# Introduction: Adaptive trials & sample size re-calculation

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Part of the BBS training: Advanced group-sequential and adaptive
confirmatory clinical trial designs
Basel, 13 Sep 2022

#### **Learning objectives**

#### Participants should understand:

- What are adaptive clinical trials
  - Major subtypes, distinctions, definitions
- Essential statistical methodology of adaptive trials
  - p-value combinations
  - conditional error functions
  - CRP principle
  - Conditional power and sample size adjustment

# What are adaptive designs?

- There are many different types of adaptive trial designs
  - (Group sequential designs, early stopping)
  - Adaptive randomization
  - Adaptive dose escalation
  - Adaptive dose finding
  - Sample size re-estimation
  - Treatment arm selection
  - Enrichment designs
  - ...
- Various «schools» of adaptive designs have developed in parallel, depending on the application area

# What are adaptive designs?

#### Key distinctions:

- Exploratory or confirmatory? → Confirmatory
- Adaptations of which trial features? → Any
- Using unblinded data? → Yes\*
- Predetermined adaptations or ad-hoc? → Both
- Based on interim data or external information? → Both

#### Excluded here:

- Blinded design modifications (e.g. blinded sample size re-estimation; generally not controversial)
- Bayesian designs (frequent in early development phases)
- Response-adaptive randomization

#### Our focus:

Frequentist confirmatory adaptive designs

Our focus:

# Some definitions of adaptive designs

#### Dragalin (PhRMA), 2006:

 A multistage study design that uses accumulating data to decide how to modify aspects of the study without undermining the validity and integrity of the trial. [...] preplanning, as much as possible, based on intended adaptations.

#### FDA draft guidance, 2010:

 A study that includes a prospectively planned opportunity for modification of one or more specified aspects of the study design and hypotheses based on analysis of data (usually interim data) from subjects in the study.

#### EMA reflection paper, 2007:

 A study is called 'adaptive' if statistical methodology allows the modification of a design element [...] at an interim analysis with full control of the type I error.

#### FDA draft guidance, 2018:

 A clinical trial design that allows for prospectively planned modifications to one or more aspects of the design based on accumulating data from subjects in the trial.

## Why adaptive designs

- In the 1980's, group sequential designs were introduced and grew popular. They provided a rigorous theory for early stopping but no other adaptations.
- In practice, however, adaptations of running trials were sometimes needed and done. Their impact on the inference was unclear and often ignored.
- **Quiz**: What is the maximal Type I error for a two-stage group-sequ. test with nominal level 5%\* if n<sub>2</sub> is chosen in light of the observed first stage effect?
  - 5%?
- 8.2%?
- 11.5%?

# **Ignition: Bauer (1989)**

- Idea borrowed from meta-analysis (MA):
  - MA combines the inference from separate trials
  - Now: combine the inference from separate stages of one trial
  - This also allows adapting the second stage based on the first

#### Method as well:

- Take the product of the p-values from both trial stages
- If  $p_1p_2$  is «too small» then reject  $H_0$ .
- Quiz: What is «too small»?
  - Hint: How are  $p_1$  and  $p_2$  distributed under the null hypothesis?

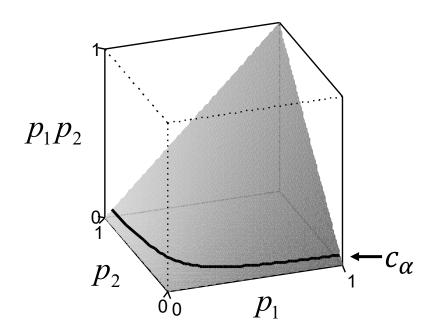
# Fisher's product test

- $p_1, p_2 \sim_{H_0} U[0,1]$  iid
- $-2 \ln(p_1)$ ,  $-2 \ln(p_2) \sim_{H_0} \chi^2_2$  iid
- $-2(\ln(p_1) + \ln(p_2)) \sim_{H_0} \chi^2_4$
- Rejecting  $H_0$  when  $-2(\ln(p_1) + \ln(p_2)) \ge \chi^2_{4,1-\alpha}$  is a level  $\alpha$  test
- Equivalently, rejecting  $H_0$  when

$$p_1 p_2 \le c_{\alpha} = \exp\left(-\frac{1}{2}\chi^2_{4,1-\alpha}\right)$$

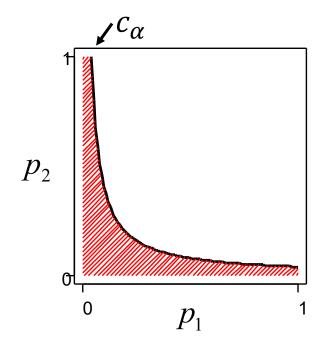
# Let's look at it geometrically

p-value combination



Reject if  $p_1p_2 \leq c_{\alpha}$ 

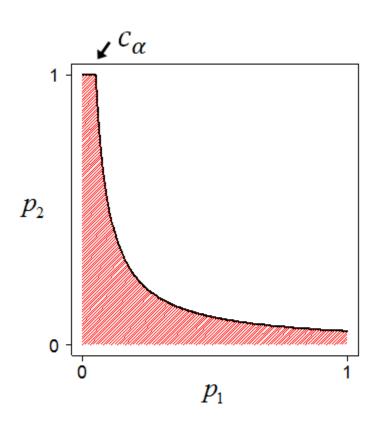
Projection onto the plane



Reject if  $p_2 \le c_\alpha / p_1$ 

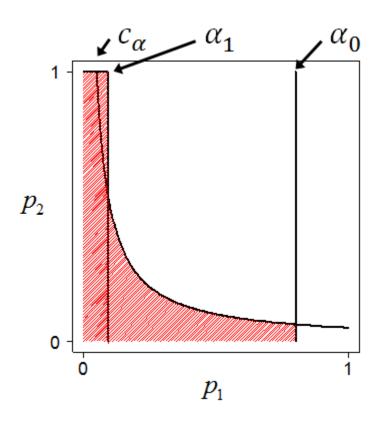
Quiz: How large is the red area?

#### The conditional error function



- Area of rejection region:  $\int_0^{c_\alpha} 1 \, dp_1 + \int_{c_\alpha}^1 c_\alpha/p_1 \, dp_1 = c_\alpha c_\alpha \ln(c_\alpha)$
- But we know this must be α!
  - As  $p_1, p_2 \sim_{H_0} U[0,1]$  iid, areas correspond to probabilities.
  - The rejection region has proba  $\alpha$ .
- This level curve **defines** a level  $\alpha$  test of  $H_0$ . It is called a conditional error function (c.e.f.).
- Every p-value combination defines a family of c.e.f.'s that fills the unit square, and vice versa.

## **Early stopping**



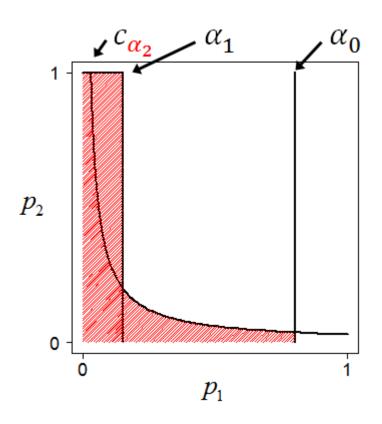
#### • Impose bounds $\alpha_1$ and $\alpha_0$

- Assume  $c_{\alpha} \leq \alpha_1 < \alpha_0$
- $p_1 \le \alpha_1 \rightarrow \text{stop for efficacy}$
- $p_1 > \alpha_0 \rightarrow \text{stop for futility}$
- Otherwise, perform second stage and reject  $H_0$  if  $p_2 \le c_\alpha / p_1$

#### • Red area must remain $\alpha$

• 
$$\alpha_1 + c_{\alpha} (\ln(\alpha_0) - \ln(\alpha_1)) = \alpha$$

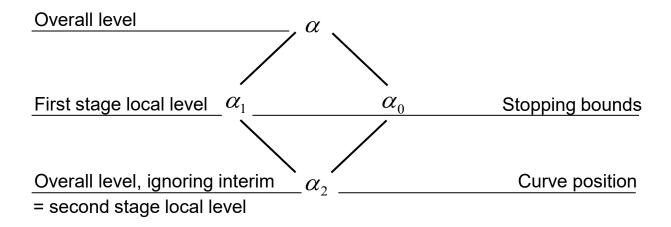
#### **Change height of curve**



- Reject after second stage if  $p_2 \le c_{\alpha_2}/p_1$ 
  - This uses a different c.e.f. of the same family
  - The final test is performed at the local level  $\alpha_2$
- Red area must remain  $\alpha$  $\alpha_1 + c_{\alpha_2} (\ln(\alpha_0) - \ln(\alpha_1)) = \alpha$

#### The «alpha calculus»

Four parameters are interdependent



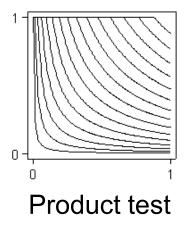
- Level condition:  $\alpha_1 + c_{\alpha_2} (\ln(\alpha_0) \ln(\alpha_1)) = \alpha$
- Quiz:
  - How would you specify a futility stop when control looks better?
  - How would you specify a «Pocock-type» test?

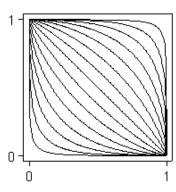
#### Inverse normal method & more

Another natural way to combine p-values:

$$\frac{1}{\sqrt{2}} \left( \Phi^{-1} (1 - p_1) + \Phi^{-1} (1 - p_2) \right) \sim_{H_0} N(0, 1)$$

Same mechanism, with a different family of c.e.f.'s

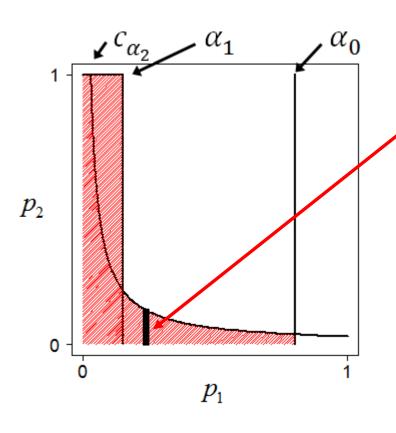




Inverse normal method (INM)

- In principle, any such family defines an adaptive test by this mechanism
  - In practice, mainly these two are used. And out of these, mostly INM.

## How do trial adaptations fit into this?



- This height is the Type I error probability given the first stage data
- We could now change the second stage into any design that respects this level
- The resulting overall procedure remains a level α test

## Why does this work?

- For continuously distributed test statistics based on separate stages,  $p_1, p_2$  will generally be iid U[0,1] under  $H_0$  even if the second stage is modified based on the interim analysis
- More generally, it still works if  $p_1$ ,  $p_2$  are only «p-clud»
  - $P_{H_0}(p_1 \le u) \le u$  and  $P_{H_0}(p_2 \le u \mid p_1) \le u$  for all  $u \in [0,1]$
- For more details on probabilistic foundations, see Brannath et al. 2012.

# **Conditional Rejection Principle (CRP)**

- Start with a (classical) level  $\alpha$  test
- At an IA, review the data and possibly external information
- No reason to adapt → Continue as planned
- Reason to adapt
  - → Compute cond. Type I error of the pre-defined design:

 $P_{H_0}$  (reject  $H_0$  | interim data)

And choose (based on all info) a new design at **this** level to finish the trial

• This is a level  $\alpha$  test, and the IA need not be preplanned

# **Conditional Rejection Principle (CRP)**

- How could that new second-stage design look like?
  - Increase the remaining sample size (e.g., to achieve a desired conditional power → see later)
    - Note: Health authorities view sample size reductions more critically
  - Replace the second stage by another two-stage design 

     multistage designs by «recursive combination»
  - ...and more
- Caveat
  - Adaptations must not jeopardize interpretability of results or credibility of the trial!

## **Relation: Group sequ.** ↔ **adaptive**

- Group sequential designs follow a cumulative philosophy: their test statstics are cumulative
- Adaptive designs follow a stagewise philosophy: they use stagewise inferences (test statistics, p-values)
  - However, the decision rules of adaptive designs combine the stagewise inferences – so overall they do provide cumulative inference
  - For example, Fisher's product test rejects  $H_0$  if  $p_2 \le c_{\alpha_2}/p_1$
- The INM in particular reduces exactly to the group sequential test if no adaptations are done\*. The test statistics, critical values and decision rules are identical.
- → Next slide

## **Relation: Group sequ.** ↔ adaptive

- Test active vs. placebo with normally distr. endpoint
- Group sequential:  $X_{ki} \sim N(\mu, \sigma^2)$  iid,  $Y_{ki} \sim N(\nu, \sigma^2)$  iid
  - k = 1,2 (stage);  $i = 1, ..., n_k$ ;  $\sigma^2$  known
  - $n = n_1 + n_2$  total sample size per arm;  $n_1 = n_2$  without loss of generality
- The Z-test:
  - Overall:  $Z = \sqrt{\frac{n}{2}} \frac{\bar{X} \bar{Y}}{\sigma} \sim H_0 N(0,1)$
  - Per stage:  $Z_k = \sqrt{\frac{n}{4}} \frac{\bar{X}_k \bar{Y}_k}{\sigma} \sim_{H_0} N(0,1); \, p_k = 1 \Phi(Z_k)$
  - Group sequential: Using  $Z_1$  and Z
  - Inverse normal method:

Combining 
$$p_1$$
 and  $p_2$  to  $\frac{1}{\sqrt{2}} (\Phi^{-1}(1-p_1) + \Phi^{-1}(1-p_2)) = \frac{1}{\sqrt{2}} (Z_1 + Z_2) = Z$ 

## **Relation: Group sequ.** ↔ **adaptive**

- The INM therefore generalizes the group sequ. test
  - Standard group sequential software can be used
- It is easily communicated with commonly used (Z-) statistics
- It is also the uniformly most powerful test if no adaptations are done
- All this is why the INM is often the preferred method

#### Weights

- More general version of the INM
  - Combine stagewise statistics using  $w_1Z_1 + w_2Z_2$  instead of  $\frac{1}{\sqrt{2}}(Z_1 + Z_2)$ , with weights  $w_k$
  - Weights can be freely chosen under the constraint  $w_1^2 + w_2^2 = 1$
  - But they must be prespecified and remain fixed regardless of adaptations
    - Otherwise, the type I error may be inflated
  - Natural choice:  $w_k = \sqrt{\frac{n_k}{n_1 + n_2}}$
  - Then all patients carry equal weight, and again we have  $w_1Z_1 + w_2Z_2 = Z$
  - The case  $n_1 = n_2$  above was a special case of this

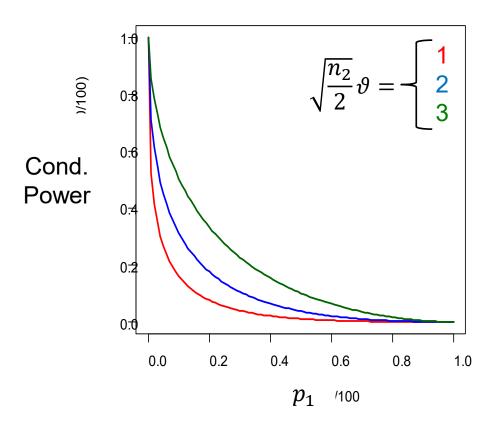
## Efficiency vs. flexibility

- Quiz: What happens to the INM if we change the remaining sample size at the IA?
  - Not all patients carry equal weight → inefficient
- A curious debate
  - Tsiatis, Mehta (2003): "On the inefficiency of the adaptive design [...]"
  - Brannath et al. (2006): "On the efficiency of adaptive designs [...]"
- What do you think?
- In my view, trialists should weigh efficiency (power) against flexibility (adaptation)

- The conditional power is the power of the trial (at some alternative), given interim data
- Let's look at the inverse normal method
- Situation as before:  $X_{ki} \sim N(\mu, \sigma^2)$  iid,  $Y_{ki} \sim N(\nu, \sigma^2)$  iid
  - k = 1,2 (stage);  $i = 1, ..., n_k$
  - $n = n_1 + n_2$  total sample size per arm
  - Denote  $\vartheta = \frac{\mu \nu}{\sigma}$
- → Next slide

• 
$$CP_{\vartheta} = P_{\vartheta} \left( \frac{1}{\sqrt{2}} \left( \Phi^{-1} (1 - p_1) + \Phi^{-1} (1 - p_2) \right) \ge u_{\alpha} \mid p_1 \right)$$
  
 $= P_{\vartheta} \left( \frac{1}{\sqrt{2}} (Z_1 + Z_2) \ge u_{\alpha} \mid Z_1 = z_1 \right)$   
 $= P_{\vartheta} \left( Z_2 \ge \sqrt{2} u_{\alpha} - z_1 \right)$   
 $= P_{\vartheta} \left( Z_2 - \sqrt{\frac{n_2}{2}} \vartheta \ge \sqrt{2} u_{\alpha} - z_1 - \sqrt{\frac{n_2}{2}} \vartheta \right)$   
 $= 1 - \Phi \left( \sqrt{2} u_{\alpha} - z_1 - \sqrt{\frac{n_2}{2}} \vartheta \right)$ 

#### Properties



- Increases with  $n_2$
- Increases with  $\vartheta$
- Decreases for increasing  $p_1$

- Common applications
  - Stopping for futility if  $CP_{\vartheta}$  is «too small» (e.g. below 20%)
  - Adjusting the second stage size to achieve a desired  $CP_{\vartheta}$  (e.g. 90%)

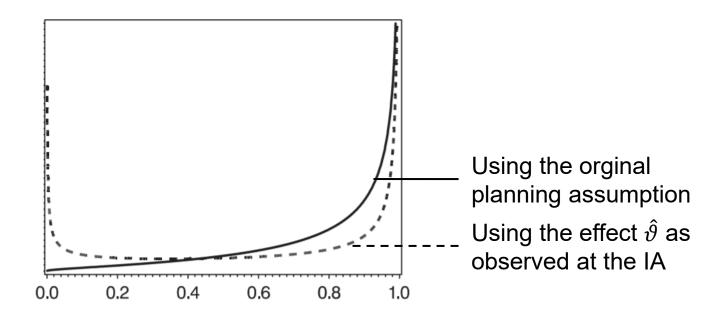
In the example, solve 
$$0.9=1-\Phi\left(\sqrt{2}u_{\alpha}-z_{1}-\sqrt{\frac{n_{2}}{2}}\vartheta\right)$$
 for  $n_{2}$ 

Conduct the second stage and perform the final inference as planned through the adaptive design

• **Quiz**: What  $\vartheta$  would you use in  $CP_{\vartheta}$ ?

- Several options for  $\theta$  in  $CP_{\theta}$ 
  - The originally assumed effect size for sample size calculation (minimally clinically relevant effect – should not have changed!)
  - The effect size  $\hat{\vartheta}$  as observed at the interim analysis (hoping that this comes closer to the «truth»)
    - Caution: Interim estimates such as  $\hat{\vartheta}$  are notoriously volatile!  $\rightarrow$  Next slide
  - Averaging across several choices
    - Weighted average of originally assumed and observed effect size
    - Integrating over some distribution for  $\vartheta$  («predictive power»)

- Using the interim effect estimate is risky
  - Because we rely **doubly** on little data: through  $z_1$  and through  $\hat{\vartheta}$
  - The density of  $CP_{\vartheta}$  tends towards extremes if we use  $\hat{\vartheta}$



# The «Constrained Promising Zone» (CPZ) Approach

- A recent proposal for a more refined use of conditional power to re-calculate the sample size
  - Builds upon the previously proposed «Promising Zone» approach by Mehta and Pocock (2011) which had been shown to be (overly) conservative (Glimm 2012, Jennison and Turnbull 2015)
- Idea: Boost the sample size within reasonable limits when the interim treatment effect appears «promising»

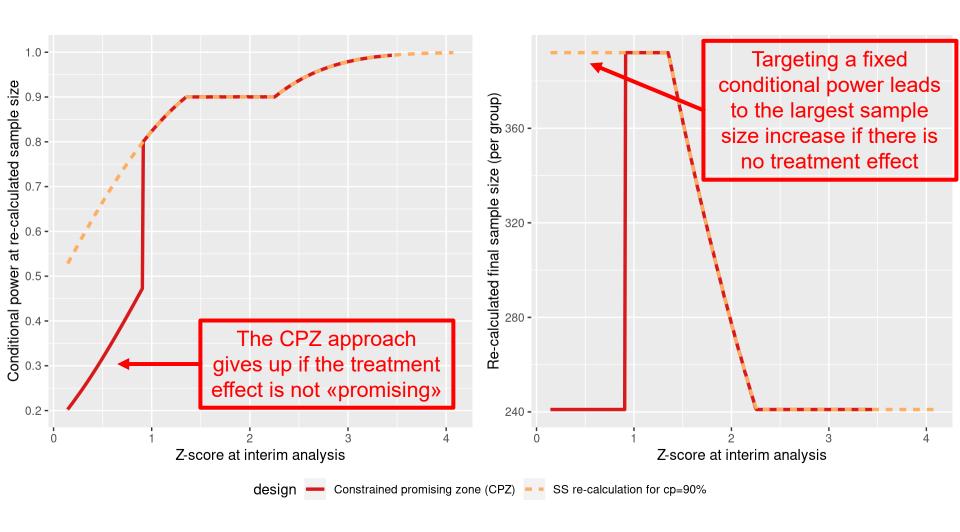
# The «Constrained Promising Zone» (CPZ) Approach

- Concretely, pre-specify:
  - Impose limits to allowed total sample size per arm:  $n_{min}$ ,  $n_{max}$
  - Set smallest clinically meaningful effect size  $\vartheta_{min}$ , and smallest / largest desired conditional power at this point:  $CP_{min}$ ,  $CP_{max}$
  - Choose a combination test, e.g. INM with  $w_1 = \sqrt{\frac{n_1}{n_{min}}}$ ,  $w_2 = \sqrt{\frac{n_{min}-n_1}{n_{min}}}$
- Then re-calculate the sample size at the IA:
  - If  $n^*$  exists between  $n_{min}$  and  $n_{max}$  such that  $CP_{\vartheta_{\min}}(z_1, n^*) = CP_{max}$ , then set the total sample size (per arm) to  $n^*$
  - Otherwise, if  $CP_{\vartheta_{\min}}(z_1, n_{\max}) \ge CP_{\min}$ , then set it to  $n_{\max}$
  - Finally, otherwise, set it to  $n_{min}$  because the IA is not «promising»

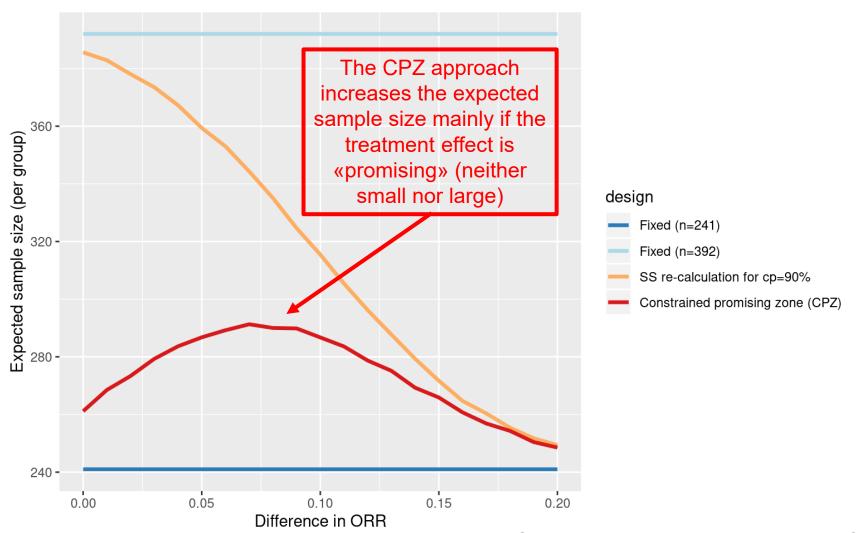
# The «Constrained Promising Zone» (CPZ) Approach - Example

- 1:1 randomization with Overall Response Rate (ORR) as primary endpoint
  - ORR=20% on Control; Drug increases this by 10-13%
  - 2.5% significance level (one-sided)
  - $n_1 = 120$
  - $n_{min} = 241$ ,  $n_{max} = 392$  (90% power for  $\Delta$ =13% and  $\Delta$ =10%, resp.)
- Compare two approaches
  - Sample size increase for a conditional power of 90% (if true  $\Delta$ =10%)
  - CPZ design with  $CP_{min} = 80\%$ ,  $CP_{max} = 90\%$
- Corresponding R-code is in this vignette
  - Simulation of a Trial with a Binary Endpoint and Unblinded Sample
     Size Re-Calculation with rpact

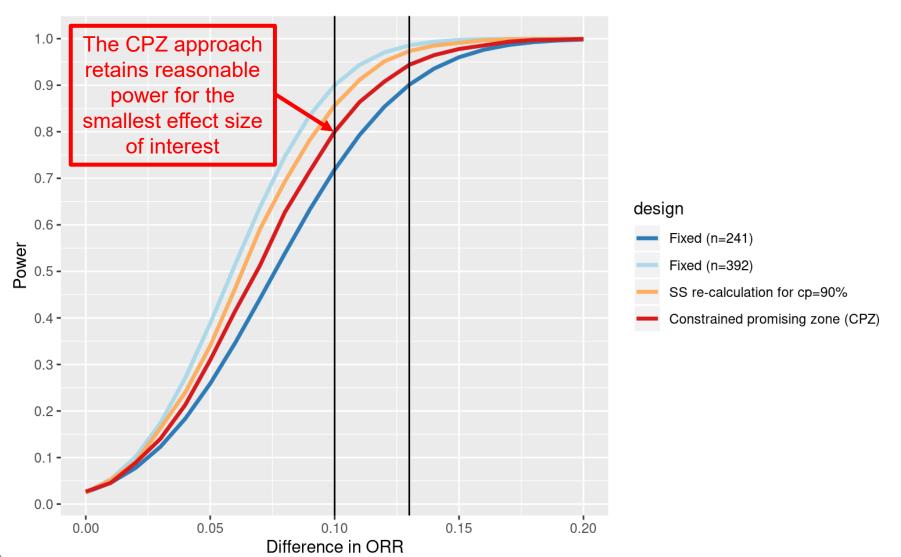
# Cond. power and total sample size depending on the interim Z-score



# Expected sample size depending on effect size



#### Power depending on effect size



# Regulatory guidance on unblinded sample size adaptation

#### EMA guidance on adaptive designs 2007

- The option to reassess sample size in an ongoing trial should not be seen as a substitute for careful planning. The relevance of a particular size of treatment effect should be discussed at the planning stage of the trial and not deferred to the point where interim results are already available.
- Whenever possible, methods for blinded sample size reassessment that properly control the type I error should be used [...]. In cases where sample size needs to be reassessed based on unblinded data, sufficient justification should be made.

#### FDA adaptive designs guidance 2019

- [such designs] might be used when there is considerable uncertainty about the true treatment effect size.
- [...] to appropriately control the Type I error [...and] prospective planning [...of] the statistical hypothesis testing method [...and] the rule governing the sample size modification.
- [...] additional challenges in maintaining trial integrity [...]

# Our recommendations for unblinded sample size adaptation

- Approach is accepted by health authorities, but more justification is needed than for blinded sample size adaptation
- Main application: Considerable uncertainty about the size of the treatment effect and reluctance to fund a group-sequential trial powered to the smallest clinically relevant effect size
  - «Start small and invest more resources if results look promising»
- Extensive literature of such designs versus «more efficient» group-sequential designs
  - E.g., Liu et al, 2018: «...under reasonable decision rules for increasing sample size [...] there is little or no loss of efficiency for the adaptive designs in terms of unconditional power. The two approaches, however, have very different conditional power profiles.»
- Extensive clinical trials simulations and comparisons to group-sequential designs are highly recommended
  - Can also help to explore potential bias in estimation
  - rpact can produce median unbiased estimators and other inference adjusted for the adaptive design

## Final thoughts on adaptive designs

- Allowance for adaptations of the trial design without inflating type I error
  - Adaptations should be pre-planned in most circumstances
  - ...but can be occasionally be used to react to unforeseen circumstances
- Can be extended to multi-arm and enrichment designs (covered later)
- Adaptive designs are more complicated than fixed or group-sequential designs in terms of trial planning, logistics, and regulatory requirements to ensure trial integrity and avoid operational bias
- Two attitudes:
  - The social event trial: «Let's come together, let's see and then adapt until significance» (Koch 2006)
  - Much better: «A multistage study design that uses accumulating data to decide how to modify aspects of the study without undermining the validity and integrity of the trial.» (Dragalin 2006)
- Adaptive designs are not a remedy for sloppy planning!

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#### Reviews

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- Tymofyeyev (2014): A Review of Available Software and Capabilities for Adaptive Designs. Chapter in: Practical Considerations for Adaptive Trial Design and Implementation. Springer

#### **Commercial software**

- ADDPLAN: <a href="http://www.iconplc.com/innovation/addplan/">http://www.iconplc.com/innovation/addplan/</a>
- EastAdapt and EastSurv: <a href="http://www.cytel.com/software/east">http://www.cytel.com/software/east</a>

#### R packages

- adaptTest: <a href="https://cran.r-project.org/web/packages/adaptTest/index.html">https://cran.r-project.org/web/packages/adaptTest/index.html</a>
- AGSDest: <a href="https://cran.r-project.org/web/packages/AGSDest/index.html">https://cran.r-project.org/web/packages/AGSDest/index.html</a>
- asd: <a href="https://cran.r-project.org/web/packages/asd/index.html">https://cran.r-project.org/web/packages/asd/index.html</a>
- rpact: <a href="https://www.rpact.com/">https://www.rpact.com/</a>