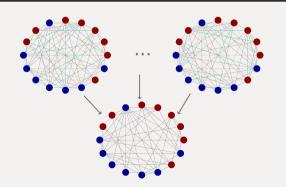
# ESTIMATING CAUSAL EFFECTS USING PROXY INTERFERENCE NETWORKS

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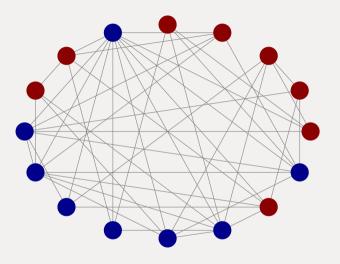


#### BACKGROUND

- Causal Inference. Estimate the effect of treatment on an outcome.
- Interference. Treatment of one unit affect the outcomes of others.
- Treatments spreads through a network.
  - ► Nodes: units; Edges: magntiude of pairwise interfernce.

#### **BACKGROUND**

- Causal Inference. Estimate the effect of treatment on an outcome.
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- Treatments spreads through a network.
  - ► Nodes: units; Edges: magntiude of pairwise interfernce.
- Examples:
  - Social networks. Transmission of information, behavior, encouragements, etc.
  - ► Epidemiology. Mitigating spread of infectious diseases or addictive drugs.
  - ► A/B testing in marketplaces.



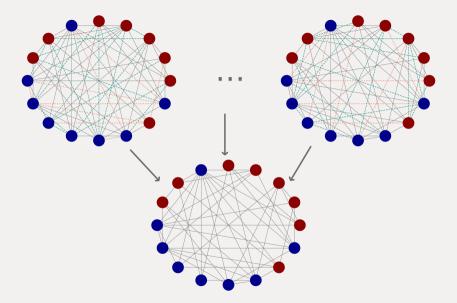
#### THE CHALLENGE

- Accurately measuring social networks is challenging.
- We observe only proxy measurements of the true network.
  - ► Measurements error.
  - ► Multiple sources of data.
  - ► Multilayer networks.
- True network remains latent.

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How can we estimate causal effects using proxy networks?



# ILLUSTRATIVE EXAMPLE - PALUCK ET AL. (2016)

- Field experiement in 56 middle-schools.
- Study how anti-conflict education spread through social networks.
- Measured social networks using self-reported friendships.
  - ► Bi-layer networks: frequently interacted and best friends.
  - Measured at pre- and post-intervention period.

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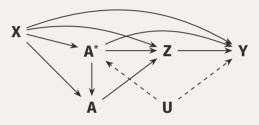
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- Measured social networks using self-reported friendships.
  - ▶ Bi-layer networks: frequently interacted and best friends.
  - ► Measured at pre- and post-intervention period.
- Which of the networks, if any, is the true network?
- **Objective:** Estimate the intervention effects using the proxy networks.

#### FORMAL SETUP

- Finite population  $i \in \{1, ..., N\}$ .
- Treatments:  $\mathbf{Z} \in \{0, 1\}^N$ .
- Outcomes:  $\mathbf{Y} \in \mathbb{R}^N$ .
- Covariates/features: X.
- True interference network:  $\mathbf{A}^* \in \{0, 1\}^{N \times N}$ .
- Proxy networks:  $\mathbf{A} = (\mathbf{A}^1, \dots, \mathbf{A}^B)$ .

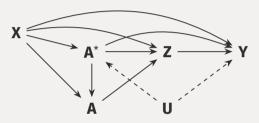
## STRUCTURAL CAUSAL MODEL

■ Population-level directed acyclic graph (DAG):



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Population-level directed acyclic graph (DAG):



- Requires probabilistic models:
  - 1. True network.  $p(\mathbf{A}^*|\mathbf{X},\theta)$ .
  - 2. Proxy networks.  $p(\mathbf{A}|\mathbf{A}^*, \mathbf{X}, \gamma)$ .
  - 3. Outcomes.  $p(Y|Z, A^*, X, \eta)$ .

#### **CAUSAL ESTIMANDS**

Causal effects are the impact of hypothetical interventions on **Z**. Can be viewed as population-level treatment assignment policies.

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Causal effects are the impact of hypothetical interventions on **Z**. Can be viewed as population-level treatment assignment policies.

- 1. Static.  $\mathbb{E}[Y_i | do(Z = z), X, A^*]$ .
  - ► Treating all (**z** = 1) versus none (**z** = 0).
- 2. **Dynamic.**  $\mathbb{E}[Y_i|do(\mathbf{Z}=h(\mathbf{X},\mathbf{A}^*)),\mathbf{X},\mathbf{A}^*].$ 
  - ► Treating units with specific features, e.g., above certain age.
- 3. Stochastic.  $\mathbb{E}_{\pi_{\kappa}(\mathbf{Z})}\mathbb{E}[Y_i|do(\mathbf{Z}),\mathbf{X},\mathbf{A}^*].$ 
  - ightharpoonup Expected impact of randomly treating  $\alpha_1$  vs  $\alpha_0$  percent of units.

■ Observed data  $\mathbf{O} = (\mathbf{Y}, \mathbf{Z}, \mathbf{X}, \mathbf{A})$ . Latent variables  $(\mathbf{A}^*, \eta, \gamma, \theta)$ .

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- Mixed space of continuous  $(\eta, \gamma, \theta)$  and discrete  $\mathbf{A}^*$ . Discrete have  $O(N^2)$  terms!
- Propose two sampling schemes:
  - 1. Modularization. "break" the posterior into smaller, more manageable parts.
  - 2. Gibbs. Iterate between continuous and discrete. Sample discrete with Local Informed Proposals.

#### **SIMULATIONS**

Two figures: MAPE of estimated treatment effects and MAE of exposure mapping.

## DATA ANALYSIS

Results of Paluck et al. (2016) analysis.

#### FIGURES AND TABLES



Figure 1: Figure caption.

	Heading 1	Heading 2
Row 1	v <sub>11</sub>	v <sub>12</sub>
Row 2	v <sub>21</sub>	$V_{22}$
Row 3	v <sub>31</sub>	V <sub>32</sub>

Table 1: Table caption.

# Thanks for using **Focus**!

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# **APPENDIX**

More math details.