432 Class 12 Slides

github.com/THOMASELOVE/2020-432

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Setup

```
library(magrittr); library(janitor); library(here)
library(knitr)
library(naniar)
library(broom)
library(mice)
  # mice = multiple imputation through chained equations
library(tidyverse)
theme_set(theme_bw())
```

Today's Goals

Use multiple imputation to deal with missing data in fitting:

- linear regression with 1m
- logistic regression with glm

using the mice package. (MICE = Multiple Imputation through Chained Equations)

Useful (if somewhat dated) Sources

- https://thomasleeper.com/Rcourse/Tutorials/mi.html.
- https://stats.idre.ucla.edu/r/faq/how-do-i-perform-multipleimputation-using-predictive-mean-matching-in-r/

Section 1

Multiple Imputation: Potential and Pitfalls

Sterne et al. 2009 BMJ

Multiple imputation for missing data in epidemiological and clinical research: potential and pitfalls

In this article, we review the reasons why missing data may lead to bias and loss of information in epidemiological and clinical research. We discuss the circumstances in which multiple imputation may help by reducing bias or increasing precision, as well as describing potential pitfalls in its application. Finally, we describe the recent use and reporting of analyses using multiple imputation in general medical journals, and suggest guidelines for the conduct and reporting of such analyses.

- https://www.bmj.com/content/338/bmj.b2393
- https://doi.org/10.1136/bmj.b2393

Types of Missing Data (from Sterne et al.)

- Missing completely at random There are no systematic differences between the missing values and the observed values. For example, blood pressure measurements may be missing because of breakdown of an automatic sphygmomanometer.
- Missing at random Any systematic difference between the missing values and the observed values can be explained by differences in observed data. For example, missing blood pressure measurements may be lower than measured blood pressures but only because younger people may be more likely to have missing blood pressure measurements.
- Missing not at random Even after the observed data are taken into account, systematic differences remain between the missing values and the observed values. For example, people with high blood pressure may be more likely to miss clinic appointments because they have headaches

"Missing at random" is an assumption that justifies the analysis, not a property of the data.

Pitfalls When Using Multiple Imputation (Sterne et al.)

Data that are missing not at random

- Some data are inherently missing not at random because it is not possible to account for systematic differences between the missing values and the observed values using the observed data.
- In such cases multiple imputation may give misleading results. Those results can be either more or less misleading than a complete case analysis.
- For example, consider a study investigating predictors of depression. If
 individuals are more likely to miss appointments because they are
 depressed on the day of the appointment, then it may be impossible to
 make the missing at random assumption plausible, even if a large
 number of variables is included in the imputation model.
- Where complete cases and multiple imputation analyses give different results, the analyst should attempt to understand why, and this should be reported in publications.

Ways to Deal with Missing Data (from Sterne et al.)

- There are circumstances in which analyses of complete cases will not lead to bias. Missing data in predictor variables do not cause bias in analyses of complete cases if the reasons for the missing data are unrelated to the outcome. Specialist methods to address missing data may lessen the loss of precision and power resulting from exclusion of individuals with incomplete predictor variables but are not required in order to avoid bias.
- Single Imputation of missing values usually causes standard errors to be too small, since it fails to account for the fact that we are uncertain about the missing values.
- If we assume data are missing at random, then unbiased and statistically more powerful analyses (compared with analyses based on complete cases) can generally be done by including individuals with incomplete data.

Multiple Imputation (from Sterne et al.)

- Multiple imputation ... aims to allow for the uncertainty about the missing data by creating several different plausible imputed data sets and appropriately combining results obtained from each of them.
- The first stage is to create multiple copies of the dataset, with the
 missing values replaced by imputed values. The imputation procedure
 must fully account for all uncertainty in predicting the missing values
 by injecting appropriate variability into the multiple imputed values; we
 can never know the true values of the missing data.

Multiple Imputation (from Sterne et al.)

- The second stage is to use standard statistical methods to fit the model of interest to each of the imputed datasets. Estimated associations in each of the imputed datasets will differ because of the variation introduced in the imputation of the missing values, and they are only useful when averaged together to give overall estimated associations. Standard errors are calculated using Rubin's rules, which take account of the variability in results between the imputed datasets, reflecting the uncertainty associated with the missing values.
 - Valid inferences are obtained because we are averaging over the distribution of the missing data given the observed data.

A Small Example (Sterne et al.)

Consider, for example, a study investigating the association of systolic blood pressure with the risk of subsequent coronary heart disease, in which data on systolic blood pressure are missing for some people.

The probability that systolic blood pressure is missing is likely to:

- decrease with age (doctors are more likely to measure it in older people),
- decrease with increasing body mass index, and
- decrease with history of smoking (doctors are more likely to measure it in people with heart disease risk factors or comorbidities).

If we assume that data are missing at random and that we have systolic blood pressure data on a representative sample of individuals within strata of age, smoking, body mass index, and coronary heart disease, then we can use multiple imputation to estimate the overall association between systolic blood pressure and coronary heart disease.

Today's Data

```
fram_raw <- read_csv(here("data/framingham.csv")) %>%
    clean_names()
```

See https://www.framinghamheartstudy.org/ for more details.

This particular data set has been used by lots of people, in many different settings, and variations of it are all over the internet. I don't know who the originators were.

Data Cleanup

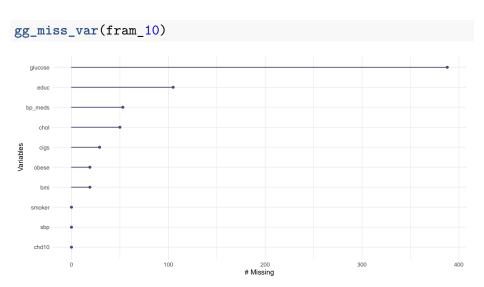
```
fram_10 <- fram_raw %>%
    mutate(educ = fct recode(factor(education),
                          "Some HS" = "1".
                          "HS grad" = "2",
                          "Some Coll" = "3".
                          "Coll grad" = "4")) %>%
    mutate(obese = as.numeric(bmi >= 30)) %>%
    rename(smoker = "current_smoker",
           cigs = "cigs_per_day",
           stroke = "prevalent_stroke",
           highbp = "prevalent hyp".
           chol = "tot chol",
           sbp = "sys_bp", dbp = "dia_bp",
           hrate = "heart_rate",
           chd10 = "ten_year_chd") %>%
    select(sbp, chd10, educ, smoker, cigs, bp_meds,
           chol, bmi, obese, glucose)
```

Data Descriptions (variables we'll use today)

The variables describe n=4238 adult subjects who were examined at baseline and then followed for ten years to see if they developed incident coronary heart disease during that time.

Variable	Description
educ	four-level factor: educational attainment
smoker	$1 = current \ smoker \ at\ time\ of\ examination,\ else\ 0$
cigs	number of cigarettes smoked per day
bp_meds	1 = using anti-hypertensive medication at time of exam
chol	total cholesterol (mg/dl)
sbp	systolic blood pressure (mm Hg)
bmi	body mass index in kg/m^2
obese	1 if subject's bmi is 30 or higher, else 0
glucose	blood glucose level in mg/dl
chd10	$1 = {\sf coronary\ heart\ disease\ in\ next\ 10\ years}$

Which variables are missing data?



Counts of Missing Data, by Variable

```
miss var summary(fram 10) %>%
   filter(n_miss > 0)
# A tibble: 7 x 3
 variable n_miss pct_miss
 <chr>
                 <dbl>
         <int>
1 glucose 388 9.16
      105 2.48
2 educ
3 bp_meds 53 1.25
4 chol
        50 1.18
5 cigs
          29 0.684
6 bmi
          19 0.448
7 obese
          19
                 0.448
```

Track missingness with shadow

```
fram_10_sh <- bind_shadow(fram_10)</pre>
```

Two Key Settings for Multiple Imputation

- Use linear regression to predict sbp accounting for missingness via multiple imputation
 - Predictors include glucose, obese, educ, and smoker.
- Use logistic regression to predict chd10 accounting for missingness via multiple imputation
 - Predictors include glucose, bp_meds, chol, bmi, cigs and educ

Section 2

Setting 1: Linear Model for sbp

Model 2 (CC): Two-predictor model for sbp

Suppose we ignore the missingness and just run the model on the data with complete information on sbp, glucose and obese.

```
m2_cc <- fram_10_sh %$% lm(sbp ~ glucose + obese)

tidy(m2_cc, conf.int = TRUE) %>% select(-statistic) %>%
    kable(digits = 3)
```

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	121.671	1.244	0	119.232	124.110
glucose	0.111	0.015	0	0.082	0.139
obese	13.532	1.045	0	11.484	15.580

Edited Summary of Model 2 (CC)

Suppose we ignore the missingness and just run the model.

```
Residual standard error: 21.42 on 3833 degrees of freedom (402 observations deleted due to missingness)
Multiple R-squared: 0.05857, Adjusted R-squared: 0.05808
F-statistic: 119.2 on 2 and 3833 DF, p-value: < 2.2e-16
```

```
glance(m2_cc) %>%
    select(r.squared, adj.r.squared, AIC, BIC) %>%
    kable(digits = c(4, 4, 0, 0))
```

r.squared	adj.r.squared	AIC	BIC
0.0586	0.0581	34401	34426

Model 4 (CC): Four-predictor model for sbp

```
m4_cc <- fram_10_sh %$%
   lm(sbp ~ glucose + obese + smoker + educ)

tidy(m4_cc, conf.int = TRUE) %>% select(-statistic) %>%
   kable(digits = 3)
```

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	127.107	1.388	0	124.385	129.829
glucose	0.106	0.015	0	0.078	0.135
obese	12.304	1.066	0	10.213	14.395
smoker	-4.704	0.699	0	-6.075	-3.332
educHS grad	-3.698	0.833	0	-5.332	-2.065
educSome Coll	-4.724	1.010	0	-6.704	-2.744
educColl grad	-5.954	1.158	0	-8.225	-3.683

Edited Summary of Model 4 (CC)

Suppose we ignore the missingness and just run the model.

```
Residual standard error: 21.2 on 3733 degrees of freedom (498 observations deleted due to missingness)
Multiple R-squared: 0.08257, Adjusted R-squared: 0.0811
F-statistic: 56 on 6 and 3733 DF, p-value: < 2.2e-16
```

```
glance(m4_cc) %>%
    select(r.squared, adj.r.squared, AIC, BIC) %>%
    kable(digits = c(4, 4, 0, 0))
```

r.squared	adj.r.squared	AIC	BIC
0.0826	0.0811	33466	33516

Subset of Variables to be used in our models 2 and 4

```
fram_sub <- fram_10 %>%
    select(sbp, glucose, obese, educ, smoker)

miss_var_summary(fram_sub)

# A tibble: 5 x 3
   variable n miss pct miss
```

Create multiple imputations for this subset

```
set.seed(4322020)
fram_mice24 <- mice(fram_sub, m = 20)</pre>
```

```
iter imp variable
 1
       glucose
                obese
                       educ
       glucose obese
                       educ
       glucose obese
                       educ
 1
       glucose obese
                       educ
 1
       glucose obese
                       educ
 1
       glucose obese
                       educ
       glucose obese
                       educ
    8
      glucose obese
                       educ
       glucose obese
                       educ
    10
        glucose obese educ
    11
        glucose obese educ
    12
        glucose obese educ
        glucose
                 obese
                        educ
```

Summary Information about Imputation Process

```
summary(fram_mice24)
```

```
Class: mids
Number of multiple imputations:
Imputation methods:
     sbp glucose obese educ smoker
            "pmm" "polyreg"
                                        11 11
PredictorMatrix:
      sbp glucose obese educ smoker
sbp
glucose
obese 1 1
educ 1
smoker
```

Run Model 2 on each imputed data frame

```
m2_mods <- with(fram_mice24, lm(sbp ~ glucose + obese))
summary(m2_mods)</pre>
```

```
# A tibble: 60 x 5
           estimate std.error statistic p.value
  term
  <chr>
             <dbl>
                    <dbl>
                            <dbl>
                                   <dbl>
1 (Intercept) 122. 1.17 104. 0.
        0.111 0.0137 8.10 7.07e-16
2 glucose
3 obese
        13.4
                    0.986 13.6 4.54e-41
                   1.16 104. 0.
4 (Intercept) 121.
5 glucose 0.120
                    0.0136
                             8.78 2.32e-18
6 obese 13.2
                    0.984
                            13.4 2.13e-40
7 (Intercept) 122.
                    1.17
                           104. 0.
8 glucose
        0.108
                    0.0136 7.89 3.90e-15
                    0.984 13.7 6.50e-42
9 obese
       13.5
10 (Intercept) 121.
                    1.18
                           103. 0.
# ... with 50 more rows
```

Pool Results across the 20 imputations

```
m2_pool <- pool(m2_mods)</pre>
summary(m2 pool, conf.int = TRUE, conf.level = 0.95)
             estimate std.error statistic df
(Intercept) 121.1956852 1.24145482 97.62392 1251.744
glucose
       0.1154547 0.01466823 7.87107 1050.433
obese 13.2926318 0.99045467 13.42074 4115.498
              p.value 2.5 % 97.5 %
(Intercept) 0.00000e+00 118.7601235 123.631247
glucose 8.65974e-15 0.0866723 0.144237
      0.00000e+00 11.3508052 15.234458
obese
```

Model 2 (Complete Cases vs. Multiple Imputation)

tidy(m2_cc, conf.int = TRUE) %>% kable(digits = 3)

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	121.671	1.244	97.792	0	119.232	124.110
glucose	0.111	0.015	7.577	0	0.082	0.139
obese	13.532	1.045	12.954	0	11.484	15.580

```
summary(m2_pool, conf.int = TRUE, conf.level = 0.95) %>%
select(-df) %>% kable(digits = 3)
```

	estimate	std.error	statistic	p.value	2.5 %	97.5 %
(Intercept)	121.196	1.241	97.624	0	118.760	123.631
glucose	0.115	0.015	7.871	0	0.087	0.144
obese	13.293	0.990	13.421	0	11.351	15.234

More Details on Multiple Imputation Modeling

m2_pool

```
Class: mipo m = 20
              estimate
                              ubar
                                               b
(Intercept) 121.1956852 1.3856592382 1.481436e-01
             0.1154547 0.0001906054 2.338243e-05
glucose
obese
            13.2926318 0.9718971045 8.669863e-03
                      t dfcom
                                    df
(Intercept) 1.5412100706 4235 1251.744 0.112257637
glucose
           0.0002151569 4235 1050.433 0.128808274
           0.9810004604 4235 4115.498 0.009366584
obese
                lambda
                               fmi
(Intercept) 0.100927729 0.102360806
           0.114109966 0.115791878
glucose
obese
           0.009279665 0.009760773
```

fmi = fraction of missing information due to nonresponse

Model 4 run on each imputed data frame

```
# A tibble: 140 x 5
               estimate std.error statistic p.value
  term
  <chr>
                 <dbl>
                          <dbl>
                                   <dbl>
                                           <dbl>
1 (Intercept) 127.
                         1.29
                                   98.4 0.
2 glucose
                 0.102
                        0.0135
                                   7.54 5.62e-14
                11.9
                         0.985
                                   12.0 6.82e-33
3 obese
                -4.42
                         0.656
4 smoker
                                   -6.74 1.80e-11
5 educHS grad -3.70
                         0.780
                                   -4.75 2.10e- 6
6 educSome Coll -5.34
                         0.945
                                   -5.65 1.68e- 8
7 educColl grad -6.21
                         1.09
                                   -5.70 1.26e- 8
8 (Intercept) 127.
                         1.29
                                   98.5 0.
                 0.112
                         0.0135
                                   8.31 1.28e-16
9 glucose
10 obese
                11.7
                         0.984
                                   11.9 3.71e-32
```

Pool Results across the five imputations

```
m4_pool <- pool(m4_mods)
summary(m4_pool, conf.int = TRUE, conf.level = 0.95)</pre>
```

```
estimate std.error statistic df
(Intercept)
             126.9270253 1.3588718 93.406183 1571.582
glucose
              0.1075469 0.0145208 7.406405 1064.584
obese
         11.7897138 0.9896541 11.912964 4146.672
smoker -4.4254492 0.6561702 -6.744362 4213.845
educHS grad -3.6929816 0.7939553 -4.651372 3139.413
educSome Coll -5.2738134 0.9571700 -5.509798 3704.931
educColl grad -6.1994411 1.0983288 -5.644431 3830.221
                               2.5 %
                 p.value
                                         97.5 %
(Intercept)
            0.000000e+00 124.26163280 129.5924178
glucose
            2.633449e-13 0.07905428 0.1360396
            0.000000e+00 9.84946106 13.7299665
obese
smoker 1.745493e-11 -5.71188874 -3.1390097
educHS grad 3.433553e-06 -5.24970562 -2.1362576
educSome Coll 3.837089e-08
                          -7.15044529 -3.3971816
```

Complete Cases Result (Model 4)

```
tidy(m4_cc, conf.int = TRUE) %>% select(-statistic) %>%
   kable(digits = 3)
```

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	127.107	1.388	0	124.385	129.829
glucose	0.106	0.015	0	0.078	0.135
obese	12.304	1.066	0	10.213	14.395
smoker	-4.704	0.699	0	-6.075	-3.332
educHS grad	-3.698	0.833	0	-5.332	-2.065
educSome Coll	-4.724	1.010	0	-6.704	-2.744
educColl grad	-5.954	1.158	0	-8.225	-3.683

Multiple Imputation Result (Model 4)

```
summary(m4_pool, conf.int = TRUE) %>%
select(-statistic, -df) %>% kable(digits = 3)
```

	estimate	std.error	p.value	2.5 %	97.5 %
(Intercept)	126.927	1.359	0	124.262	129.592
glucose	0.108	0.015	0	0.079	0.136
obese	11.790	0.990	0	9.849	13.730
smoker	-4.425	0.656	0	-5.712	-3.139
educHS grad	-3.693	0.794	0	-5.250	-2.136
educSome Coll	-5.274	0.957	0	-7.150	-3.397
educColl grad	-6.199	1.098	0	-8.353	-4.046

More Details on Multiple Imputation Modeling

m4_pool

```
Class: mipo
                 = 20
                 estimate
                                  ubar
                                                  h
              126.9270253 1.6900562422 0.1490250146
(Intercept)
                0.1075469 0.0001870152 0.0000227033
glucose
obese
               11.7897138 0.9721197883 0.0069480605
smoker
               -4.4254492 0.4295449894 0.0009660582
               -3.6929816 0.6069005757 0.0223471066
educHS grad
educSome Coll
               -5.2738134 0.8950889474 0.0200814547
educColl grad
               -6.1994411 1.1828536383 0.0223547953
                         t dfcom
                                       df
                                                  riv
(Intercept)
              1.8465325075 4231 1571.582 0.092586425
              0.0002108536 4231 1064.584 0.127468096
glucose
              0.9794152518 4231 4146.672 0.007504696
obese
smoker
              0.4305593505 4231 4213.845 0.002361478
              0.6303650376
                            4231 3139,413 0,038662778
educHS grad
                            4231 3704.931 0.023556907
educSome Coll
              0.9161744748
```

Estimate R^2 or adjusted R^2 ?

```
pool.r.squared(m2 mods)
          est lo 95 hi 95 fmi
R^2 0.05923026 0.04601681 0.07387826 NaN
pool.r.squared(m2_mods, adjusted = TRUE)
             est lo 95 hi 95 fmi
adj R^2 0.05878594 0.04561876 0.07339091 NaN
pool.r.squared(m4 mods)
          est lo 95 hi 95 fmi
R^2 0.08144661 0.0661401 0.09804029 NaN
pool.r.squared(m4 mods, adjusted = TRUE)
             est lo 95 hi 95 fmi
```

adj R^2 0.08014394 0.06494473 0.09663925 NaN

Compare Model 4 to Model 2 after imputation

The models must be nested for this to be appropriate. We'll use the Wald test after a linear regression fit.

```
[,1]
[1,] 0
```

Section 3

Setting 2: Logistic Model for chd10

Model 3 (CC): Three-predictor model for chd10

Suppose we ignore the missingness and just run the model on the data with complete information on glucose, bp_meds and cigs.

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	0.063	0.151	0	0.046	0.084
glucose	1.011	0.002	0	1.007	1.014
bp_meds	2.736	0.211	0	1.791	4.105
cigs	1.015	0.004	0	1.007	1.022

Model 6 (CC): Six-predictor model for chd10

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	0.012	0.410	0.000	0.005	0.026
glucose	1.009	0.002	0.000	1.006	1.013
bp_meds	2.418	0.217	0.000	1.564	3.676
cigs	1.016	0.004	0.000	1.009	1.023
educHS grad	0.595	0.117	0.000	0.472	0.747
educSome Coll	0.634	0.144	0.001	0.475	0.835
educColl grad	0.753	0.157	0.070	0.550	1.017
chol	1.005	0.001	0.000	1.003	1.007
bmi	1.034	0.011	0.003	1.012	1.057

Subset of Variables to be used in our models 3 and 6

Create multiple imputations for this subset

```
set.seed(432202036)
fram_mice36 <- mice(fram_sub36, m = 10)</pre>
```

```
imp variable
1
       glucose
                bp_meds
                          cigs
                                educ
                                      chol
                                            bmi
1
       glucose
                bp meds
                          cigs
                                educ
                                      chol
                                            bmi
1
    3
                          cigs educ
       glucose
                bp meds
                                      chol
                                            bmi
1
       glucose
                bp meds
                          cigs educ
                                      chol
                                            bmi
1
                          cigs
    5
       glucose
                bp meds
                                educ
                                      chol
                                            bmi
1
       glucose
                bp meds
                          cigs
                                educ
                                      chol
                                            bmi
1
       glucose
                bp meds
                          cigs
                                educ
                                      chol
                                            bmi
1
    8
       glucose
                bp_meds
                          cigs
                                educ
                                      chol
                                            bmi
       glucose
                bp_meds
                          cigs
                                educ
                                      chol
                                            bmi
1
    10
                                 educ
                                       chol
                                              bmi
        glucose
                 bp_meds
                           cigs
       glucose
                bp_meds
                          cigs
                                educ
                                      chol
                                            bmi
2
                bp_meds
                          cigs
                                educ
                                      chol
       glucose
                                            bmi
       glucose
                bp meds
                          cigs
                                educ
                                      chol
                                            bmi
```

Summary information about Imputation Process

summary(fram_mice36)

```
Class: mids
Number of multiple imputations:
                                   10
Imputation methods:
    chd10
            glucose bp_meds
                                     cigs
                                                educ
                                                          chol
               "mmm"
                         "pmm"
                                    "pmm" "polyreg"
                                                          "mmq"
      bmi
    "pmm"
PredictorMatrix:
        chd10 glucose bp_meds cigs educ chol bmi
chd10
glucose
bp_meds
cigs
educ
chol
```

Run Model 3 on each imputed data frame

	term	estimate	std.error	statistic	p.value
	<chr></chr>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
1	(Intercept)	-2.89	0.147	-19.7	1.87e-86
2	glucose	0.0117	0.00156	7.52	5.68e-14
3	bp_meds	1.05	0.201	5.23	1.71e- 7
4	cigs	0.0151	0.00343	4.38	1.16e- 5
5	(Intercept)	-2.72	0.138	-19.7	3.03e-86
6	glucose	0.00974	0.00146	6.68	2.39e-11
7	bp_meds	1.06	0.198	5.34	9.35e- 8
8	cigs	0.0148	0.00344	4.30	1.73e- 5
9	(Intercept)	-2.85	0.148	-19.3	5.08e-83
10	glucose	0.0112	0.00157	7.11	1.15e-12

Pool Results across the 10 imputations

	estimate	std.error	statistic	p.value	2.5 %	97.5 %
(Intercept)	0.061	0.156	-17.99	0	0.045	0.082
glucose	1.011	0.002	6.35	0	1.007	1.014
bp_meds	2.865	0.202	5.21	0	1.927	4.259
cigs	1.015	0.003	4.41	0	1.008	1.022

Comparing Model 3 Results Complete Cases

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	0.063	0.151	0	0.046	0.084
glucose	1.011	0.002	0	1.007	1.014
bp_meds	2.736	0.211	0	1.791	4.105
cigs	1.015	0.004	0	1.007	1.022

After Multiple Imputation

	estimate	std.error	p.value	2.5 %	97.5 %
(Intercept)	0.061	0.156	0	0.045	0.082
glucose	1.011	0.002	0	1.007	1.014
bp_meds	2.865	0.202	0	1.927	4.259
cigs	1.015	0.003	0	1.008	1.022

Run Model 6 on each imputed data frame

```
m6 mods <- with(fram mice36, glm(chd10 ~ glucose +
               bp meds + cigs + educ + chol + bmi,
                    family = binomial))
summary(m6 mods)
```

```
# A tibble: 90 x 5
              estimate std.error statistic p.value
  term
  <chr>
                <dbl> <dbl>
                                  <dbl>
                                         <dbl>
                                -11.3 1.23e-29
1 (Intercept) -4.29 0.379
2 glucose
         0.0109 0.00154 7.04 1.92e-12
         0.917 0.205 4.47 7.91e- 6
3 bp meds
         0.0166 0.00344 4.82 1.47e- 6
4 cigs
                               -5.02 5.18e- 7
5 educHS grad -0.547
                      0.109
6 educSome Coll -0.443
                      0.133
                                  -3.33 8.61e- 4
                                  -1.68 9.29e- 2
7 educColl grad -0.245
                      0.146
8 chol
               0.00417
                      0.000952
                                  4.38 1.16e- 5
9 bmi
               0.0270
                      0.0106
                                  2.56 1.05e- 2
  (Intercept)
              -4.19
                      0.376
                                 -11.1 7.78e-29
```

Pool Results across the 10 imputations

	estimate	std.error	statistic	p.value	2.5 %	97.5 %
(Intercept)	0.013	0.384	-11.23	0.00	0.006	0.028
glucose	1.010	0.002	6.03	0.00	1.007	1.013
bp_meds	2.510	0.207	4.45	0.00	1.674	3.764
cigs	1.017	0.003	4.87	0.00	1.010	1.024
educHS grad	0.591	0.110	-4.76	0.00	0.476	0.734
educSome Coll	0.675	0.134	-2.93	0.00	0.519	0.879
educColl grad	0.811	0.147	-1.42	0.15	0.608	1.082
chol	1.004	0.001	4.40	0.00	1.002	1.006
bmi	1.031	0.011	2.84	0.00	1.009	1.052

Comparing Model 6 Results

Complete Cases

term	estimate	std.error	p.value	conf.low	conf.high
(Intercept)	0.012	0.410	0.000	0.005	0.026
glucose	1.009	0.002	0.000	1.006	1.013
bp_meds	2.418	0.217	0.000	1.564	3.676
cigs	1.016	0.004	0.000	1.009	1.023
educHS grad	0.595	0.117	0.000	0.472	0.747
educSome Coll	0.634	0.144	0.001	0.475	0.835
educColl grad	0.753	0.157	0.070	0.550	1.017
chol	1.005	0.001	0.000	1.003	1.007
bmi	1.034	0.011	0.003	1.012	1.057

Comparing Model 6 Results

After Multiple Imputation

	estimate	std.error	p.value	2.5 %	97.5 %
(Intercept)	0.013	0.384	0.000	0.006	0.028
glucose	1.010	0.002	0.000	1.007	1.013
bp_meds	2.510	0.207	0.000	1.674	3.764
cigs	1.017	0.003	0.000	1.010	1.024
educHS grad	0.591	0.110	0.000	0.476	0.734
educSome Coll	0.675	0.134	0.003	0.519	0.879
educColl grad	0.811	0.147	0.155	0.608	1.082
chol	1.004	0.001	0.000	1.002	1.006
bmi	1.031	0.011	0.005	1.009	1.052

Compare Model 6 to Model 3 after imputation

Again, these models need to be nested. We'll use the likelihood ratio test after a logistic regression fit.

[1] 8.610224e-12

Pitfalls When Using Multiple Imputation (Sterne et al.)

Omitting the outcome variable from the imputation procedure

Often an analysis explores the association between one or more predictors and an outcome but some predictors have missing values.

- Here, the outcome carries information about the missing values of the predictors and this information must be used.
- Consider a model relating systolic blood pressure to time to coronary heart disease, fitted to data that have some missing values of systolic blood pressure.
 - When missing systolic blood pressure values are imputed, individuals who develop coronary heart disease should have larger values, on average, than those who remain disease free.
 - Failure to include the coronary heart disease outcome and time to this
 outcome when imputing the missing systolic blood pressure values would
 falsely weaken the association between systolic blood pressure and
 coronary heart disease.

Pitfalls When Using Multiple Imputation (Sterne et al.)

Dealing with non-normally distributed variables

Many multiple imputation procedures assume that data are normally distributed, so including non-normally distributed variables may introduce bias.

- A pragmatic approach here is to transform such variables to approximate normality before imputation and then transform the imputed values back to the original scale.
- Different problems arise when data are missing in binary or categorical variables. Some procedures handle these types of missing data better than others.

Options within mice for imputation approaches

Default methods include:

- pmm predictive mean matching (default choice for quantitative variables)
- logreg logistic regression (default for binary categorical variables)
- polyreg polytomous logistic regression (for nominal multi-categorical variables)
- polr proportional odds logistic regression (for ordinal categories)

but there are cart methods and many others available, too.

Pitfalls When Using Multiple Imputation (Sterne et al.)

Plausibility of missing at random assumption

- For example, the missing at random assumption may be reasonable if a variable that is predictive of missing data in a covariate of interest is included in the imputation model, but not if the variable is omitted from the model.
- Multiple imputation analyses will avoid bias only if enough variables predictive of missing values are included in the imputation model.
- It is sensible to include a wide range of variables in imputation models, including all variables in the substantive analysis, plus, as far as computationally feasible, all variables predictive of the missing values themselves and all variables influencing the process causing the missing data.

Guidelines for reporting, I (Sterne et al.)

How should we report on analyses potentially affected by missing data?

- Report the number of missing values for each variable of interest, or the number of cases with complete data for each important component of the analysis. Give reasons for missing values if possible, and indicate how many individuals were excluded because of missing data when reporting the flow of participants through the study. If possible, describe reasons for missing data in terms of other variables (rather than just reporting a universal reason such as treatment failure.)
- Clarify whether there are important differences between individuals
 with complete and incomplete data—for example, by providing a table
 comparing the distributions of key exposure and outcome variables in
 these different groups
- Describe the type of analysis used to account for missing data (eg, multiple imputation), and the assumptions that were made (eg, missing at random)

Guidelines for reporting, II (Sterne et al.)

How should we report on analyses that involve multiple imputation?

- Provide details of the imputation modeling (software used, key settings, number of imputed datasets, variables included in imputation procedure, etc.)
- If a large fraction of the data is imputed, compare observed and imputed values.
- Where possible, provide results from analyses restricted to complete cases, for comparison with results based on multiple imputation. If there are important differences between the results, suggest explanations.
- It is also desirable to investigate the robustness of key inferences to possible departures from the missing at random assumption, by assuming a range of missing not at random mechanisms in sensitivity analyses.

Next Up

- Minute Paper after Class 12 due Wednesday at 2 PM
- For those of you who still need to do work on your proposal, the next revision deadline is 9 AM Wednesday
- You'll have access to Quiz 1 at 5 PM Wednesday
- No class Thursday. Next Tuesday's class will be about ridge regression and the lasso.