

1 EXTENSIVE STUDY OF THE WOBBLING PROPERTIES IN  $^{163}\text{Lu}$  BASED ON  
2 THE PARITY CONCEPT

3 ROBERT POENARU<sup>1,2,a</sup>, APOLODOR ARISTOTEL RADUTA<sup>1,3,b</sup>

4 <sup>1</sup>“Horia Hulubei” National R&D Institute for Physics and Nuclear Engineering,  
5 Reactorului 30, RO-077125, P.O.B. MG-6, Măgurele-Bucharest, Romania  
6 *E-mail<sup>a</sup>*: robert.poenaru@drd.unibuc.ro (corresponding author)

7 <sup>1</sup>“Horia Hulubei” National R&D Institute for Physics and Nuclear Engineering,  
8 Reactorului 30, RO-077125, P.O.B. MG-6, Măgurele-Bucharest, Romania

9 <sup>2</sup>Doctoral School of Physics, University of Bucharest, Romania

10 <sup>3</sup>Academy of Romanian Scientists, Bucharest, Romania

11 *E-mail<sup>b</sup>*: raduta@nipne.ro

12 Received: January 21, 2021 (RJP v2.0 r2018a)

13 *Abstract.* A new interpretation on the wobbling structure in  $^{163}\text{Lu}$  is developed,  
14 based on the concept of parity symmetry. It is known that four wobbling bands are  
15 experimentally observed in this isotope, where three of them are considered as wobbling  
16 phonon excitations (namely  $TSD_2$ ,  $TSD_3$ , and  $TSD_4$ ) and the yrast band for the  
17 ground state (that is  $TSD_1$ ). In the present work, the trial function that is used for  
18 obtaining the wobbling spectrum is analyzed in terms of its behavior under the rotation  
19 operation. Indeed, due to a specific symmetry to rotations with  $\pi$  around the 2-axis  
20 of the triaxial system, the parity becomes a good quantum number. As such, the trial  
21 function admits solutions with negative parity, which belong to the rotational states  
22 in  $TSD_4$ . A unified description of all the triaxial super-deformed bands in  $^{163}\text{Lu}$  is  
23 achieved with the new formalism.

24 *Key words:* Wobbling Motion, Nuclear Structure, Parity Symmetry.

## 1. INTRODUCTION

25 Wobbling motion in nuclei was extensively studied in the recent years, and the  
26 scientific community finally shed some light on this elusive phenomenon. This kind  
27 of collective motion was firstly predicted by Bohr and Mottelson, more than 50 years  
28 ago [1].

## 2. THEORETICAL BACKGROUND

29 In a previous work, a complete description of the triaxial characteristics of  
30 the Lu isotopes was given, where results for the wobbling energies and transition  
31 probabilities were presented [2].

32 In this paper, the wobbling spectrum is represented. See Figure 1 for more  
33 details.

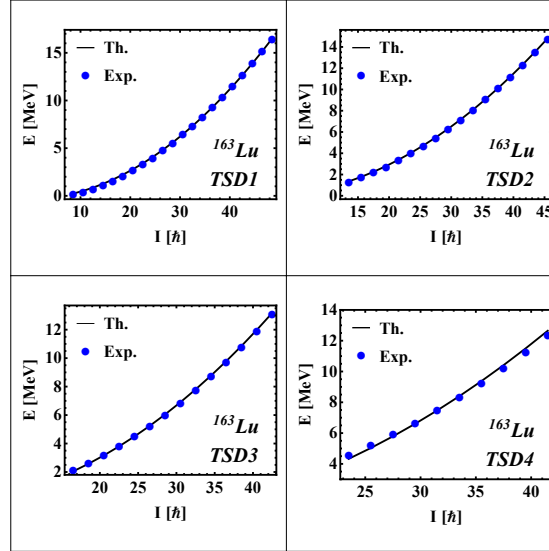


Fig. 1 – The excitation energies for the wobbling spectrum of  $^{163}\text{Lu}$ . Comparison with the available experimental data.

34 The trajectories of a rotational state from  $TSD_1$  is graphically represented in  
 35 Figure 2.

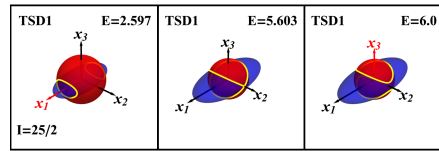


Fig. 2 – The contour plots with the energy function  $\mathcal{H}$  of the nucleus, evaluated for the obtained fit parameters.

36 The trajectories shown in Figure 2 are given by the intersection of two surfaces,  
 37 namely the energy ellipsoid (generated from the expression of the energy function  
 38 written in spherical coordinates) and the total angular momentum of the triaxial sys-  
 39 tem. Each inset from the figure represents a trajectory at a given spin  $I$  but different  
 40 values of the total energy for the rotor. The first inset corresponds to the real energy  
 41 of the isotope for that particular spin state. The second inset represents the energy at  
 42 which the trajectories around 1-axis and -1-axis are tangent to each other. This partic-  
 43 ular energy marks the point of a phase transition, where the triaxial nucleus changes  
 44 its rotational axis from 1-axis to the 3-axis. Finally, the third inset represents the tra-  
 45 jectories belonging to very high energy states, where rotation is done around 3-axis.  
 46 It is worth mentioning that such motion is forbidden for this isotope, since the energy

at which the nucleus exhibits the 3-axis rotation is much larger than the excitation energy that corresponds to that particular spin.

A new interpretation on the wobbling motion, but based on the quasiparticle plus triaxial rotor model was given recently by Chen et. al. [3].

$$|\Psi\rangle = 1 \quad (1)$$

The equation 1 is good. This equation is studied in detail by the same team in [2] and also [4]. Nuclear wobbling motion was first predicted theoretically for even-even nuclei [1].

*Acknowledgments.* We are grateful.

#### REFERENCES

1. Aage Bohr and Ben R Mottelson. *Nuclear structure*, volume 1. World Scientific, 1998.
2. AA Raduta, R Poenaru, and Al H Raduta. Wobbling motion in lu within a semi-classical framework. *Journal of Physics G: Nuclear and Particle Physics*, 45(10):105104, 2018.
3. QB Chen and S Frauendorf. Interpretation of the quasiparticle plus triaxial rotor model. *arXiv preprint arXiv:2012.03499*, 2020.
4. AA Raduta, CM Raduta, and R Poenaru. A new boson approach for the wobbling motion in even-odd nuclei. *Journal of Physics G: Nuclear and Particle Physics*, 48(1):015106, 2020.