

New Results Concerning Collective Motion in Triaxial Nuclei

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Table of Contents

1 Nuclear Shapes

Nuclear Deformation

Most of the nuclei are either *spherical* or *axially symmetric* in their ground-state.

Deformation parameter β (*Bohr, 1969*): preserves axial symmetry



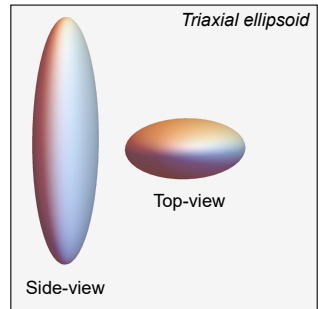
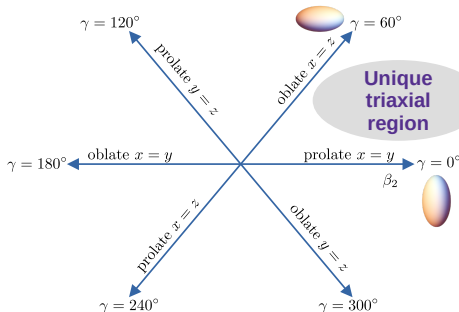
Figure 1: **spherical:** $\beta = 0$ **prolate:** $\beta > 0$ **oblate:** $\beta < 0$

Nuclear Triaxiality

Non-axial shape

Deviations from symmetric shapes can occur across the chart of nuclides → **triaxial nuclei**.

The triaxiality parameter γ (*Bohr, 1969*): departure from axial symmetry



Fingerprints for Triaxiality

- Experimentally, stable triaxial nuclei represent a real challenge
- Clear signatures for confirming stable triaxiality in nuclei
 - ① Chiral symmetry breaking (*Frauendorf, 1997*)
 - ② **Wobbling motion** (*Bohr & Mottelson, 1975*)

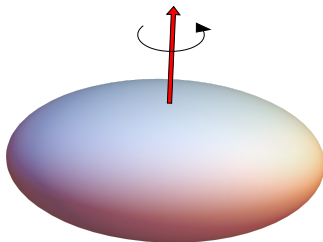
Wobbling Motion (WM)

- Unique to non-axial nuclei
- Predicted 50 years ago for even- A nuclei
- First experimental evidence for ^{163}Lu (*Ødegård, 2001*)
- Currently: confirmed wobblers within the mass regions $A \approx [100, 130, 160, 180]$.

Energy of Deformed Nuclei

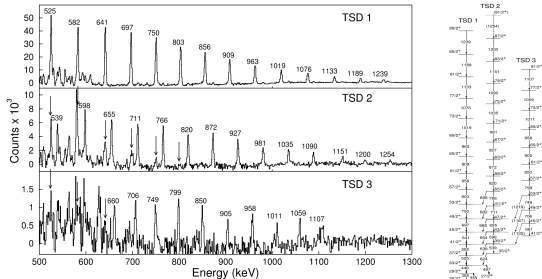
Collective Motion

- A nucleus - *droplet* - can generate angular momentum from the rotation and vibration of the droplet itself
- Each individual nucleon contributes to the total angular momentum \rightarrow *collectiveness*
- **⚠** Rotation can occur only if the nuclear potential is *deformed*



Triaxial Rotor Energy

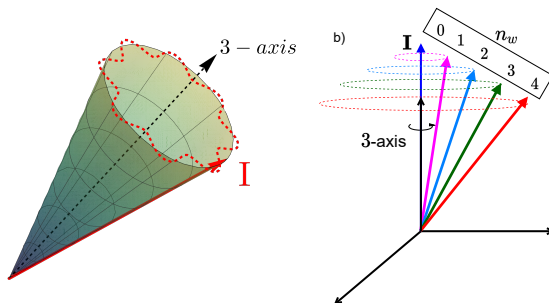
- A triaxial nucleus can rotate about any of the three axes
- Rotation about the axis with **the largest moment of inertia** (MOI) is energetically the most favorable: $E_{\text{rot}} \propto \frac{\hbar^2}{2\mathcal{I}_{\text{max}}} I(I+1)$
- MOI anisotropy \rightarrow the *main rotation* around \mathcal{I}_{max} is disturbed by the other two axes \rightarrow *total motion of the rotating nucleus has an oscillating behavior*



Figures from Ødegård et al., 2001

Wobbling Motion

- Total angular momentum \mathbf{I} disaligned w.r.t. body-fixed axes
- The a.m. **precesses** and **wobbles** around the axis with \mathcal{J}_{\max}
- The precession of \mathbf{I} can increase by **tilting**
- Tilting by an energy quanta \sim *vibrational character* \rightarrow **wobbling phonon** $n_w = 0, 1, 2, \dots$

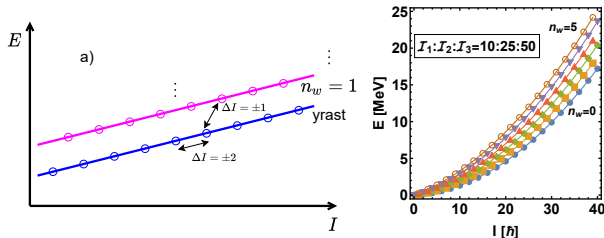


Wobbling Spectrum

Even-A Nuclei

- Employing the Harmonic Approximation (*Bohr, 1969*)
- \hat{H} composed of a *rotational* part and *harmonic oscillation* (i.e., wobbling) part:

$$\hat{H} = \frac{\hbar^2}{2\mathcal{J}_{\max}} I(I+1) + \hbar\omega_{\text{wob}} \left(n_w + \frac{1}{2} \right), \quad n = 0, 1, 2, \dots \quad (1)$$



New Results for $A=130$

Recent findings for even-even nuclei

- Two wobbling bands have been identified experimentally in ^{130}Ba (*Petrache et al., 2019*)
- DFT+PRM description of the wobbling motion described the excited spectra (*Chen et al., 2019*)
- Stable triaxiality for $\beta = 0.24$ and $\gamma = 21.5^\circ$
- Infer spin-dependence for $\mathcal{I}_{1,2,3}$

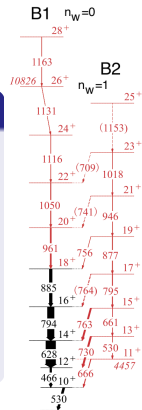


Figure from Petrache et al., 2019

New Results for $A=130$ II

Harmonic Approximation

- Employed an energy spectrum of harmonic type according to Eq. 1:

$$E_{I,n_w} = \frac{\hbar^2}{2\mathcal{J}_3} I(I+1) + \hbar\omega_{\text{wob}}(n_w + \frac{1}{2}) \quad (2)$$

- wobbling frequency - linear dependence on I (fixed MOI ordering $\mathcal{J}_3 > \mathcal{J}_{1,2}$)

$$\hbar\omega_{\text{wob}}(I) = 2f(\mathcal{J}_1, \mathcal{J}_2, \mathcal{J}_3) \cdot I \quad (3)$$

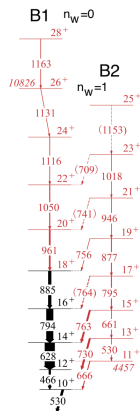


Figure from Petrache et al., 2019

New Results for A=130 III

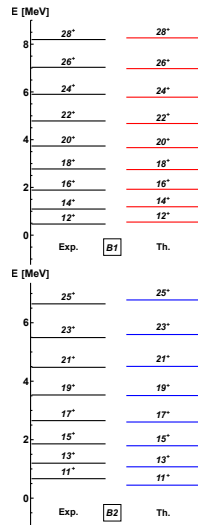
Harmonic Approximation

- Reproduced the excited spectra for $\{B1, B2\}$
- Fix a *free parameter set*: $\mathcal{P} = [\mathcal{J}_1, \mathcal{J}_2, \mathcal{J}_3]$
- Adopt a fitting procedure:

$$\chi^2 = \frac{1}{N_T} \sum_{i=1}^{N_T} \frac{\left(E_{\text{exp}}^{(i)} - E_{\text{th}}^{(i)}\right)^2}{E_{\text{exp}}^{(i)}} \quad (4)$$

Results for ^{130}Ba PRELIMINARY!

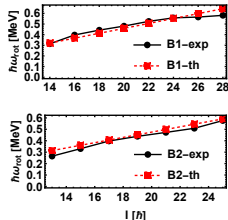
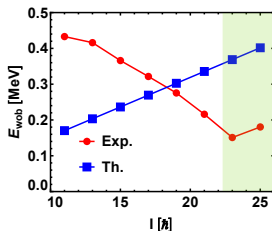
$\mathcal{J}_1^{\text{fit}}$	$\mathcal{J}_2^{\text{fit}}$	$\mathcal{J}_3^{\text{fit}}$	$[\hbar^2 \text{MeV}^{-1}]$
27	22	43	



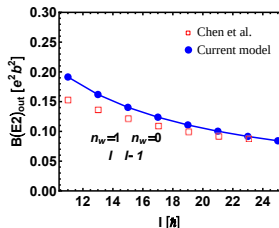
Poenaru, 2022, unpublished

New Results for $A=130$ IV

- **Left:** Wobbling energy* $E_{\text{wob}}(I) = E_{B2}(I) - E_{B1}(I)$
- **Center:** Rotational frequency $\hbar\omega_{\text{rot}}$ - collective
- **Right:** Interband transition probabilities $I_{B2} \rightarrow I_{B1}$



Poenaru, 2022, unpublished



Electromagnetic transitions

Even- A nuclei conclusions

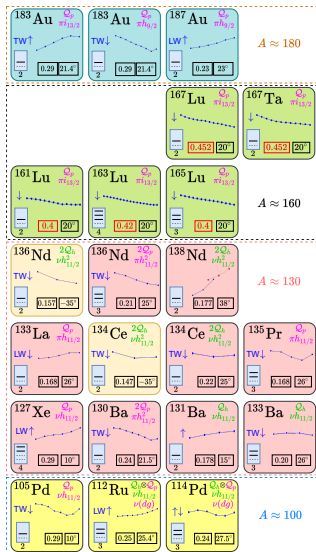
- Deformation parameters $\beta = 0.24$ and $\gamma = 21.5^\circ$ were adopted for *quadrupole moments* and *transition probabilities*
- PRM values are calculated by Chen et al through a similar approach of minimizing the χ^2 -function
- Main rotation occurs along 3-axis
- Approximation only reproduces E_{wob} in the high-spin limit

I	$B(E2)_{\text{out}}/B(E2)_{\text{in}}$		
	Th.	PRM*	Exp.
11	0.37	-	-
13	0.32	0.51	0.32
15	0.27	0.42	0.36
17	0.24	0.35	0.22
19	0.21	0.29	0.22
21	0.19	0.25	0.41
23	0.18	-	-
25	0.16	-	-

Poenaru, 2022, unpublished

Wobbling Motion in Odd-Mass Nuclei

Experimental Evidence



Wobbling nuclei (up to date)
Poenaru, 2022, in progress