

# R/qtl Workshop

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Karl Broman

Biostatistics and Medical Informatics  
University of Wisconsin – Madison

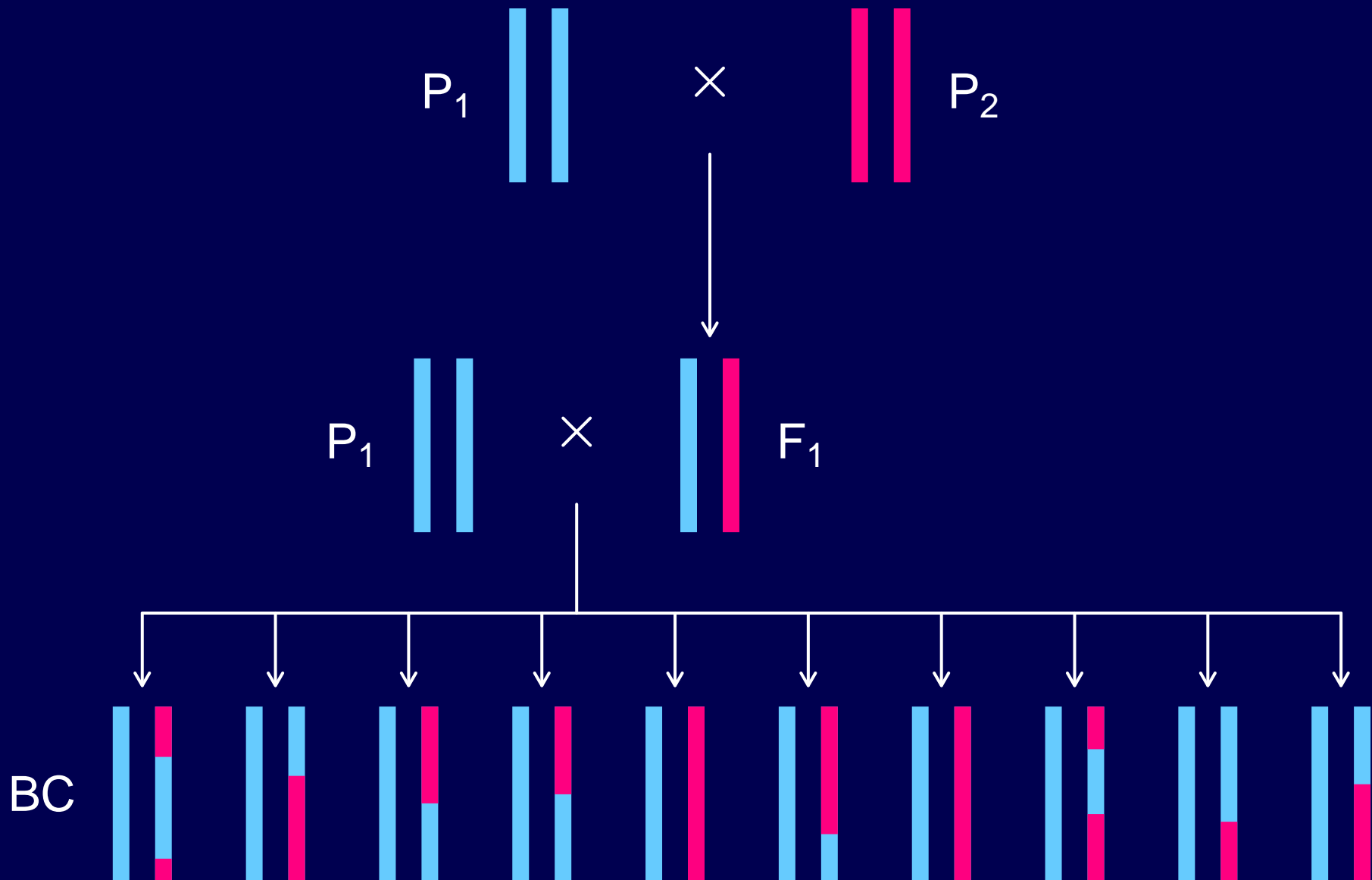
`rqtl.org`

`kbroman.org`

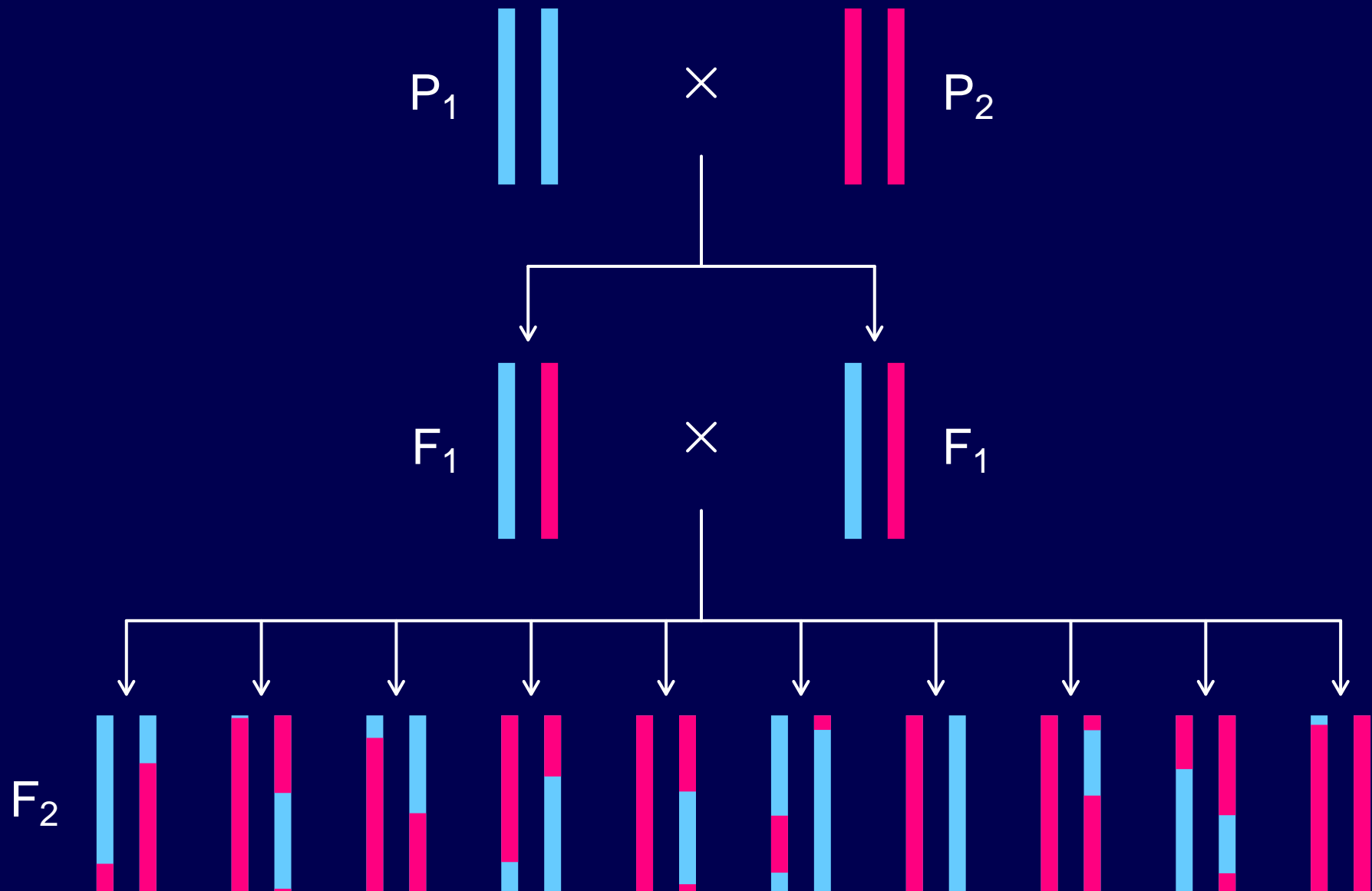
`github.com/kbroman`

`@kwbroman`

# Backcross



# Intercross



# Goals

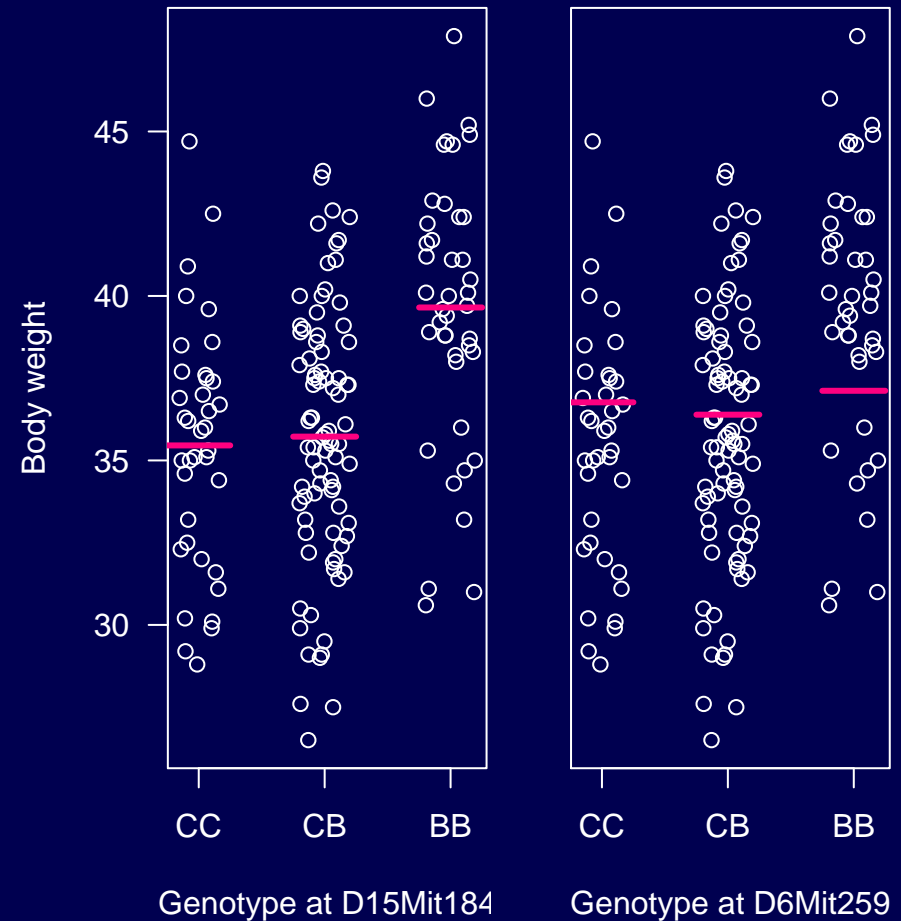
- Identify quantitative trait loci (QTL)  
(and interactions among QTL)
- Interval estimates of QTL location
- Estimated QTL effects

→ R

- R, RStudio, and R/qtl
- `read.cross()`
- `summary()`, `plot()`
- `nind()`, `nmar()`, `totmar()`, `nchr()`

# ANOVA at marker loci

- Also known as **marker regression**.
- Split mice into groups according to genotype at a marker.
- Do a t-test / ANOVA.
- Repeat for each marker.



# ANOVA at marker loci

## Advantages

- Simple.
- Easily incorporates covariates.
- Easily extended to more complex models.
- Doesn't require a genetic map.

## Disadvantages

- Must exclude individuals with missing genotype data.
- Imperfect information about QTL location.
- Suffers in low density scans.
- Only considers one QTL at a time.

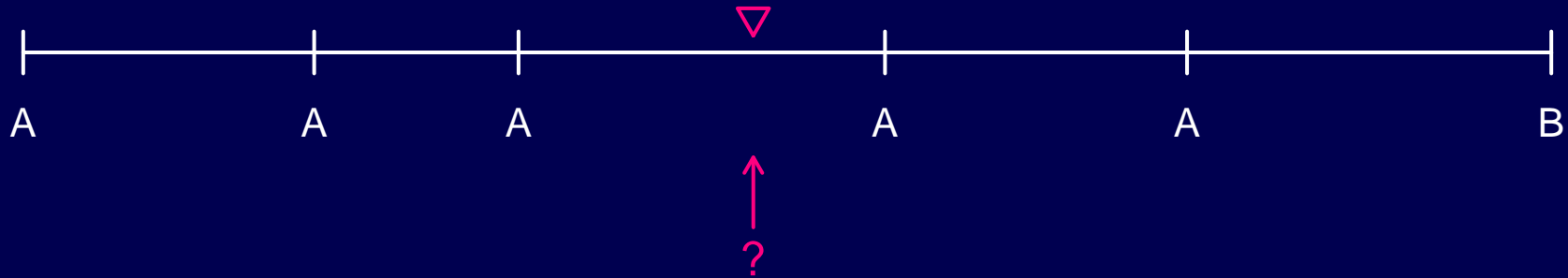
# Interval mapping

## Lander & Botstein (1989)

- Assume a **single** QTL model.
- Each position in the genome, one at a time, is posited as the putative QTL.
- Let  $q$  = the unobserved QTL genotype  
Assume  $y|q \sim N(\mu_q, \sigma)$
- We don't know  $q$ , but we can calculate  $\Pr(q \mid \text{marker data})$
- Estimate  $\mu_q, \sigma$  by *maximum likelihood* using an iterative EM algorithm



# Genotype probabilities



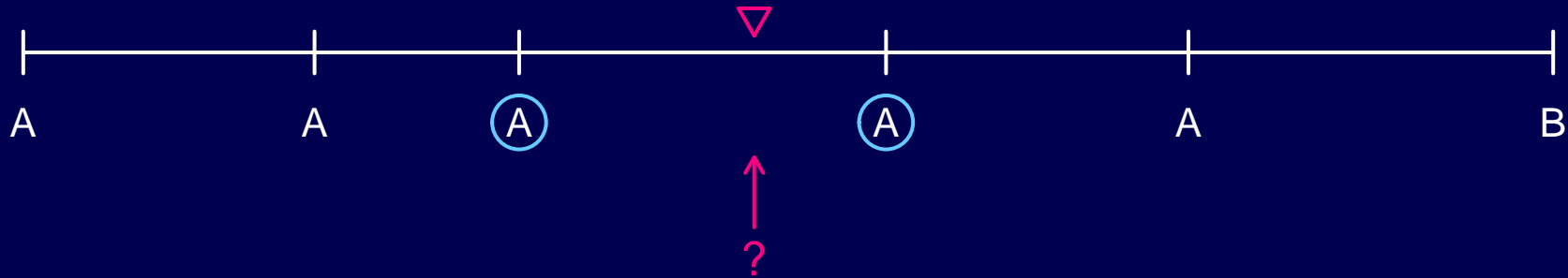
Calculate  $\Pr(q \mid \text{marker data})$ , assuming

- No crossover interference
- No genotyping errors

Or use the **hidden Markov model (HMM)** technology

- To allow for genotyping errors
- To incorporate dominant markers
- (Still assume no crossover interference.)

# Genotype probabilities



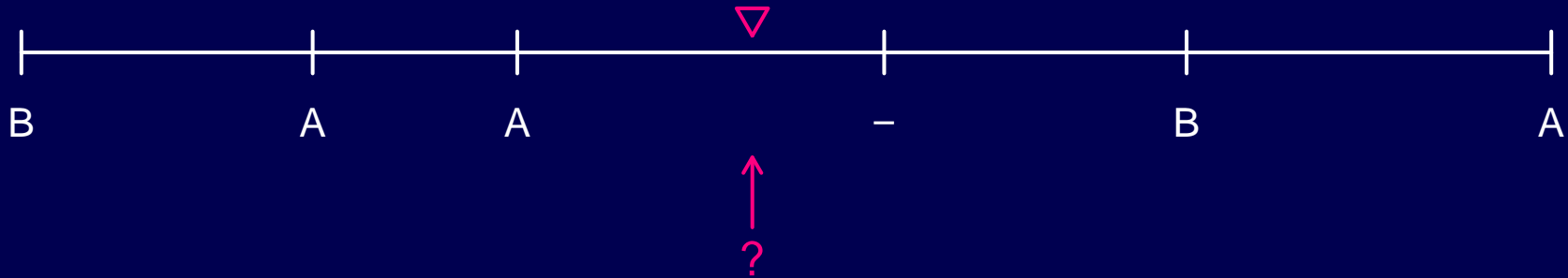
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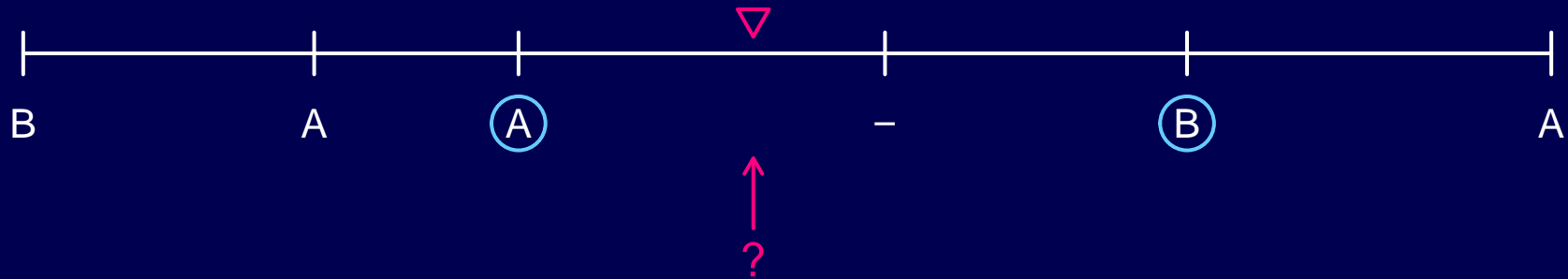
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# Genotype probabilities



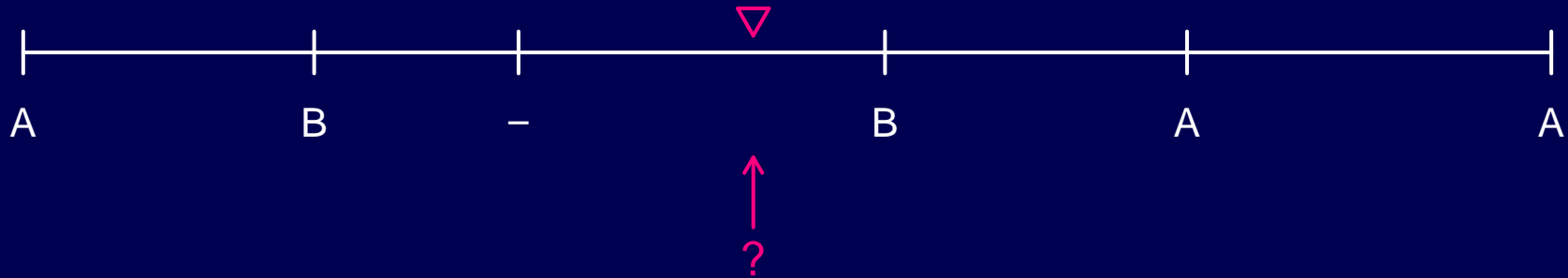
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# Genotype probabilities



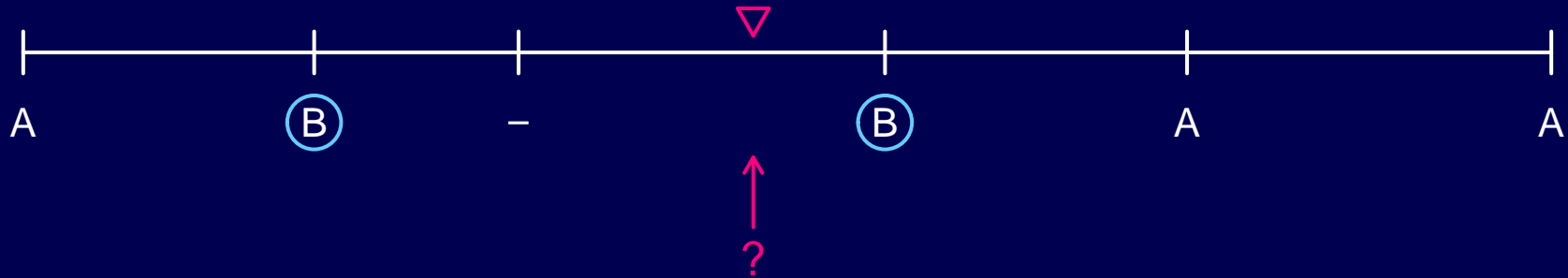
Calculate  $\Pr(q \mid \text{marker data})$ , assuming

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# Genotype probabilities



Calculate  $\Pr(q \mid \text{marker data})$ , assuming

- No crossover interference
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Or use the **hidden Markov model (HMM)** technology

- To allow for genotyping errors
- To incorporate dominant markers
- (Still assume no crossover interference.)

# LOD scores

The LOD score is a measure of the **strength of evidence** for the presence of a QTL at a particular location.

$\text{LOD}(\lambda) = \log_{10}$  likelihood ratio comparing the hypothesis of a QTL at position  $\lambda$  versus that of no QTL

$$= \log_{10} \left\{ \frac{\Pr(\mathbf{y} | \text{QTL at } \lambda, \hat{\mu}_{0\lambda}, \hat{\mu}_{1\lambda}, \hat{\sigma}_{\lambda})}{\Pr(\mathbf{y} | \text{no QTL}, \hat{\mu}, \hat{\sigma})} \right\}$$

$\hat{\mu}_{0\lambda}, \hat{\mu}_{1\lambda}, \hat{\sigma}_{\lambda}$  are the MLEs, assuming a single QTL at position  $\lambda$ .

No QTL model: The phenotypes are independent and identically distributed (iid)  $N(\mu, \sigma^2)$ .

→ R

- `calc.genoprob()`
- `scanone()`
- `iplotScanone()` from **R/qtlcharts**



# Interval mapping

## Advantages

- Takes proper account of missing data.
- Allows examination of positions between markers.
- Gives improved estimates of QTL effects.
- Provides pretty graphs.

## Disadvantages

- Increased computation time.
- Requires specialized software.
- Difficult to generalize.
- Only considers one QTL at a time.

# LOD thresholds

Large LOD scores indicate evidence for the presence of a QTL

Question: How large is large?

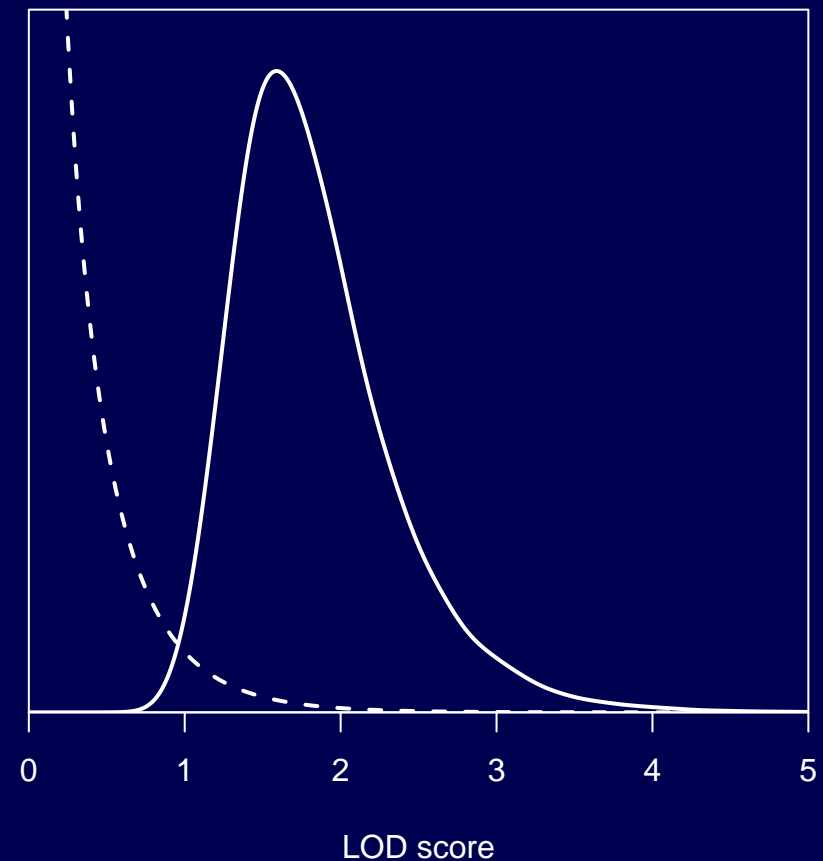
**LOD threshold** = 95 %ile of distr'n of max LOD, genome-wide, if there are no QTLs anywhere

**Derivation:**

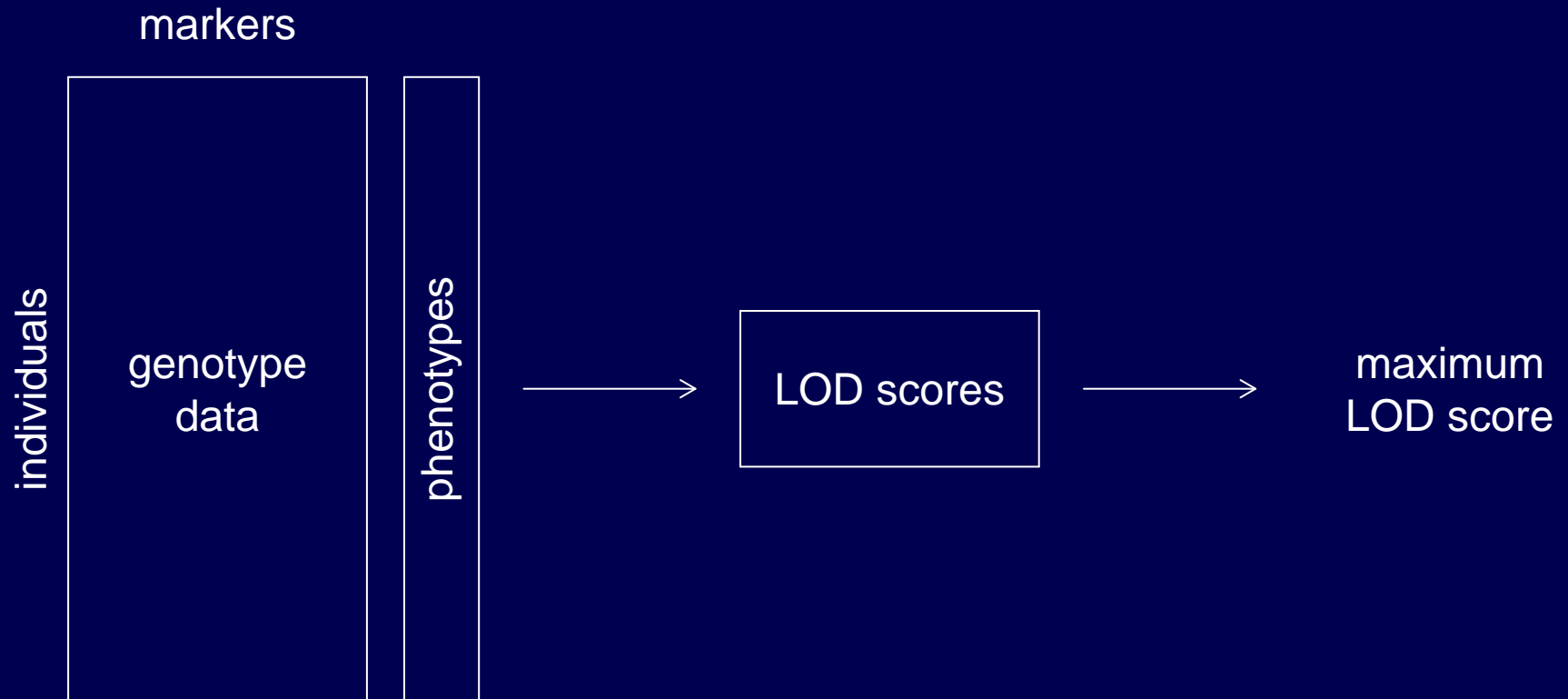
- Analytical calculations (L & B 1989)
- Simulations (L & B 1989)
- Permutation tests (Churchill & Doerge 1994)

# Null distribution of the LOD score

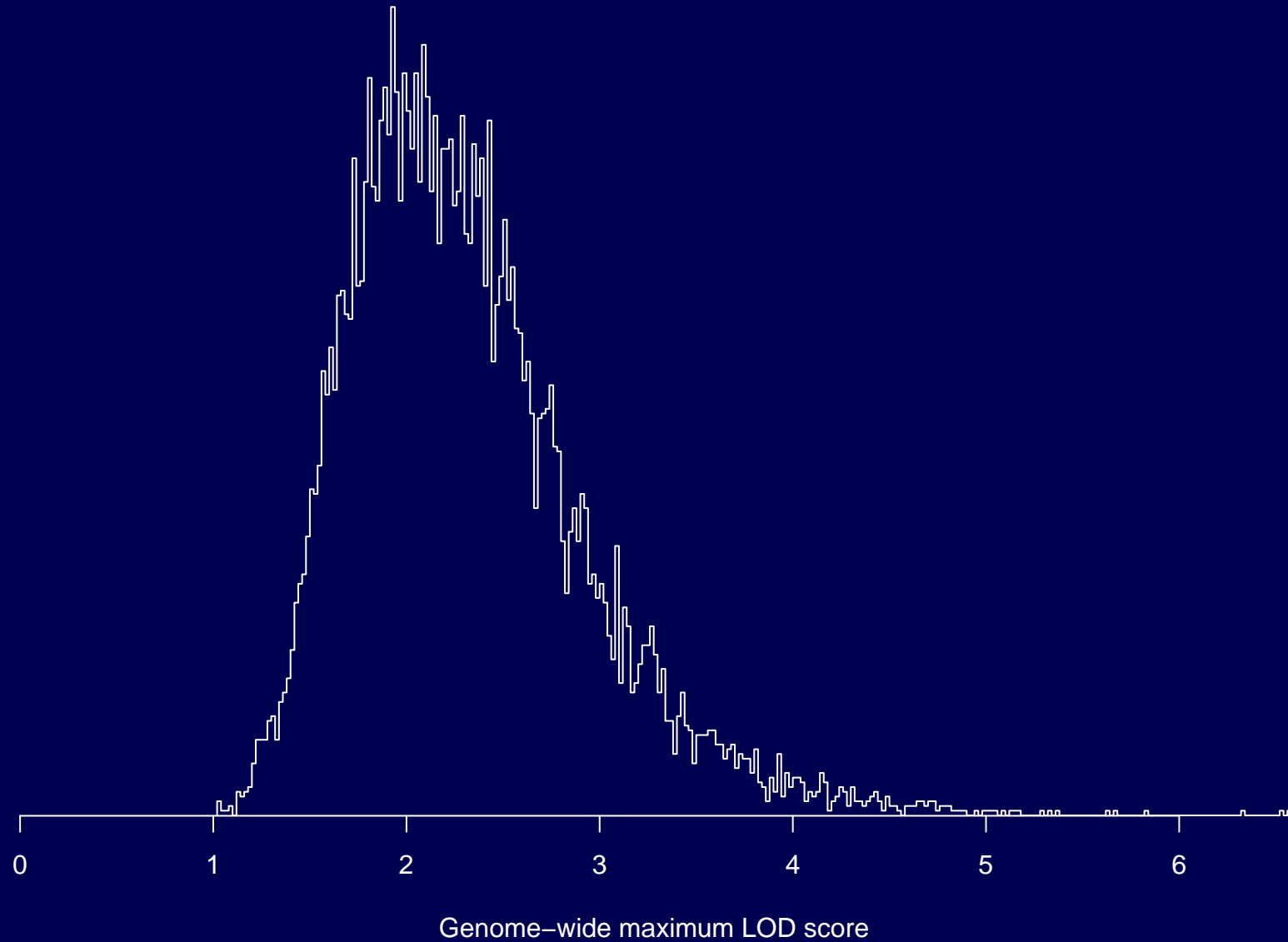
- Null distribution derived by computer simulation of backcross with genome of typical size.
- Dashed curve: distribution of LOD score at any one point.
- Solid curve: distribution of maximum LOD score, genome-wide.



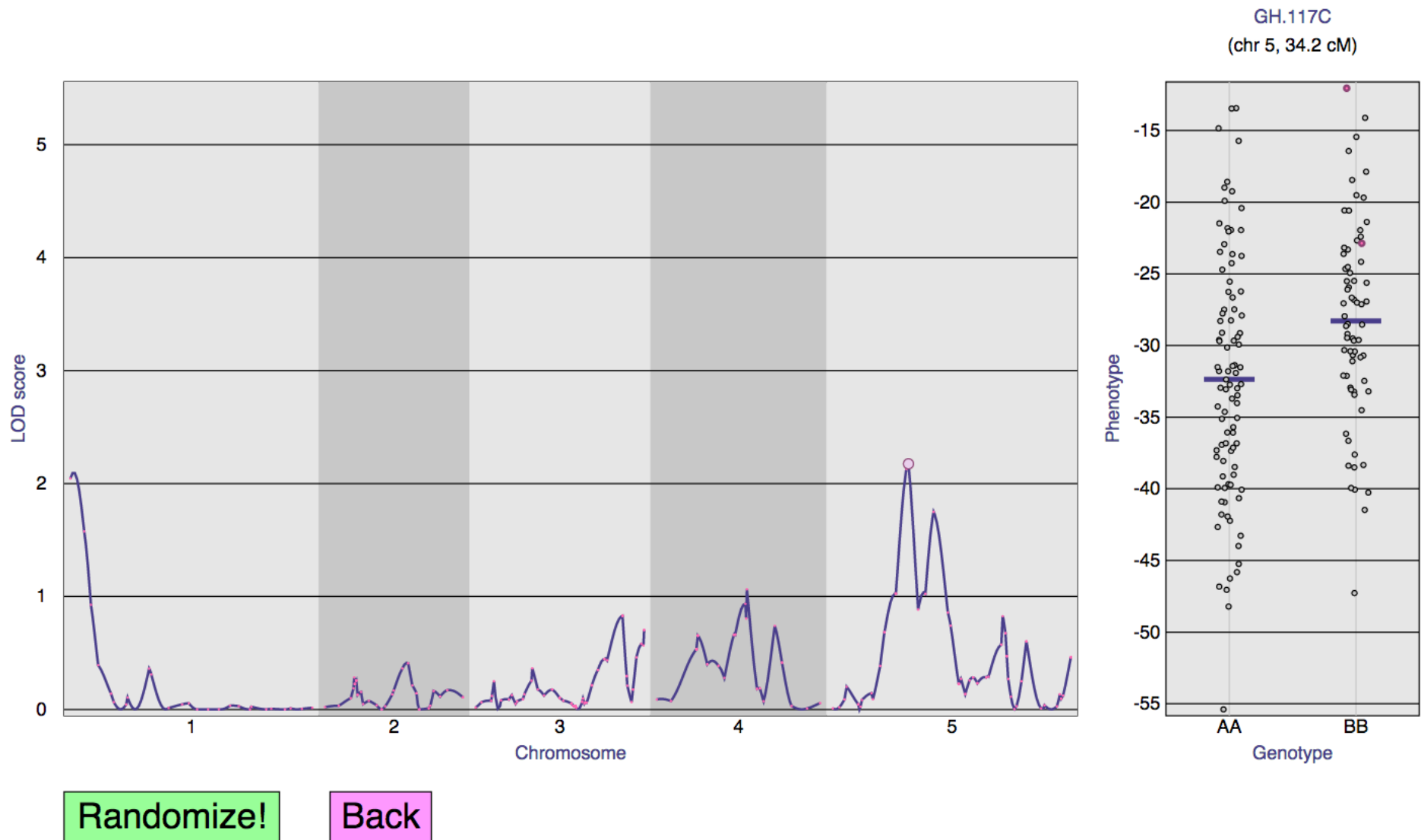
# Permutation test



# Permutation results



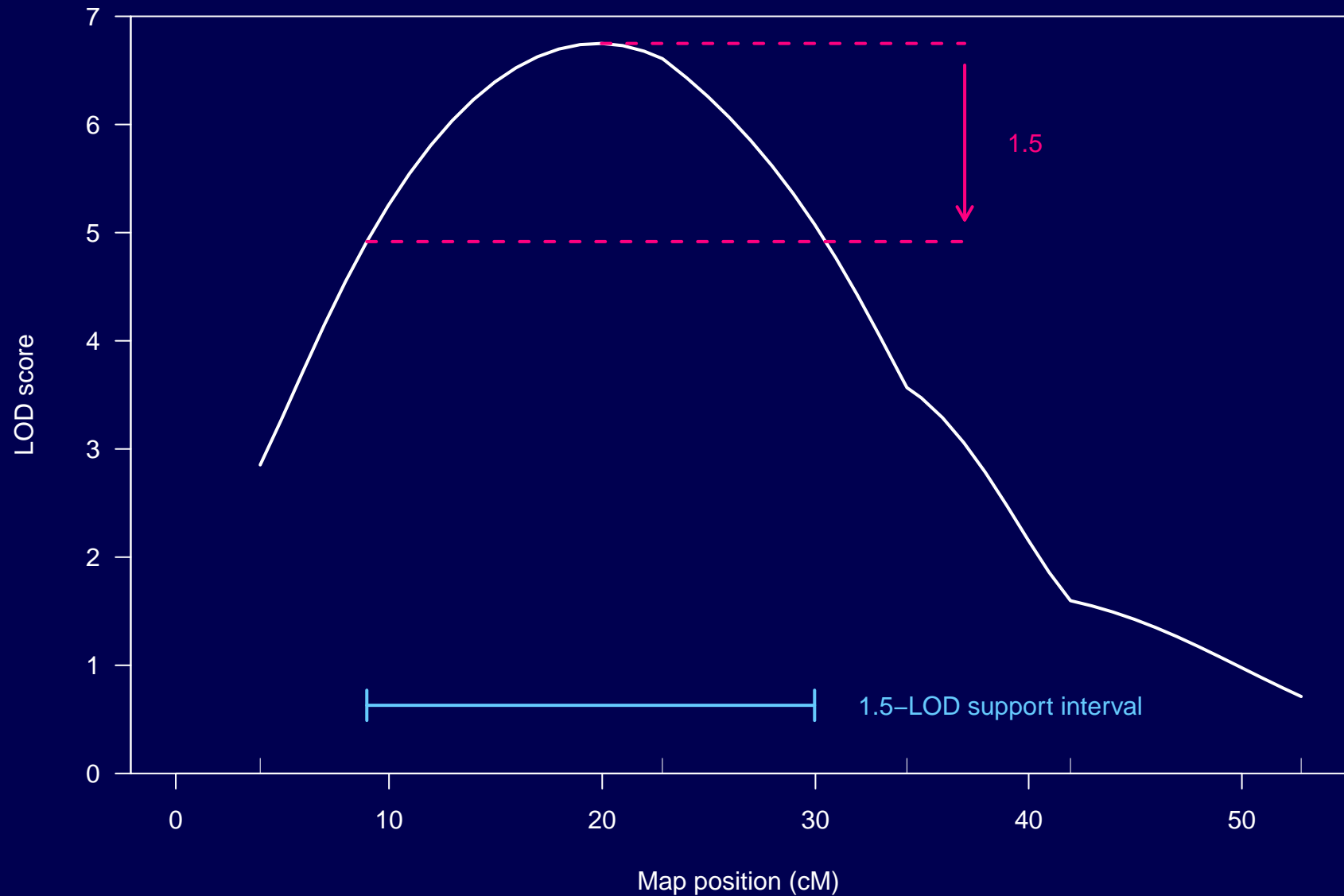
# Interactive plot



→ R

- `scanone()` for permutations

# LOD support intervals





→ R

- `lodint()`
- `bayesint()`

# Haley-Knott regression

A quick approximation to Interval Mapping.

$$E(y_i|q_i) = \mu_q$$

$$\begin{aligned} E(y_i|M_i) &= E[ E(y_i|q_i) |M_i] = \sum_j \Pr(q = j|M_i)\mu_j \\ &= \sum_j p_{ij}\mu_j \end{aligned}$$

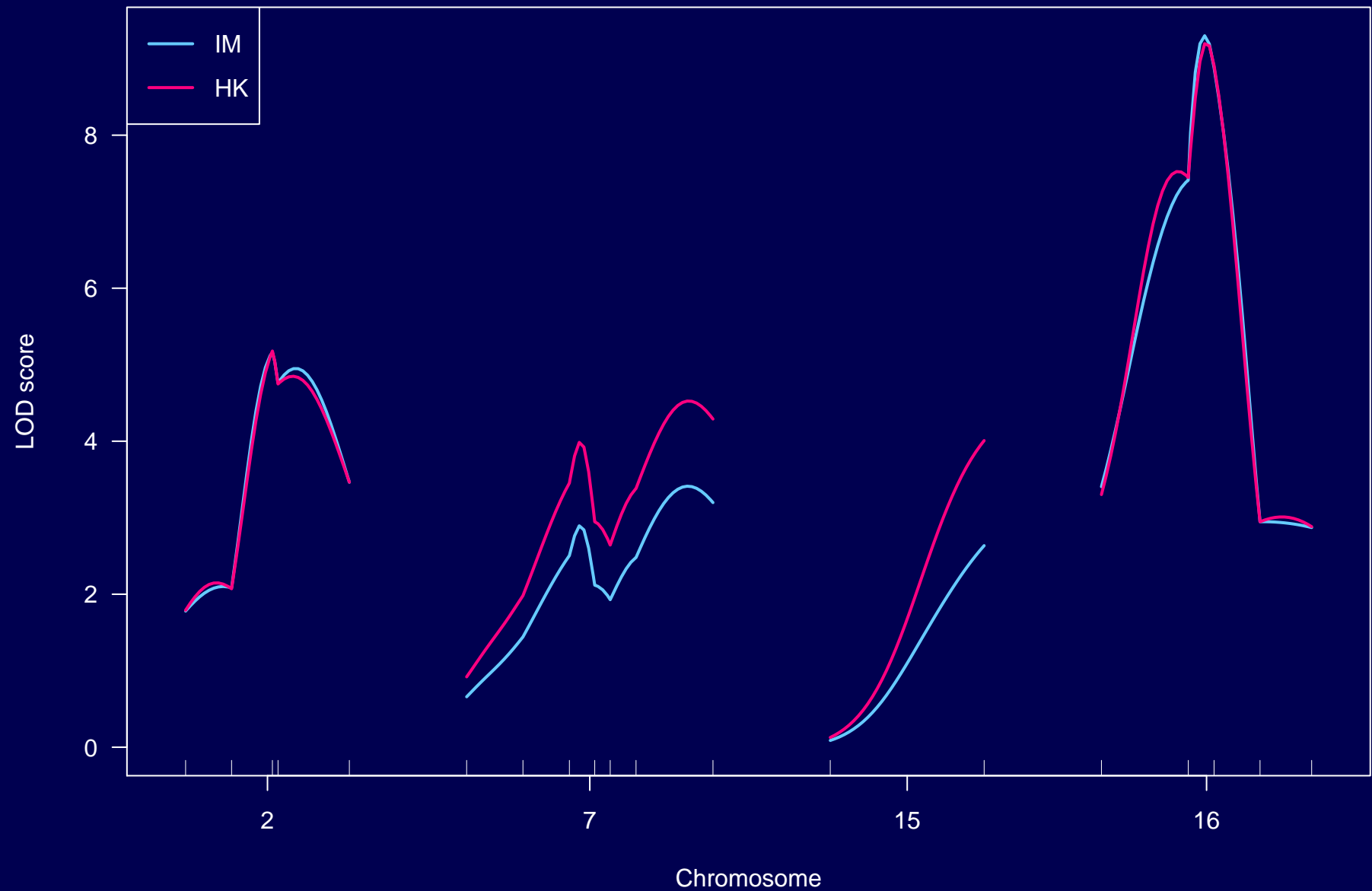
Regress  $y$  on  $p_i$ , pretending the residual variation is normally distributed (with constant variance).

$$\text{LOD} = \frac{n}{2} \log_{10} \left( \frac{\text{RSS}_0}{\text{RSS}_1} \right)$$

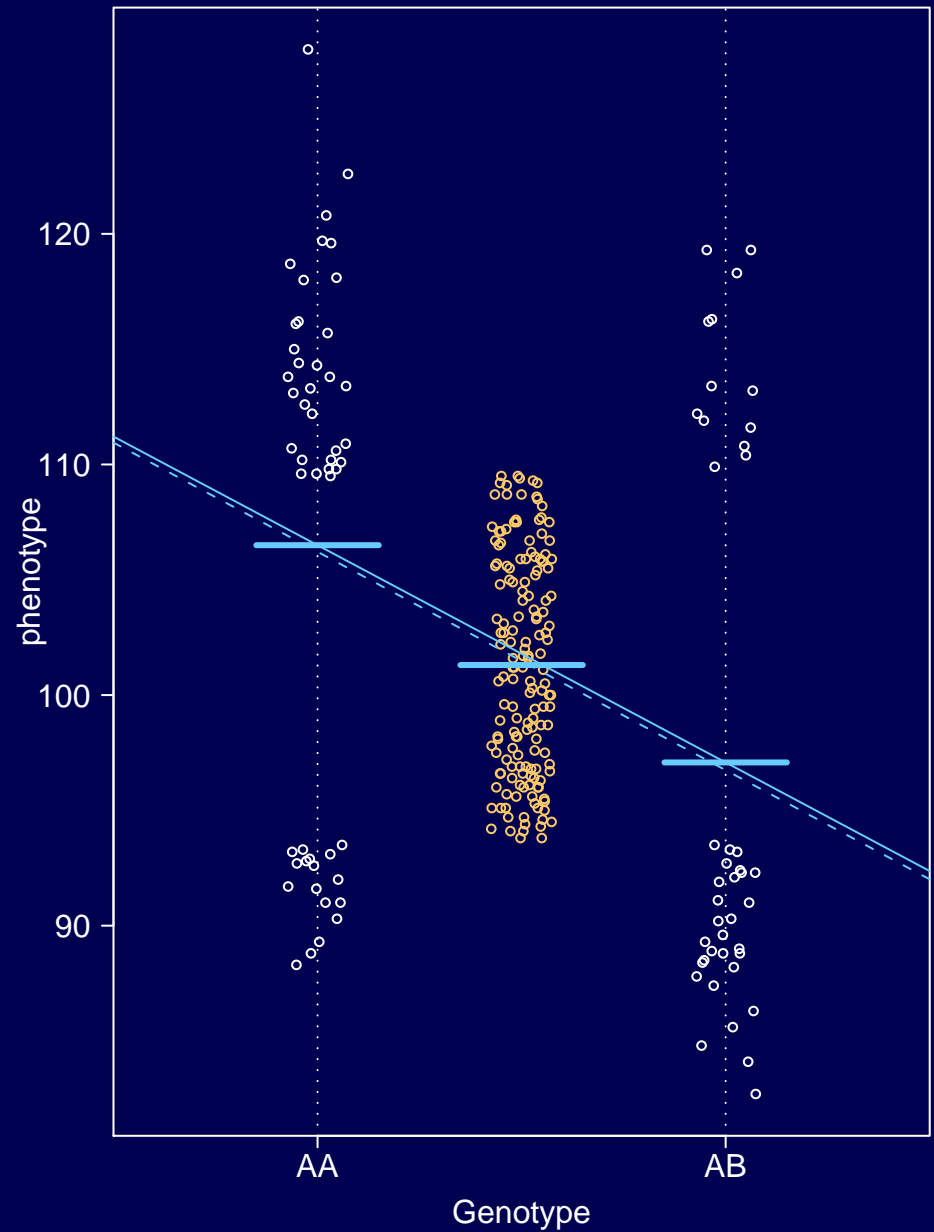
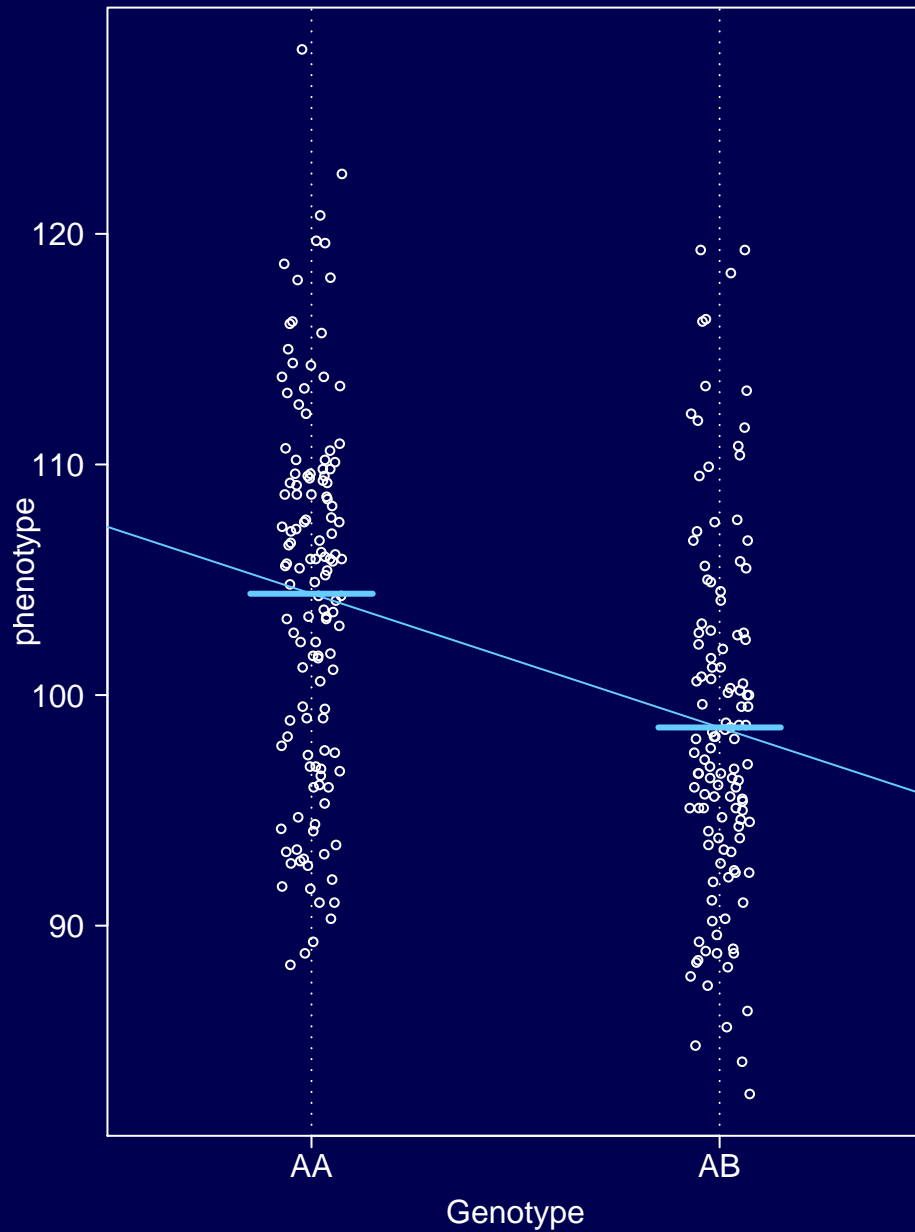
→ R

- `scanone()` with `method="hk"`

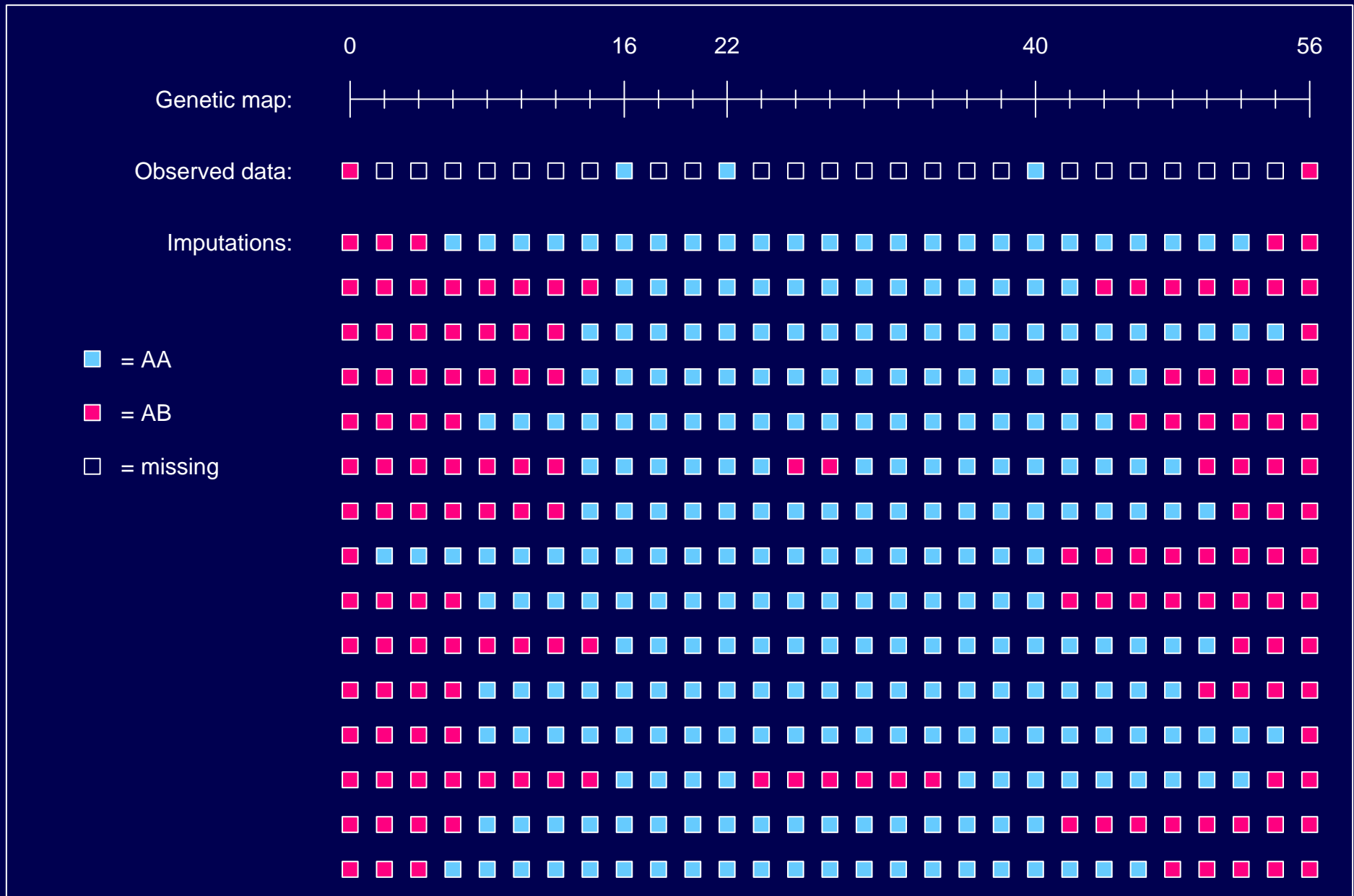
# Haley-Knott results



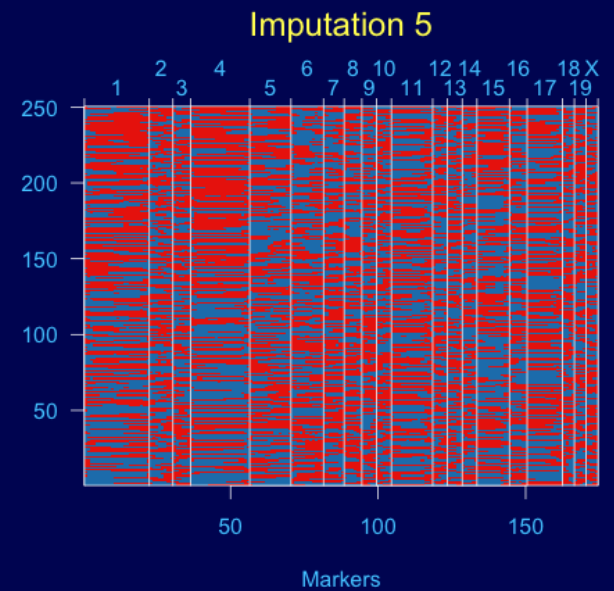
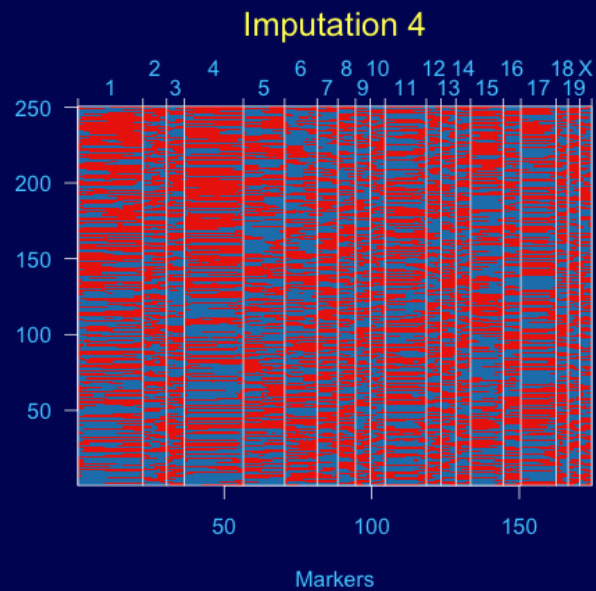
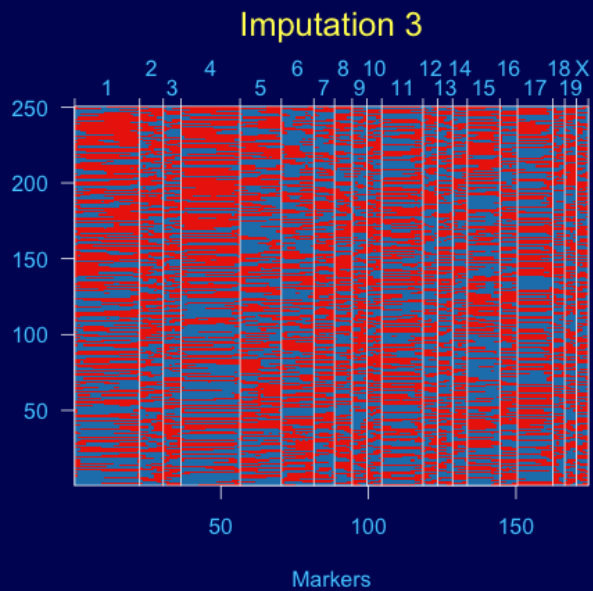
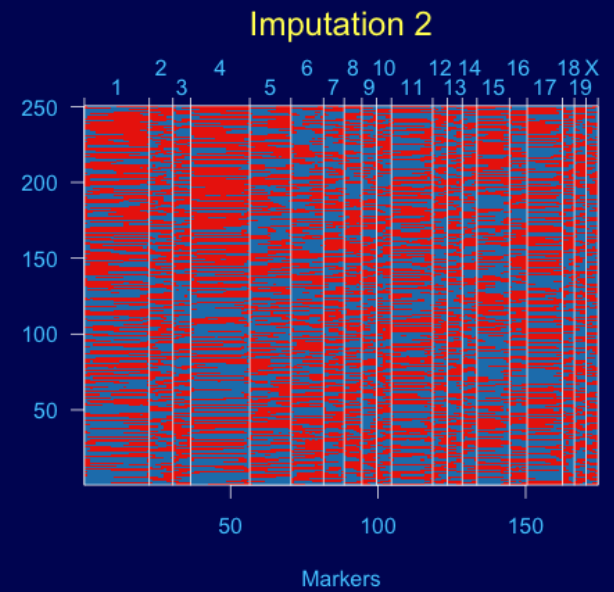
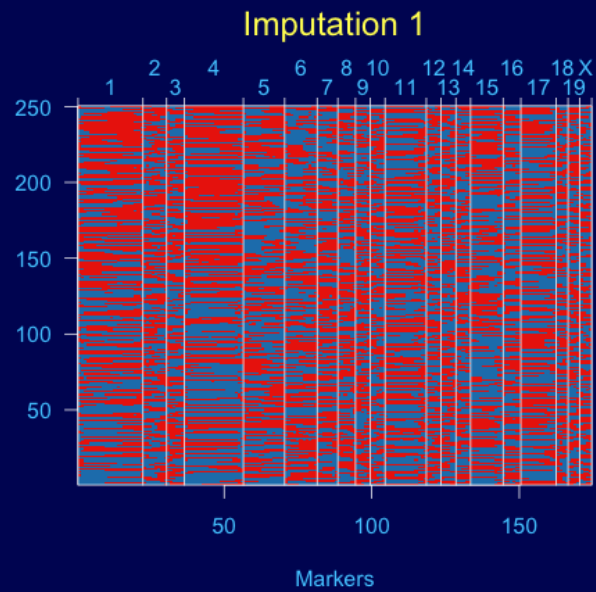
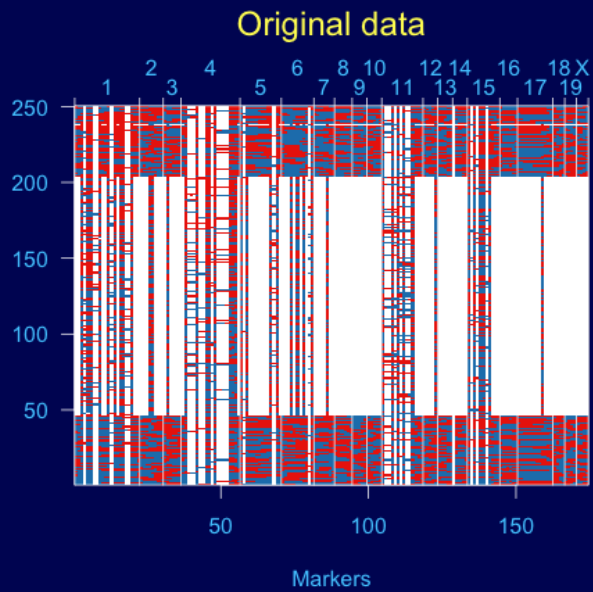
# H-K with selective genotyping



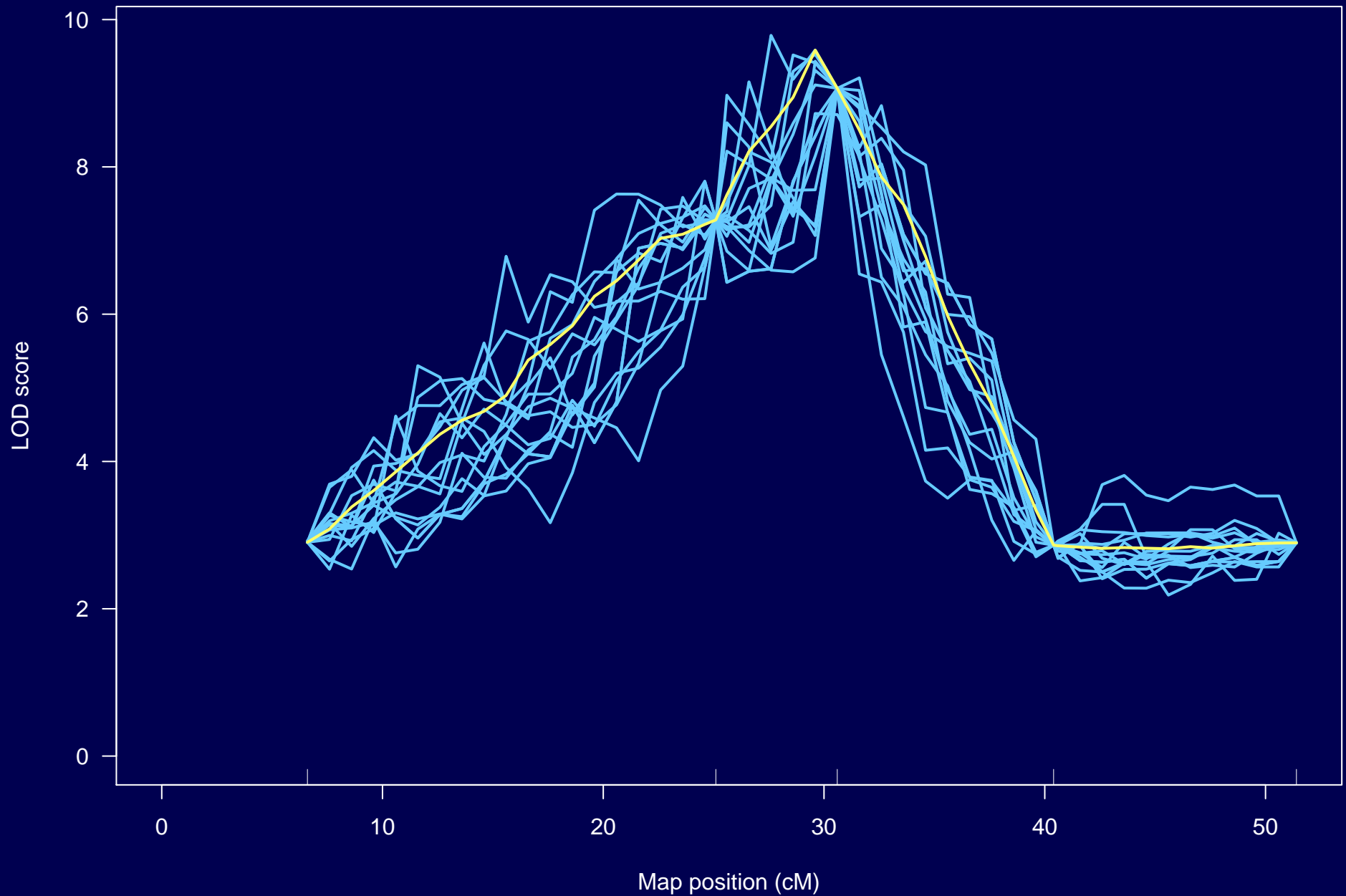
# Multiple imputation



# Multiple imputations



# Imputation LOD curves





→ R

- `sim.geno()`
- `scanone()` with `method="imp"`

# Summary comparison

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Approach	Speed	Extensibility	Stability	Missing data	Parallelization
HK	++	+	+	—	++
EM	+	—	—	+	—
Imputation	—	+	+	+	+

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# Non-normal traits

- Standard interval mapping assumes normally distributed residual variation. (Thus the phenotype distribution is a mixture of normals.)
- **In reality**: we see dichotomous traits, counts, skewed distributions, outliers, and all sorts of odd things.
- Interval mapping, with LOD thresholds derived from permutation tests, generally performs just fine anyway.
- Alternatives to consider:
  - Nonparametric approaches (Kruglyak & Lander 1995)
  - Transformations (*e.g.*, log, square root, normal quantiles)
  - Specially-tailored models (*e.g.*, a generalized linear model, the Cox proportional hazard model, and the two-part model in Broman 2003)

→ R

- `nqrank()`
- `scanone()` with `model="binary"` or `model="np"`

# Covariates

- **Examples:** treatment, sex, age, weight
- Control residual variation → increase power
- Look for QTL  $\times$  covariate interactions

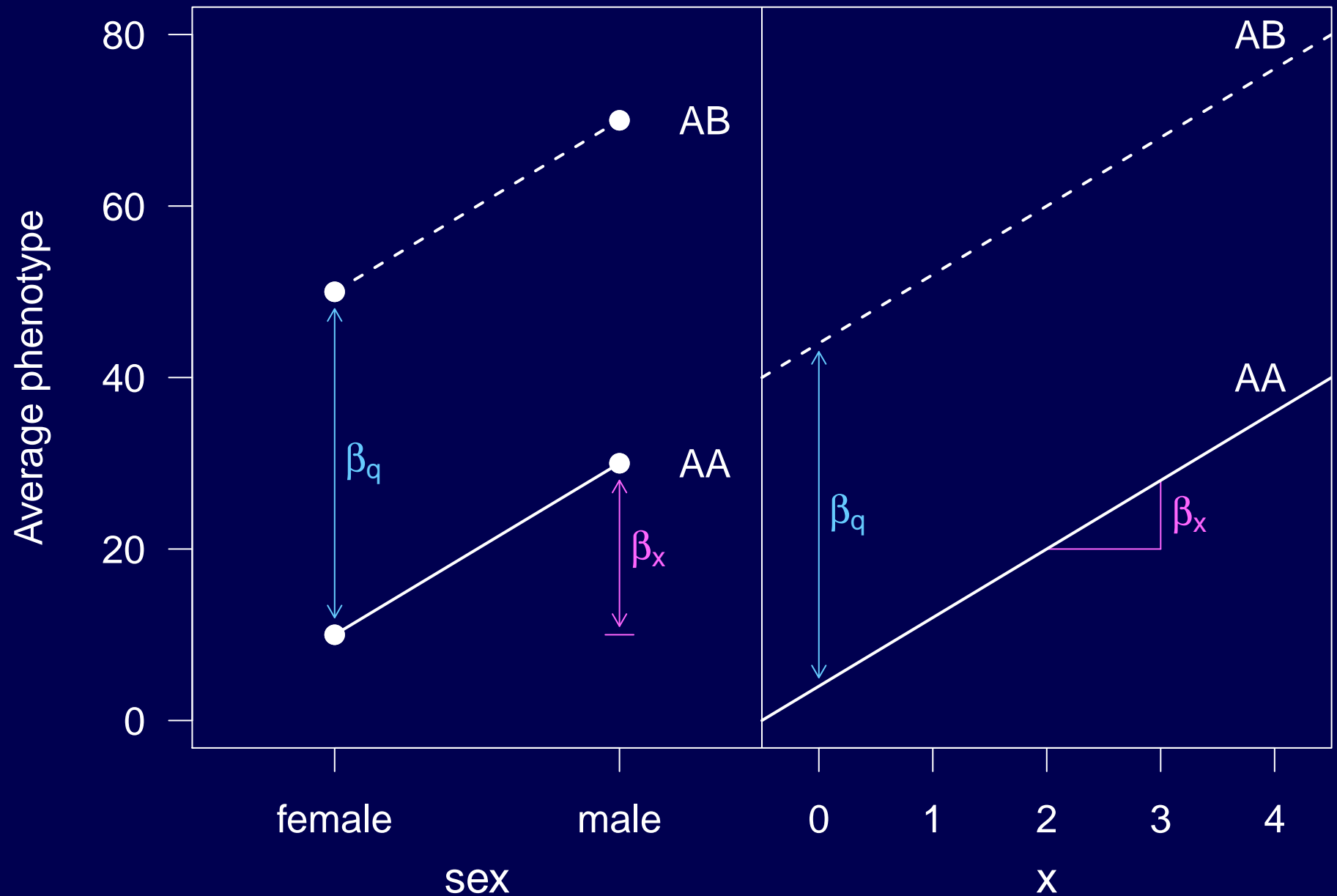
# Additive covariate

$$H_0 : y = \mu + \beta_x x + \epsilon$$

$$H_a : y = \mu + \beta_x x + \beta_q q + \epsilon$$

- If covariate has strong effect on the phenotype, accounting for it can give improved power to detect QTL.
- In permutations, keep phenotype and covariate together
- Use care when the covariate is another phenotype

# Additive covariate



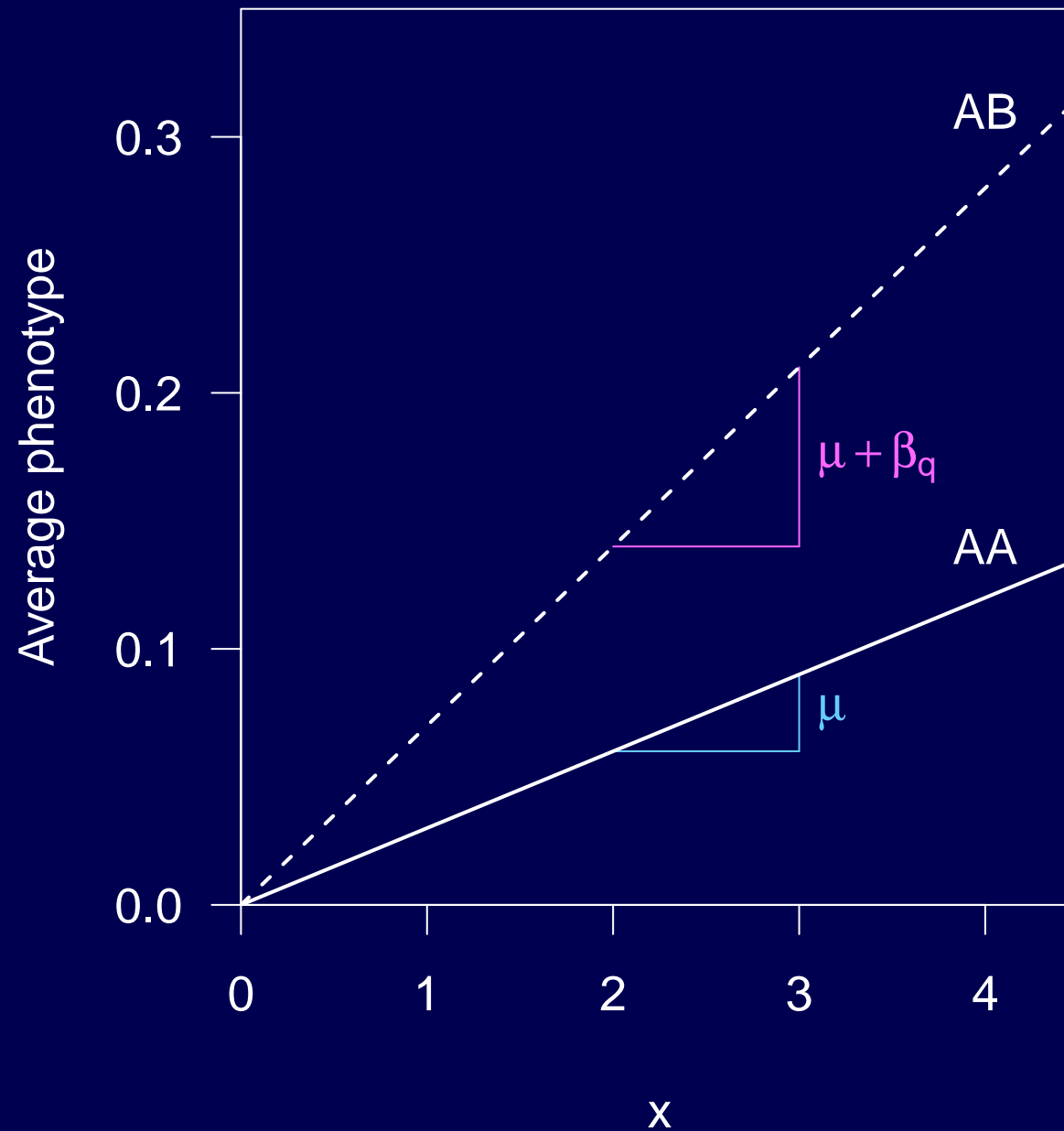
# Adjust then scan?

- Consider adjusted phenotype  $y' = y/x$
- The QTL model is  $(y/x) = \mu + \beta_q q + \epsilon$
- Equivalently

$$y = \begin{cases} \mu x + \epsilon' & \text{if } q = 0 \\ (\mu + \beta_q)x + \epsilon' & \text{if } q = 1 \end{cases}$$



# Adjust then scan?



# Interactive covariate

$$H_0 : y = \mu + \beta_x x + \epsilon$$

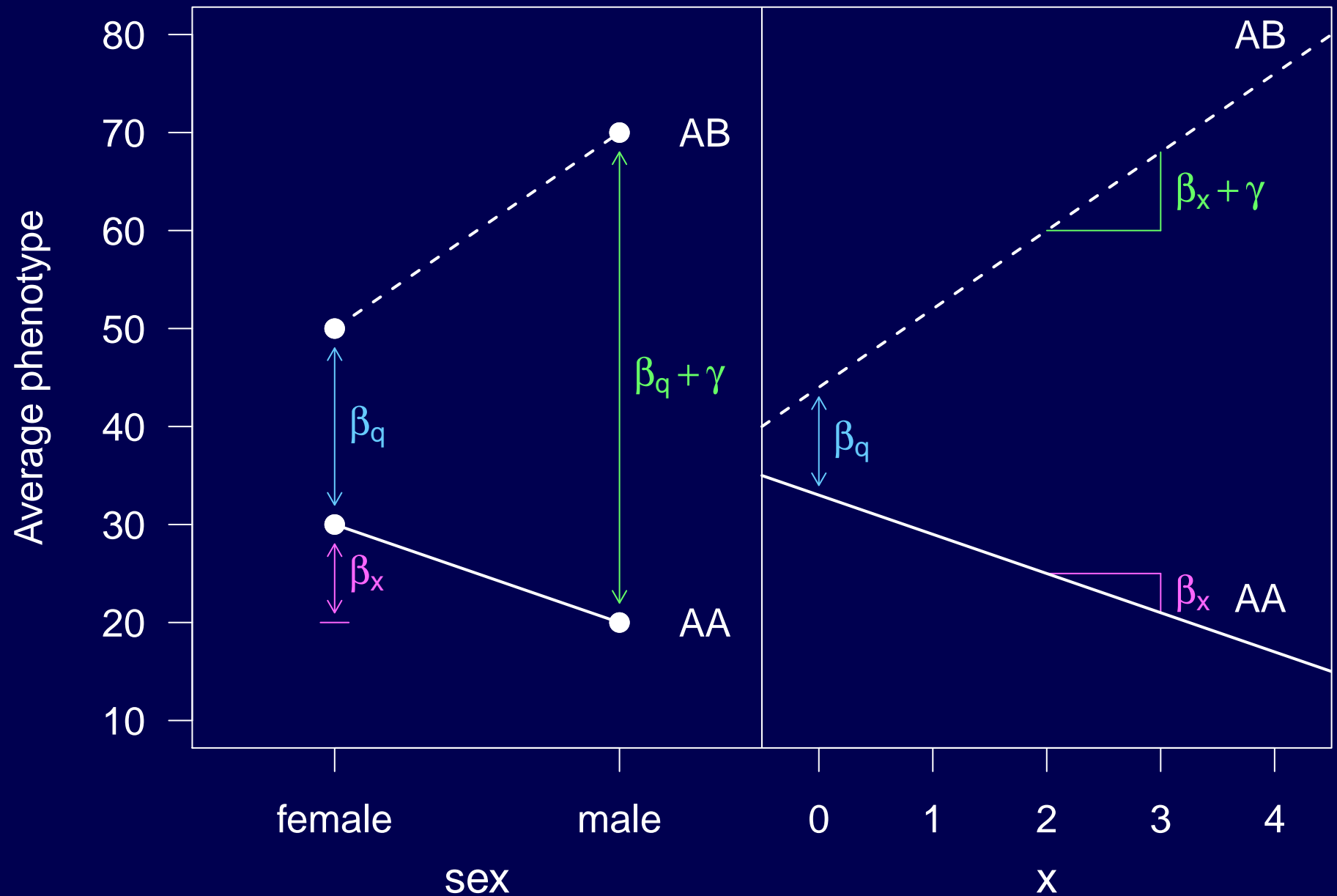
$$H_a : y = \mu + \beta_x x + \beta_q q + \epsilon$$

$$H_i : y = \mu + \beta_x x + \beta_q q + \gamma x q + \epsilon$$

Can consider 3 LOD scores:

- $LOD_a$  comparing  $H_a$  and  $H_0$
- $LOD_f$  comparing  $H_i$  and  $H_0$
- $LOD_i$  comparing  $H_i$  and  $H_a$

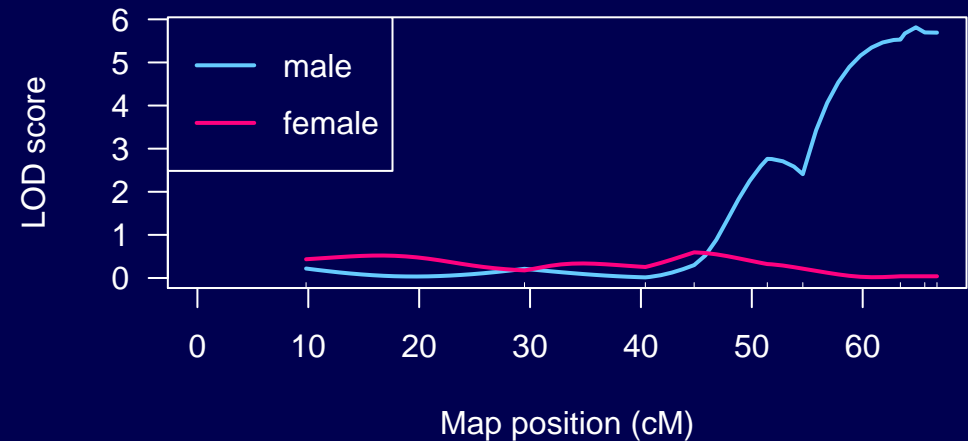
# Interactive covariate



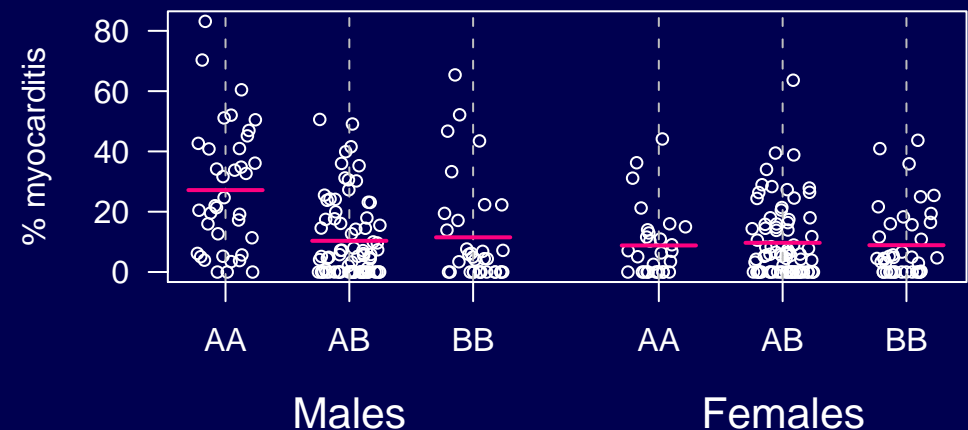
# Split on sex?

- Informative, understandable
- But tempting to falsely conclude “**sex-specific QTL**”
- Absence of evidence **is not** *evidence of absence*.
- Use explicit test of QTL  $\times$  sex interaction

Chromosome 6



D6Mit373

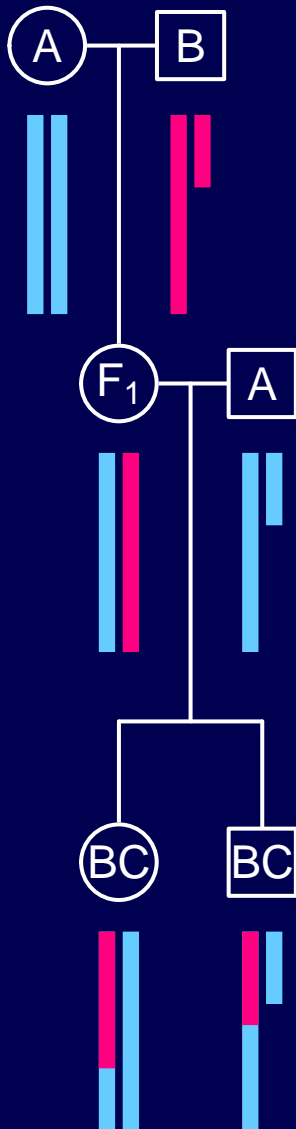


→ R

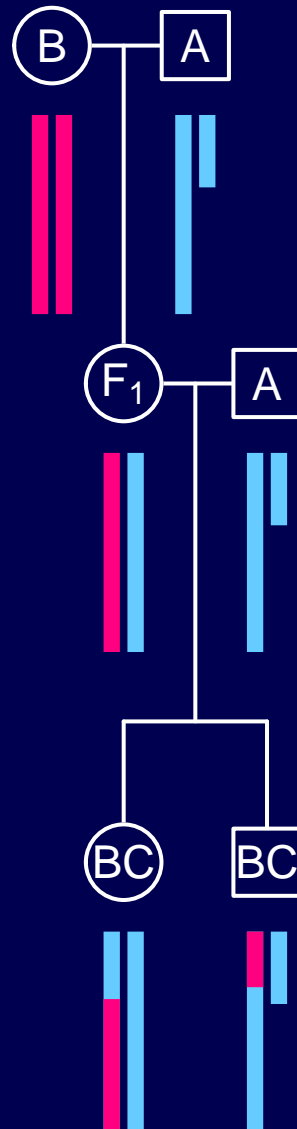
- `scanone()` with `addcovar` and `intcovar`
- `set.seed()` to do permutations
- `subset()` to split on sex

# X chr in backcross

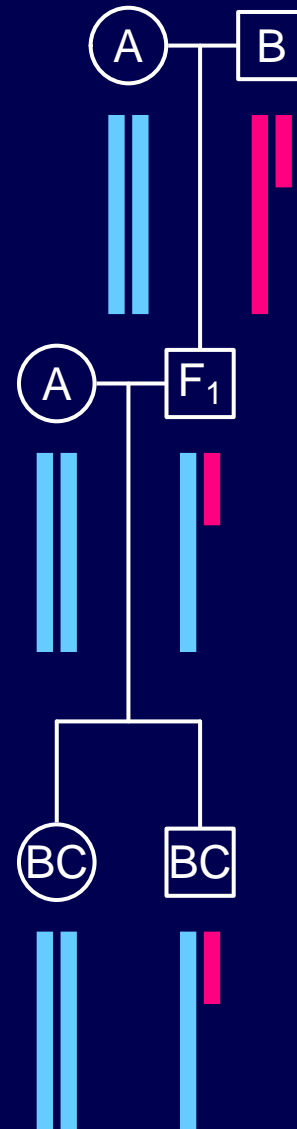
$(A \times B) \times A$



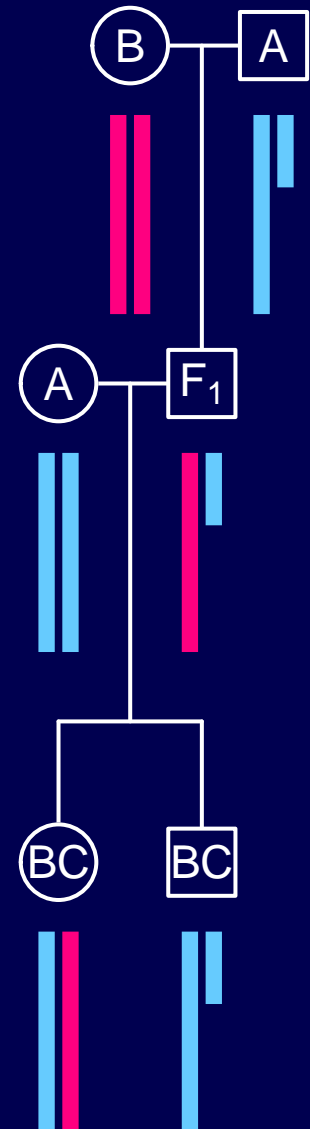
$(B \times A) \times A$



$A \times (A \times B)$

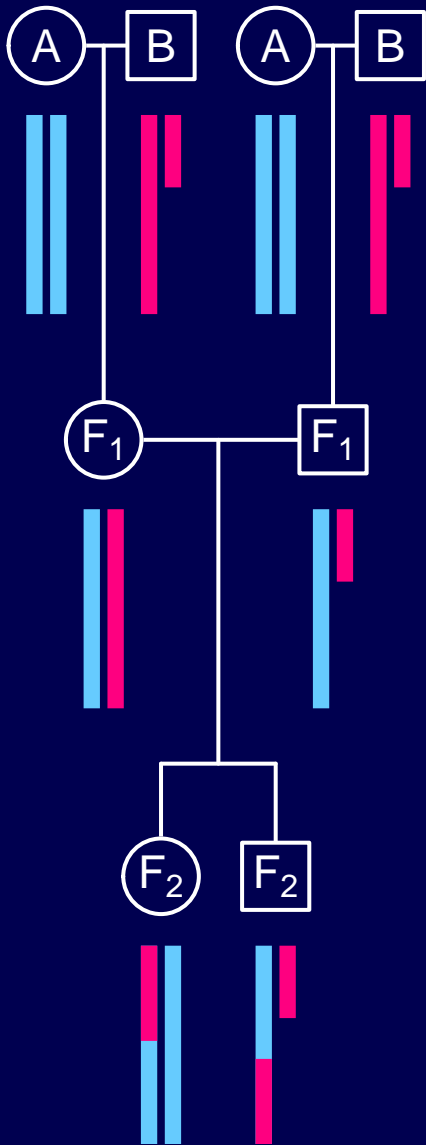


$A \times (B \times A)$

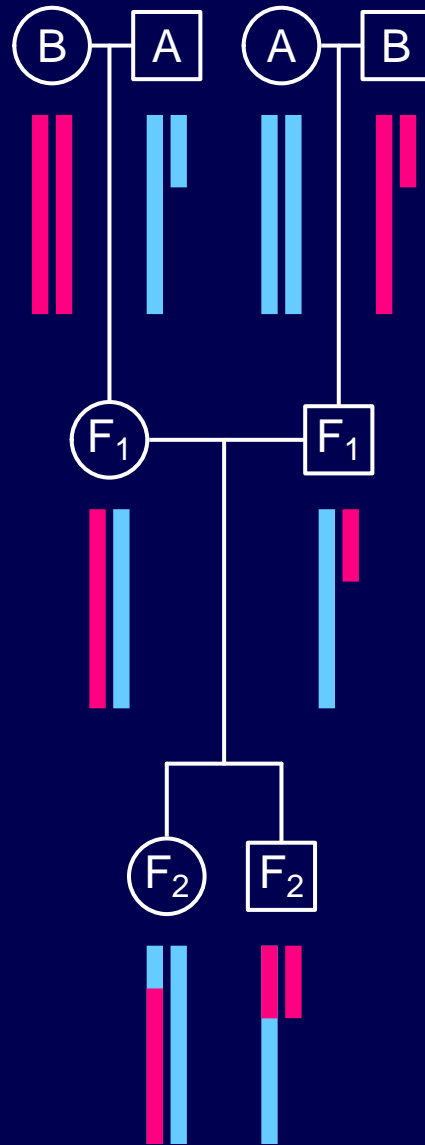


# X chr in intercross

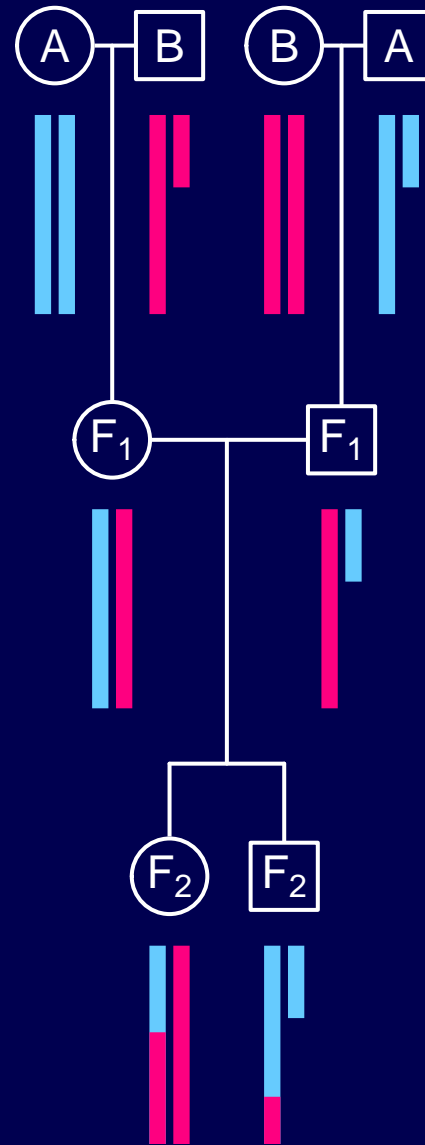
(A x B) x (A x B)



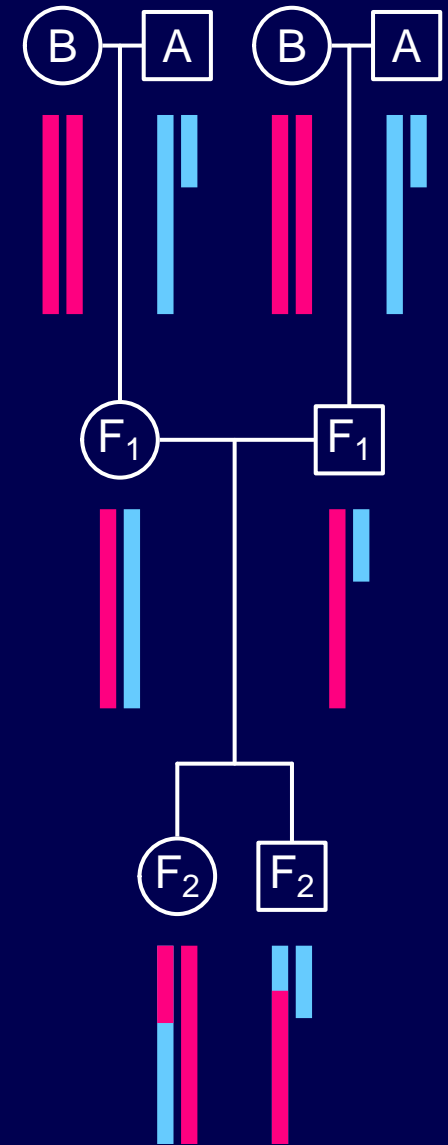
(B x A) x (A x B)



(A x B) x (B x A)



(B x A) x (B x A)



# Example

Intercross: both dir, both sexes

♀ forward      AA or AB

♀ reverse      AB or BB

♂ forward      AY or BY

♂ reverse      AY or BY



→ R

- `scanone()` permutations with `perm.Xsp=TRUE`

# Data diagnostics

- Plot phenotypes
- Look for sample duplicates
- Look for excessive missing data
- Investigate segregation distortion
- Verify genetic maps/marker positions
- Look for genotyping errors
- Look at counts of crossovers

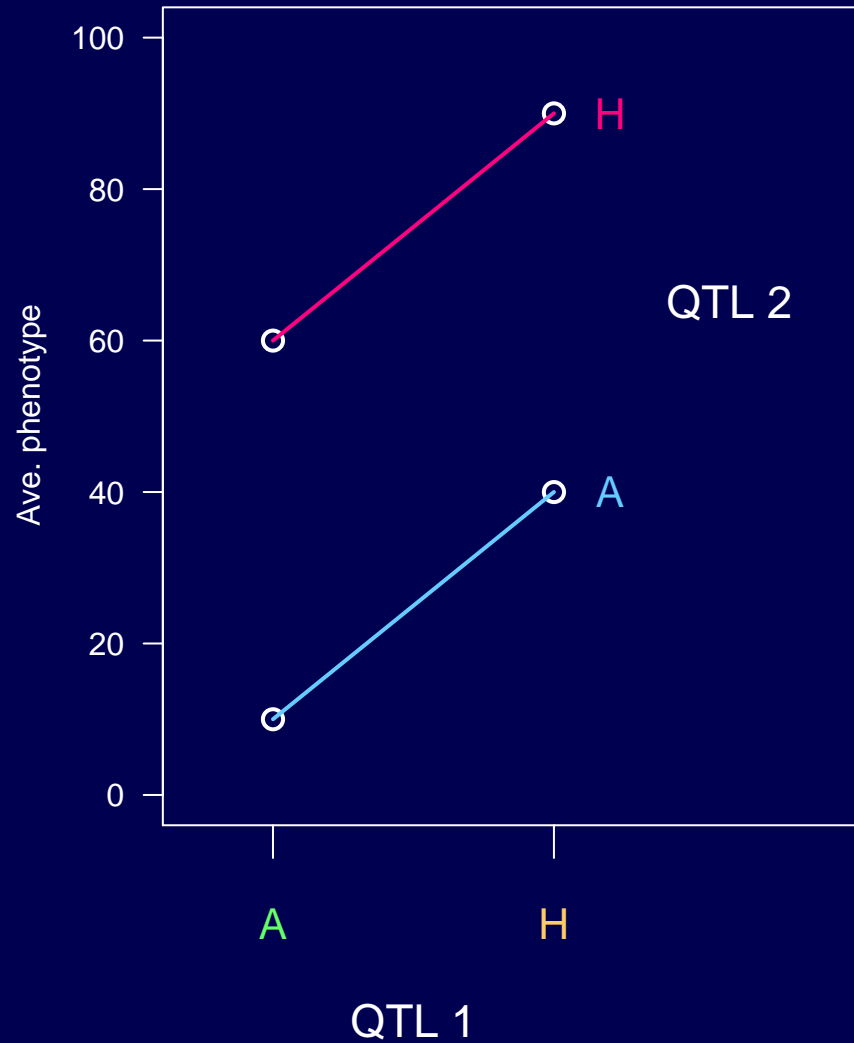
See Ch 3 in the R/qtl book, [rqtl.org/book](http://rqtl.org/book)

# Modeling multiple QTL

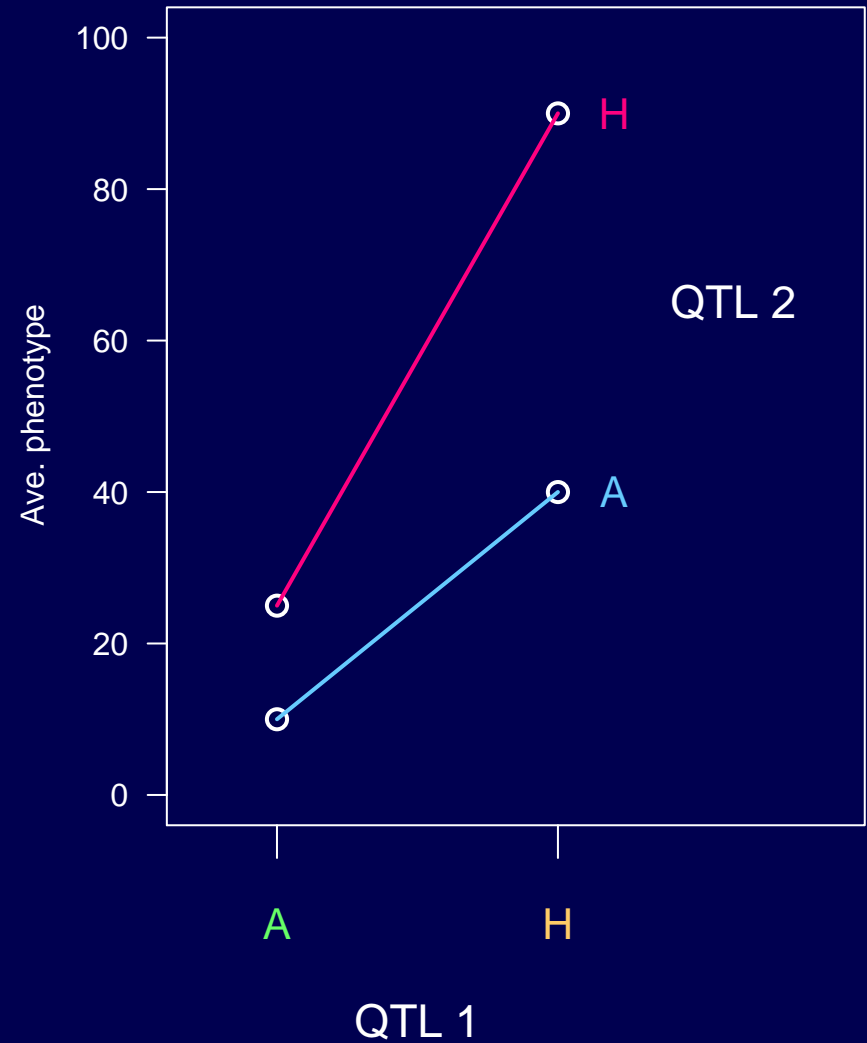
- Reduce residual variation → increased power
- Separate linked QTL
- Identify interactions among QTL (epistasis)

# Epistasis in BC

Additive

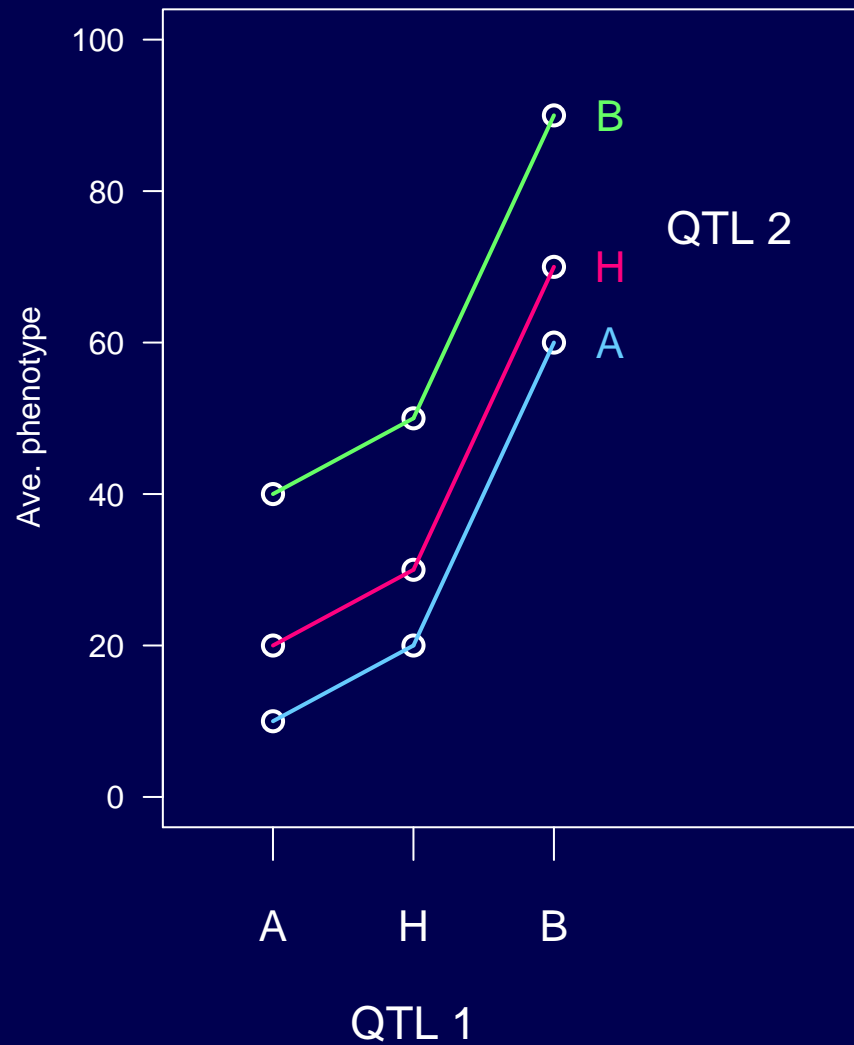


Epistatic

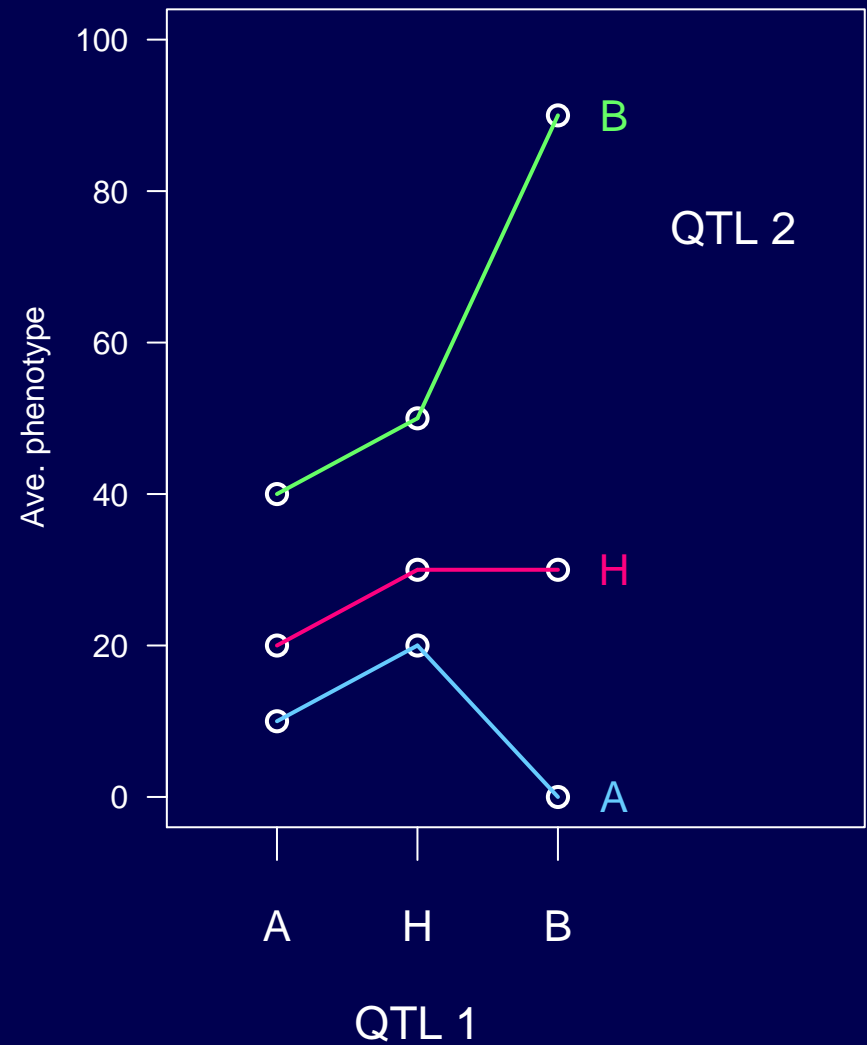


# Epistasis in $F_2$

Additive



Epistatic



## 2-dim, 2-QTL scan

For all pairs of positions, fit the following models:

$$H_f : y = \mu + \beta_1 \mathbf{q}_1 + \beta_2 \mathbf{q}_2 + \gamma \mathbf{q}_1 \mathbf{q}_2 + \epsilon$$

$$H_a : y = \mu + \beta_1 \mathbf{q}_1 + \beta_2 \mathbf{q}_2 + \epsilon$$

$$H_1 : y = \mu + \beta_1 \mathbf{q}_1 + \epsilon$$

$$H_0 : y = \mu + \epsilon$$

$\log_{10}$  likelihoods:

$$l_f(\mathbf{s}, \mathbf{t})$$

$$l_a(\mathbf{s}, \mathbf{t})$$

$$l_1(\mathbf{s})$$

$$l_0$$

## 2-dim, 2-QTL scan

LOD scores:

$$\text{LOD}_f(s, t) = l_f(s, t) - l_0$$

$$\text{LOD}_a(s, t) = l_a(s, t) - l_0$$

$$\text{LOD}_i(s, t) = l_f(s, t) - l_a(s, t)$$

$$\text{LOD}_1(s) = l_1(s) - l_0$$

# Summaries

Consider each pair of chromosomes,  $(j, k)$ ,  
and let  $c(s)$  denote the chromosome for position  $s$ .

$$M_f(j, k) = \max_{c(s)=j, c(t)=k} \text{LOD}_f(s, t)$$

$$M_a(j, k) = \max_{c(s)=j, c(t)=k} \text{LOD}_a(s, t)$$

$$M_1(j, k) = \max_{c(s)=j \text{ or } k} \text{LOD}_1(s)$$

$$M_i(j, k) = M_f(j, k) - M_a(j, k)$$

$$M_{fv1}(j, k) = M_f(j, k) - M_1(j, k)$$

$$M_{av1}(j, k) = M_a(j, k) - M_1(j, k)$$



→ R

- `scantwo()`
- `iplotScantwo()` in **R/qtlcharts**

# Hypothesis testing?

- In the past, QTL mapping has been regarded as a task of hypothesis testing.

Is this a QTL?

Much of the focus has been on adjusting for test multiplicity.

- It is better to view the problem as one of model selection.

What set of QTL are well supported?

Is there evidence for QTL-QTL interactions?

**Model** = a defined set of QTL and QTL-QTL interactions  
(and possibly covariates and QTL-covariate interactions).

# Model selection

- Class of models
  - Additive models
  - + pairwise interactions
  - + higher-order interactions
  - Regression trees
- Model fit
  - Maximum likelihood
  - Haley-Knott regression
  - extended Haley-Knott
  - Multiple imputation
  - MCMC
- Model comparison
  - Estimated prediction error
  - AIC, BIC, penalized likelihood
  - Bayes
- Model search
  - Forward selection
  - Backward elimination
  - Stepwise selection
  - Randomized algorithms

# Target

- Selection of a model includes two types of errors:
  - Miss important terms (QTLs or interactions)
  - Include extraneous terms
- Unlike in hypothesis testing, we can make both errors at the same time.
- Identify as many correct terms as possible, while controlling the rate of inclusion of extraneous terms.

# What is special here?

- Goal: identify the major players
- A continuum of ordinal-valued covariates (the genetic loci)
- Association among the covariates
  - Loci on different chromosomes are independent
  - Along chromosome, a very simple (and known) correlation structure

# Exploratory methods

- Condition on a large-effect QTL
  - Reduce residual variation
  - Conditional LOD score:

$$\text{LOD}(q_2 \mid q_1) = \log_{10} \left\{ \frac{\text{Pr}(\text{data} \mid q_1, q_2)}{\text{Pr}(\text{data} \mid q_1)} \right\}$$

- Piece together the putative QTL from the 1d and 2d scans
  - Omit loci that no longer look interesting (drop-one-at-a-time analysis)
  - Study potential interactions among the identified loci
  - Scan for additional loci (perhaps allowing interactions), conditional on these

→ R

- `scanone()` with marker as additive covariate
- `makeqtl()`, `fitqtl()`, `addqtl()`, `refineqtl()`

# Automation

- Assistance to non-specialists
- Understanding performance
- Many phenotypes



# Additive QTL

$$y = \mu + \sum \beta_j \mathbf{q}_j + \epsilon \quad \text{which } \beta_j \neq 0?$$

$$\text{pLOD}(\gamma) = \text{LOD}(\gamma) - \mathbf{T} |\gamma|$$

# Additive QTL

$$y = \mu + \sum \beta_j \mathbf{q}_j + \epsilon \quad \text{which } \beta_j \neq 0?$$

$$\text{pLOD}(\gamma) = \text{LOD}(\gamma) - \mathbf{T} |\gamma|$$

$$0 \text{ vs } 1 \text{ QTL: } \text{pLOD}(\emptyset) = 0$$

$$\text{pLOD}(\{\lambda\}) = \text{LOD}(\lambda) - \mathbf{T}$$

# Additive QTL

$$y = \mu + \sum \beta_j \mathbf{q}_j + \epsilon \quad \text{which } \beta_j \neq 0?$$

$$\text{pLOD}(\gamma) = \text{LOD}(\gamma) - \mathbf{T} |\gamma|$$

For the mouse genome:

$$\mathbf{T} = 2.69 \text{ (BC) or } 3.52 \text{ (F}_2\text{)}$$

→ R

- `stepwiseqtl()`
- `plotLodProfile()`

# References

- Broman KW (2001) Review of statistical methods for QTL mapping in experimental crosses. *Lab Animal* 30:44–52  
*A review for non-statisticians.*
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