

# New Data on Wobbling Motion for $A \approx 130$ Mass Region

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# Outline

- 1 Nuclear Triaxiality
- 2 Wobbling Motion in Nuclei
- 3 Current status of nuclear "wobblers"
- 4 Latest findings on  $^{135}\text{Pr}$

# Nuclear Deformation

## Nuclear shapes

Most generally described in terms of the **nuclear radius**:

$$R(\theta, \varphi) = R_0 \left( 1 + \sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda\mu} Y_{\lambda}^{\mu}(\theta, \varphi) \right)$$

## Quadrupole deformations $\lambda = 2$

- Most relevant modes are the **quadrupole vibrations**  $\lambda = 2 \implies$  *Play a crucial role in the rotational spectra of nuclei:*
- $\alpha_{2\mu}$  reduced to only two deformation parameters:  $\beta_2$  (**eccentricity**) and  $\gamma$  (**triaxiality**) (*Bohr and Mottelson, 1969*).

# Axial shapes

- Most of the nuclei are either **spherical** or **axially symmetric** in their ground-state.
- Nuclear moments of inertia  $\mathcal{I}_{1,2,3}$ : only two are equal.

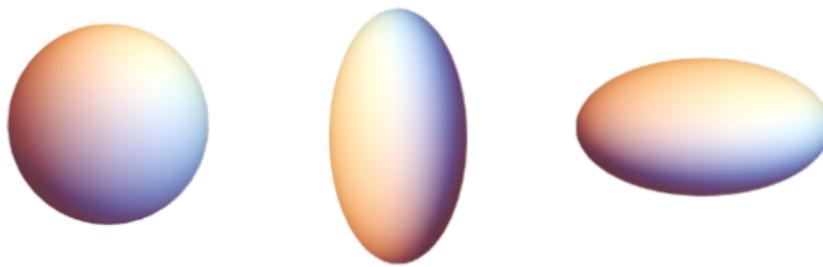
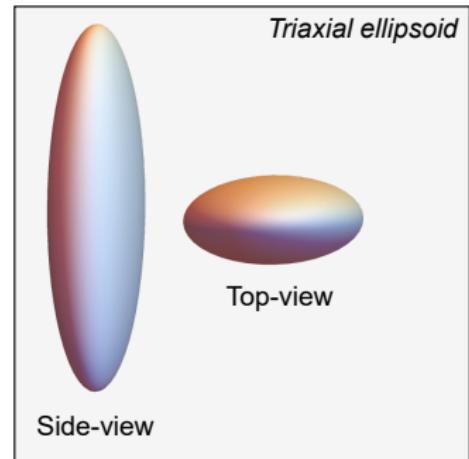
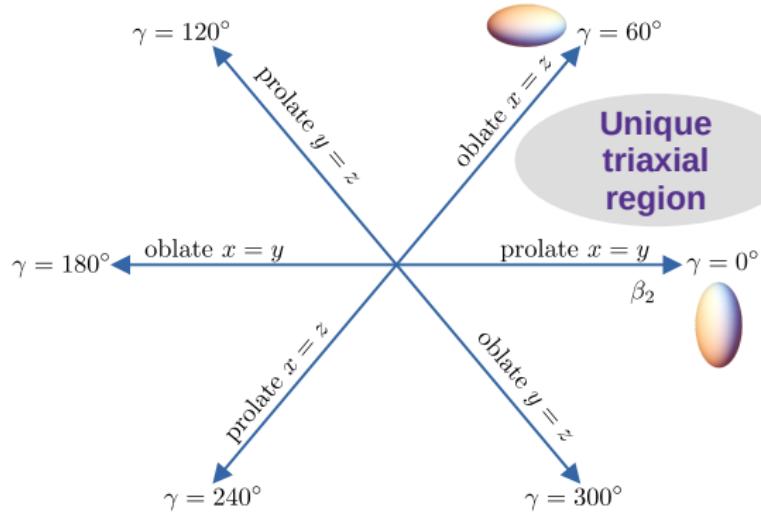


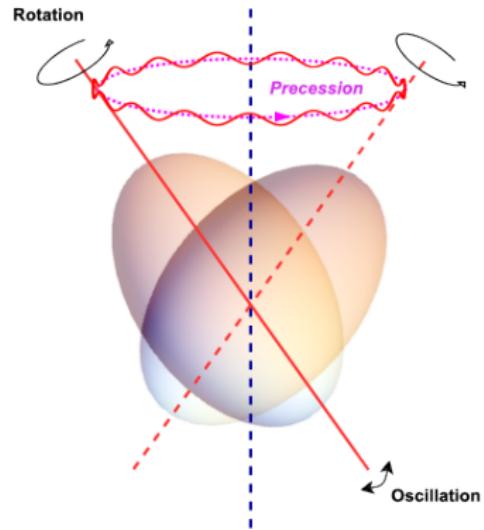
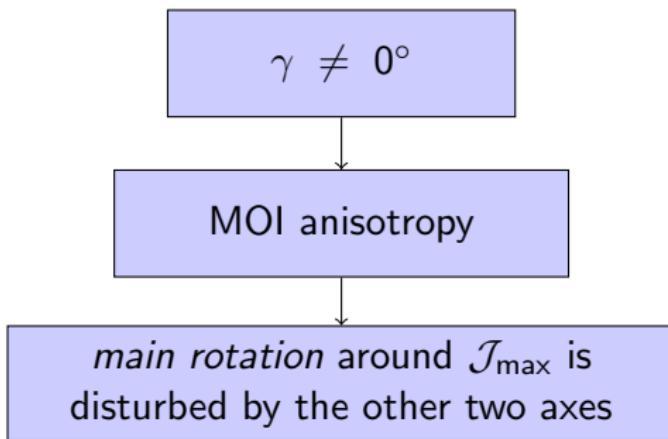
Figure: **spherical**:  $\beta_2 = 0$  **prolate**:  $\beta_2 > 0$  **oblate**:  $\beta_2 < 0$ . ( $\gamma = 0^\circ$ ).

# Non-axial shapes

- The triaxiality parameter  $\gamma \neq 0^\circ$ : departure from axial symmetry.
- Moments of inertia:  $I_1 \neq I_2 \neq I_3$ .



# Wobbling Motion



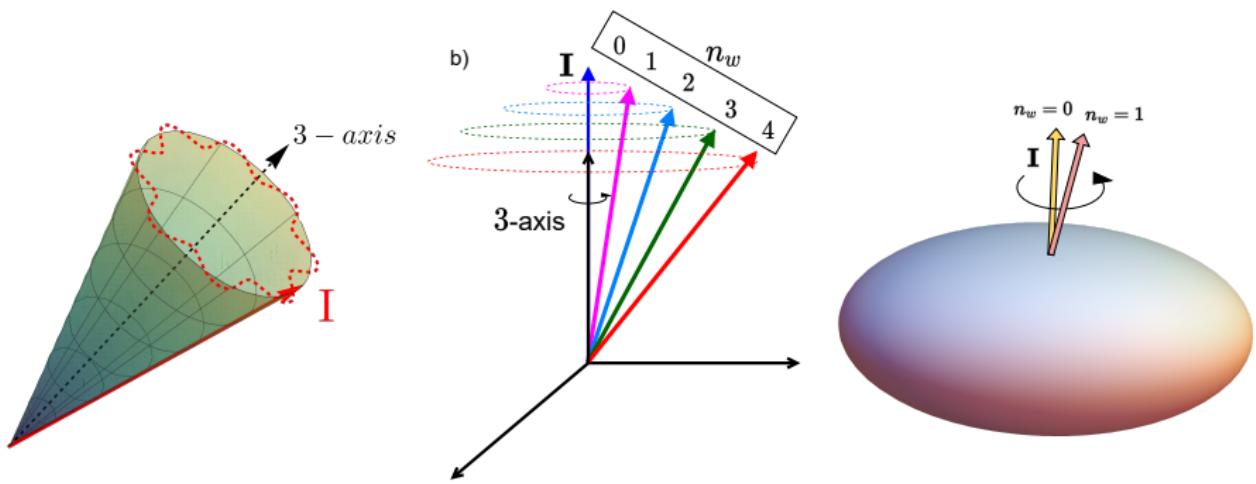
## Wobbling Effect

- The **total angular momentum** of the nucleus **precesses** and **oscillates** around  $J_{\max}$ .

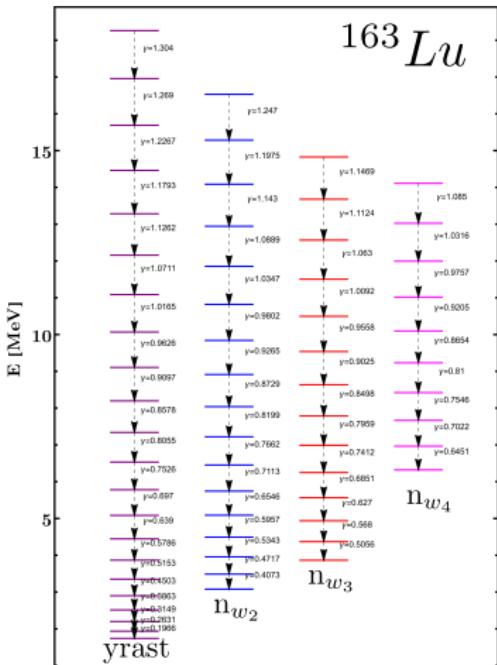
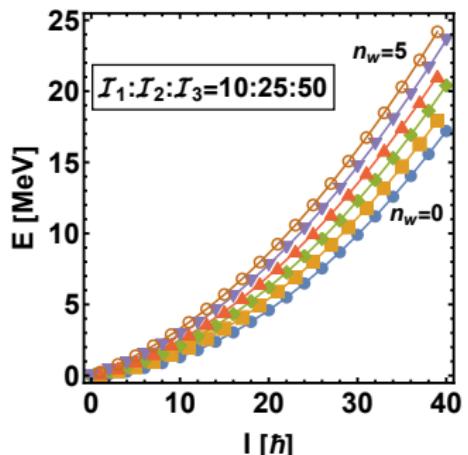
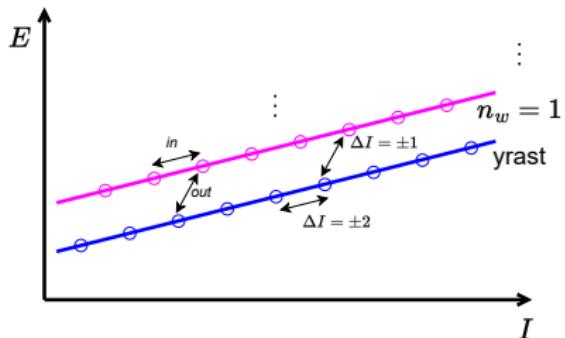
# Wobbling Motion

## Harmonic oscillation

- Precession of  $\mathbf{I}$  is affected by **rotational frequency** and/or **tilting**
- Tilting only by "specific" amount  $\rightarrow$  **harmonic character**  $\rightarrow$  **wobbling phonon**:  $n_w = 0, 1, 2, \dots$



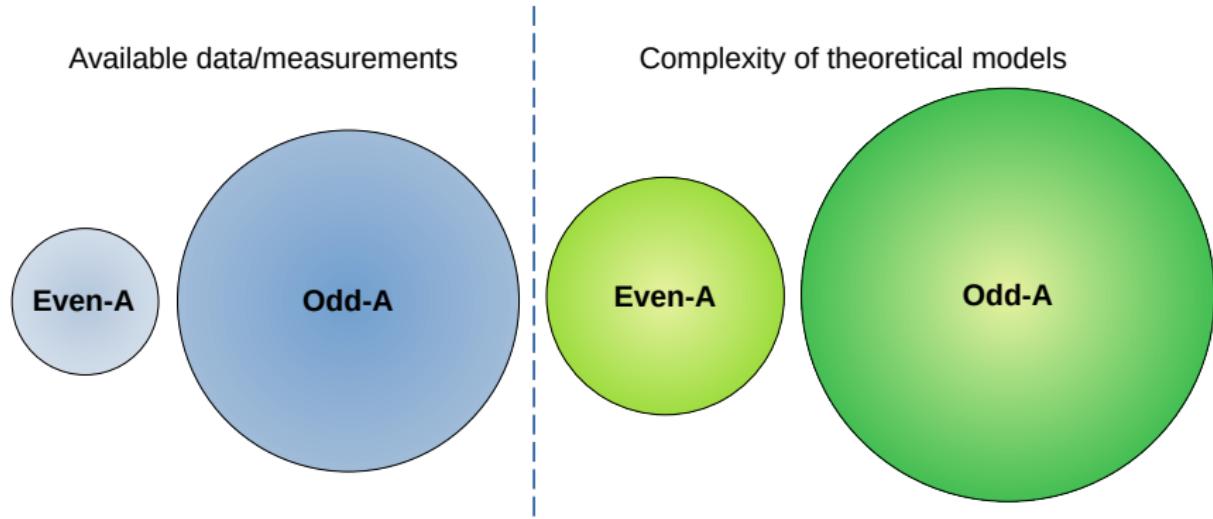
# Wobbling Motion II



R. Poenaru, 2023.

# Even- $A$ vs. Odd- $A$ Picture

- Predicted for even- $A$  nuclei more than 50 years ago.
- First experimental evidence:  $^{163}\text{Lu}$  (*Ødegård, 2001*).
- Current mass-regions for wobblers:  $A \approx [130, 160, 180]$ .



$A \approx 100$ 

## Excitation energies vs. Wobbling Energies:

$$E_{\text{wob}}(I_{\text{even}}) = E_{I,n} - E_{I,0} ,$$

$$E_{\text{wob}}(I_{\text{odd}}) = E_{I,n} - \frac{1}{2} (E_{I-1,0} + E_{I+1,0})$$

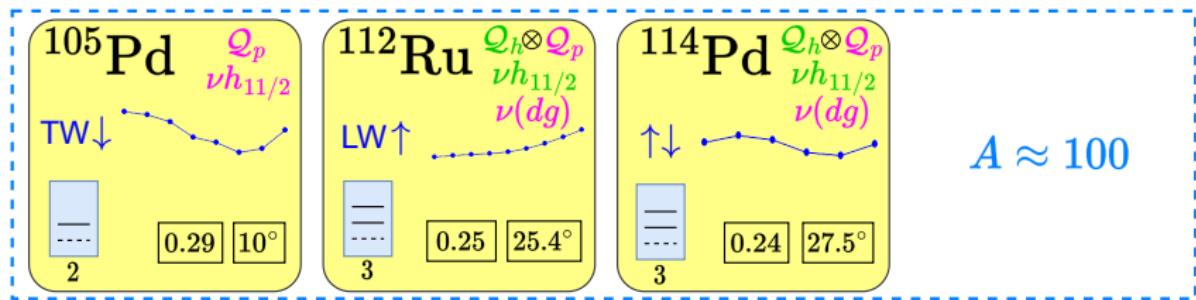


Figure: Experimentally confirmed wobblers, R Poenaru, 2023.

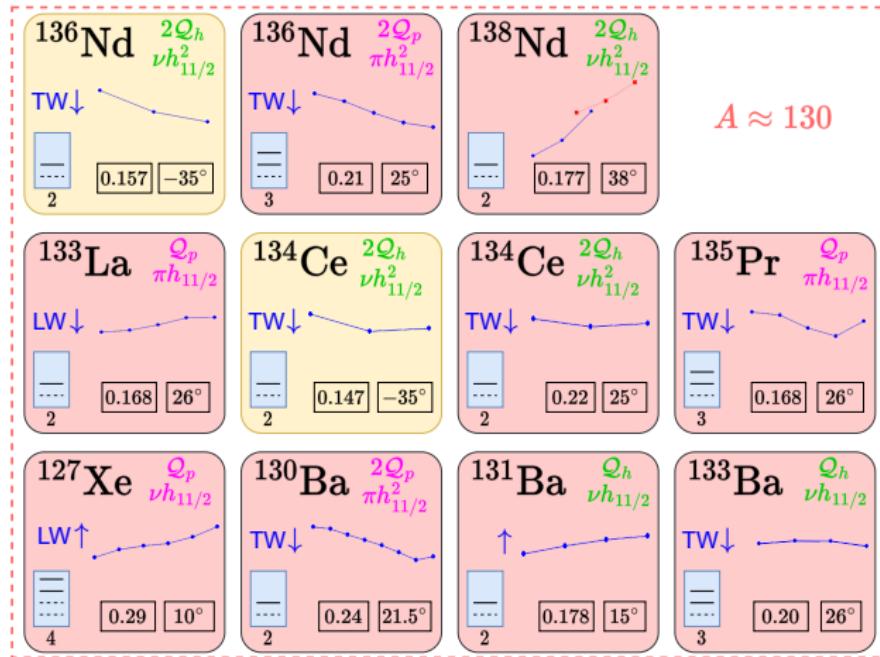
$A \approx 130$ 

Figure: Experimentally confirmed wobblers, R Poenaru, 2023.

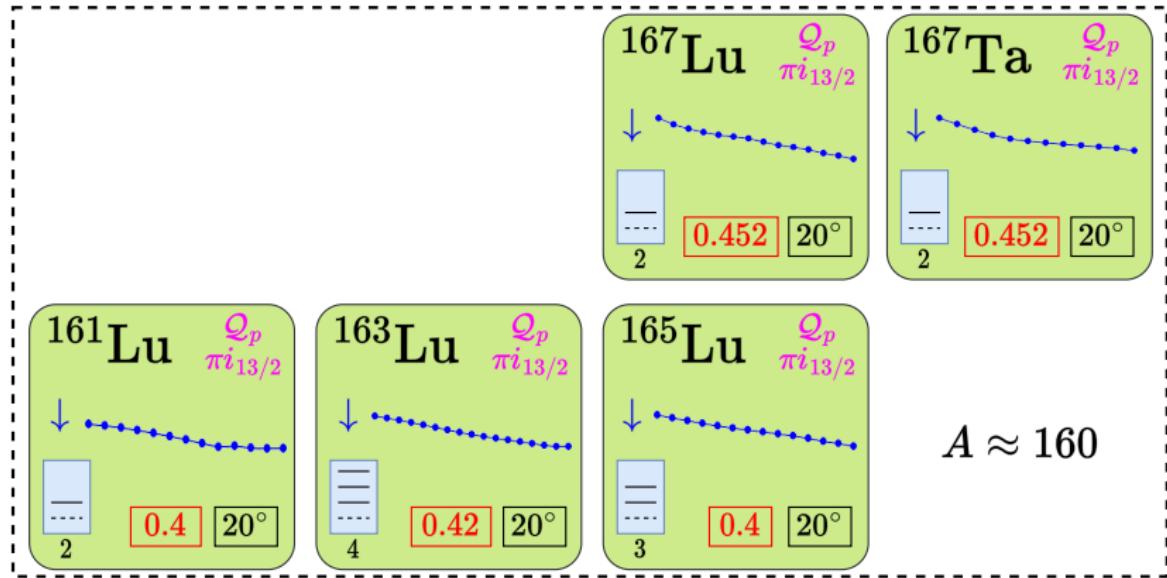
$A \approx 160$ 

Figure: Experimentally confirmed wobblers, R Poenaru, 2023.

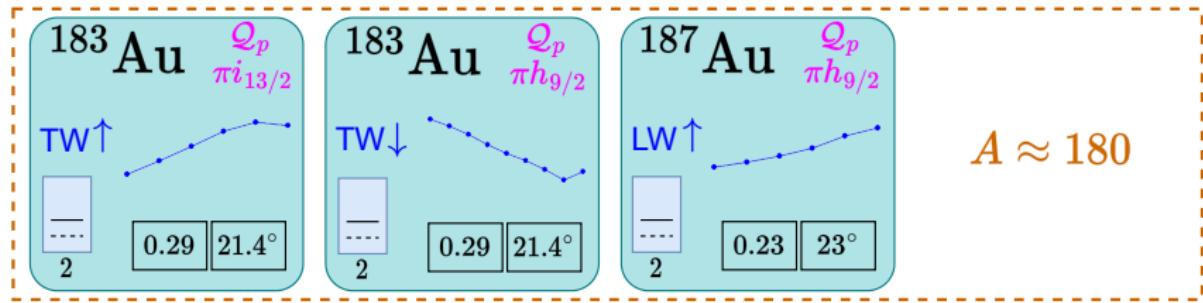
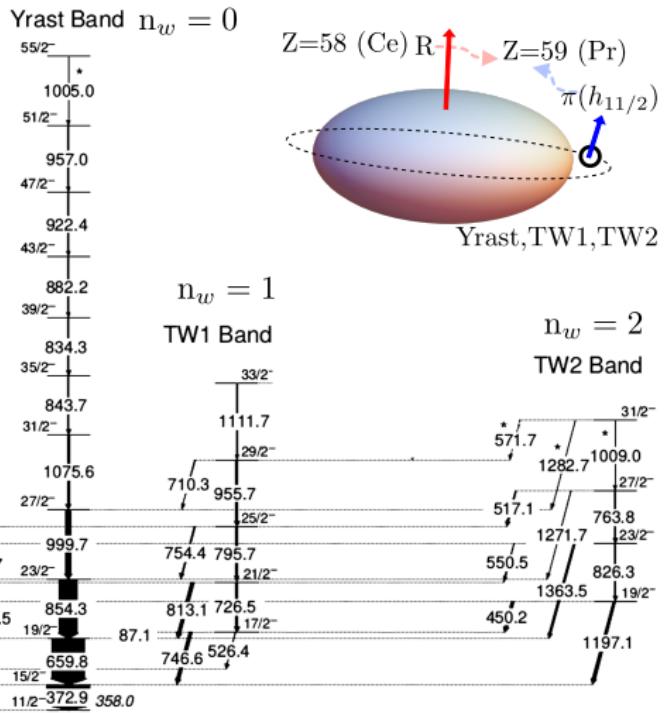
$A \approx 180$ 

Figure: Experimentally confirmed wobblers, R Poenaru, 2023.

# Wobbling Motion in $^{135}\text{Pr}$

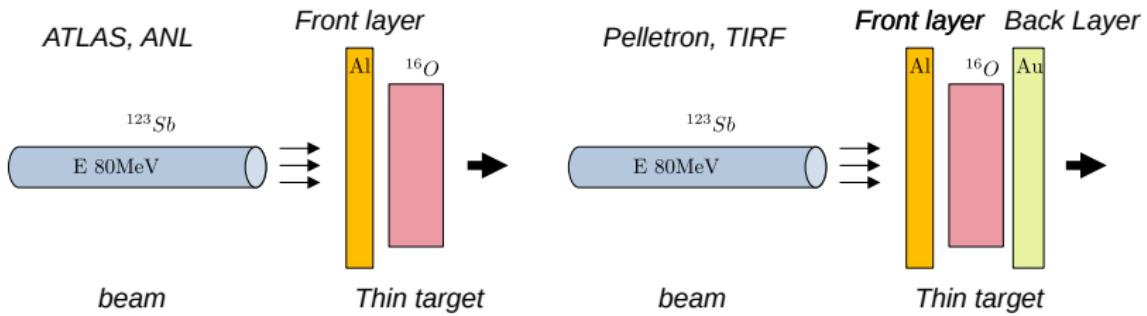
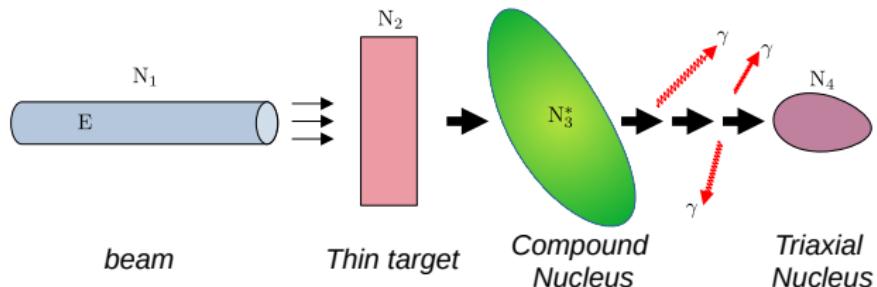
## What we know so far

- Two-wobbling phonon bands were measured (*Matta et. al. 2015 + Sensharma et. al. 2019*)
- Exp. measurements:  
Fusion-Evaporation reactions:  
 $^{123}\text{Sb} ({}^{16}\text{O}, 4n) {}^{135}\text{Pr}$
- **1st round:** ATLAS,  
ANL (USA), **2nd round:**  
Pelletron-TIFR, Mumbai.



# Fusion Evaporation Reactions

**Fusion-evaporation reactions:** Long-lived + enhanced deformation



# Theoretical Framework

## New Boson Method

- A rotor Hamiltonian was used to describe the wobbling spectrum of  $^{135}\text{Pr}$
- $\hat{H}_{\text{rot}} = \sum_{k=1,2,3} A_k (\hat{I}_k - \hat{j}_k)^2$
- The eigenvalues were obtained via a special algebra of the angular momentum operators  $\hat{I}_{\pm,0}$ .
- Using a set of Dyson-like boson operators for the angular momentum representation.

# Results for $^{135}\text{Pr}$

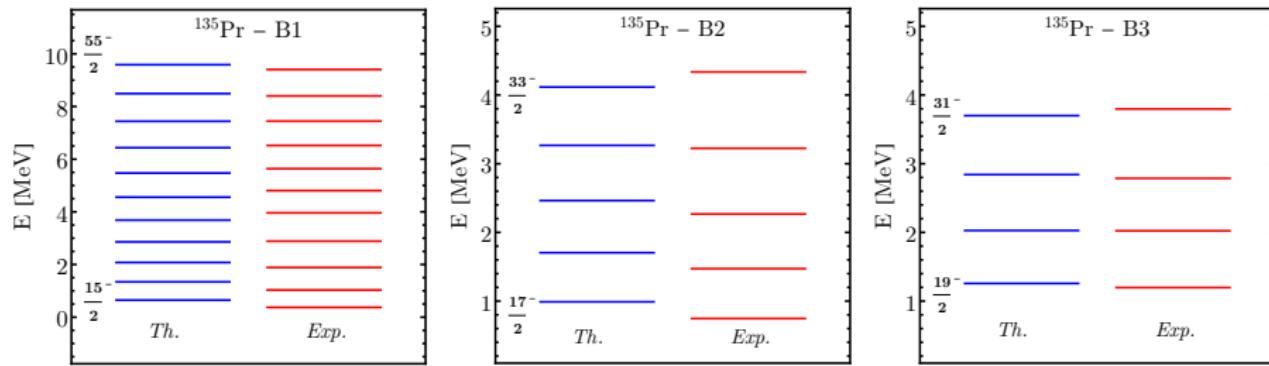


Figure: The excitation energies in  $^{135}\text{Pr}$ . Exp data: *Sensharma, 2019*.

$\mathcal{I}_1$	$\mathcal{I}_2$	$\mathcal{I}_3$	$\theta$ [degrees]	N.o. states	RMS [MeV]
91	9	51	-119	20	0.174

A.A. Raduta, C.M. Raduta, R Poenaru, Journal of Physics G 48, 2020.

# New experiments

Article

## Wobbling Motion in Nuclei

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*Figure:* 26th of April, 2023, *Cited our work from JPG.*

- Performed new measurements on the  $\gamma$  rays emitted during the fusion-evaporation reactions.  $^{100}\text{Mo} (40\text{Ar}, 1p4n) ^{135}\text{Pr}$  ( $E_{\text{beam}} = 152 \text{ MeV}$ )
- University of Jyväskylä, Finland, JUROGAM II spectrometer.

# Key factors

There are some *key values* that can point out a **wobbling character** of a nucleus.

- Mixing ratios ( $|\delta| > 1$ )
- Reduced transition probabilities (mostly E2)
- Quadrupole moments ( $\uparrow$ )

## Contradicting values

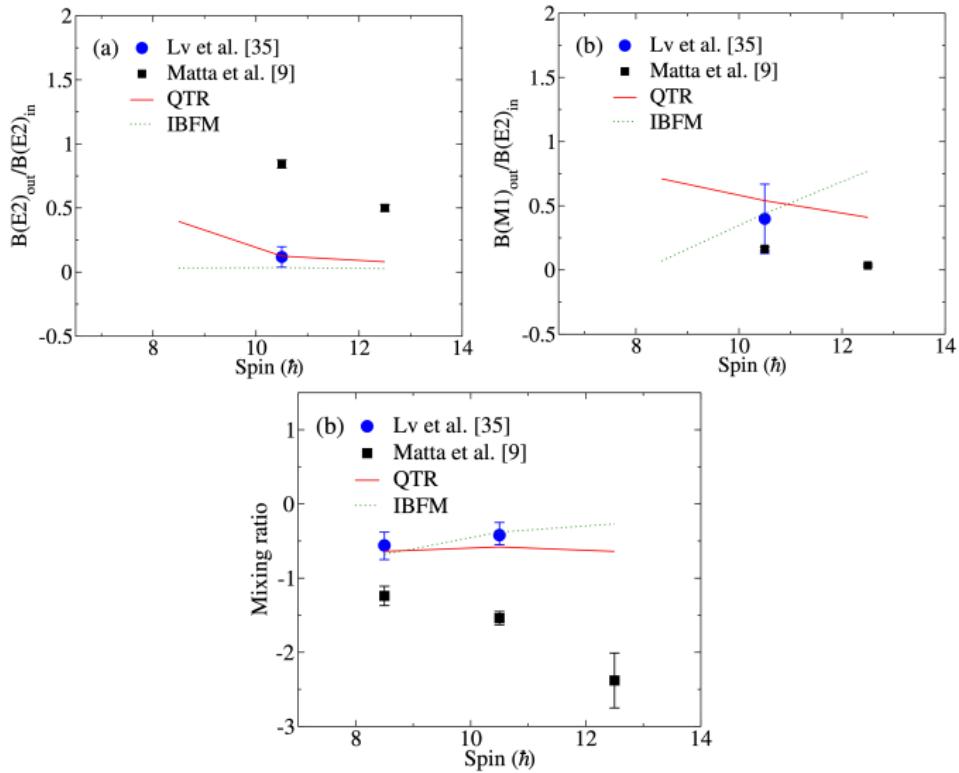
Lv et. al. obtained different experimental values, pointing **against wobbling character**.

- small mixing ratios
- smaller branching ratios
- ...

# Moments of inertia

- Values obtained by Matta et. al.:  $\mathcal{I}_{1,2,3} = 19, 8, 3 \text{ } \hbar^2 \text{MeV}^{-1}$ .  
 $\epsilon = 0.16, \gamma = 26^\circ$ .
- Values obtained by Sensharma et. al.:  $\mathcal{I}_{1,2,3} = 7.4, 5.6, 1.8 \text{ } \hbar^2 \text{MeV}^{-1}$ .  
 $\epsilon = 0.16, \gamma = 26^\circ$ .
- Values obtained by Raduta et. al.:  $\mathcal{I}_{1,2,3} = 91, 9, 51 \text{ } \hbar^2 \text{MeV}^{-1}$ .  
Quadrupole deformations not needed.

# New experimental data



# Conclusions

- Disagreement between the experimental measurements for an odd-mass nucleus.
- First work pointing out contradictory behavior of  $^{135}\text{Pr}$  in terms of collective excitations
- The smaller values of mixing ratios and branching ratios show that the three triaxial bands in the isotope are at normal deformation, show collective nature, but no wobbling.

**Future perspectives:** Re-calibrate the existing theoretical interpretation of the triaxial nature of the wobblers near  $A \approx 130$  mass region.

Thank you for your attention!