

21.08.2020

Digital Image Processing (CSE/ECE 478)

Lecture-3: Recap/Discussion

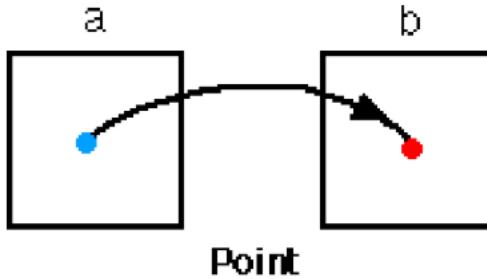
Ravi Kiran



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Spatial Domain Processing

- ▶ Manipulating Pixels Directly in Spatial Domain
- ▶ 3 approaches
- ▶ 1. Point to Point



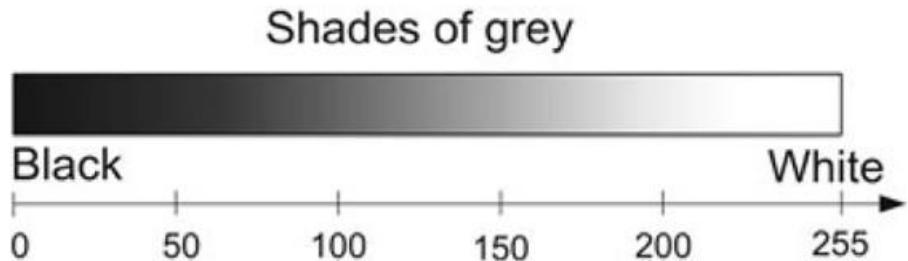
Linear Intensity Transforms

- $T(z) = z + K$

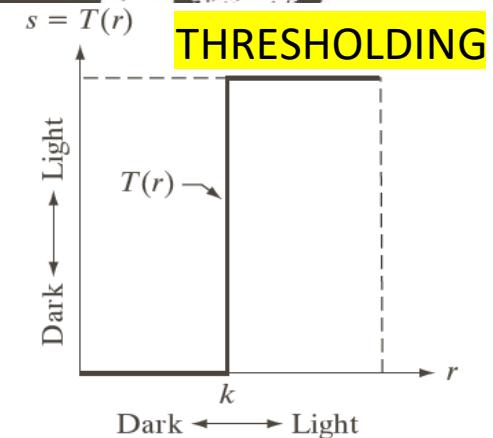
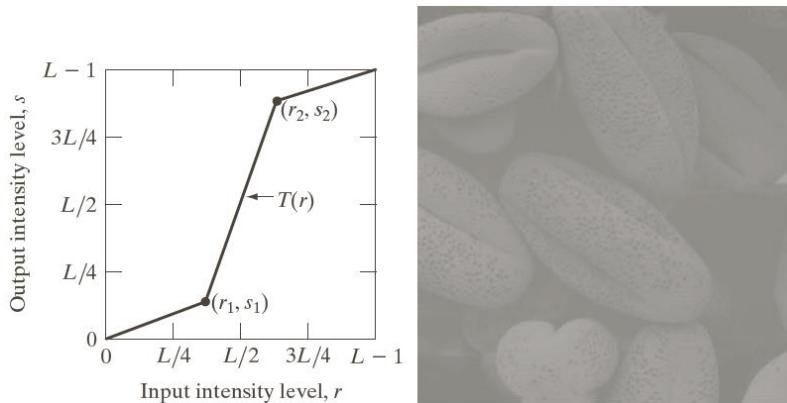
- $T(z) = z - K$

- $T(z) = Kz$

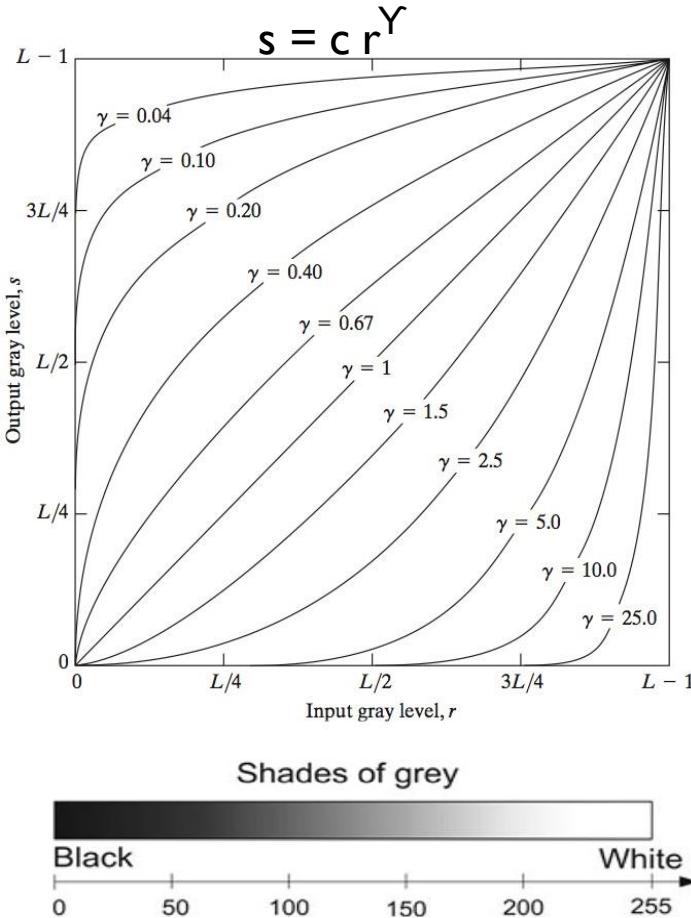
- $T(z) = K_1z + K_2$



Piecewise-Linear Transformations



Power-Law Transformations

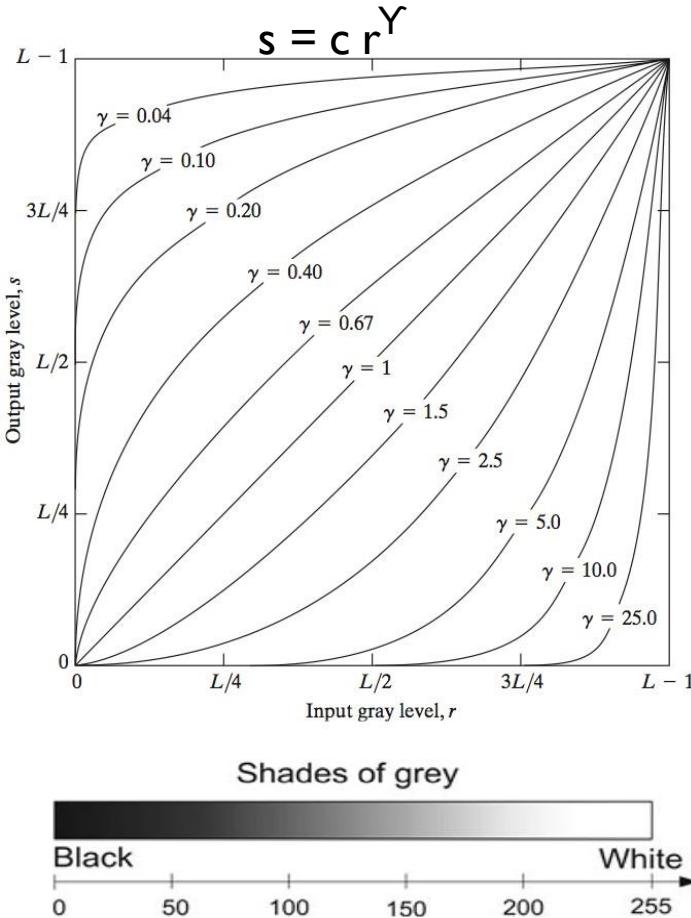


a
b
c
d

FIGURE 3.9
(a) Aerial image.
(b)–(d) Results of applying the transformation in Eq. (3.2-3) with $c = 1$ and $\gamma = 3.0, 4.0$, and 5.0 , respectively.
(Original image for this example courtesy of NASA.)



Power-Law Transformations



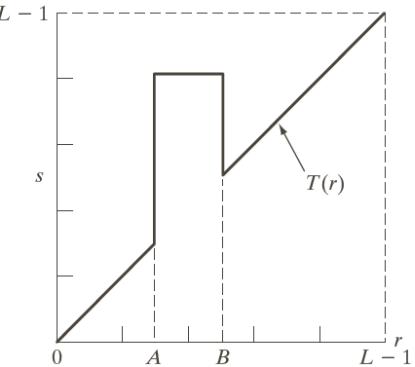
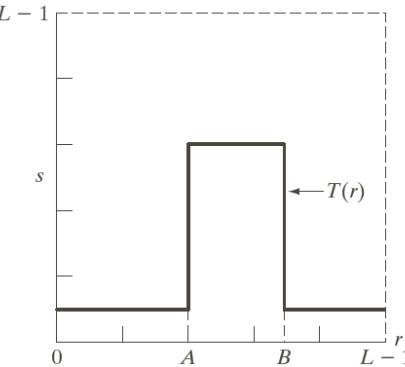
Demo:

<https://colab.research.google.com/drive/11qlLOVKleZnONtPuxAryAf9WkUC7kEMI#scrollTo=eaU5WQaqOpSCr&line=12&uniquifier=1>

Intensity Slicing

a | b

FIGURE 3.11 (a) This transformation highlights intensity range $[A, B]$ and reduces all other intensities to a lower level. (b) This transformation highlights range $[A, B]$ and preserves all other intensity levels.



a | b | c

Bit plane slicing

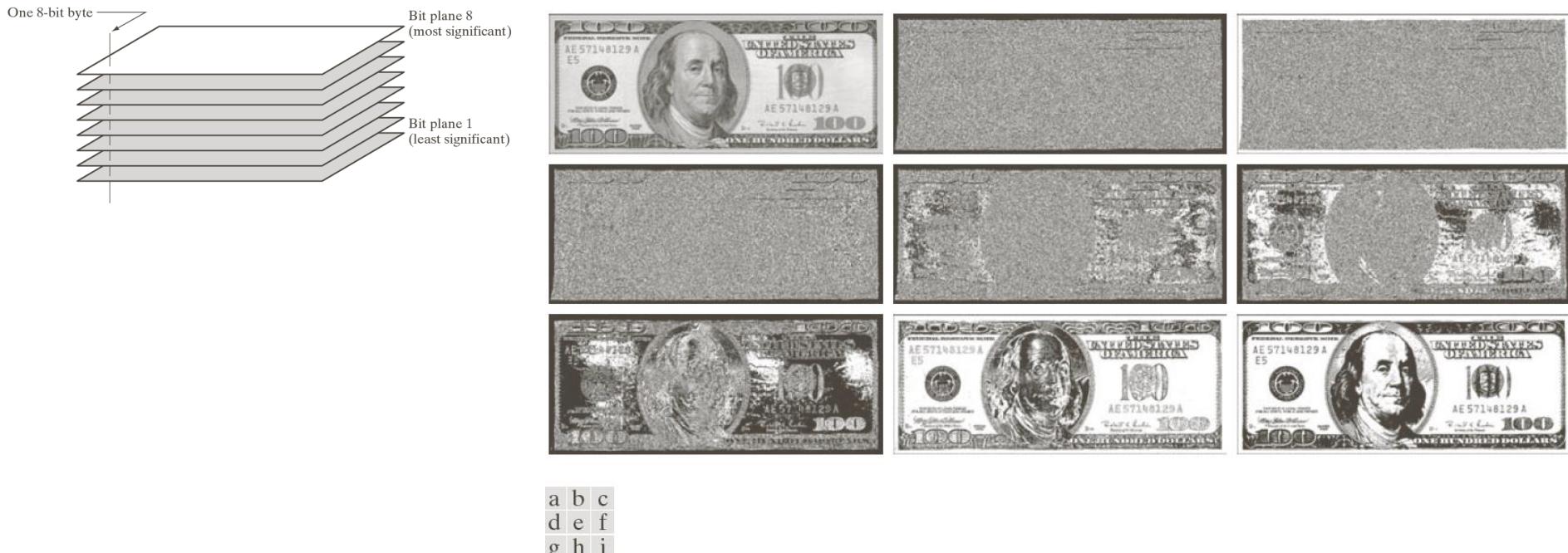


FIGURE 3.14 (a) An 8-bit gray-scale image of size 500×1192 pixels. (b) through (i) Bit planes 1 through 8, with bit plane 1 corresponding to the least significant bit. Each bit plane is a binary image.

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Digital Image Processing (CSE/ECE 478)

Lecture-4: Histogram Processing

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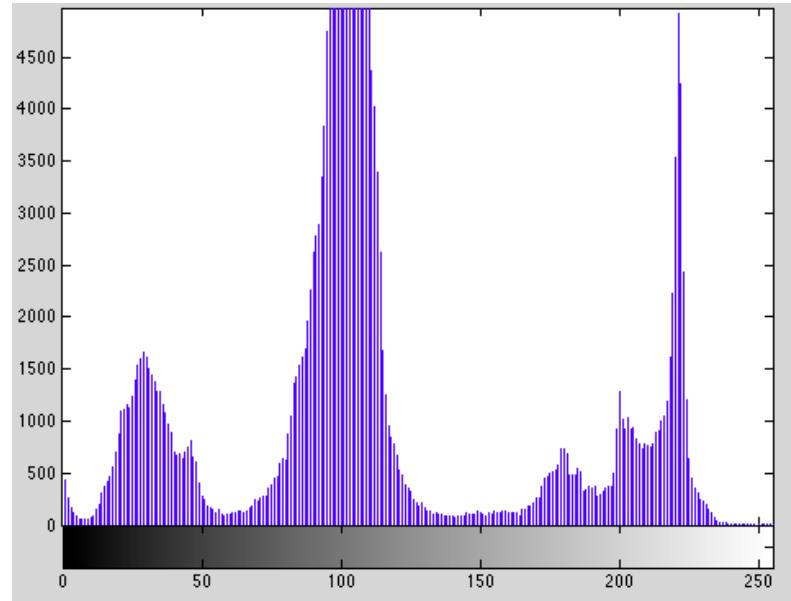
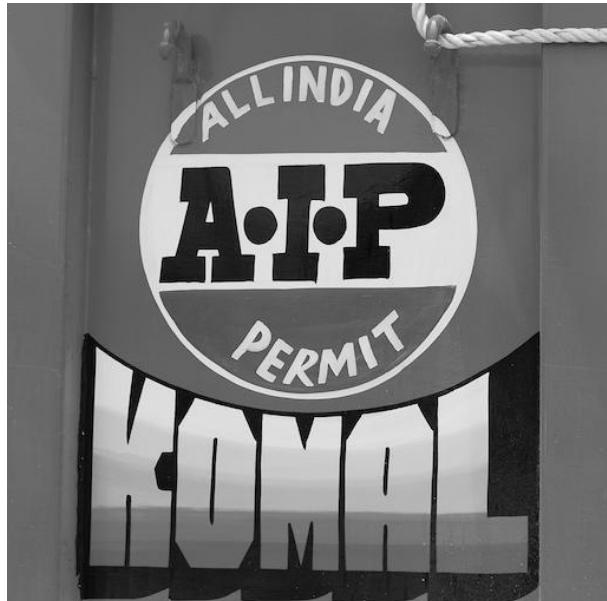
Piecewise-Linear Transformations



Histogram: An image representation + visualization

$$h_r(i) = n_i$$

$i \rightarrow$ intensity value, range $[0, L-1]$
 $n_i \rightarrow$ number of pixels with intensity i



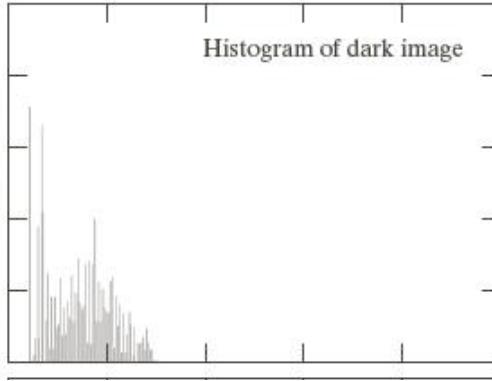
Histograms

- ▶ What can we infer from histograms?

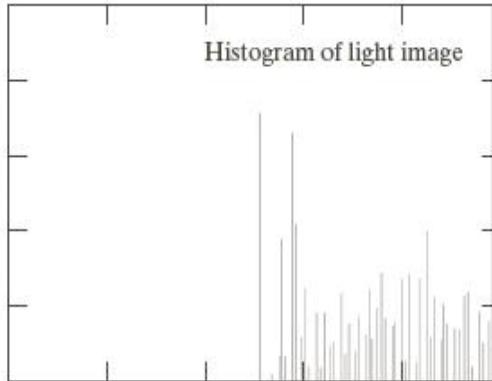


Histogram viewing standard in most DSLR cameras

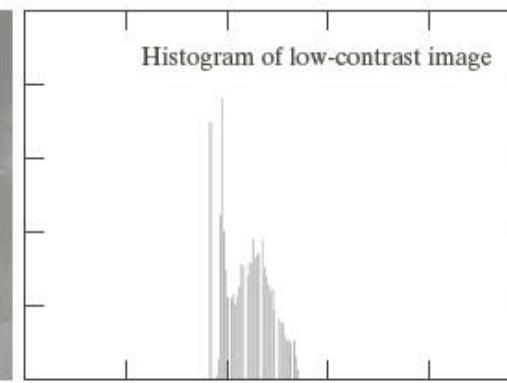
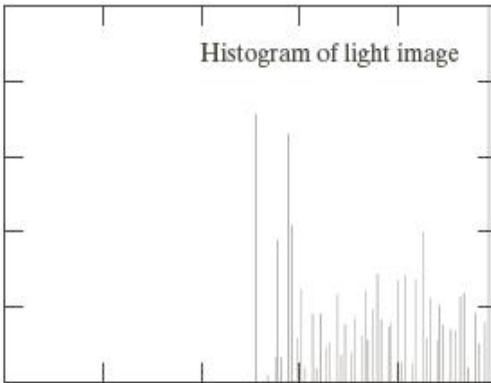
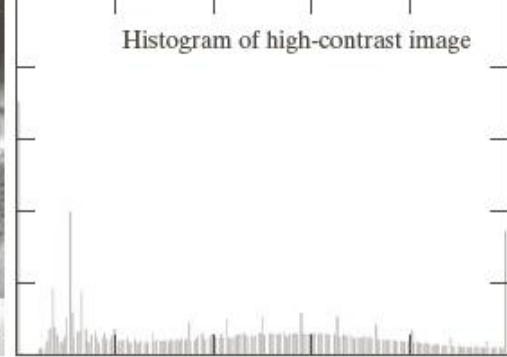
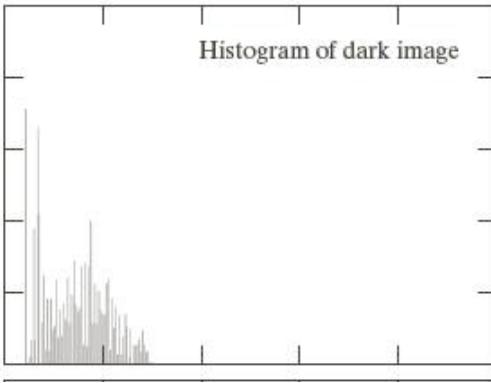
Histograms and Contrast



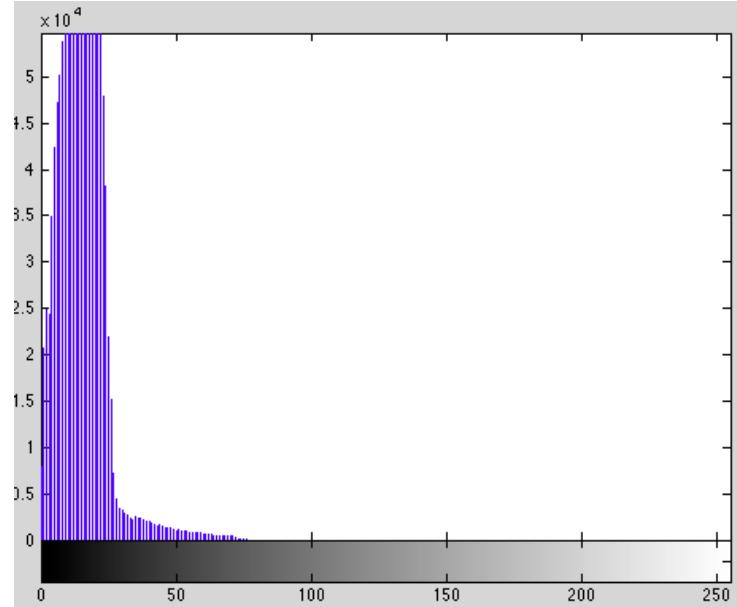
$$\frac{I_{max} - I_{min}}{I_{max} + I_{min}}$$



Histograms and Contrast



Histograms

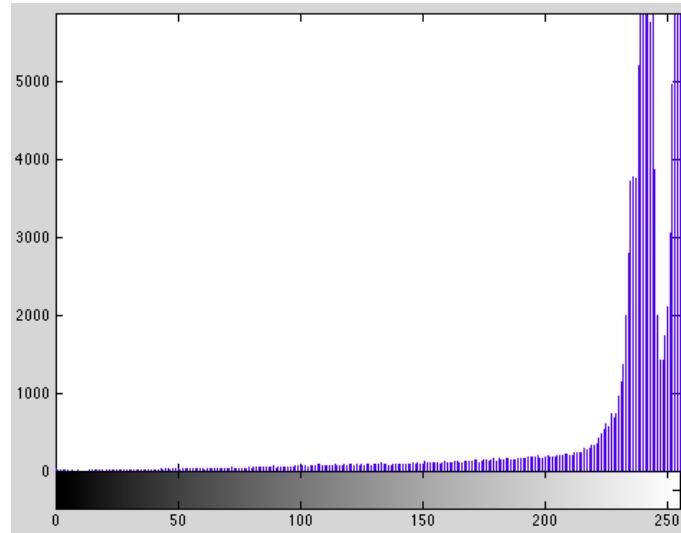


Under exposure

Histograms

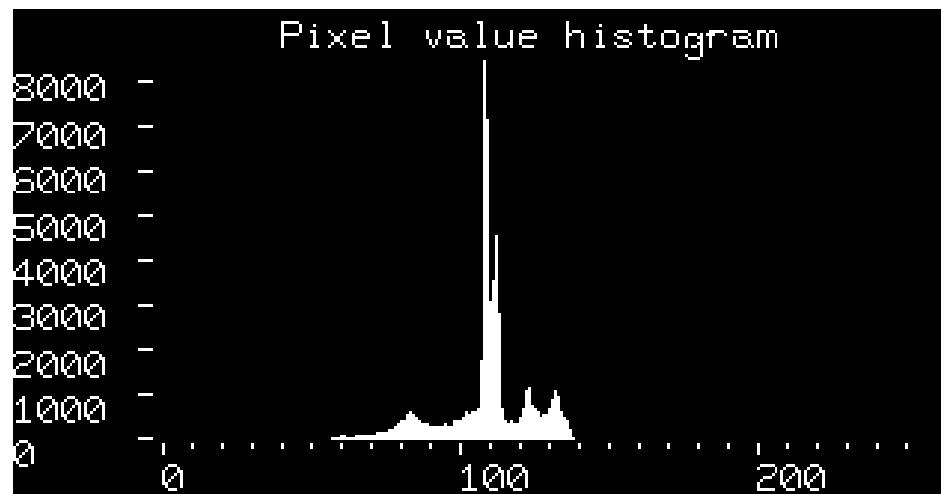


PentaxForums.com P



Over exposure

A low-contrast image and its histogram



Contrast Stretching



$$f_{\text{ac}}(a) = a_{\text{min}} + (a - a_{\text{low}}) \cdot \frac{a_{\text{max}} - a_{\text{min}}}{a_{\text{high}} - a_{\text{low}}}$$

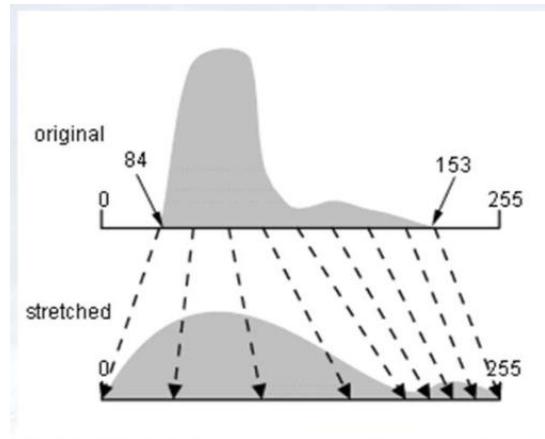
Contrast Stretching

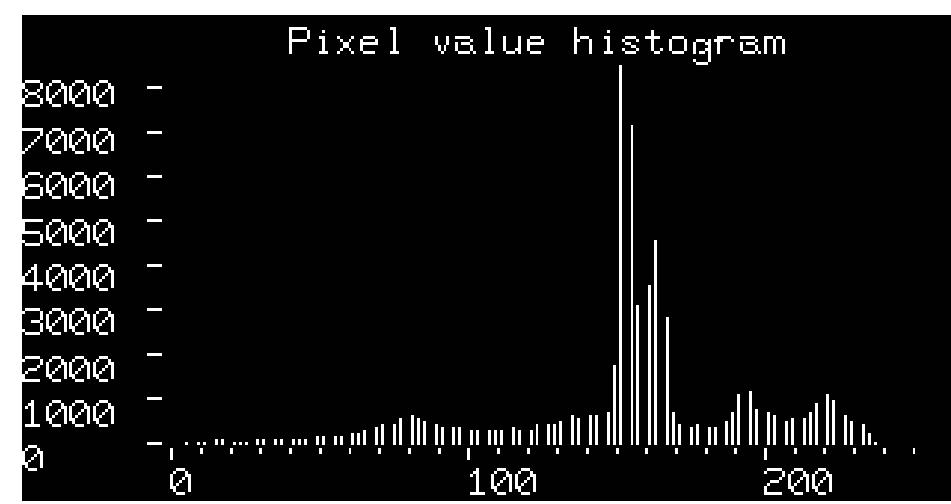
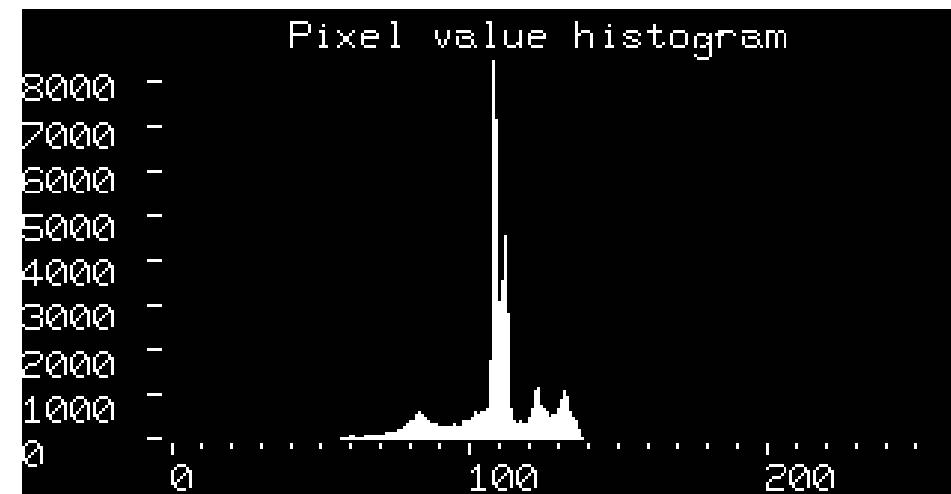


$$f_{ac}(a) = a_{\min} + (a - a_{\text{low}}) \cdot \frac{a_{\max} - a_{\min}}{a_{\text{high}} - a_{\text{low}}}$$

If $a_{\min} = 0$ and $a_{\max} = 255$

$$f_{ac}(a) = (a - a_{\text{low}}) \cdot \frac{255}{a_{\text{high}} - a_{\text{low}}}$$





Contrast Stretching

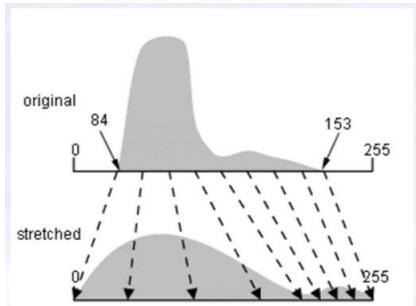
Suppose we have a single pixel with intensity 255 in the original intensity range. What happens ?



$$f_{ac}(a) = a_{min} + (a - a_{low}) \cdot \frac{a_{max} - a_{min}}{a_{high} - a_{low}}$$

If $a_{min} = 0$ and $a_{max} = 255$

$$f_{ac}(a) = (a - a_{low}) \cdot \frac{255}{a_{high} - a_{low}}$$



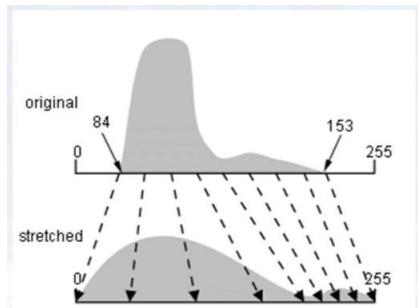
Contrast Stretching



$$f_{ac}(a) = a_{\min} + (a - a_{\min}) \cdot \frac{a_{\max} - a_{\min}}{a_{\text{high}} - a_{\text{low}}}$$

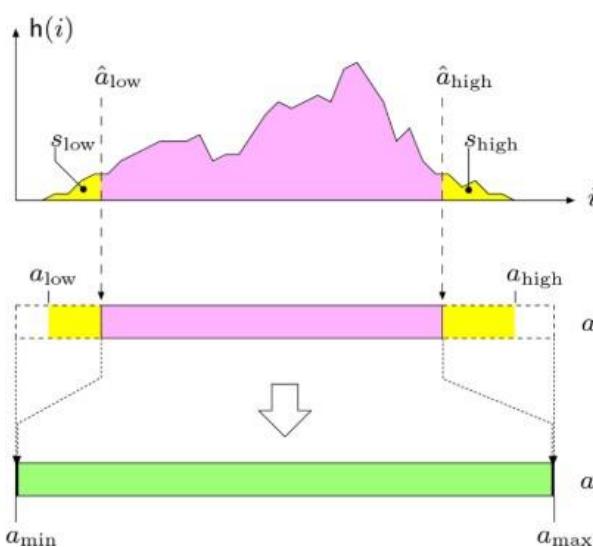
If $a_{\min} = 0$ and $a_{\max} = 255$

$$f_{ac}(a) = (a - a_{\min}) \cdot \frac{255}{a_{\text{high}} - a_{\text{low}}}$$



Suppose we have a single pixel with intensity 0 in the original intensity range.
What happens ?

Contrast Stretching ver. 2

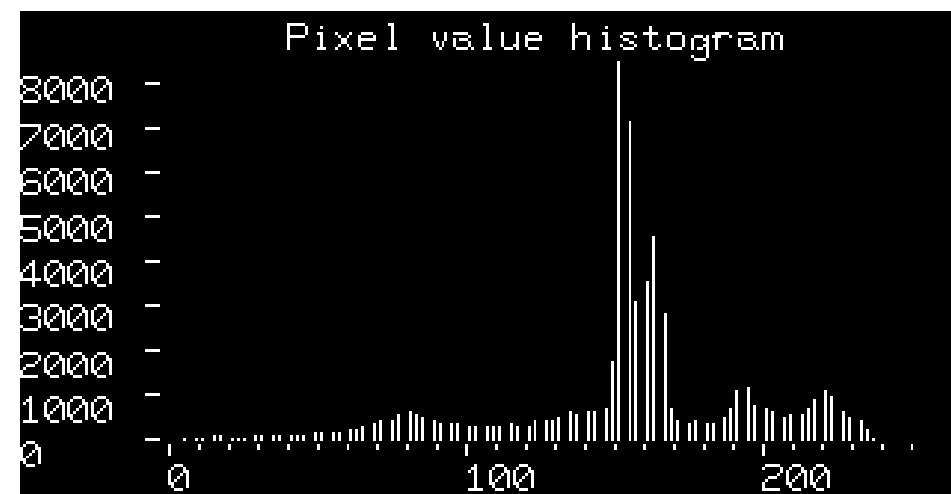
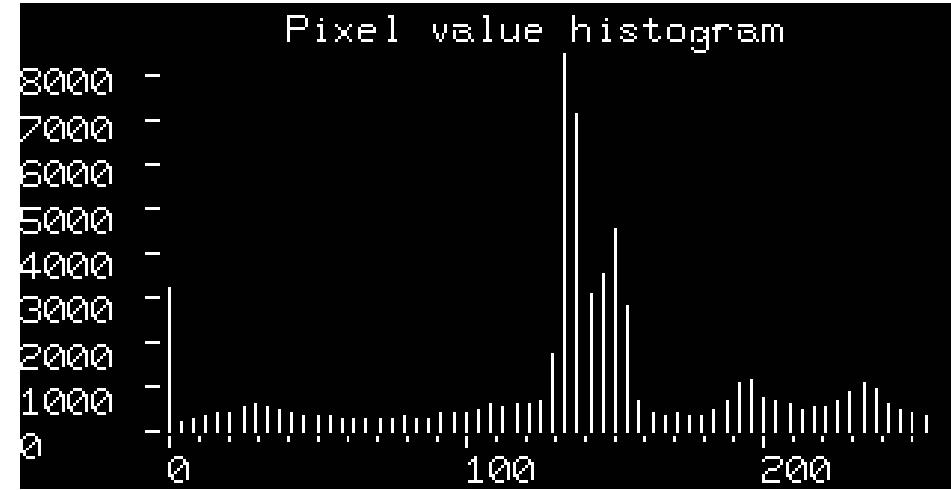


$$\hat{a}_{\text{low}} = \min\{ i \mid H(i) \geq M \cdot N \cdot s_{\text{low}} \}$$

$$\hat{a}_{\text{high}} = \max\{ i \mid H(i) \leq M \cdot N \cdot (1 - s_{\text{high}}) \}$$

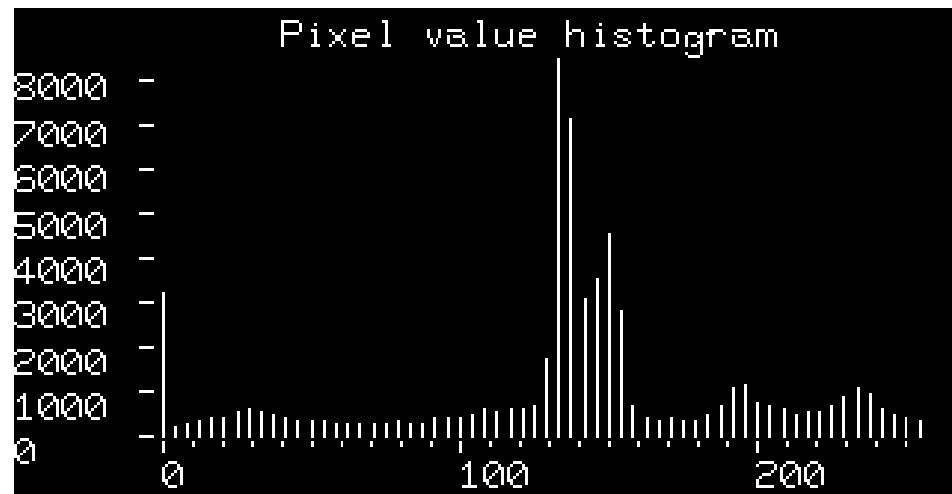
$$f_{\text{mac}}(a) = \begin{cases} a_{\min} & \text{for } a \leq \hat{a}_{\text{low}} \\ a_{\min} + (a - \hat{a}_{\text{low}}) \cdot \frac{a_{\max} - a_{\min}}{\hat{a}_{\text{high}} - \hat{a}_{\text{low}}} & \text{for } \hat{a}_{\text{low}} < a < \hat{a}_{\text{high}} \\ a_{\max} & \text{for } a \geq \hat{a}_{\text{high}} \end{cases}$$

Ver. 2



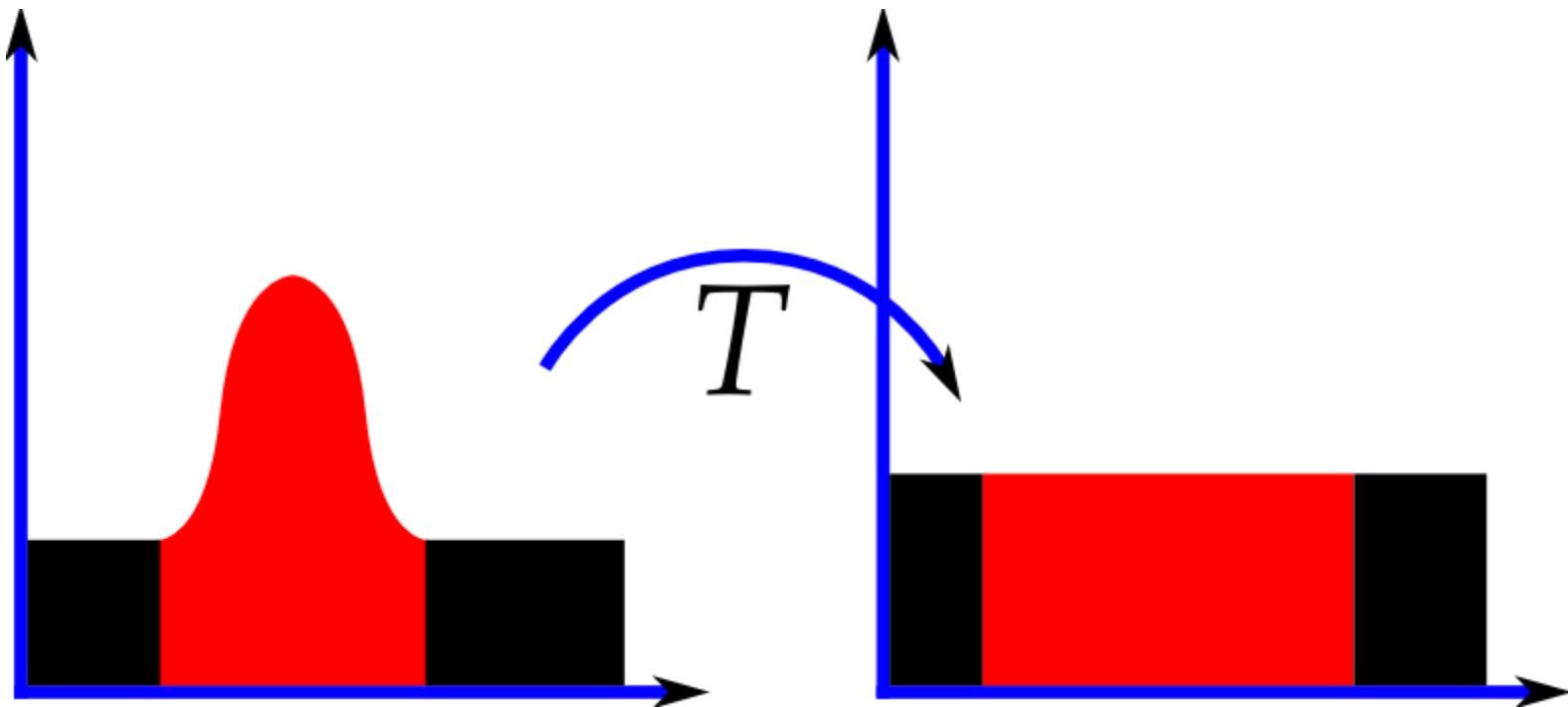
Are all intensities well represented ?

Ver. 2

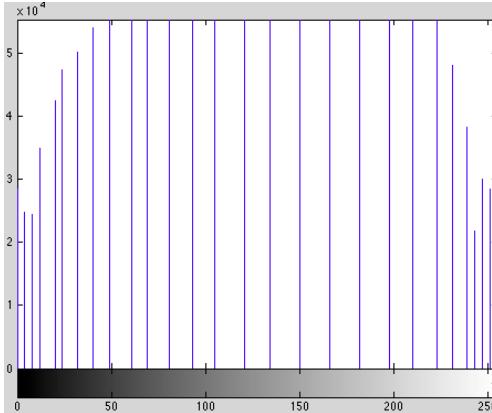
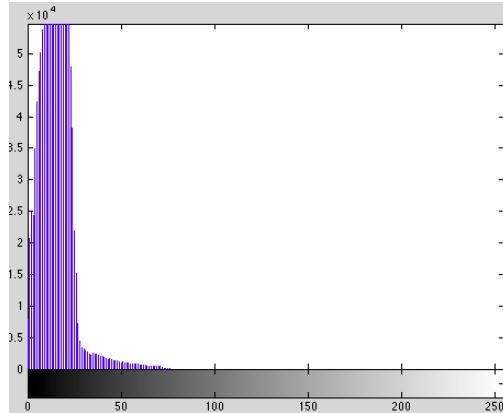
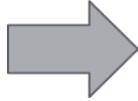




Histogram Equalization



Histogram Equalization



The issue with contrast stretching



$$f_{ac}(a) = a_{\min} + (a - a_{\min}) \cdot \frac{a_{\max} - a_{\min}}{a_{\text{high}} - a_{\text{low}}}$$

If $a_{\min} = 0$ and $a_{\max} = 255$

$$f_{ac}(a) = (a - a_{\min}) \cdot \frac{255}{a_{\text{high}} - a_{\text{low}}}$$

Histogram Equalization

Histogram Equalization

Histogram Equalization

Histogram Equalization



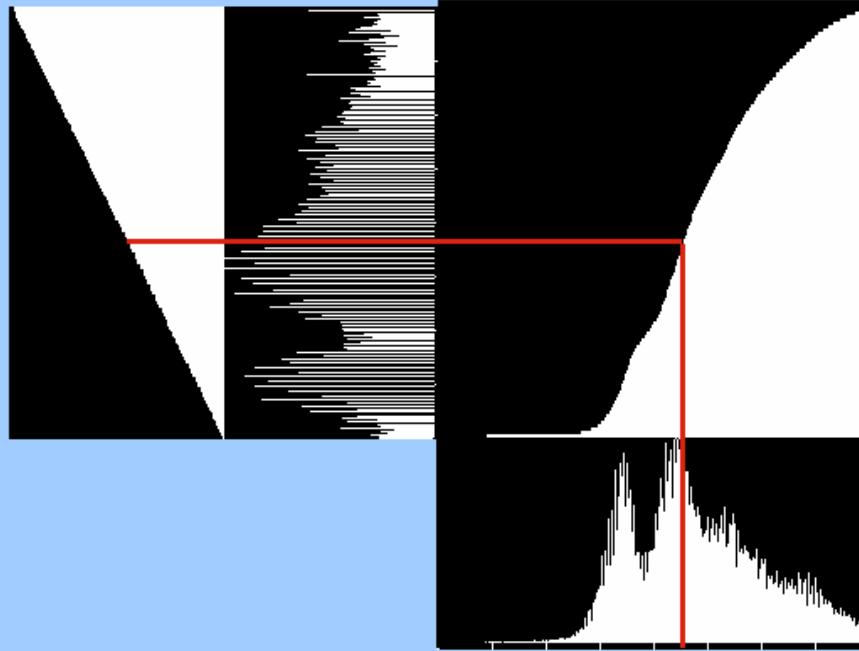
Contrast
Stretching



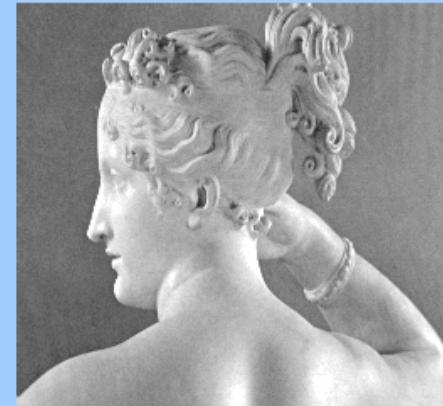
Histogram
Equalization



Equalized histogram



Histogram of riginal image

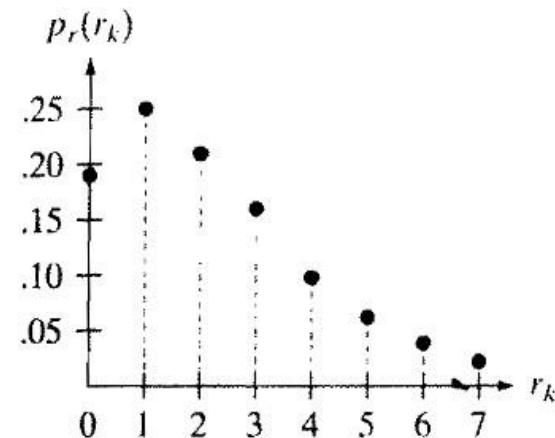


Histogram Equalization - Example

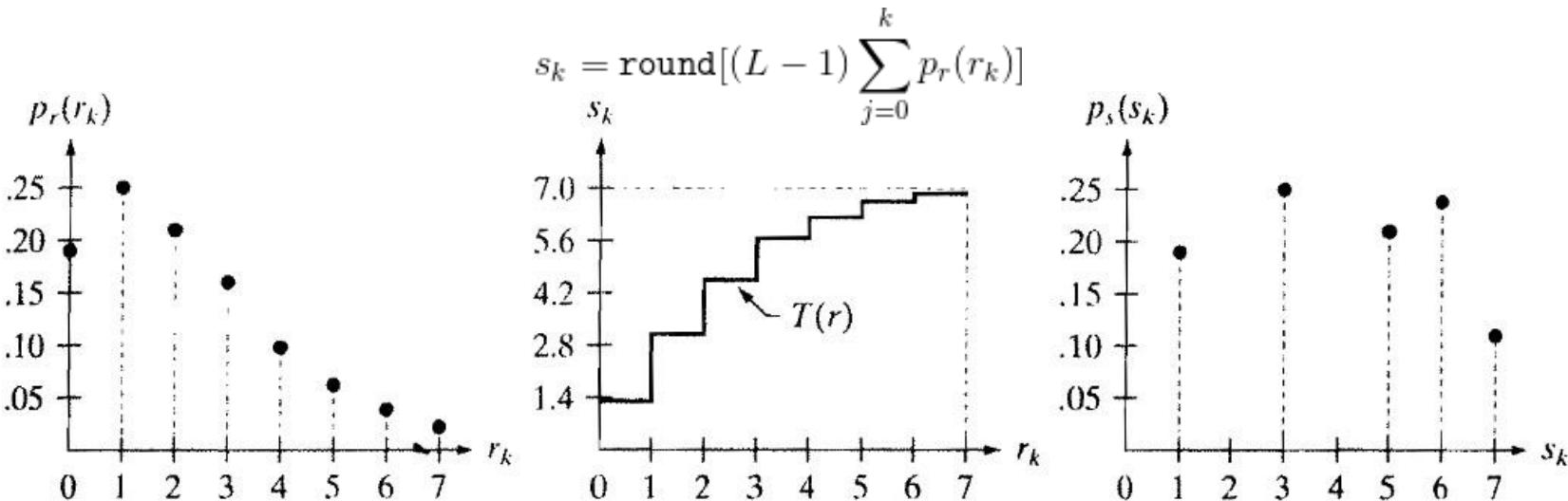
64 x 64 image

3-bits / pixel

| r_k | n_k | $p_r(r_k) = n_k/MN$ |
|-----------|-------|---------------------|
| $r_0 = 0$ | 790 | 0.19 |
| $r_1 = 1$ | 1023 | 0.25 |
| $r_2 = 2$ | 850 | 0.21 |
| $r_3 = 3$ | 656 | 0.16 |
| $r_4 = 4$ | 329 | 0.08 |
| $r_5 = 5$ | 245 | 0.06 |
| $r_6 = 6$ | 122 | 0.03 |
| $r_7 = 7$ | 81 | 0.02 |



Histogram Equalization - Example



a b c

FIGURE 3.19 Illustration of histogram equalization of a 3-bit (8 intensity levels) image. (a) Original histogram. (b) Transformation function. (c) Equalized histogram.

Histogram Equalization

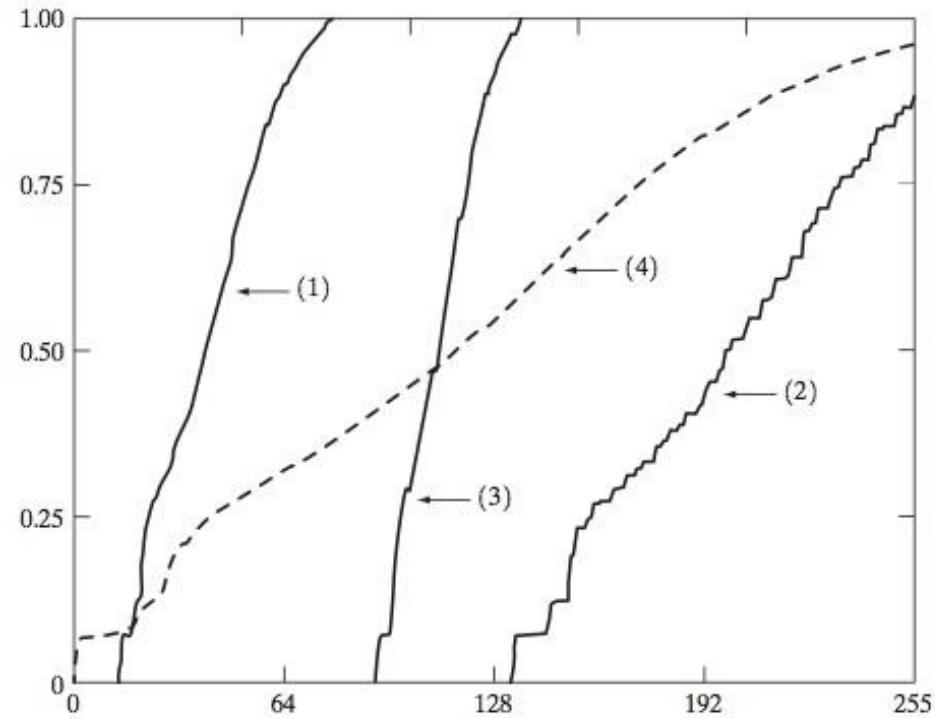
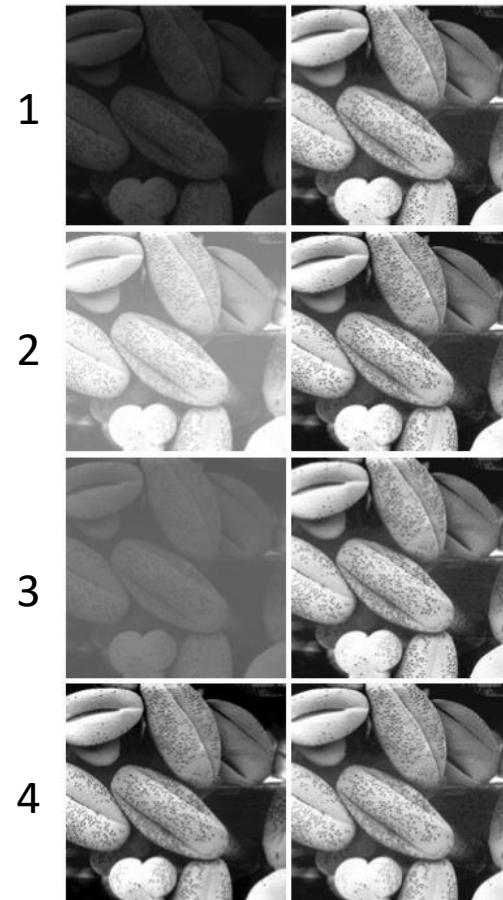


Image Courtesy: Gonzalez and Woods

Histogram Equalization v/s Contrast Enhancement

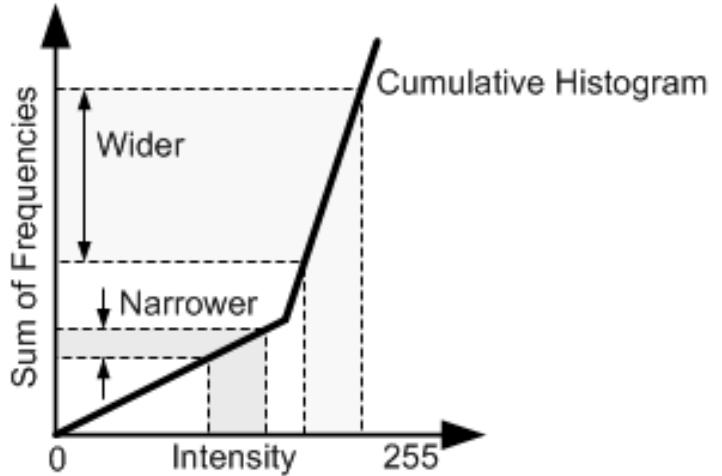


Contrast Enhancement



Histogram equalization

Histogram Equalization : A Visual Explanation

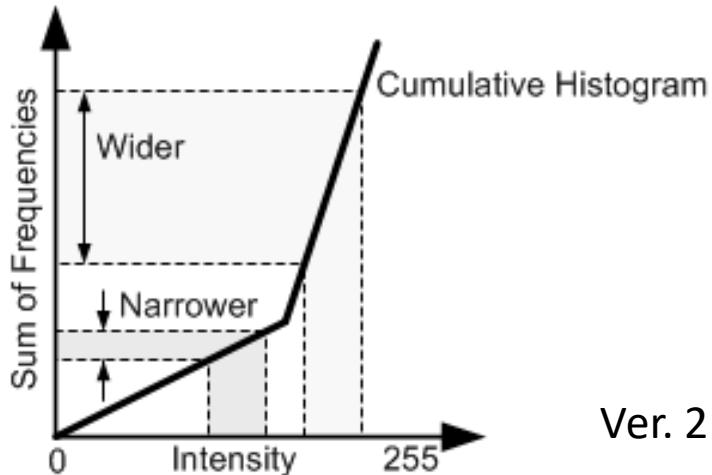


$$s = T(r) = (L - 1) \int_0^r p_r(w) dw$$

$$s_k = T(r_k) = \text{round} \left((L - 1) \sum_{j=0}^{j=k} p_r(r_j) \right)$$

Histogram Equalization (ver. 2)

$$h[i] = \text{constant}, \quad 0 \leq i \leq L - 1$$



$$s = T(r) = (L - 1) \int_0^r p_r(w) dw$$

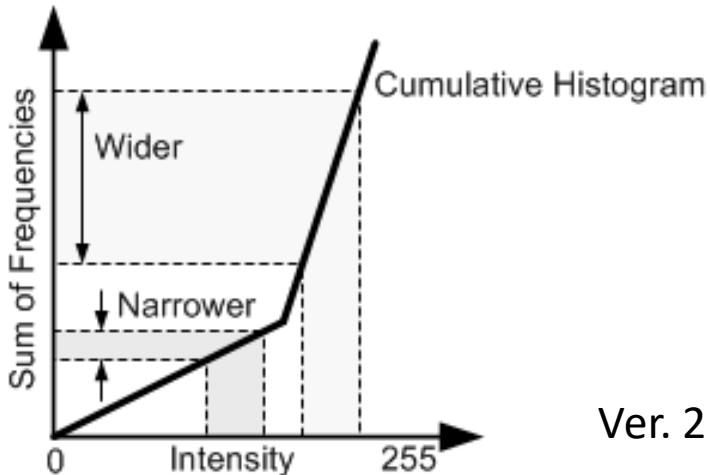
$$s_k = T(r_k) = \text{round} \left((L - 1) \sum_{j=0}^{j=k} p_r(r_j) \right)$$

Ver. 2

$$s_k = T(r_k) = \text{round} \left((L - 1) * \frac{cdf(r_k) - cdf_{min}}{1 - cdf_{min}} \right)$$

Histogram Equalization (ver. 2)

$$h[i] = \text{constant}, \quad 0 \leq i \leq L - 1$$



$$s = T(r) = (L - 1) \int_0^r p_r(w) dw$$

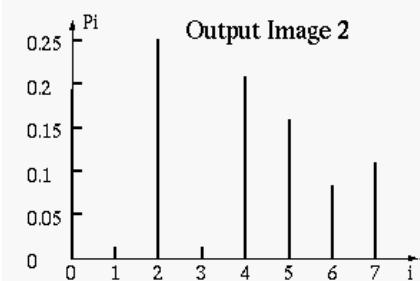
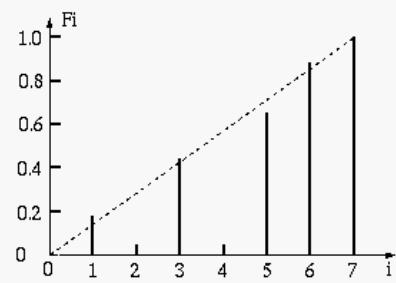
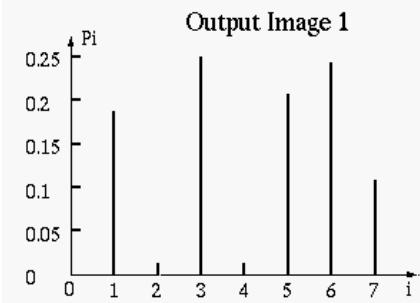
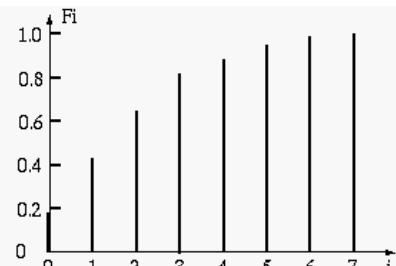
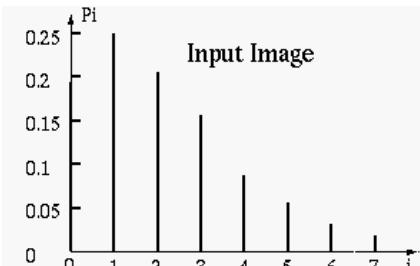
$$s_k = T(r_k) = \text{round} \left((L - 1) \sum_{j=0}^{j=k} p_r(r_j) \right)$$

Ver. 2

$$s_k = T(r_k) = \text{round} \left((L - 1) * \frac{cdf(r_k) - cdf_{min}}{1 - cdf_{min}} \right)$$

$$cdf_{min} = p_r(r_a) \text{ where } r_a = \min\{r_t | p_r(r_t) > 0\}; 0 \leq r_t \leq (L - 1)$$

Histogram Equalization (default v/s ver. 2)



$$s_k = T(r_k) = \text{round} \left((L - 1) \sum_{j=0}^{j=k} p_r(r_j) \right)$$

Ver. 2 $s_k = T(r_k) = \text{round} \left((L - 1) * \frac{cdf(r_k) - cdf_{min}}{1 - cdf_{min}} \right)$

$cdf_{min} = p_r(r_a)$ where $r_a = \min\{r_t | p_r(r_t) > 0\}; 0 \leq r_t \leq (L - 1)$

Histogram Equalization

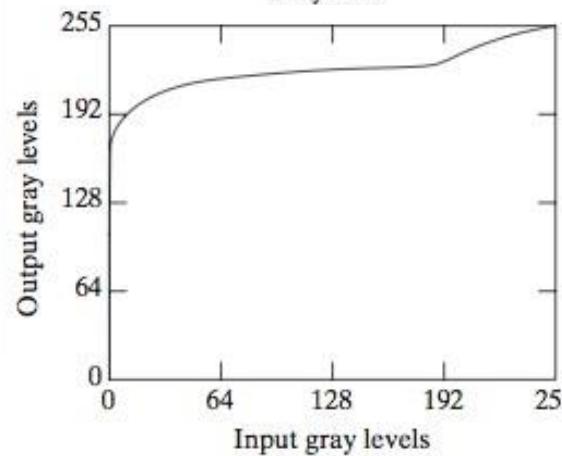
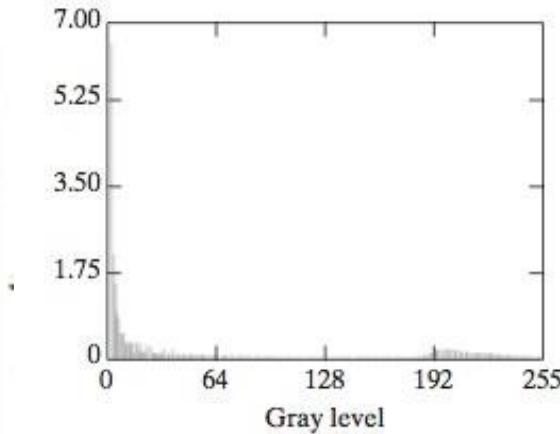
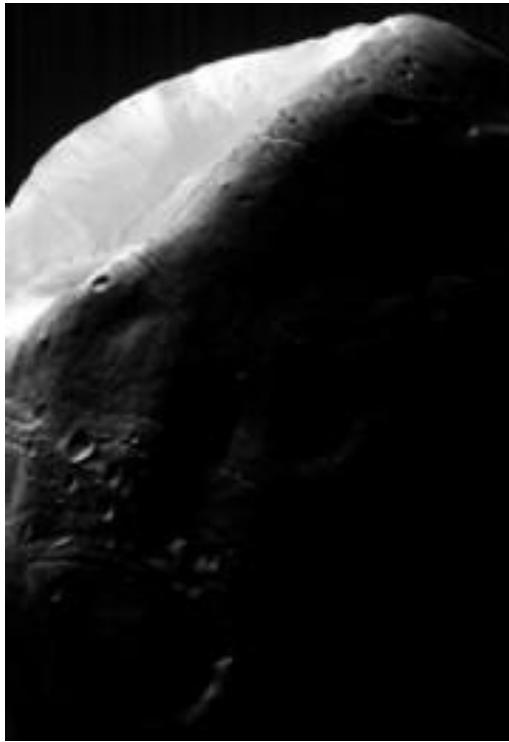
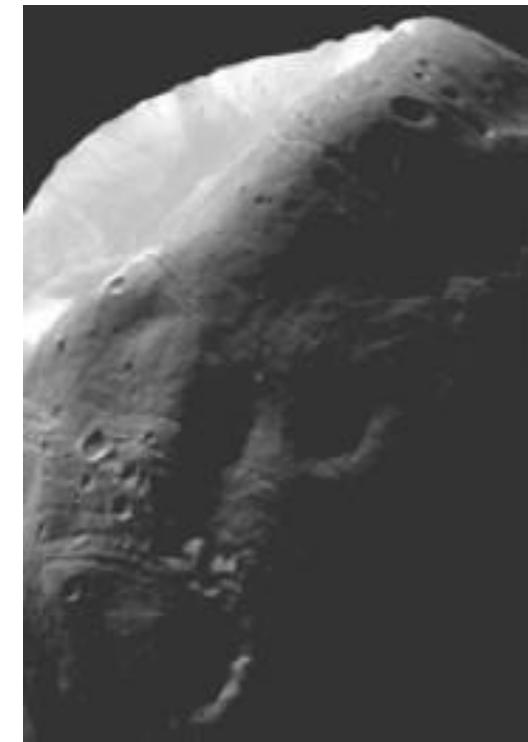
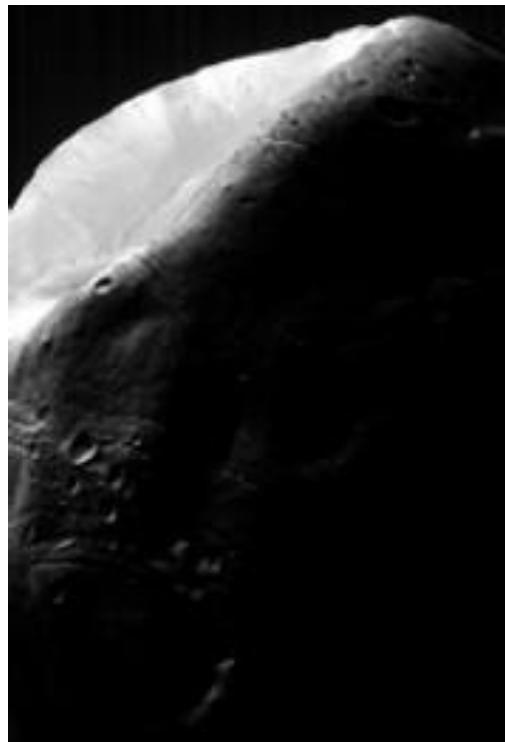
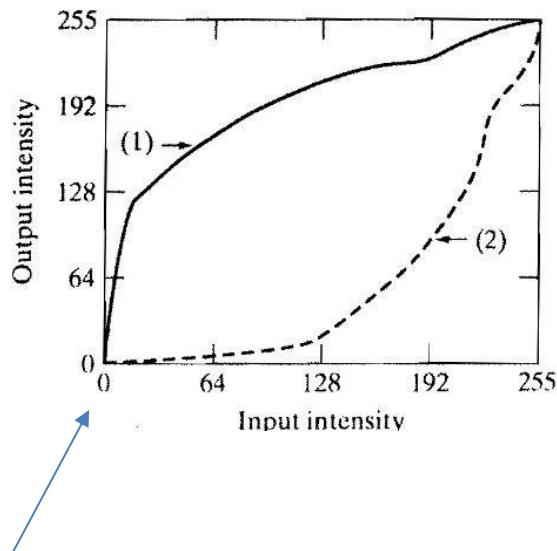


Image Courtesy: Gonzalez and Woods

Histogram specification

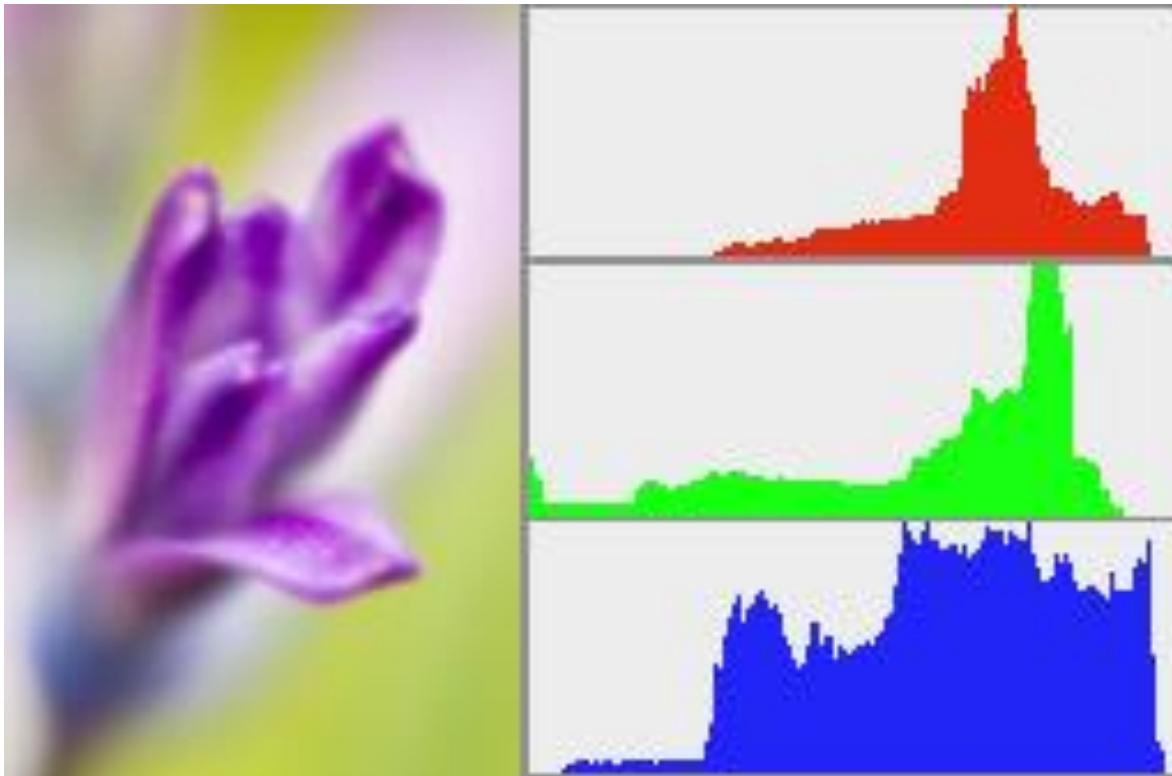
Histogram Specification / Matching [Section 3.3.2]

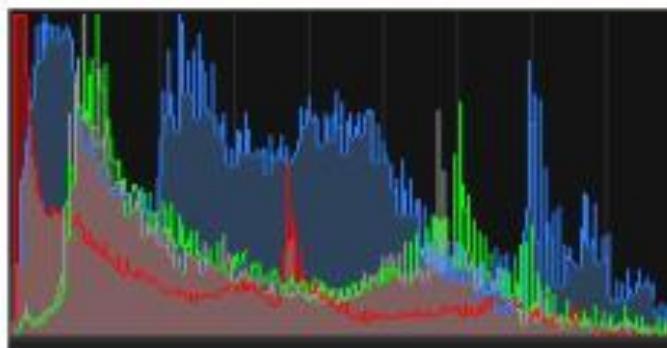
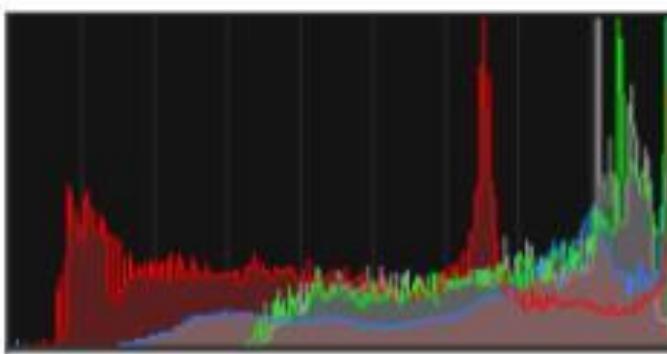
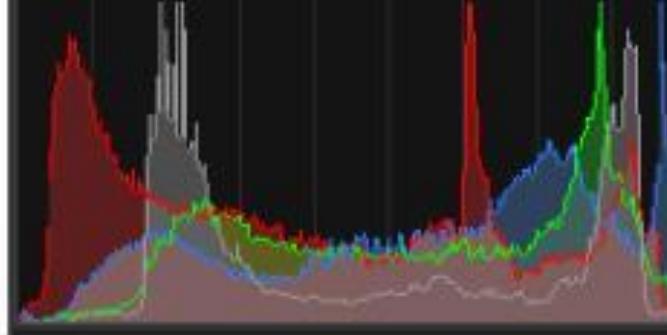


Compare with the curves we saw for contrast enhancement. What's the difference?

Image Courtesy: Gonzalez and Woods

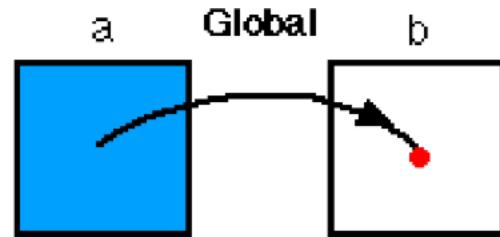
Histograms for RGB images





Histogram Processing

▶ Global to Point



Histogram : Discussion

- A visualization
- A useful statistical representation of image intensities
 - Not dependent on image size
- Drawbacks
 - No spatial information
 - Intensity-centric
 - Raw (unnormalized form): Image-size dependent
- Equalization:
 - An image ‘normalization’ approach
 - Improves global contrast, but can also boost noise

References

- ▶ GW Chapter – 3.3.1 to 3.3.3
- Transformations of Random Variables
 - <http://www.randomservices.org/random/dist/Transformations.html>
 - Section 1 of <http://www.cs.cmu.edu/~minx/transform.pdf>
 - Leibnitz Integration Rule :
https://en.wikipedia.org/wiki/Leibniz_integral_rule#Alternative_derivation
 - [Univariate transformation of a random variable](#)

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| |
|------------|
| 20171172 |
| 20171205 |
| 20171208 |
| 2018101002 |
| 2018101003 |
| 2018101005 |

Mini Quiz 1 Link

<https://forms.office.com/Pages/ResponsePage.aspx?id=vDsaA3zPK06W7IZ1VVQKHNFN1LYrWjxAktM68Sb-hiFUOEEdKVEIEOU8xTjNZTjNCUDFRTjhHQ09BNC4u>