule-based arguments are valid (in the three kinds of validity coherence, conclusiveness and presumptiveness), and whether defeating circumstances are rebutting, undercutting or undermining. The computational tool can be used to support the manual modeling of a complex legal domain, making that more manageable. As an example, we provide a new domain model, namely Chinese copyright infringement law, both formally (as a case model) and computationally (in Prolog).

2. The case model formalism

The case model formalism was introduced in [16]. The formalism uses a classical formal logical language L generated from a finite set of propositional constants in a standard way writing $\neg$ for negation, $\wedge$ for conjunction, $\vee$ for disjunction, $\leftrightarrow$ for equivalence, $\top$ for a tautology, and $\bot$ for a contradiction. The associated classical, deductive, monotonic consequence relation is denoted $\vDash$.

Case models formalize cases and their ordering. The cases in a case model must be logically consistent, mutually incompatible and different; and the comparison relation must be total and transitive. Here follow the core definitions.

Definition 2.1: A *case model* is a pair $(C, \geq)$ with finite $C \in L$, such that the following hold, for all φ, ψ and $\chi \in C$:

1. $\nvDash \neg\varphi$;
2. If $\nvDash \varphi \leftrightarrow \psi$, then $\vDash \neg\,(\varphi \wedge \psi)$;
3. If $\vDash \varphi \leftrightarrow \psi$, then $\varphi = \psi$;
4. $\varphi \geq \psi$ or $\psi \geq \varphi$;
5. If $\varphi \geq \psi$ and $\psi \geq \chi$, then $\varphi \geq \chi$.

Definition 2.2 (*Arguments*) An *argument* is a pair (φ, ψ) with φ and $\psi \in L$. The sentence φ expresses the argument's premises, the sentence ψ its conlusions, and the sentence $\varphi \wedge \psi$ the *case made* by the arguments. Generalizing, a sentence $\chi \in L$ is a *premise* of the argument when $\varphi \vDash \chi$, a *conclusion* when $\psi \vDash \chi$, and a *position* in the case made by the argument when $\varphi \wedge \psi \vDash \chi$. An argument (φ, ψ) is *(properly) presumptive* when $\varphi \nvDash \psi$; otherwise *not-presumptive*. An argument (φ, ψ) is a *presumption* when $\vDash \varphi$, i.e., when its premises are logically tautologous.

Definition 2.3 *(Coherent arguments)* Let $(C, \geq)$ be a case model. Then we define, for all φ and $\psi \in L$:

$(C, \geq) \vDash (\varphi, \psi)$ if and only if $\exists \omega \in C : \omega \in \varphi \wedge \psi$.

We then say that the argument from φ to ψ is *coherent* with respect to the case model.

Definition 2.4 (*Conclusive arguments*) Let $(C, \geq)$ be a case model. Then we define, for all φ and $\psi \in L$:

$(C, \geq) \vDash \varphi \Rightarrow \psi$ if and only if $\exists \omega \in C : \omega \in \varphi \wedge \psi$ and $\forall \omega \in C$: if $\omega \in \varphi$, then $\omega \in \varphi \wedge \psi$.

We then say that the argument from φ to ψ is *conclusive* with respect to the case model.

Definition 2.5 (*Presumptively valid arguments*) Let $(C, \geq)$ be a case model. Then we define, for all φ and $\psi \in L$:

$(C, \geq) \vDash \varphi \rightsquigarrow \psi$ if and only if $\exists \omega \in C$:

1. $\omega \vDash \varphi \wedge \psi$; and
2. $\forall \omega' \in C$: if $\omega' \vDash \varphi$, then $\omega \geq \omega'$.

We then say that the argument from φ to ψ is *(presumptively) valid* with respect to the case model.

Verheij has also defined some kinds of argument attacking in his formalism[17].

Definition 2.6 (*Successful attack*) Let $(C, \geq)$ be a case model, and (φ, ψ) a presumptively valid argument. Then circumstances χ are *defeating* or *successful attacking* the argument when $(\varphi \wedge \chi, \psi)$ is not presumptively valid. We write $(C, \geq) \vDash \varphi \rightsquigarrow \psi \times \chi$. Defeating circumstances are *excluding* when $(\varphi \wedge \chi, \psi)$ is not coherent. A case $\omega \in C$ provides grounding for the attack if $\omega \vDash \varphi \wedge \chi$.

Definition 2.7 (*Rebutting attack*) When circumstance χ successfully attack presumptively valid argument (φ, ψ), the circumstances are rebutting when $(\varphi \wedge \chi, \neg\psi)$ is presumptively valid.

Definition 2.8 (*Undercutting attack*) When circumstances χ successfully attack presumptively valid argument (φ, ψ), and are not rebutting, the circumstances are *undercutting*.

Definition 2.9 (*Undermining attack*) When circumstances χ successfully attack a presumption $(\top, \varphi)$, the circumstances are *undermining*.

3. Implementation in Prolog

We have implemented the case model formalism in Prolog. We use the previously developed model of Dutch tort law [17] as an illustration. Cases are represented as Prolog lists, of which the elements consist of strings and their negations (represented using not/1). For instance, [not(dut),dmg,unl,imp,not(cau)] represents the case in which there is no duty (not(dut)) to repair the damages (dmg) although the act is unlawful (unl) and imputable (imp]), but there is no causality (not(cau)). Case models are represented as lists of cases and their ordering, where case models and cases are referred to using identifiers.

Listing 1 provides a part of the representation of the case model for Dutch tort law (model_num(1)). The representation of the case model starts with a series of definitions of cases followed by the ordering. Here case_num(104) is the non-causality case just discussed. The full model consists of the 16 cases discussed in [17]. The ordering is represented as a list of cases and lists of cases, each representing an equivalence class of the total preorder, in decreasing level of preference. Hence the first element of this list represents the case or cases that are maximal in the total preorder. Here there is one maximal case case_num(101): not(dmg),

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case ( model_num ( 1 ) , case_num ( 101 ) , [ not ( dmg ) ] ) .
...
case ( model_num ( 1 ) , case_num ( 104 ) , [ not ( dut ) , dmg , unl , imp , not ( cau ) ] ) .
case ( model_num ( 1 ) , case_num ( 105 ) , [ dut , dmg , unl , imp , cau , vrt , not ( vst ) , not ( vun ) , ift
      , not ( ila ) , not ( ico ) , not ( jus ) , prp ] ) .
...
case ( model_num ( 1 ) , case_num ( 114 ) , [ not ( dut ) , dmg , not ( unl ) , vrt , not ( vst ) , jus ] ) .
...
case_order ( model_num ( 1 ) , [ case_num ( 101 ) , case_num ( 102 ) , case_num ( 103 ) , case_num
      ( 104 ) , [ case_num ( 105 ) , case_num ( 106 ) , ... , case_num ( 113 ) ] , ... ] ) .
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Listing 1: Definition of the Dutch tort law case model in Prolog

representing that there are no damages. When an equivalence class consists of several cases, such as [case_num(105),...,case_num(113)], it is represented as a list of cases (actually: of case identifiers).

The predicate case_model_valid/1 (with a case identifier as single argument) checks whether a case model fulfills the definition, i.e. whether all cases are consistent, incompatible and different (cf. Definition 2.1 above). Consistency is determined by checking whether a case contains an element and its negation. For instance, a case [not(dmg), dmg] would not be consistent. This straightforward way of consistency checking is allowed by our use of a language of elementary literals instead of a full propositional language. Incompatibility is checked by determining for every pair of cases whether there is an element in one case of which the negation is in the other. For instance, cases case_num(101): not(dmg) and case_num(104): not(dut),dmg,... can be distinguished by not(dmg) and dmg, hence are incompatible. Difference is checked by determining for every pair of cases whether there is an element in one case that is not in the other. Note that a pair of incompatible cases implies that they are different. Checking elements 4 and 5 in the formal definition of case models is not directly representd since we use an explicit representation of the total preorder as a list of equivalence classes. In this representation another validity check is helpful, namely whether each case of which an identifier appears in the ordering is defined and whether each case identifier of a defined case appears in the ordering exactly once. This check has been implemented using the predicate ordering_valid/1.

Arguments are represented by a list of premises and a list of conclusions. For instance, argument([dmg,unl,imp,cau],[dut]) represents the argument to the one-element conclusion that there is a duty to repair the damages (dut) from the four-element premises that there are damages (dmg) by an unlawful act (unl) that is imputable (imp) to the actor and that has caused the damages (cau).

The three kinds of validity of arguments can be checked using the predicates coherent/1, conclusive/1 and presumptively_valid/1, each taking an argument (represented using argument/2) as input. Coherence is checked by first determining the case made by an argument, found by appending the list of premises to the list of conclusions, and then checking whether there is a case in the case model that contains all elements of the case made by the argument. For instance, argument([dmg,unl,imp,cau],[dut])) is coherent by the case with identifier 105 whereas argument([dmg],[not(dmg)]) is not as its case made is not consistent.

The conclusiveness of an argument is checked by first checking whether the argument is coherent and then checking, if all cases in the case model that contain the argument's premises also contain its conclusions. For instance, argument([dmg],[dut]) is coherent (e.g., by case 105) but not conclusive (by case 104). The argument argument([dut],[dmg]) is conclusive since it is coherent (e.g., by 105) and indeed all cases of dut are also cases of dmg.

Presumptive validity of an argument is checked by first determining a maximally preferred case that witnesses the argument's coherence (i.e., finding a case in which both the premises and the conclusions of the argument hold and that is maximal in the ordering with this property) and then checking for each case in which the argument's premises hold whether such a witnessing case is of equal or lower ordering. For instance, argument([vrt],[unl]) is presumptively valid since for instance case 105 is a case of maximal ordering that shows the arguments coherence, and there is no case of the premises that is higher in the ordering. The coherent argument argument([vrt],[not(unl)]) is not presumptively valid since maximally ordered cases that show the coherence of the argument (such as case 114) are not maximal among the cases in which the premises hold (e.g., case 105 is higher in the ordering).

Attack of arguments has been implemented using the predicates successful_attack/2, rebutting_attack/2, undercutting_attack/2 and undermining_attack/2. The predicate successful_attack/2 takes an argument and defeating circumstances (as a list) as input. The predicate checks whether the argument is presumptively valid and whether the argument to the same conclusions but from the premises with the defeating circumstances appended is also presumptively valid. For instance, since argument([vrt],[unl]) is presumptively valid, while argument([vrt, jus],[unl]) is not (it is not even coherent), the Prolog query ?− successful_attack(argument([vrt],[unl]), [jus]) returns true as an answer.

The three kinds of attack—rebutting, undercutting and undermining—are defined in terms of successful attack as follows. Rebutting attack requires a successful attack of an argument such that also the argument from the premises to the opposite of the argument's conclusion is presumptively valid. Note that this only makes sense for arguments with a single element as conclusion as we use no Prolog expression for the negation of a series of conclusions. For instance, rebutting_attack(argument([vrt],[unl]), [jus]) holds since it represents a successful attack and also argument([vrt],[not(unl)]) is presumptively valid. Successful attacks that are not rebutting attacks are undercutting. Undermining attack is a special kind of successful attack, namely an attack of an argument with a tautology as premise. In the program, a tautology is represented as an empty Prolog list [ ].

The Prolog program can be used to validate hand-made domain models, such as the case model for Dutch tort law of [17]. In Figure 1, we show the argument structure that is valid in the hand-made formal case model of that paper (left). On the right, we show Prolog clauses that all evaluate to true given the Prolog version of that case model (partially shown in Listing 1). Each supporting arrow (with a normal arrow head) evaluates as a presumptively valid argument, as expected, some even more strongly as a conclusive argument. Each attacking arrow (ending in a cross) evaluates as a successful attack, in fact all attacks in this model are rebutting attacks. In other words, the model is computationally validated.
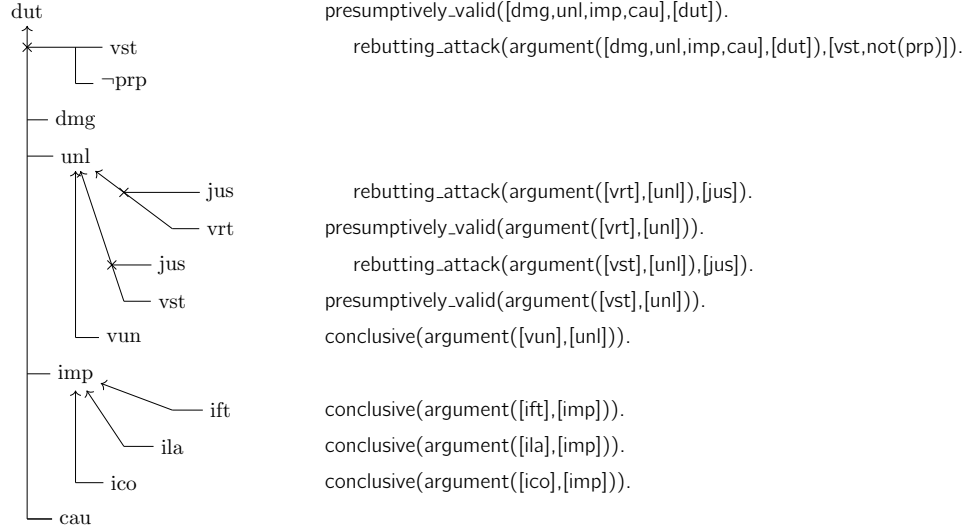
dut

　　vst

　　¬prp

　dmg

　unl

　　　jus

　　　vrt

　　jus

　　vst

　　vun

　imp

　　　ift

　　　ila

　　ico

　cau

presumptively_valid([dmg,unl,imp,cau],[dut]).

rebutting_attack(argument([dmg,unl,imp,cau],[dut]),[vst,not(prp)]).

rebutting_attack(argument([vrt],[unl]),[jus]).

presumptively_valid(argument([vrt],[unl])).

rebutting_attack(argument([vst],[unl]),[jus]).

presumptively_valid(argument([vst],[unl])).

conclusive(argument([vun],[unl])).

conclusive(argument([ift],[imp])).

conclusive(argument([ila],[imp])).

conclusive(argument([ico],[imp])).

Figure 1. The Dutch tort law model: argument structure (left); in Prolog (right)

4. Case study: Copyright infringement in Chinese Criminal Law

The article of Copyright Infringement in Chinese Criminal Law[21] is below:

> **Article 217** Whoever, for the purpose of making profits, commits any of the following acts of infringement on copyright shall, if the amount of illegal gains is relatively large, or if there are other serious circumstances, be sentenced to fixed-term imprisonment of not more than three years or criminal detention and shall also, or shall only, be fined; if the amount of illegal gains is huge or if there are other especially serious circumstances, he shall be sentenced to fixed-term imprisonment of not less than three years but not more than seven years and shall also be fined:
> (1) copying and publishing a written work, musical work, motion picture, television programme or other visual works, computer software or other works without permission of the copyright owner;
> (2) publishing a book of which another person has the exclusive publishing right;
> (3) copying and publishing audio or video recording without permission of the producer; or
> (4) producing or selling an artwork where the signature of the author is forged.

In order to recognize the propositions in the case model easily, each elementary proposition in this model has been given an abbreviation. These abbreviations are shown in table 3.

In Art. 217, there are 4 kinds of situation in copyright infringement, if someone violates other people's copyright for the purpose of making profits, then he will be sentenced to the crime of copyright infringement. The judge will sentenced

Table 1. Elementary propositions in the case model of copyright infringement

ifg	copyright infringement
fpp	for the purpose of making profits
pac	publish and copy
ite	the items in Art. 217:1
pco	without permission of the copyright owner
pec	the action is not belong to "without permission of the copyright owner"
epr	publishing a book of which another person has the exclusive publishing right
avp	the audio or video recording which the producer is someone else
psa	producing or selling an artwork where the signature of the author is forged
ils	amount of illegal gains is large or other serious circumstances
ihe	amount of illegal gains is huge or other especially serious circumstances
crc	the person commits the crime of copyright infringement
l3fti	the person shall be sentenced to fixed-term imprisonment of not more than three years
cdt	the person shall be sentenced to criminal detention
fin	the person shall be fined
m3fti	the person shall be sentenced to fixed-term imprisonment of not less than three years but not more than seven years
hps	there is a reason which will give the defendant a heavier punishment
lps	there is a reason which will give the defendant a lighter punishment
cpb	the defendant satisfies the conditions of probation
pbt	the defendant will be put on probation

him to 4 different kinds of punishment according to the degree of severity of his crime. Above all, several rules about copyright infringement can be extracted.

If the defendant has following actions:

1. *publish or copied something which can be considered as one of the items shown in Art. 217:1 without permission of the copyright owner*;
2. *publish a book of which another person has the exclusive publishing right*;
3. *publish or copied the audio or video resording which the producer is someone else*;
4. *produce or sell an artwork where the signature of the author if forged*,

Then the defendant will be regarded as violating someone else's copyright.

If the defendant was regarded as violating someone else's copyright for the purpose of making profits, then the defendant will be sentenced to the crime of copyright infringement. This rule can be represented as $ifg \wedge fpp \Rightarrow crc$.

If *the amount of defendant's illegal gains was large or existed other serious circumstances*, the defendant shall be sentenced to 3 kinds of punishments, *fixed-term imprisonment of not more than 3 years and fined* ($crc \wedge ils \rightsquigarrow l3fti \wedge fin$); *criminal detention and fined* ($crc \wedge ils \rightsquigarrow cdt \wedge fin$) and only *fined* ($crc \wedge ils \rightsquigarrow fin$).

If *the amount of defendant's illegal gains was huge or existed other especially serious circumstances*, then the defendant shall be sentenced to *fixed-term imprisonment of not less that three years but not more than seven years and fined*, this can be represented as $crc \wedge ihe \Rightarrow m3fti \wedge fin$.

There are two kinds of punishments which are possible to be put on probation, if the defendant satisfied the conditions of probation: 1. fixed-term imprisonment of not more than 3 years and fined ($crc \wedge l3fti \wedge fin \wedge cpb \Rightarrow pbt$); 2. criminal detention and fined ($crc \wedge cdt \wedge fin \wedge cpb \Rightarrow pbt$).

According to Art. 217's relevant judicial explanations, there are 3 defeating circumstance: 1. The action is not belong to "without permission of the copyright owner"; 2. The defendant is sentenced to the crime of copyright infringement, however, he also satisfies with the conditions of being given a heavier punishment; 3. The defendant is sentenced to the crime of copyright infringement, however, he also satisfies with the conditions of being given a lighter punishment.

If we add these defeating circumstance to the rules we listed above, then some of the rules will be changed. For example,

- $pac \wedge ite \wedge pco \rightsquigarrow ifg \times pec$
- $crc \wedge ils \rightsquigarrow l3fti \wedge fin \times hps$
- $crc \wedge ihe \Rightarrow m3fti \wedge fin \times lps$

In the light of Art. 217 and the judicial explanations related to it, a case model can be built. The model has 46 cases. Case 1 is built by the principle of "presumption of innocence". Case 2 shows the scenario that although the defendant has published and copied the items shown in Art. 217:1 without the permission of the copyright owner, he still will not be considered as copyright infringement because his action is not belong to "without permission of the copyright owner". Case 3 shows the scenario that the defendant violated someone else's copyright, but he didn't do it for making profits, so he will not be judge through Art. 217.

From Case 4 to Case 13, different punishments for the defendant's action in Art. 217:1 are listed. In the same way, different punishments for the defendant in Art. 217:2, Art. 217:3 and Art. 217:4 will also be listed into the case model. Table 2 lists part of cases in the model, Case 14 to Case 46 have similar components with Case 4 to Case 13, except the acts of infringement on copyright are different. In this model, Case 1 is the most preferred case, as we consider the "presumption of innocence" is the most important principle in the process of decision making. Besides, in some situations, the defendant will not be regarded as violating someone else's copyright, for instance, the defendant's action is not belong to "without permission of the copyright owner" or his purpose is not for making profits. In this model, these situations are also very important. So we put them in second place. The rest of cases in the preferred relation are the specific punishments of copyright infringement, we put them in third place.

Table 2.: The case list of the case model

1	¬pac, ¬ite, ¬pco, ¬epr, ¬avp, ¬psa, ¬ifg
2	pac, ite, pco, pec, ¬ifg
3	pac, ite, pco, ¬pec, ¬epr, ¬avp, ¬psa, ifg, ¬fpp
4	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, hps, ¬lps, ¬m3fti, ¬l3fti, ¬cdt, ¬fin
5	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, ¬hps, lps, ¬m3fti, ¬l3fti, ¬cdt, ¬fin
6	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ihe, ¬ils, crc, ¬hps, ¬lps, m3fti, ¬l3fti, ¬cdt, fin
7	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, hps, ¬lps, ¬m3fti, ¬l3fti, ¬cdt, ¬fin
8	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, lps, ¬m3fti, ¬l3fti, ¬cdt, ¬fin
9	pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti, ¬l3fti, ¬cdt, fin

10 pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti, l3fti, ¬cdt, fin, cpb, pbt
11 pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti, ¬l3fti, cdt, fin, cpb, pbt
12 pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti, l3fti, ¬cdt, fin, ¬cpb, ¬pbt
13 pac, ite, pco, ¬epr, ¬avp, ¬psa, ifg, fpp, ¬ihe, ils, crc, ¬hps, ¬lps, ¬m3fti, ¬l3fti, cdt, fin, ¬cpb, ¬pbt
14 ... ...

case 1 > case 2 ∼ case 3 ∼ ... > case 4 ∼ case 5 ∼ case 6 ∼ case 7 ∼ ... ∼ case 8 ∼ case 9 ∼ case 10 ∼ case 11 ∼ case 12 ∼ case 13 ∼ ...

From this copyright infringement model, we can get the argument diagram illustrated in Figure 2. This argument has multi-steps, and it is corresponding to the model we built.
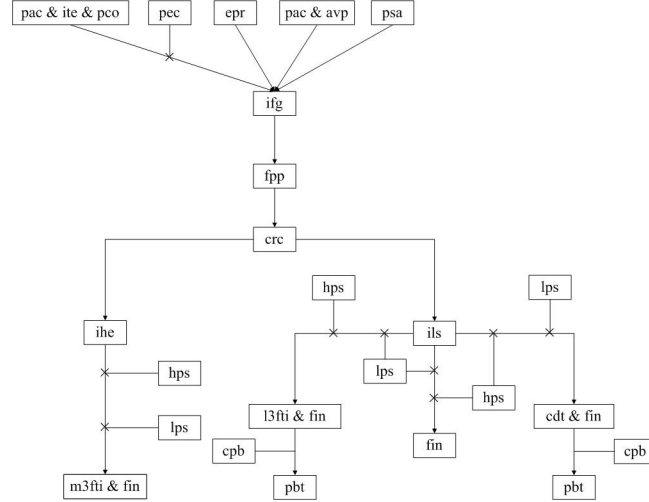

Figure 2. Arguments and their attacks in the case model of Chinese copyright infringement

According to the definitions of Verheij's case model formalism, the rule $epr \Rightarrow ifg$ is valid in this model. As the model shows, case 14 and case 15 implicate sentence $epr \wedge ifg$ which is the case made by the argument (epr, ifg), so this argument is coherent. Besides, all the cases which imply the premise epr, also imply the conclusion ifg. So argument (epr, ifg) is conclusive in the case model. And these arguments are also conclusive in the model:

- $(C, \geq) \models pac \wedge avp \Rightarrow ifg$
- $(C, \geq) \models ifg \wedge fpp \Rightarrow crc$
- $(C, \geq) \models crc \wedge l3fti \wedge fin \wedge cpb \Rightarrow pbt$

According to the definitions of Verheij's case model formalism, the rule $pac \wedge ite \wedge pco \rightsquigarrow ifg \times pec$ is also valid in the copyright infringement model. The attack from pec successfully attacked the presumptively valid argument $(pac \wedge ite \wedge pco, ifg)$, and made the argument $(pac \wedge ite \wedge pco \wedge pec, \neg ifg)$ presumptively valid. In the light of the copyright infringement model, Case 2 has implied the case

made by the argument $(pac \wedge ite \wedge pco \wedge pec, \neg ifg)$, so this argument is coherent. Furthermore, Case 2 is the strongest case in the cases which implied the premise of this argument. So we say the argument $(pac \wedge ite \wedge pco \wedge pec, \neg ifg)$ is presumptively valid in the case model. The arguments below are also presumptively valid:

- $(C, \subseteq) \models crc \wedge ils \rightsquigarrow l3fti \wedge fin \times hps$
- $(C, \subseteq) \models crc \wedge ils \rightsquigarrow cdt \wedge fin \times hps$
- $(C, \subseteq) \models crc \wedge ihe \rightsquigarrow m3fti \wedge fin \times lps$

The Chinese copyright infringement model is represented as model_num(2) in the program.

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case(model_num(2),case_num(201),[not(pac),not(ite),not(pco),not(epr),not(avp),
    not(psa),not(ifg)]).
case(model_num(2),case_num(202),[pac,ite,pco,pec,not(ifg)]).
case(model_num(2),case_num(203),[pac,ite,pco,not(pec),not(epr),not(avp),not(psa)
    ,ifg,not(fpp)]).
case(model_num(2),case_num(204),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    ihe,not(ils),crc,hps,not(lps),not(m3fti),not(l3fti),not(cdt),not(fin)]).
case(model_num(2),case_num(205),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    ihe,not(ils),crc,not(hps),lps,not(m3fti),not(l3fti),not(cdt),not(fin)]).
case(model_num(2),case_num(206),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    ihe,not(ils),crc,not(hps),not(lps),m3fti,not(l3fti),not(cdt),fin]).
case(model_num(2),case_num(207),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,hps,not(lps),not(m3fti),not(l3fti),not(cdt),not(fin)]).
case(model_num(2),case_num(208),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),lps,not(m3fti),not(l3fti),not(cdt),not(fin)]).
case(model_num(2),case_num(209),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),not(lps),not(m3fti),not(l3fti),not(cdt),fin]).
case(model_num(2),case_num(210),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),not(lps),not(m3fti),l3fti,not(cdt),fin,cpb,pbt]).
case(model_num(2),case_num(211),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),not(lps),not(m3fti),not(l3fti),cdt,fin,cpb,pbt]).
case(model_num(2),case_num(212),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),not(lps),not(m3fti),l3fti,not(cdt),fin,not(cpb),
    not(pbt)]).
case(model_num(2),case_num(213),[pac,ite,pco,not(epr),not(avp),not(psa),ifg,fpp,
    not(ihe),ils,crc,not(hps),not(lps),not(m3fti),not(l3fti),cdt,fin,not(cpb),
    not(pbt)]).
...

case_order(model_num(2),[case_num(201),[case_num(202),case_num(203), ...],[
    case_num(204),case_num(205),case_num(207),case_num(208), ... ,case_num(206)
    ,case_num(209),case_num(210),case_num(211),case_num(212),case_num(213),
    ...]]).
```

The following query shows that it is a valid model. Also, the arguments and attacks shown above can be verified by this program.

```
?- case_model_valid(model_num(2)).
true.

?- successful_attack(argument([pac,ite,pco],[ifg]),[pec]).
true.

?- rebutting_attack(argument([pac,ite,pco],[ifg]),[pec]).
true.

?- undercutting_attack(argument([pac,ite,pco],[ifg]),[pec]).
false.

?- successful_attack(argument([crc,ils],[l3fti,fin]),[hps]).
true.

?- successful_attack(argument([crc,ils],[cdt,fin]),[hps]).
true.

?-successful_attack(argument([crc,ihe],[m3fti,fin]),[lps]).
true.
```

```
?− conclusive(argument([epr],[ifg])).
true.

?− conclusive(argument([pac,avp],[ifg])).
true.

?− conclusive(argument([ifg,fpp],[crc])).
true.

?− conclusive(argument([crc,l3fti,fin,cpb],[pbt])).
true.
```

As the queries shows, the program has verified that circumstance *pec* successfully attacks argument $pac \wedge ite \wedge pco \rightsquigarrow ifg$, and it is a rebutting attack, as well as the other arguments with defeating circumstances above which are also considered to be successful. The program also finds argument $epr \Rightarrow ifg$ and other three arguments to be conclusive. These results are corresponded to the analysis about Chinese copyright infringement model above.

5. Discussion and Conclusion

In this paper, two case models with different backgrounds based on Verheij's case model formalism have been discussed. As the arguments implied in these case models are corresponded to the rules in statutes, Verheij's theory has been proved that it is suitable for Chinese legal system. The preferred relation established by Verheij solves the priority relationship among the cases in case model, so that the presumptive arguments in legal reasoning can be concluded by this theory. In other words, some legal issues can be solved, such as the rules used for legal reasoning, which are beyond the statutes, for instance, "presumption of innocence" in the background of Chinese legal system. Although it is not in any statute, every judge will think about it during the process of making decisions. So we can place this rule as several cases in the preferred relation of a case model properly to solve this issue. Therefore, we believe arguments embedded values are more suitable for dealing with practical issues in legal reasoning.

The program we build in this paper intends to make the modeling process with less mistakes and its main function is automatically verifying the validity of the arguments implicated in a case model and the case model itself. This program has been proved that it is completely suitable for those models based on Verheij's theory, even these models have different backgrounds. Compare with the original hand-made modeling way, it can reduce mistakes during the process of modeling significantly, as this program can verify the model automatically. So, it is a successful attempt as a computational implementation for Verheij's case model formalism which can make Verheij's theory more useable in practical environment.

However, there is still room for improvement. For those people who are unfamiliar with legal statues, an explicit case model can be helpful for them, which means the model needs to contain as much details as possible, such as the official judicial explanations related to Chinese criminal law. But this action can bring a

problem cannot be ignored. For instance, there are 8 scenarios about the elementary proposition "amount of illegal gains is huge or other especially serious circumstances" mentioned in the Chinese copyright infringement model in the light of relevant judicial explanations, if all of these specific scenarios are added into the model, the number of cases in this model will become huge. According to the way of building a model completely based on Verheij's formalism, all these scenarios will be treated as elementary propositions and they will replace the position of *ihe*. The number of cases will increase by eight times, if we added these specific scenarios to the model by Verheij's theory directly, which also lets the process of modeling easily to make mistakes. It will be a hard job for the people who wants to build a model. This issue needed to be solved in the future research.

The results of this paper shows that Verheij's case model formalism can be used to model the object with complex argument structure, and the program developed in this paper is feasible for the models based on Verheij's theory. It also proves that the Prolog program we built can well combine cases, rules and arguments. It is not only applicable to the civil law system but also to the Chinese legal system. AI and legal reasoning technology needs to combine rule-based reasoning, case-based reasoning and argumentation together, and argumentation technology can be the bridge of both cases and rules.

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