

27.10.2020

Digital Image Processing (CSE/ECE 478)

Lecture-21: Image Compression (contd.)

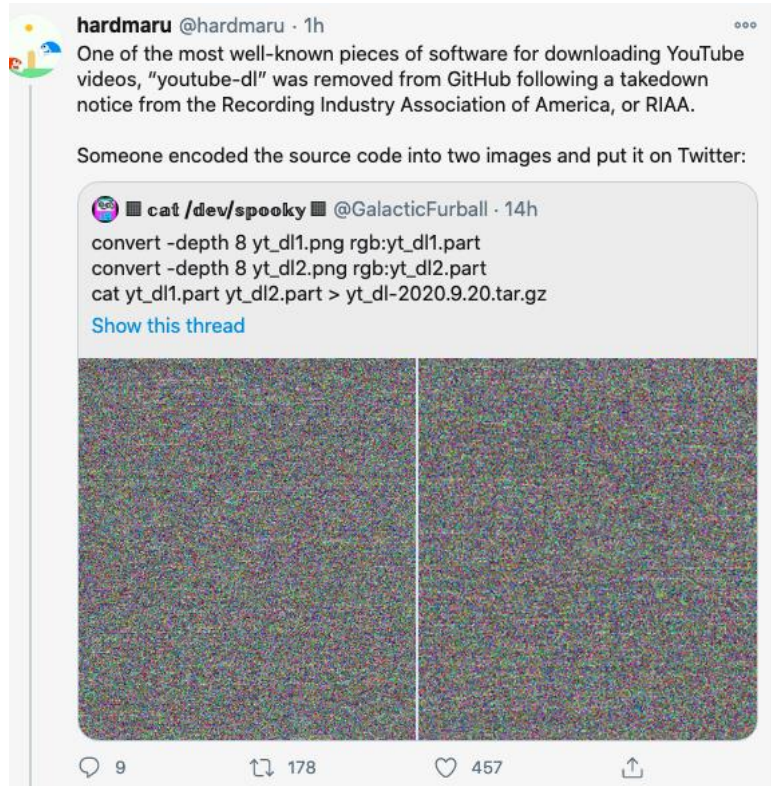
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Some slides borrowed from Vineet Gandhi @CVIT!

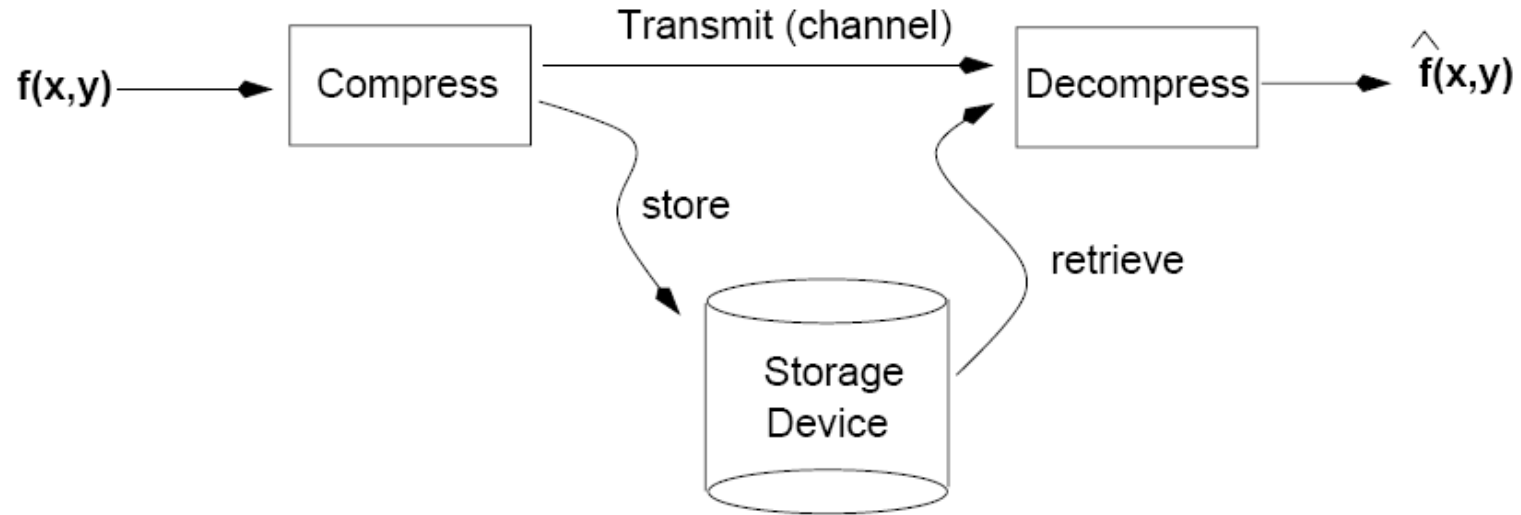
Encoding data as images



AACSLA DVD Decryption Code

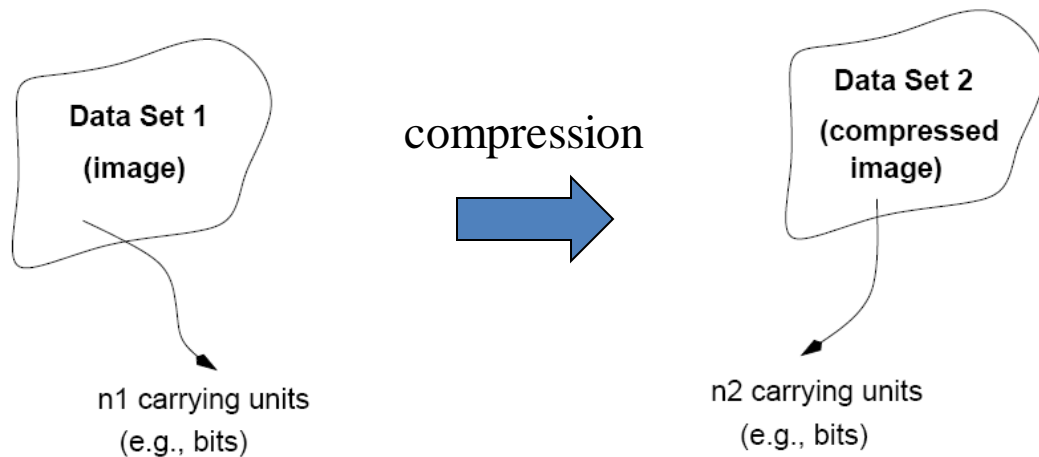
Image Compression

- Goal: Reduce amount of data required to represent a digital image



.. By exploiting redundancies in image data

Compression Ratio



Compression ratio: $C_R = \frac{n_1}{n_2}$

Types of Redundancy

(1) Coding Redundancy

(2) Spatial/Temporal Redundancy

(3) Psychovisual Redundancy

- Image compression attempts to reduce one or more of these redundancy types.

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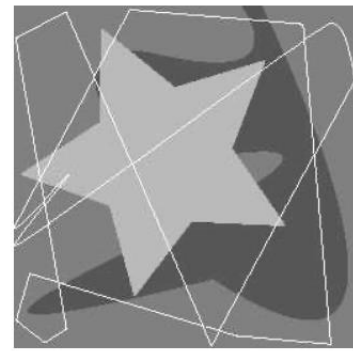
Coding - Definitions

- **Code:** a list of symbols (letters, numbers, bits etc.)
- **Code word:** a sequence of symbols used to represent some information (e.g., gray levels).
- **Code word length:** number of symbols in a code word.

Example: (binary code, symbols: 0,1, length: 3)

| | |
|--------|--------|
| 0: 000 | 4: 100 |
| 1: 001 | 5: 101 |
| 2: 010 | 6: 110 |
| 3: 011 | 7: 111 |

Coding Redundancy



- Case 1: $l(r_k) = \text{constant length}$

Example:

| r_k | $p_r(r_k)$ | Code 1 | $l_1(r_k)$ |
|-------------|------------|--------|------------|
| $r_0 = 0$ | 0.19 | 000 | 3 |
| $r_1 = 1/7$ | 0.25 | 001 | 3 |
| $r_2 = 2/7$ | 0.21 | 010 | 3 |
| $r_3 = 3/7$ | 0.16 | 011 | 3 |
| $r_4 = 4/7$ | 0.08 | 100 | 3 |
| $r_5 = 5/7$ | 0.06 | 101 | 3 |
| $r_6 = 6/7$ | 0.03 | 110 | 3 |
| $r_7 = 1$ | 0.02 | 111 | 3 |

$$\text{Average \# of bits: } L_{avg} = E(l(r_k)) = \sum_{k=0}^{L-1} l(r_k)P(r_k)$$

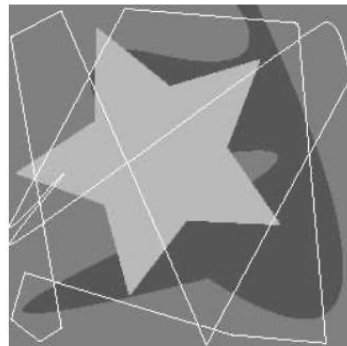
$$\text{Total \# of bits: } NML_{avg}$$

Assume an image with $L = 8$

$$\text{Assume } l(r_k) = 3, \quad L_{avg} = \sum_{k=0}^7 3P(r_k) = 3 \sum_{k=0}^7 P(r_k) = 3 \text{ bits}$$

Total number of bits: $3NM$

Coding Redundancy (cont'd)



- Case 2: $l(r_k) = \text{variable length}$

Table 6.1 Variable-Length Coding Example variable length

| r_k | $p_r(r_k)$ | Code 1 | $l_1(r_k)$ | Code 2 | $l_2(r_k)$ |
|-------------|------------|--------|------------|--------|------------|
| $r_0 = 0$ | 0.19 | 000 | 3 | 11 | 2 |
| $r_1 = 1/7$ | 0.25 | 001 | 3 | 01 | 2 |
| $r_2 = 2/7$ | 0.21 | 010 | 3 | 10 | 2 |
| $r_3 = 3/7$ | 0.16 | 011 | 3 | 001 | 3 |
| $r_4 = 4/7$ | 0.08 | 100 | 3 | 0001 | 4 |
| $r_5 = 5/7$ | 0.06 | 101 | 3 | 00001 | 5 |
| $r_6 = 6/7$ | 0.03 | 110 | 3 | 000001 | 6 |
| $r_7 = 1$ | 0.02 | 111 | 3 | 000000 | 6 |

$$C_R = \frac{n_1}{n_2}$$

$$L_{avg} = \sum_{k=0}^7 l(r_k)P(r_k) = 2.7 \text{ bits}$$

Total number of bits: $2.7NM$

$$C_R = \frac{3}{2.7} = 1.11 \text{ (about 10\%)}$$

$$R_D = 1 - \frac{1}{1.11} = 0.099$$

Types of Redundancy

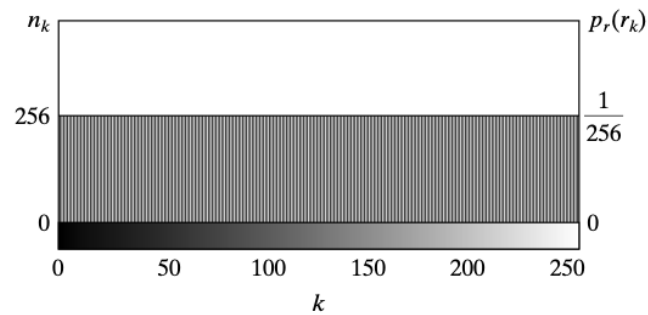
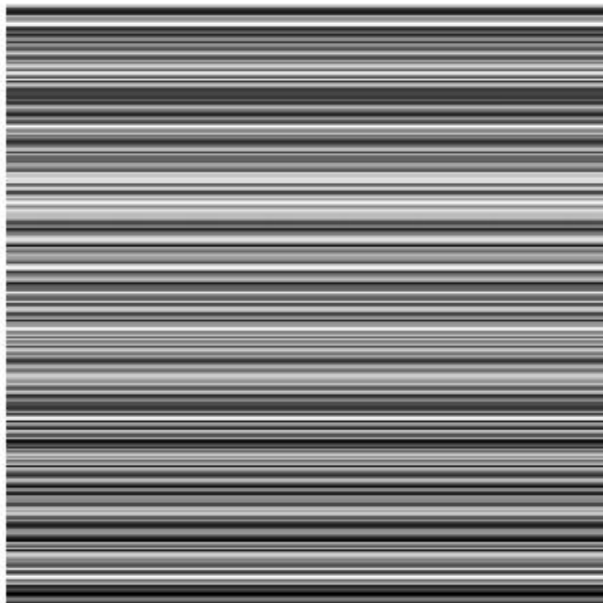
(1) Coding Redundancy

(2) Spatial/Temporal Redundancy

(3) Psychovisual Redundancy

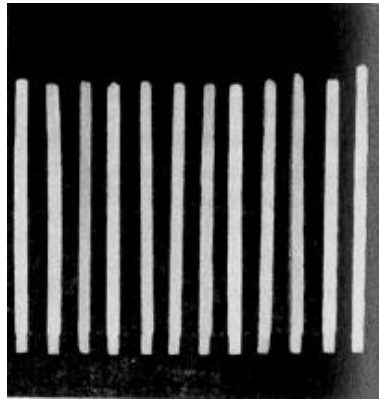
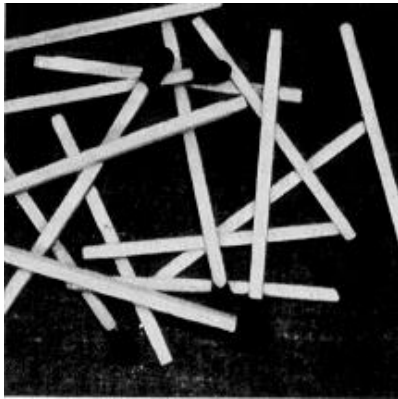
- Image compression attempts to reduce one or more of these redundancy types.

Spatial Redundancy



Spatial redundancy

- Interpixel redundancy exists → pixel values are correlated
- i.e., a pixel value can be reasonably predicted by its neighbors



$$f(x) \circ g(x) = \int_{-\infty}^{\infty} f(x)g(x+a)da$$

auto-correlation: $f(x)=g(x)$

histograms
auto-correlation

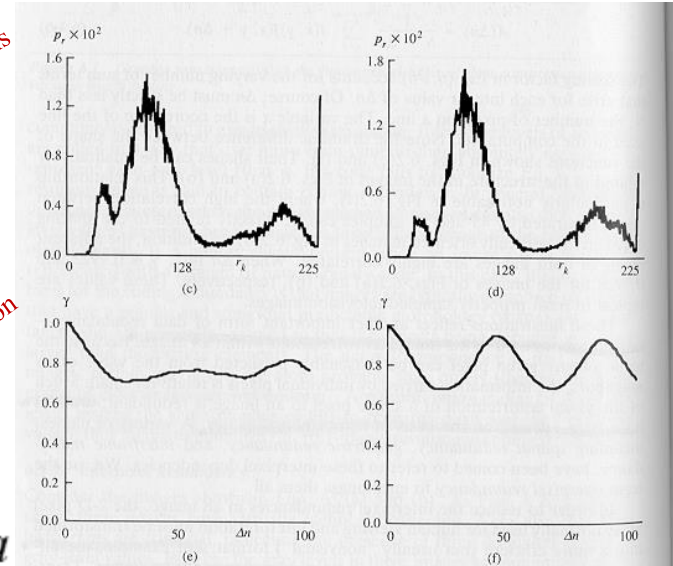


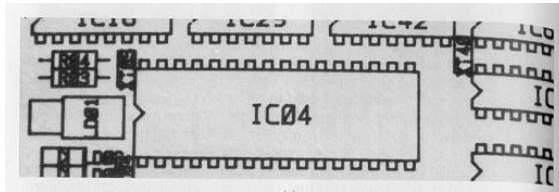
Figure 6.2 Two images and their gray-level histograms and normalized autocorrelation

Interpixel redundancy (cont'd)

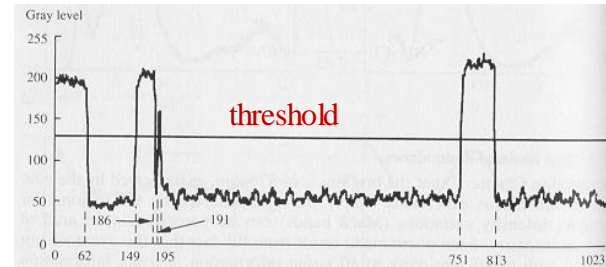
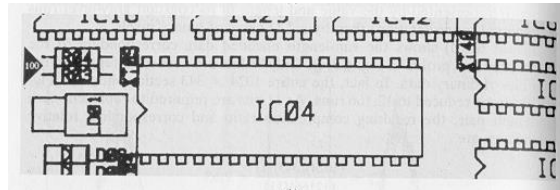
- To reduce interpixel redundancy, some kind of transformation must be applied on the data (e.g., thresholding, DFT, DWT)

Example:

original



thresholded



110000.....11.....000.....

Run-length encoding:

(1,63) (0,87) (1,37) (0,5) (1,4) (0, 556) (1,62) (0,210)

Using 11 bits/pair:

(1+10) bits/pair

88 bits are required (compared to 1024 !!)

Spatial and temporal redundancy



Types of Redundancy

(1) Coding Redundancy

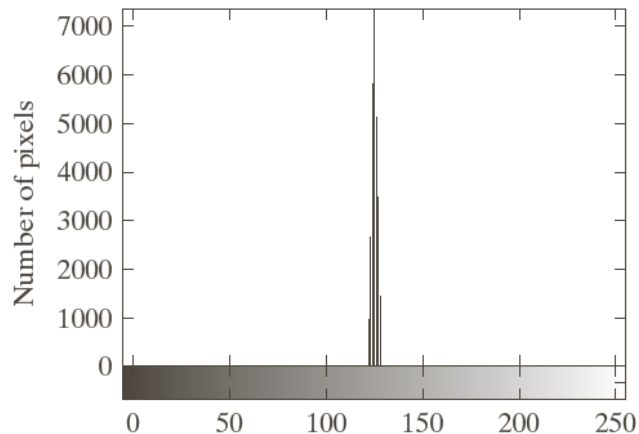
(2) Spatial/Temporal Redundancy

(3) Psychovisual Redundancy

- Image compression attempts to reduce one or more of these redundancy types.

Irrelevant information or perceptual redundancy

- Not all visual information is perceived by eye/brain, so throw away those that are not



Psychovisual redundancy (cont'd)

Example: quantization

256 gray levels



16 gray levels



16 gray levels + random noise

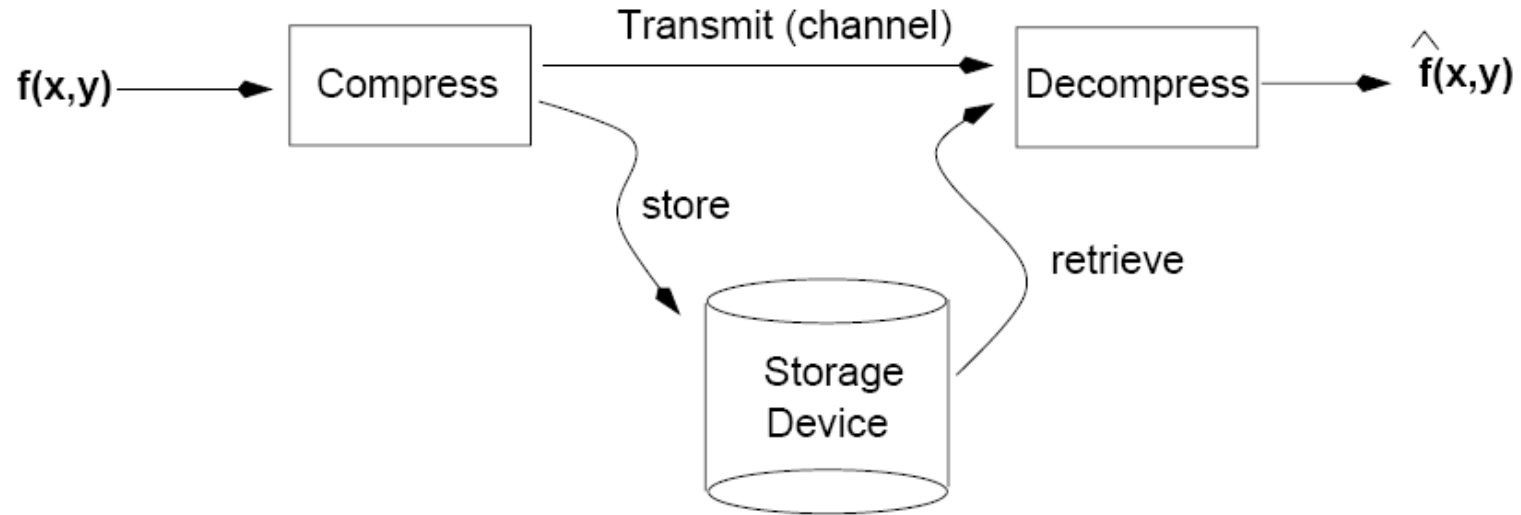


$$C=8/4 = 2:1$$

add a small pseudo-random number
to each pixel prior to quantization

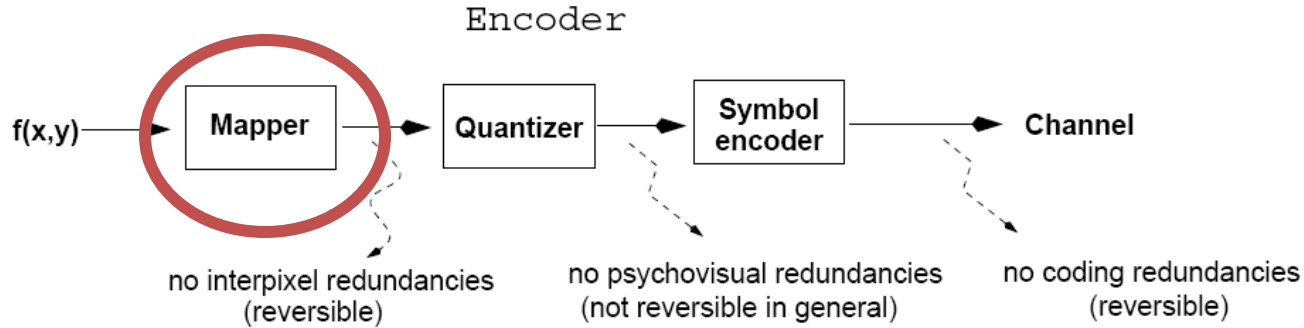
Image Compression

- Goal: Reduce amount of data required to represent a digital image (c.f. signal).



.. By exploiting redundancies in image data

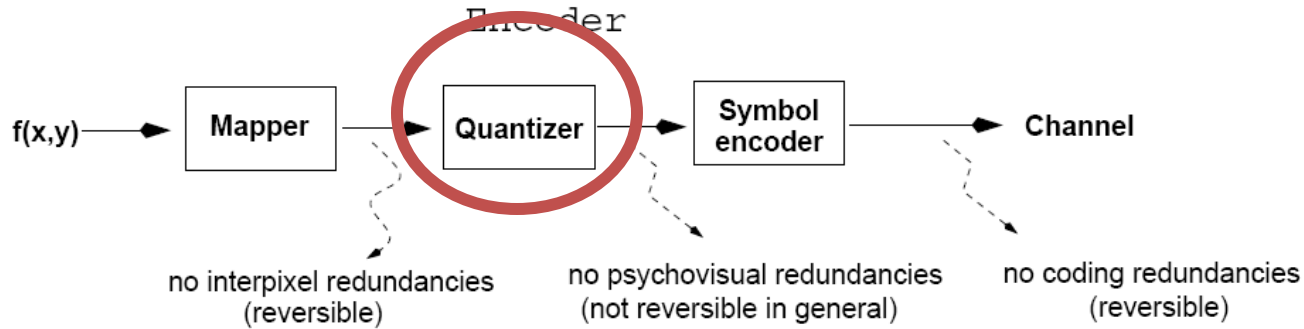
Image Compression Model



-

- **Mapper:** transforms data to account for interpixel redundancies.

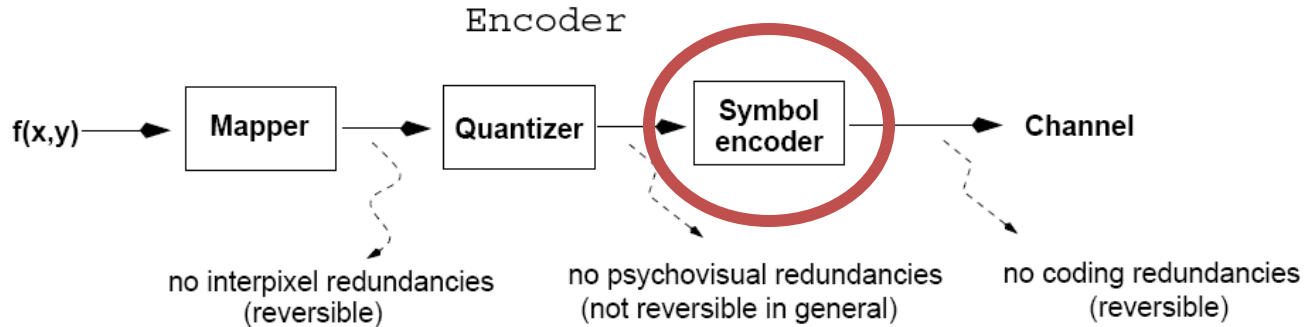
Image Compression Model (cont'd)



-

- **Quantizer:** quantizes the data to account for psychovisual redundancies.

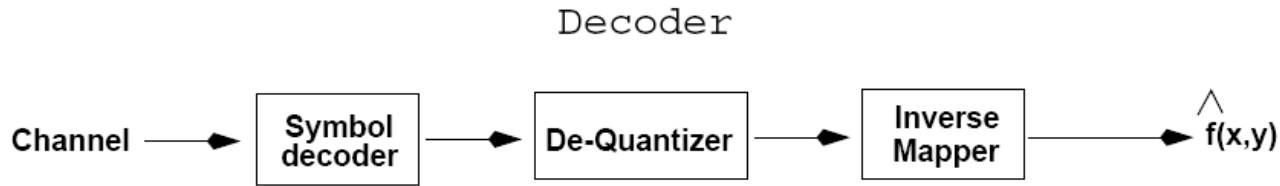
Image Compression Model (cont'd)



-

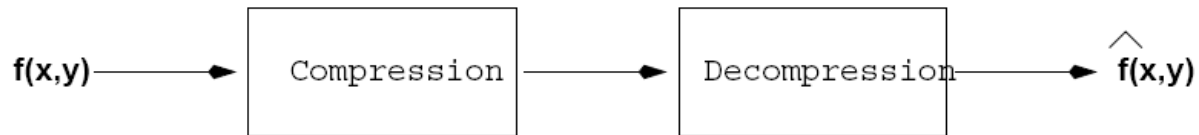
- **Symbol encoder:** encodes the data to account for coding redundancies.

Image Compression Models (cont'd)



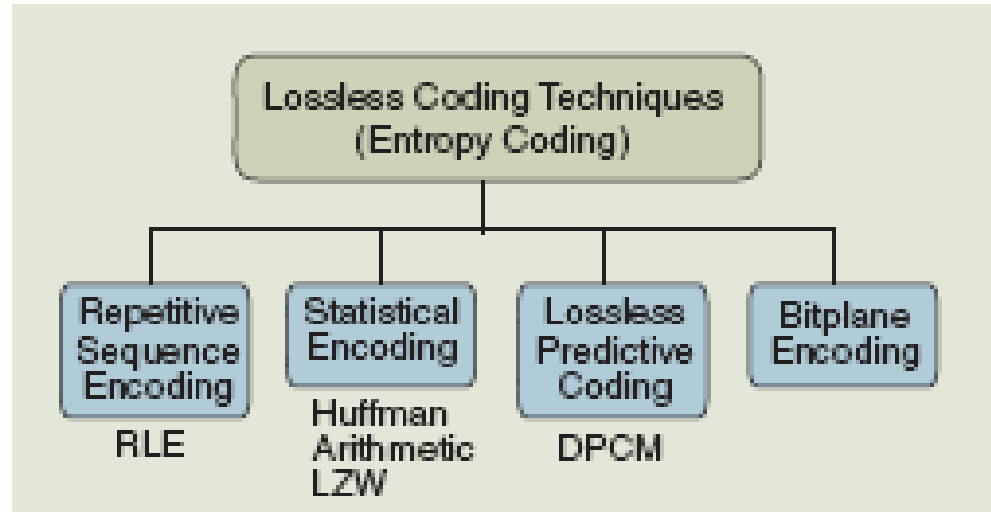
- The decoder applies the inverse steps.
- Note that quantization is **irreversible** in general.

Lossless Compression



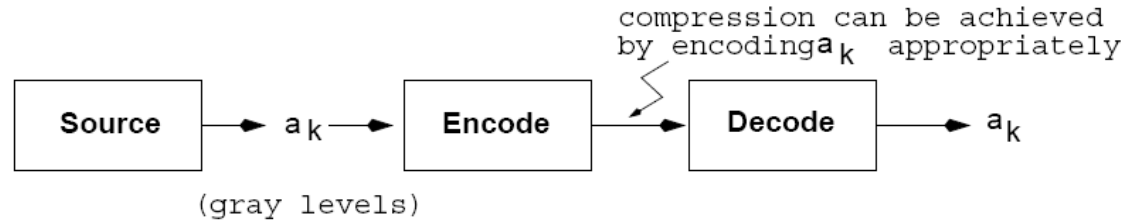
$$e(x, y) = \hat{f}(x, y) - f(x, y) = 0$$

Taxonomy of Lossless Methods



Huffman Coding

(addresses coding redundancy)



- A **variable-length coding** technique.
- Source symbols are encoded **one** at a time!
 - There is a **one-to-one correspondence** between source symbols and code words.
- **Optimal code** - minimizes code word length per source symbol.

Huffman Coding (cont'd)

- Forward Pass

1. Sort probabilities per symbol
2. Combine the lowest two probabilities
3. Repeat *Step2* until only two probabilities remain.

| Original source | | Source reduction | | | |
|-----------------|-------------|------------------|-----|-----|-----|
| Symbol | Probability | 1 | 2 | 3 | 4 |
| a_2 | 0.4 | 0.4 | 0.4 | 0.4 | 0.6 |
| a_6 | 0.3 | 0.3 | 0.3 | 0.3 | |
| a_1 | 0.1 | 0.1 | 0.2 | 0.3 | 0.4 |
| a_4 | 0.1 | 0.1 | | | |
| a_3 | 0.06 | 0.1 | 0.1 | 0.3 | 0.4 |
| a_5 | 0.04 | | 0.1 | | |

0 1 0 1 0 0 1 1 1 1 0 0

a_3 a_1 a_2 a_2 a_6

- Backward Pass

Assign code symbols going backwards

| Original source | | | Source reduction | | | |
|-----------------|-------|-------|------------------|---------|---------|---------|
| Sym. | Prob. | Code | 1 | 2 | 3 | 4 |
| a_2 | 0.4 | 1 | 0.4 1 | 0.4 1 | 0.4 1 | 0.6 0 |
| a_6 | 0.3 | 00 | 0.3 00 | 0.3 00 | 0.3 00 | |
| a_1 | 0.1 | 011 | 0.1 011 | 0.2 010 | 0.3 01 | 0.4 1 |
| a_4 | 0.1 | 0100 | 0.1 0100 | | | |
| a_3 | 0.06 | 01010 | 0.1 0101 | 0.1 011 | 0.1 011 | 0.1 011 |
| a_5 | 0.04 | 01011 | | | | |

Huffman Coding (cont'd)

- L_{avg} assuming Huffman coding:

$$L_{avg} = E(l(a_k)) = \sum_{k=1}^6 l(a_k)P(a_k) =$$

$$3 \times 0.1 + 1 \times 0.4 + 5 \times 0.06 + 4 \times 0.1 + 5 \times 0.04 + 2 \times 0.3 = 2.2 \text{ bits/symbol}$$

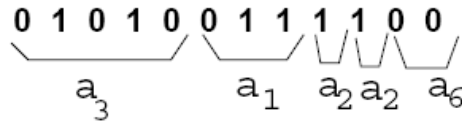
6 symbols, we need a 3-bit code

- $(a_1: 000, a_2: 001, a_3: 010, a_4: 011, a_5: 100, a_6: 101)$

$$L_{avg} = \sum_{k=1}^6 l(a_k)P(a_k) = \sum_{k=1}^6 3P(a_k) = 3 \sum_{k=1}^6 P(a_k) = 3 \text{ bits/symbol}$$

Huffman Coding/Decoding

- Coding/Decoding can be implemented using a **look-up table**.
- Decoding can be done unambiguously.



| Original source | | | Source reduction | | | |
|-----------------|-------|-------|------------------|---------|--------|-------|
| Sym. | Prob. | Code | 1 | 2 | 3 | 4 |
| a_2 | 0.4 | 1 | 0.4 1 | 0.4 1 | 0.4 1 | 0.6 0 |
| a_6 | 0.3 | 00 | 0.3 00 | 0.3 00 | 0.3 00 | 0.4 1 |
| a_1 | 0.1 | 011 | 0.1 011 | 0.2 010 | 0.3 01 | |
| a_4 | 0.1 | 0100 | 0.1 0100 | 0.1 011 | | |
| a_3 | 0.06 | 01010 | 0.1 0101 | | | |
| a_5 | 0.04 | 01011 | | | | |

| Original source | | |
|-----------------|-------|-------|
| Sym. | Prob. | Code |
| a_2 | 0.4 | 1 |
| a_6 | 0.3 | 00 |
| a_1 | 0.1 | 011 |
| a_4 | 0.1 | 0100 |
| a_3 | 0.06 | 01010 |
| a_5 | 0.04 | 01011 |

Arithmetic (or Range) Coding (addresses coding redundancy)

- The main weakness of Huffman coding is that it encodes source symbols **one** at a time.
- Arithmetic coding encodes **sequences** of source symbols together.
 - There is **no** one-to-one correspondence between source symbols and code words.
- Slower than Huffman coding but can achieve better compression.

Arithmetic Coding (cont'd)

- A sequence of source symbols is assigned to a sub-interval in $[0,1)$ which can be represented by an arithmetic code, e.g.:



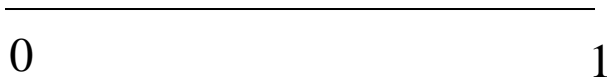
- Start with the interval $[0, 1)$; a sub-interval is chosen to represent the message which becomes smaller and smaller as the number of symbols in the message increases.

Arithmetic Coding (cont'd)

Encode message: $\alpha_1 \alpha_2 \alpha_3 \alpha_3 \alpha_4$

| Source Symbol | Probability |
|---------------|-------------|
| a_1 | 0.2 |
| a_2 | 0.2 |
| a_3 | 0.4 |
| a_4 | 0.2 |

1) Start with interval $[0, 1)$



2) Subdivide $[0, 1)$ based on the probabilities of α_i

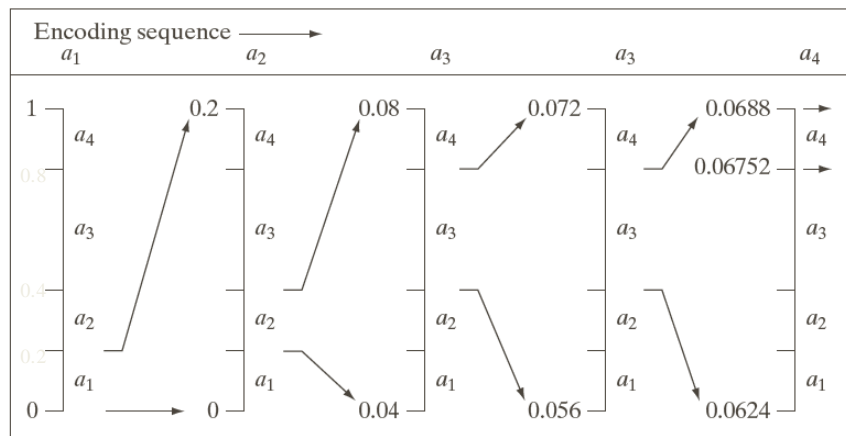


| Initial Subinterval |
|---------------------|
| $[0.0, 0.2)$ |
| $[0.2, 0.4)$ |
| $[0.4, 0.8)$ |
| $[0.8, 1.0)$ |

3) Update interval by processing source symbols

Example

| Source Symbol | Probability | Initial Subinterval |
|---------------|-------------|---------------------|
| a_1 | 0.2 | $[0.0, 0.2)$ |
| a_2 | 0.2 | $[0.2, 0.4)$ |
| a_3 | 0.4 | $[0.4, 0.8)$ |
| a_4 | 0.2 | $[0.8, 1.0)$ |



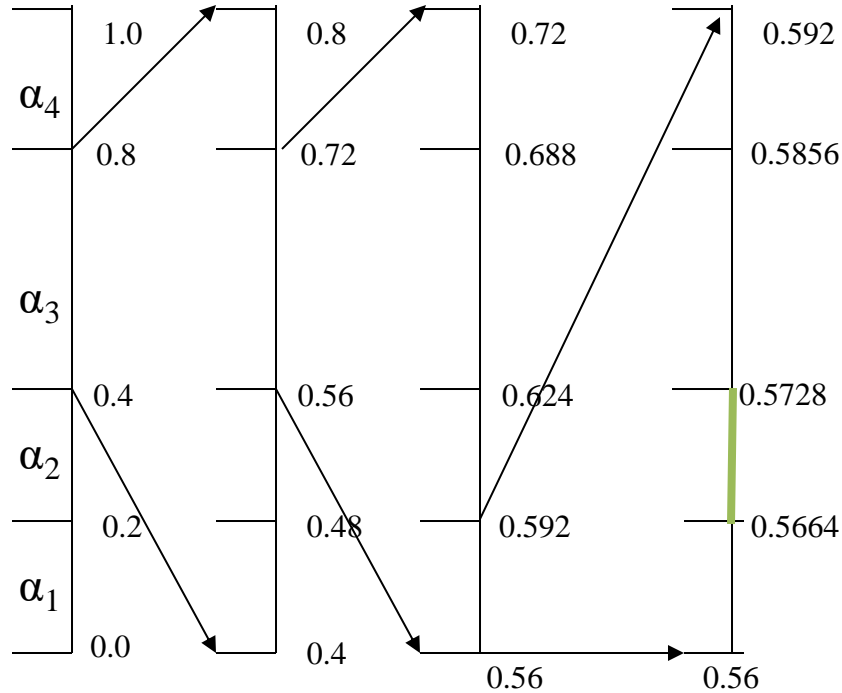
Encode

$\alpha_1 \alpha_2 \alpha_3 \alpha_3 \alpha_4$

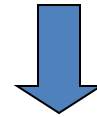


$[0.06752, 0.0688)$

Arithmetic Decoding



Decode 0.572
(code length=4)



$\alpha_3 \alpha_3 \alpha_1 \alpha_2$

LZW Coding

(addresses interpixel redundancy)

- Requires no prior knowledge of symbol probabilities.
- Assigns **fixed length** code words to **variable length** symbol sequences.
 - There is **no** one-to-one correspondence between source symbols and code words.
- Included in GIF, TIFF and PDF file formats

LZW Coding

- A **codebook** (or **dictionary**) needs to be constructed.
- Initially, the first 256 entries of the dictionary are assigned to the gray levels 0,1,2,...,255 (i.e., assuming 8 bits/pixel)

Consider a 4x4, 8 bit image

| | | | |
|----|----|-----|-----|
| 39 | 39 | 126 | 126 |
| 39 | 39 | 126 | 126 |
| 39 | 39 | 126 | 126 |
| 39 | 39 | 126 | 126 |

Initial Dictionary

| Dictionary Location | Entry |
|---------------------|-------|
| 0 | 0 |
| 1 | 1 |
| ... | ... |
| 255 | 255 |
| 256 | - |
| ... | ... |
| 511 | - |

LZW Coding (cont'd)

As the encoder examines image pixels, gray level sequences (i.e., blocks) that are not in the dictionary are assigned to a new entry.

39 39 126 126
39 39 126 126
39 39 126 126
39 39 126 126

| Dictionary Location | Entry |
|---------------------|-------|
| 0 | 0 |
| 1 | 1 |
| . | . |
| 255 | 255 |
| 256 | 39-39 |
| 511 | - |

- Is 39 in the dictionary.....Yes
- What about 39-39.....No
- * Add 39-39 at location 256



Example

39 39 126 126
 39 39 126 126
 39 39 126 126
 39 39 126 126

CR = empty

repeat

P=next pixel

CS=CR + P

If CS is found:

(1) No Output

(2) CR=CS

else:

(1) Output D(CR)

(2) Add CS to D

(3) CR=P

Concatenated Sequence: $CS = CR + P$

(CR) (P)

| Currently Recognized Sequence | Pixel Being Processed | Encoded Output | Dictionary Location (Code Word) | Dictionary Entry |
|-------------------------------|-----------------------|----------------|---------------------------------|------------------|
| | 39 | | | |
| 39 | 39 | 39 | 256 | 39-39 |
| 39 | 126 | 39 | 257 | 39-126 |
| 126 | 126 | 126 | 258 | 126-126 |
| 126 | 39 | 126 | 259 | 126-39 |
| 39 | 39 | | | |
| 39-39 | 126 | 256 | 260 | 39-39-126 |
| 126 | 126 | | | |
| 126-126 | 39 | 258 | 261 | 126-126-39 |
| 39 | 39 | | | |
| 39-39 | 126 | | | |
| 39-39-126 | 126 | 260 | 262 | 39-39-126-126 |
| 126 | 39 | | | |
| 126-39 | 39 | 259 | 263 | 126-39-39 |
| 39 | 126 | | | |
| 39-126 | 126 | 257 | 264 | 39-126-126 |
| 126 | | 126 | | |

Decoding LZW

- Use the dictionary for decoding the “encoded output” sequence.
- The dictionary need not be sent with the encoded output.
- Can be built on the “fly” by the decoder as it reads the received code words.

Run-length coding (RLC) (addresses interpixel redundancy)

- Reduce the size of a repeating string of symbols (i.e., runs):

1 1 1 1 1 0 0 0 0 0 1 \rightarrow (1,5) (0, 6) (1, 1)

a a a b b b b b b c c \rightarrow (a,3) (b, 6) (c, 2)

- Encodes a run of symbols into two bytes: (symbol, count)
- Can compress any type of data but cannot achieve high compression ratios compared to other compression methods.

Combining Huffman Coding with Run-length Coding

- Assuming that a message has been encoded using Huffman coding, additional compression can be achieved using run-length coding.

0 1 0 1 0 0 1 1 1 1 0 0

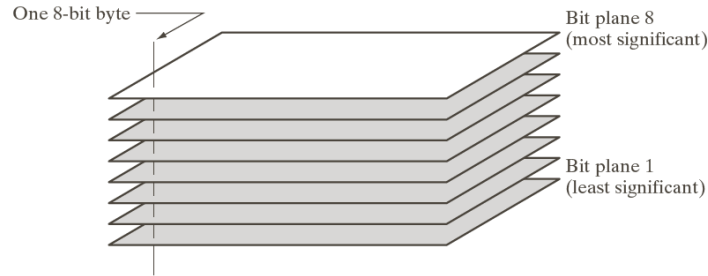
e.g., (0,1)(1,1)(0,1)(1,0)(0,2)(1,4)(0,2)

Bit-plane coding

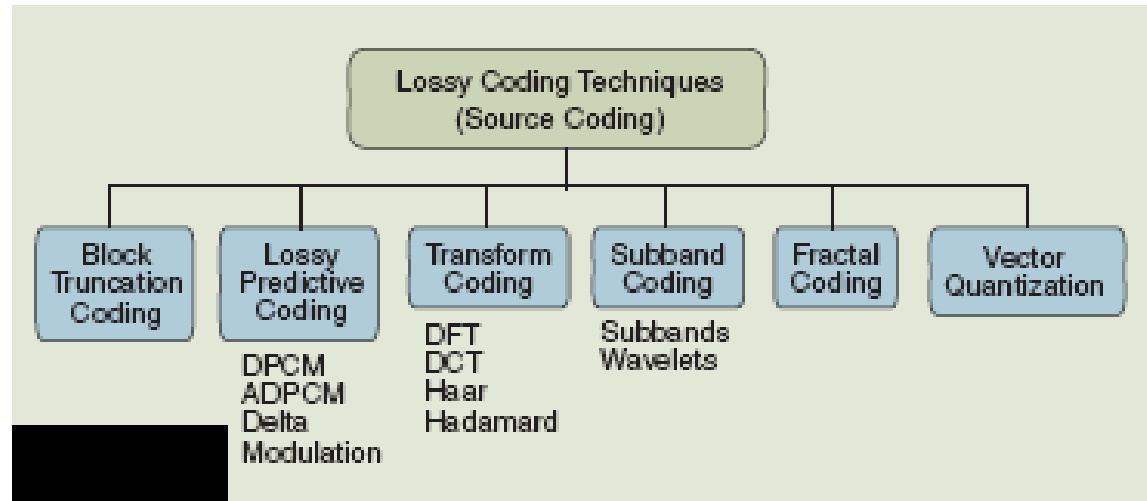
(addresses interpixel redundancy)

- Process each **bit plane** individually.

- (1) Decompose an image into a series of binary images.
- (2) Compress each binary image (e.g., using run-length coding)

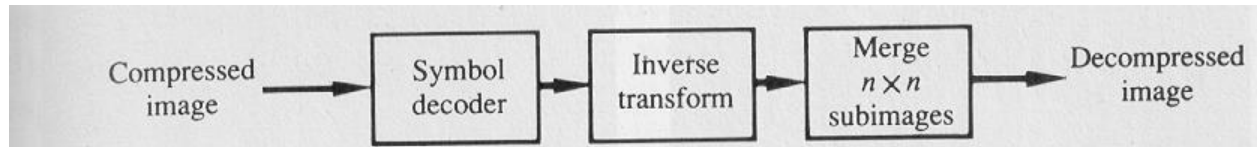
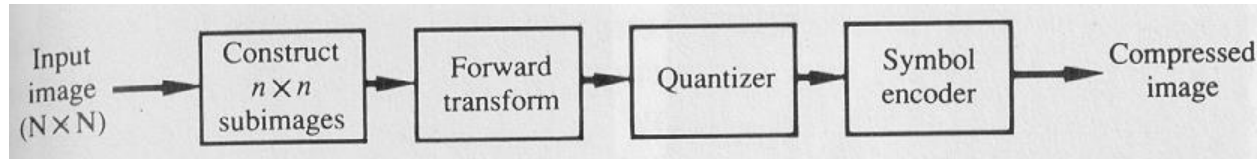


Lossy Methods - Taxonomy



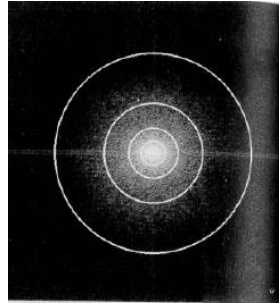
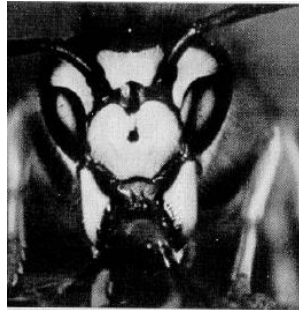
Lossy Compression

- Transform the image into some other domain to reduce interpixel redundancy.



Example: Fourier Transform

$$f(x, y) = \frac{1}{N} \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} F(u, v) e^{\frac{j2\pi(ux+vy)}{N}}, \quad x, y=0, 1, \dots, N-1$$



Note that the magnitude of the FT decreases, as u, v increase!

$$K \ll N$$

$$\hat{f}(x, y) = \frac{1}{N} \sum_{u=0}^{K-1} \sum_{v=0}^{K-1} F(u, v) e^{\frac{j2\pi(ux+vy)}{N}}, \quad x, y=0, 1, \dots, N-1$$

$\sum_{x,y} (\hat{f}(x, y) - f(x, y))^2$ is very small !!

Transform Selection

$$f(x, y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} T(u, v) h(x, y, u, v)$$

- $T(u, v)$ can be computed using various transformations, for example:
 - DFT
 - DCT (Discrete Cosine Transform)
 - KLT (Karhunen-Loeve Transformation) or Principal Component Analysis (PCA)
- JPEG using DCT for handling interpixel redundancy.

DCT (Discrete Cosine Transform)

[proposed by Nasir Ahmed, T. Natarajan, K.R.Rao (1972)]



All Real

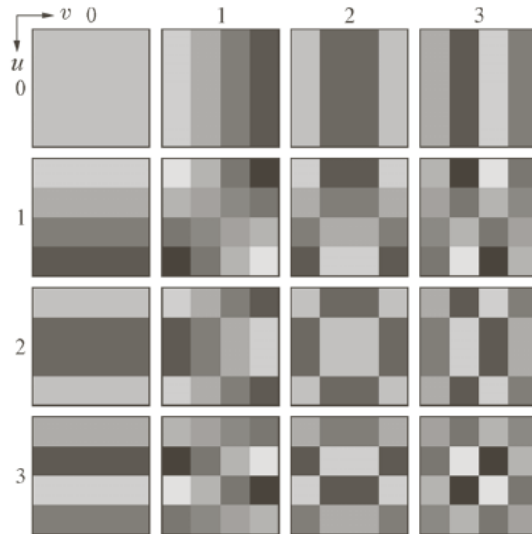
$$\text{Forward: } C(u, v) = \alpha(u)\alpha(v) \sum_{x=0}^{N-1} \sum_{y=0}^{N-1} f(x, y) \cos\left(\frac{(2x+1)u\pi}{2N}\right) \cos\left(\frac{(2y+1)v\pi}{2N}\right),$$
$$u, v=0, 1, \dots, N-1$$

$$\text{Inverse: } f(x, y) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} \alpha(u)\alpha(v) C(u, v) \cos\left(\frac{(2x+1)u\pi}{2N}\right) \cos\left(\frac{(2y+1)v\pi}{2N}\right),$$
$$x, y=0, 1, \dots, N-1$$

$$\alpha(u) = \begin{cases} \sqrt{1/N} & \text{if } u=0 \\ \sqrt{2/N} & \text{if } u>0 \end{cases} \quad \alpha(v) = \begin{cases} \sqrt{1/N} & \text{if } v=0 \\ \sqrt{2/N} & \text{if } v>0 \end{cases}$$

DCT (cont'd)

- Basis functions for a 4x4 image (i.e., cosines of different frequencies).



DCT (cont'd)

Using
8 x 8 sub-images
yields 64 coefficients
per sub-image.

Reconstructed images
by truncating
50% of the
coefficients

More compact
transformation

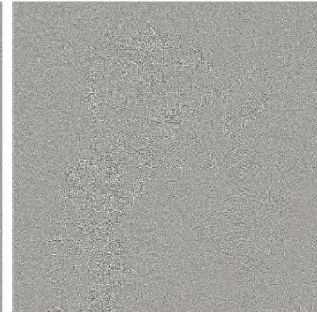
DFT



WHT



DCT



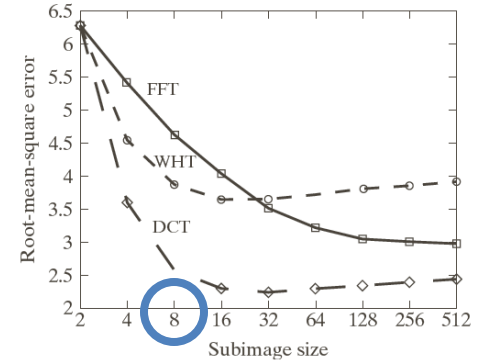
RMS error: 2.32

1.78

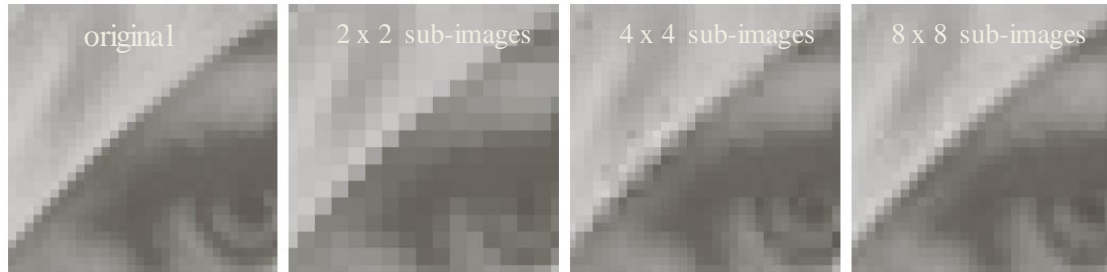
1.13

DCT (cont'd)

- Sub-image size selection:



Reconstructions

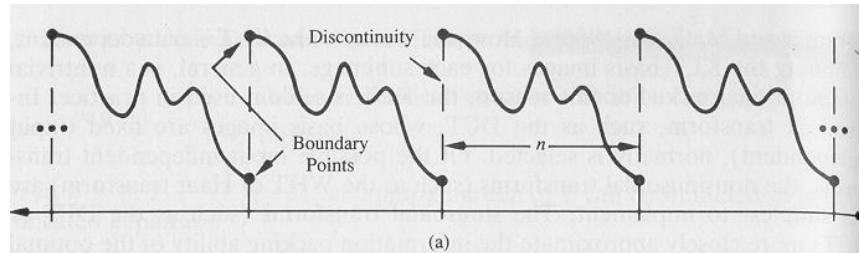


DCT (cont'd)

- DCT minimizes "blocking artifacts" (i.e., boundaries between subimages do not become very visible).

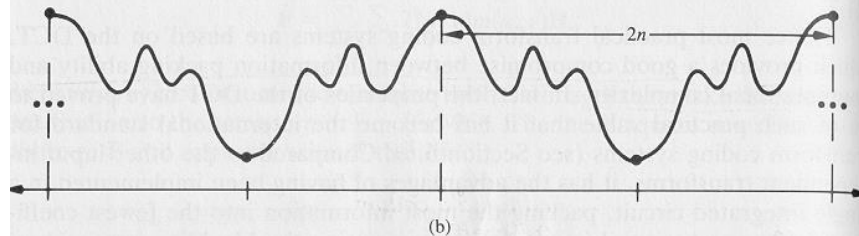
DFT

has n -point periodicity



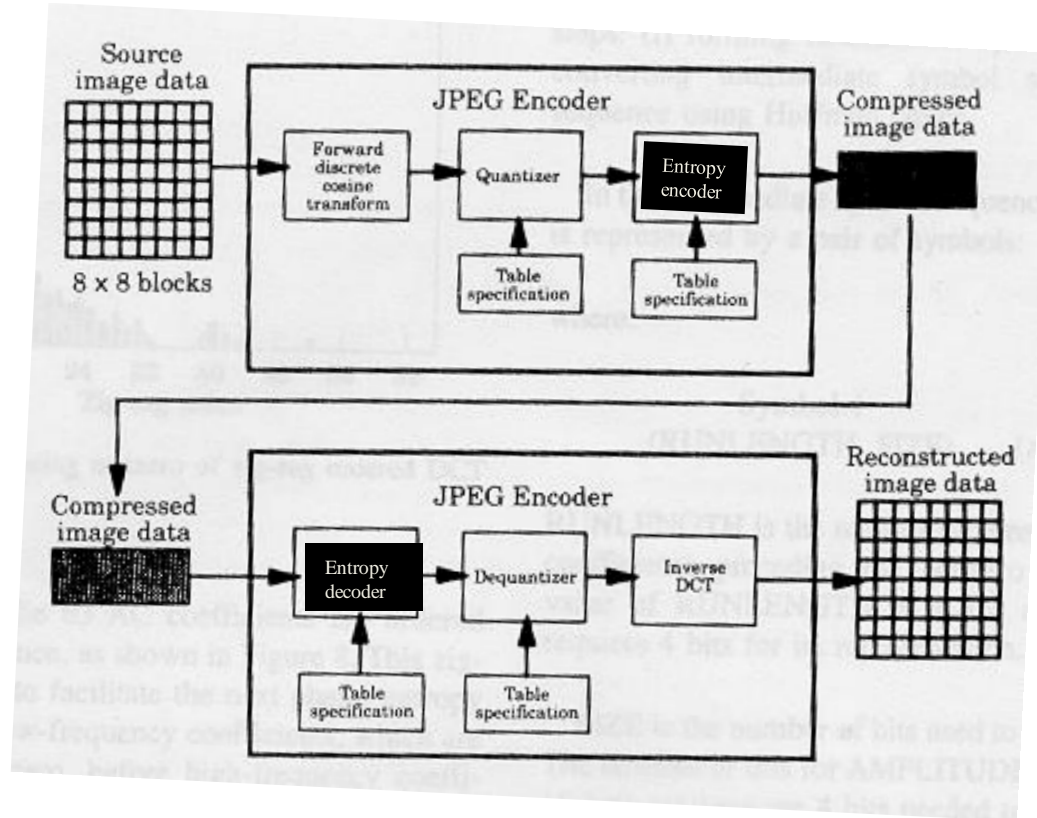
DCT

has $2n$ -point periodicity



JPEG Compression

Accepted as an international image compression standard in 1992.



JPEG - Steps

1. Divide image into 8x8 subimages.

For each subimage do:

2. Shift the gray-levels in the range $[-128, 127]$

3. Apply DCT \rightarrow 64 coefficients

1 **DC coefficient**: $F(0,0)$

63 **AC coefficients**: $F(u,v)$

Example

| (a) Original 8 x 8 block | (b) Shifted block | (c) Block after FDCT Eqn. (5) |
|---|---|---|
| 140 144 147 1140 140 155 179 175 144 152 140 147 140 148 167 179 152 155 136 167 163 162 152 172 168 145 156 160 152 155 136 160 162 148 156 148 140 136 147 162 147 167 140 155 155 140 136 162 136 156 123 167 162 144 140 147 148 155 136 155 152 147 147 136 | 12 16 19 12 11 27 51 47 16 24 12 19 12 20 39 51 24 27 8 39 35 34 24 44 40 17 28 32 24 27 8 32 34 20 28 20 12 8 19 34 19 39 12 27 27 12 8 34 8 28 -5 39 34 16 12 19 20 27 8 27 24 19 19 8 | 185 -17 14 -8 23 -9 -13 -18 20 -34 26 -9 -10 10 13 6 -10 -23 -1 6 -18 3 -20 0 -8 -5 14 -14 -8 -2 -3 8 -3 9 7 1 -11 17 18 15 3 -2 -18 8 8 -3 0 -6 8 0 -2 3 -1 -7 -1 -1 0 -7 -2 1 1 4 -6 0 |

$[-128, 127]$

(non-centered
spectrum)

JPEG Steps

4. Quantize the coefficients (i.e., reduce the amplitude of coefficients that do not contribute a lot).

$$C_q(u, v) = \text{Round}\left[\frac{C(u, v)}{Q(u, v)}\right]$$



$Q(u, v)$: quantization table

Example

- Quantization Table $Q[i][j]$

```
for i=0 to n;  
  for j=0 to n;  
     $Q[i,j] = 1 + (1+i+j)*quality$ ;  
  end j;  
end i;
```

$$1 \leq quality \leq 25$$

(best - low compression)

(worst - high compression)

(d) Quantization table
(quality = 2)

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 3 | 5 | 7 | 9 | 11 | 13 | 15 | 17 |
| 5 | 7 | 9 | 11 | 13 | 15 | 17 | 19 |
| 7 | 9 | 11 | 13 | 15 | 17 | 19 | 21 |
| 9 | 11 | 13 | 15 | 17 | 19 | 21 | 23 |
| 11 | 13 | 15 | 17 | 19 | 21 | 23 | 25 |
| 13 | 15 | 17 | 19 | 21 | 23 | 25 | 27 |
| 15 | 17 | 19 | 21 | 23 | 25 | 27 | 29 |
| 17 | 19 | 21 | 23 | 25 | 27 | 29 | 31 |

Example (cont'd)

(c) Block after FDCT
Eqn. (5)

| | | | | | | | |
|-----|-----|-----|-----|-----|----|-----|-----|
| 185 | -17 | 14 | -8 | 23 | -9 | -13 | -18 |
| 20 | -34 | 26 | -9 | -10 | 10 | 13 | 6 |
| -10 | -23 | -1 | 6 | -18 | 3 | -20 | 0 |
| -8 | -5 | 14 | -14 | -8 | -2 | -3 | 8 |
| -3 | 9 | 7 | 1 | -11 | 17 | 18 | 15 |
| 3 | -2 | -18 | 8 | 8 | -3 | 0 | -6 |
| 8 | 0 | -2 | 3 | -1 | -7 | -1 | -1 |
| 0 | -7 | -2 | 1 | 1 | 4 | -6 | 0 |

(d) Quantization table
(quality = 2)

| | | | | | | | |
|----|----|----|----|----|----|----|----|
| 3 | 5 | 7 | 9 | 11 | 13 | 15 | 17 |
| 5 | 7 | 9 | 11 | 13 | 15 | 17 | 19 |
| 7 | 9 | 11 | 13 | 15 | 17 | 19 | 21 |
| 9 | 11 | 13 | 15 | 17 | 19 | 21 | 23 |
| 11 | 13 | 15 | 17 | 19 | 21 | 23 | 25 |
| 13 | 15 | 17 | 19 | 21 | 23 | 25 | 27 |
| 15 | 17 | 19 | 21 | 23 | 25 | 27 | 29 |
| 17 | 19 | 21 | 23 | 25 | 27 | 29 | 31 |

Quantization



(e) Block after quantization
Eqn. (6)

| | | | | | | | |
|----|----|----|---|----|---|----|----|
| 61 | -3 | 2 | 0 | 2 | 0 | 0 | -1 |
| 4 | -4 | 2 | 0 | 0 | 0 | 0 | 0 |
| -1 | -2 | 0 | 0 | -1 | 0 | -1 | 0 |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | -1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

61,-3,4,-1,-4,2,0,2,-2,0,0,0,0,0,2,0,0,0,1,0,0,0,0,0,0,-1,0,0,-1,0,0,
0,0,-1,0,0,0,0,0,0,0,-1,0

JPEG Steps (cont'd)

6. Encode coefficients:

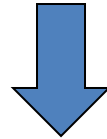
6.1 Form “intermediate” symbol sequence.

6.2 Encode “intermediate” symbol sequence into a binary sequence.

Final Symbol Sequence

(g) Intermediate symbol sequence

(6)(61),(0,2)(-3),(0,3)(4),(0,1)(-1),(0,3)(-4),(0,2)(2),(1,2)(2),(0,2)(-2),
██████████ (5,2)(2),(3,1)(1),(6,1)(-1),(2,1)(-1),(4,1)(-1),(7,1)(-1),(0,0)



(e) Encoded bit sequence (total 98 bits)

111011110100100100000100011011011011100101111111011
11011101011111011011100011101101111101001010

What is the effect of the “Quality” parameter?



(58k bytes)



(21k bytes)



(8k bytes)

lower compression

higher compression

$$1 \leq \textit{quality} \leq 25$$

ONE DOES NOT SIMPLY

USE HIGH LEVEL OF JPEG COMPRESSION

What compression scheme should be used for fingerprints ?

- Lossless or lossy compression?
- In practice lossless compression methods haven't done better than 2:1 on fingerprints!
- Does JPEG work well for fingerprint compression?

Results using JPEG compression

file size 45853 bytes
compression ratio: 12.9



Fine details have been lost.

Image has an artificial “blocky”
pattern superimposed on it.

Artifacts will affect the
performance of fingerprint
recognition.

Results using **WSQ** compression

file size 45621 bytes
compression ratio: 12.9



Fine details are better preserved.

No “blocky” artifacts.

Varying compression ratio (cont'd)

0.9 bpp compression

WSQ image, file size 47619 bytes,
compression ratio 12.4



JPEG image, file size 49658 bytes,
compression ratio 11.9



JPEG

- JPEG compression exploits two observations:
 - **#1**: Human eyes don't see color (chrominance) quite as well as brightness (luminance) → Compress in a color-dominant space (RGB --> YCbCr)
 - **#2**: Human eyes can't distinguish high frequency changes in image intensity (downsample (Cb,Cr), quantize, DCT)

Color Images



Y



Cb



Cr

- Different quantization matrices for chrominance and luminance
- Chroma subsampling (use reduced resolution of chroma channels)

JPEG Modes

- JPEG supports several different modes
 - Sequential Mode
 - Progressive Mode
 - Hierarchical Mode
 - Lossless Mode
- The default mode is “sequential”
 - Image is encoded in a **single scan** (left-to-right, top-to-bottom).

Progressive JPEG

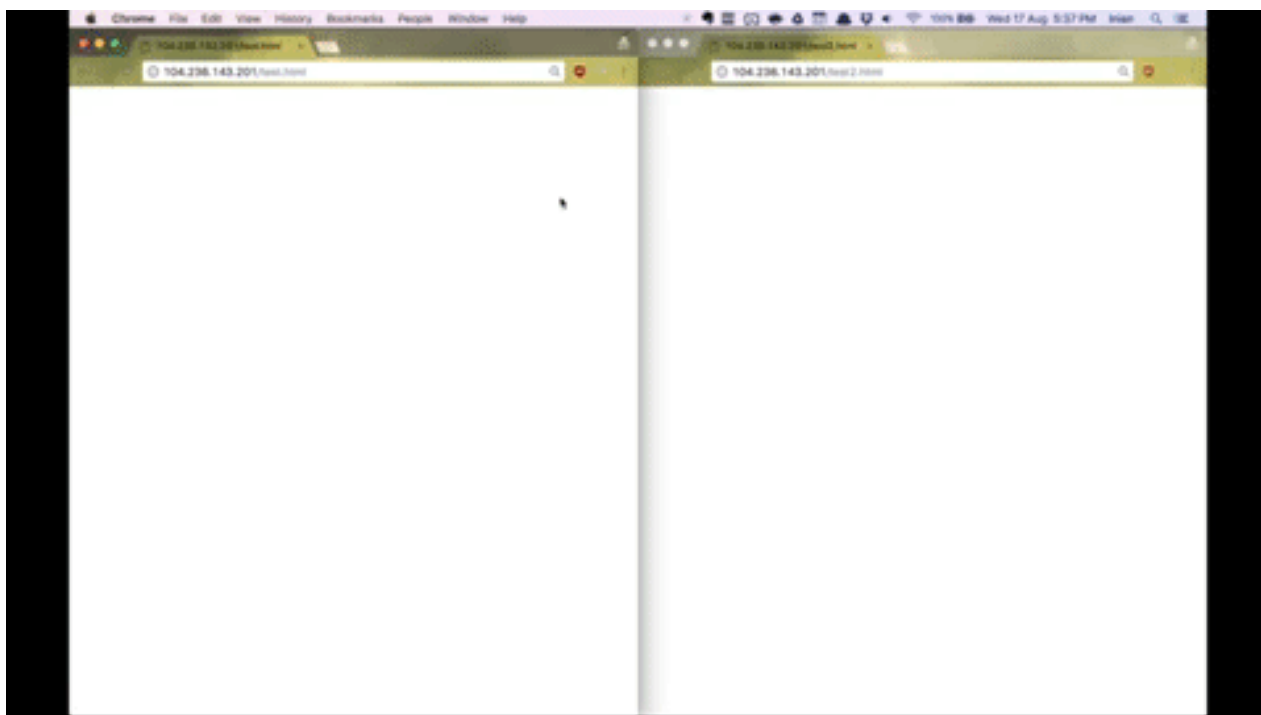
- Image is encoded in **multiple scans**, in order to produce a quick, rough decoded image when transmission time is long.

Sequential



Progressive





JPEG at 0.125 bpp (enlarged)



JPEG2000 at 0.125 bpp



Other popular formats

- GIF → lossy
- PNG → lossless
- Video
 - MPEG etc. (exploit temporal redundancy also)

Reference

- Ch 8, G&W textbook