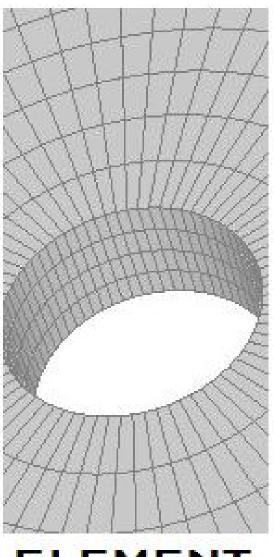
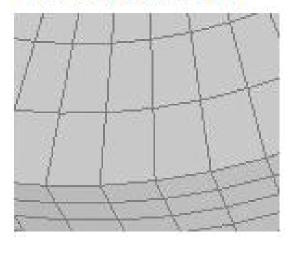
# **VOLUME B**



**ELEMENT LIBRARY** 



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## Introduction

SolidMAT contains an extensive element library. These elements provide coverage of truss, plane stress and plane strain structures, plate, beam and arbitrary shell structures, and full three-dimensional solid structures. A short description of each element and a summary of the data necessary for the use of elements are included in this section. The general outline of element descriptions is as follows,

- Element Characteristics
- Element Assignments
- Element Output

Note that many elements serve the same purpose. You should be aware that though the accuracy of the solution increases with the interpolation degree of elements, the bandwidth of the resulting system stiffness matrix also increases. The optimization of demanded accuracy level, element mesh characteristics and interpolation degrees, and storage-solution time requirements requires you to exercise your analytical skills and judgement. In return, you are rewarded, for instance, by a more accurate stress and displacement picture.

In general, the lower order quadrilateral elements give significantly better results than triangular elements in two dimensions, and similar conclusion applies in three dimensions for hexahedral and tetrahedral elements. For a number of elements in SolidMAT, a selective integration scheme is used to determine the stiffness matrix of the element. This is especially realized for elements using shear-deformable theories, in order to overcome a possible shear locking effect in which case the element stiffness matrix becomes stiff. In such a scheme, the integration of related terms (i.e. transverse shear and/or membrane-bending coupling) is not exact; the contribution of the highest order terms in the deformation field is neglected. Selective integration elements have specific advantages and disadvantages. The most obvious advantage is the reduced cost for element assembly, and as mentioned, more realistic element behavior when the element is very thin. But the same feature also forms the disadvantage of the element. Each of the selective integration elements has some specific higher-order deformation mode(s) which do not give any contribution to the strain energy in the element. So, these elements must be used cautiously.

## **■** Element Classifications

General Classification				
Туре	Geometry	Mechanics	Interpolation	
<u>0</u>	Line	Truss	Linear	
<u>1</u>	Line	Truss	Quadratic	
<u>2</u>	Line	Truss	Cubic	
<u>3</u>	Quadrilateral	Plane Stress	Linear	
<u>4</u>	Quadrilateral	Plane Stress	Quadratic	
<u>5</u>	Triangular	Plane Stress	Linear	
<u>6</u>	Triangular	Plane Stress	Quadratic	
<u>7</u>	Quadrilateral	Plane Stress	Cubic	
<u>8</u>	Quadrilateral	Plane Strain	Linear	
9	Quadrilateral	Plane Strain	Quadratic	
<u>10</u>	Quadrilateral	Plane Strain	Cubic	
<u>11</u>	Triangular	Plane Strain	Linear	
<u>12</u>	Triangular	Plane Strain	Quadratic	
<u>13</u>	Line	Beam	Linear	
<u>14</u>	Line	Beam	Quadratic	
<u>15</u>	Line	Beam	Cubic	
<u>16</u>	Quadrilateral	Shell	Linear	
<u>17</u>	Quadrilateral	Shell	Quadratic	
<u>18</u>	Triangular	Shell	Quadratic	
<u>19</u>	Quadrilateral	Doubly Curved Shell	Linear	
<u>20</u>	Quadrilateral	Doubly Curved Shell	Quadratic	
<u>21</u>	Triangular	Doubly Curved Shell	Quadratic	
<u>22</u>	Hexahedral	Solid	Linear	
<u>23</u>	Hexahedral	Solid	Quadratic	
<u>24</u>	Quadrilateral	Plate	Linear	
<u>25</u>	Quadrilateral	Plate	Quadratic	
<u>26</u>	Triangular	Plate	Quadratic	
<u>27</u>	Line	Curved Beam	Linear	
<u>28</u>	Line	Curved Beam	Quadratic	
<u>29</u>	Line	Curved Beam	Cubic	
<u>30</u>	Tetrahedral	Solid	Linear	
<u>31</u>	Tetrahedral	Solid	Quadratic	

Mechanical Classification		
Mechanics	Туре	
Truss	<u>0</u> , <u>1</u> , <u>2</u>	
Beam	<u>13, 14, 15</u>	
Curved Beam	<u>27, 28, 29</u>	
Plane Stress	<u>3</u> , <u>4</u> , <u>5</u> , <u>6</u> , <u>7</u>	
Plane Strain	<u>8, 9, 10, 11, 12</u>	
Plate	<u>24, 25, 26</u>	
Shell	<u>16, 17, 18</u>	
Doubly Curved Shell	<u>19, 20, 21</u>	
Solid	<u>22, 23, 30, 31</u>	

Geometrical Classification			
Geometry	Туре		
Line	0, 1, 2, 13, 14, 15, 27, 28, 29		
Quadrilateral	3, 4, 7, 8, 9, 10, 16, 17, 19, 20, 24, 25		
Triangular	<u>5, 6, 11, 12, 18, 21, 26</u>		
Hexahedral	<u>22, 23</u>		
Tetrahedral	<u>30, 31</u>		

Interpolation Classification		
Interpolation	Туре	
Linear	0, 3, 5, 8, 11, 13, 16, 19, 22, 24, 27, 30	
Quadratic	1, 4, 6, 9, 12, 14, 17, 18, 20, 21, 23, 25, 26, 28, 31	
Cubic	<u>2, 7, 10, 15, 29</u>	

## Element 0 - Two-node Truss Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight truss element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated analytically.

#### **Geometry and Nodes**

Element has two nodes. Three coordinates per node in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

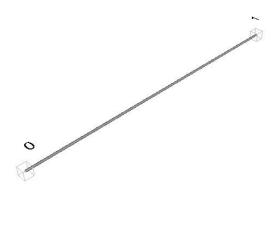


Figure – Element 0

#### Interpolation

Element has linear-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

• u<sub>1</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- Gravity loading in local 1 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit length
- mu<sub>v</sub> translational mass per unit length
- mu<sub>z</sub> translational mass per unit length

Local additional element masses can be applied as follows:

• mu<sub>1</sub> translational mass per unit length

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit length
- su<sub>v</sub> translational stiffness per unit length

• suz translational stiffness per unit length

Local additional element stiffness can be applied as follows:

• su<sub>1</sub> translational stiffness per unit length

## **Element Output**

## **Displacements**

Element output displacements are:

• u<sub>1</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{33}$  normal strain

#### **Stresses**

Element output stresses are:

•  $\sigma_{11}$  normal stress

#### **Forces**

Element output internal forces are:

• N<sub>1</sub> normal force

## Element 1 - Three-node Truss Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight truss element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated analytically.

#### **Geometry and Nodes**

Element has three nodes with the order starting from end nodes. Three coordinates for end nodes in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

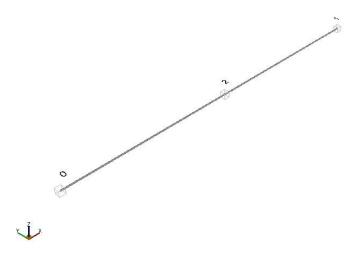


Figure – Element 1

#### Interpolation

Element has quadratic-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement

• u<sub>z</sub> displacement

Local dofs (per node) are:

• u<sub>1</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- Gravity loading in local 1 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit length
- mu<sub>y</sub> translational mass per unit length
- mu<sub>z</sub> translational mass per unit length

Local additional element masses can be applied as follows:

• mu<sub>1</sub> translational mass per unit length

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit length

- su<sub>y</sub> translational stiffness per unit length
- suz translational stiffness per unit length

Local additional element stiffness can be applied as follows:

• su<sub>1</sub> translational stiffness per unit length

## **Element Output**

#### **Displacements**

Element output displacements are:

• u<sub>1</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{33}$  normal strain

#### **Stresses**

Element output stresses are:

•  $\sigma_{11}$  normal stress

#### **Forces**

Element output internal forces are:

• N<sub>1</sub> normal force

## ■ Element 2 - Four-node Truss Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight truss element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated analytically.

#### **Geometry and Nodes**

Element has four nodes with the order starting from end nodes. Three coordinates for end nodes in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

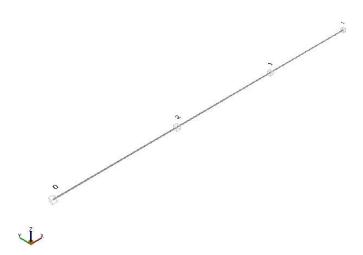


Figure – Element 2

#### Interpolation

Element has quadratic-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement

• u<sub>z</sub> displacement

Local dofs (per node) are:

• u<sub>1</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- Gravity loading in local 1 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit length
- mu<sub>y</sub> translational mass per unit length
- mu<sub>z</sub> translational mass per unit length

Local additional element masses can be applied as follows:

• mu<sub>1</sub> translational mass per unit length

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit length

- su<sub>y</sub> translational stiffness per unit length
- suz translational stiffness per unit length

Local additional element stiffness can be applied as follows:

• su<sub>1</sub> translational stiffness per unit length

## **Element Output**

#### **Displacements**

Element output displacements are:

• u<sub>1</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{33}$  normal strain

#### **Stresses**

Element output stresses are:

•  $\sigma_{11}$  normal stress

#### **Forces**

Element output internal forces are:

• N<sub>1</sub> normal force

## ■ Element 3 - Four-node Plane Stress Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane stress element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction.

#### **Geometry and Nodes**

Element has quadrilateral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

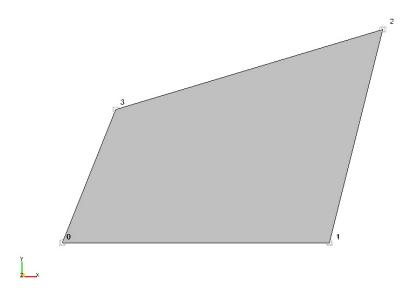


Figure – Element 3

#### Interpolation

Element has bilinear-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement

• u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

### **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>y</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\varepsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\varepsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress
- $\sigma_{12}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- ullet Q<sub>12</sub> membrane shearing force

## Element 4 - Eight-node Plane Stress Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane stress element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated by four-point Gaussian integration in each local direction.

#### **Geometry and Nodes**

Element has quadrilateral geometry and eight nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

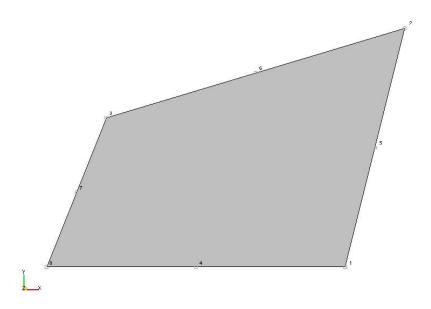


Figure - Element 4

## Interpolation

Element has biquadratic-Serendipity interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

## **Element Output**

#### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

## **■ Element 5 - Three-node Plane Stress Element**

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, triangular plane stress element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness matrix is evaluated by one-point, element mass and stability matrices are evaluated by three-point Gaussian integration in each local direction, respectively.

#### **Geometry and Nodes**

Element has triangular geometry and three nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

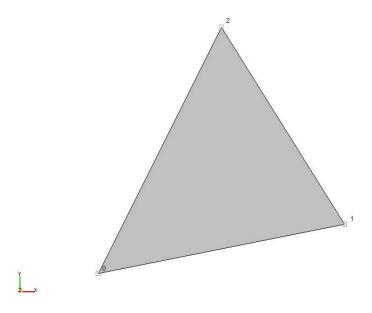


Figure – Element 5

## Interpolation

Element has linear-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

## **Element Output**

#### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

## Element 6 - Six-node Plane Stress Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, triangular plane stress element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction.

#### **Geometry and Nodes**

Element has triangular geometry and six nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

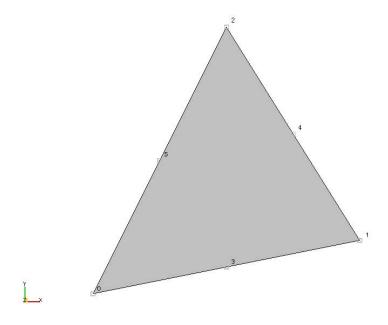


Figure – Element 6

## Interpolation

Element has quadratic-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

## **Element Output**

#### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

## Element 7 - Twelve-node Plane Stress Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane stress element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness and stability matrices are evaluated by eight-point and element mass matrix is evaluated by six-point Gaussian integration in each local direction, respectively.

#### **Geometry and Nodes**

Element has quadrilateral geometry and twelve nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

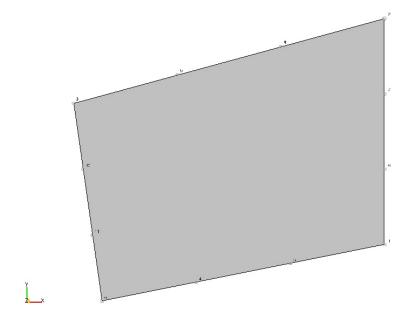


Figure – Element 7

#### Interpolation

Element has bicubic-Serendipity interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

## **Element Assignments**

#### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

## **Element Output**

#### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

## ■ Element 8 - Four-node Plane Strain Element

#### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane strain element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction.

#### **Geometry and Nodes**

Element has quadrilateral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

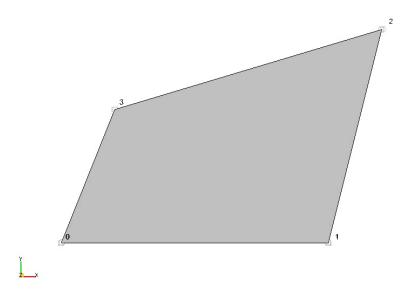


Figure - Element 8

#### Interpolation

Element has bilinear-Lagrange interpolation functions.

#### **Degrees of Freedom**

- u<sub>x</sub> displacement
- u<sub>y</sub> displacement

• u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

#### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>y</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

#### **Strains**

Element output strains are:

- $\varepsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\varepsilon_{12}$  shear strain

### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress
- $\sigma_{12}$  shear stress

# **Forces**

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- ullet Q<sub>12</sub> membrane shearing force

# Element 9 - Eight-node Plane Strain Element

# **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane strain element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated by four-point Gaussian integration in each local direction.

## **Geometry and Nodes**

Element has quadrilateral geometry and eight nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

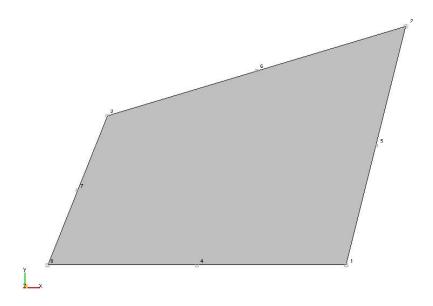


Figure – Element 9

# Interpolation

Element has biquadratic-Serendipity interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

# **Element Assignments**

### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

# **Element Output**

### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

# **Forces**

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

# ■ Element 10 - Twelve-node Plane Strain Element

### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral plane strain element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness and stability matrices are evaluated by eight-point and element mass matrix is evaluated by six-point Gaussian integration in each local direction, respectively.

### **Geometry and Nodes**

Element has quadrilateral geometry and twelve nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

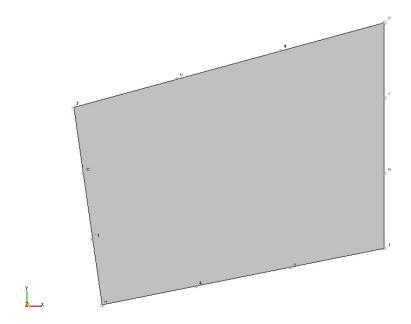


Figure – Element 10

### Interpolation

Element has bicubic-Serendipity interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

# **Element Assignments**

### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>y</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

# **Element Output**

### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- σ<sub>22</sub> normal stress

•  $\sigma_{12}$  shear stress

# **Forces**

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

# Element 11 - Three-node Plane Strain Element

# **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, triangular plane strain element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness matrix is evaluated by one-point, element mass and stability matrices are evaluated by three-point Gaussian integration in each local direction, respectively.

## **Geometry and Nodes**

Element has triangular geometry and three nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

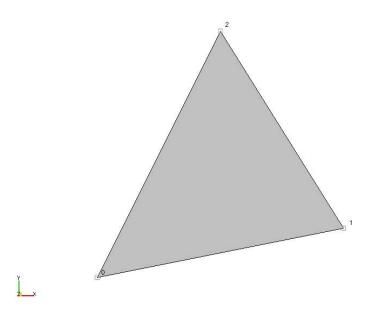


Figure – Element 11

# Interpolation

Element has linear-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

# **Element Assignments**

### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

# **Element Output**

### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- σ<sub>22</sub> normal stress

•  $\sigma_{12}$  shear stress

# **Forces**

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

# Element 12 - Six-node Plane Strain Element

# **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, triangular plane strain element. Isotropic or Orthotropic linear material models can be used with this element. By default, element internal nodes have same local axes with element local axes. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction.

## **Geometry and Nodes**

Element has triangular geometry and six nodes with counterclockwise order starting from corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

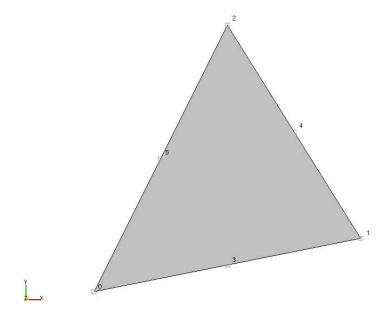


Figure – Element 12

# Interpolation

Element has quadratic-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

# **Element Assignments**

### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)
- Gravity loading in local 1 or 2 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area

# **Element Output**

### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain

#### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress

•  $\sigma_{12}$  shear stress

# **Forces**

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force

# Element 13 - Two-node Thick Beam Element

### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass matrices are evaluated analytically except for the transverse shear terms which are under-integrated against shear locking. Element stability matrix is evaluated by one-point Gaussian integration.

### **Geometry and Nodes**

Element has two nodes. Three coordinates per node in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

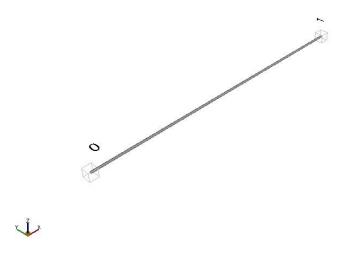


Figure – Element 13

# Interpolation

Element has linear-Lagrange interpolation functions.

# **Degrees of Freedom**

Global dofs (per node) are:

u<sub>x</sub> displacement

- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)

- f<sub>3</sub> force per unit length (uniform or linear)
- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit area

- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain

•  $\epsilon_{13}$  shear strain

# **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

# **Forces**

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

# Element 14 - Three-node Thick Beam Element

### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness and mass matrices are evaluated analytically except for the transverse shear terms which are under-integrated against shear locking. Element stability matrix is evaluated by two-point Gaussian integration.

### **Geometry and Nodes**

Element has three nodes with the order starting from end nodes. Three coordinates for each end node in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

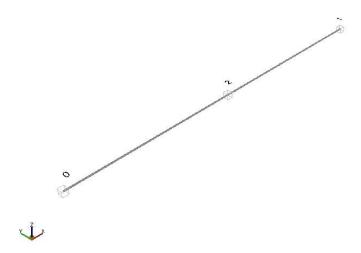


Figure - Element 14

# Interpolation

Element has quadratic-Lagrange interpolation functions.

# **Degrees of Freedom**

Global dofs (per node) are:

• u<sub>x</sub> displacement

- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- $r_v$  rotation
- r<sub>z</sub> rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- $f_z$  force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)

- f<sub>3</sub> force per unit length (uniform or linear)
- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit area

- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

#### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain

•  $\epsilon_{13}$  shear strain

# **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

# **Forces**

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

# Element 15 - Four-node Thick Beam Element

### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant cross section, straight, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness and mass matrices are evaluated analytically. Element stability matrix is evaluated by three-point Gaussian integration.

## **Geometry and Nodes**

Element has four nodes with the order starting from end nodes. Three coordinates for each end node in global x, y and z direction, and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

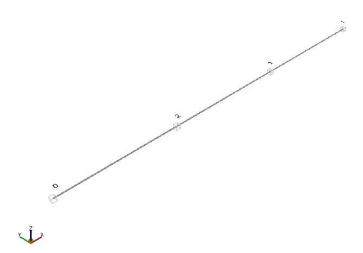


Figure – Element 15

### Interpolation

Element has cubic-Lagrange interpolation functions.

# **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement

- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- $r_z$  rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)
- f<sub>3</sub> force per unit length (uniform or linear)

- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area

- suz translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- $\bullet$  su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain

# Stresses

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

# **Forces**

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

# ■ Element 16 - Four-node Thick Shell Element

### **Element Characteristics**

#### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, flat, shear deformable (Mindlin-Reissner) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction while the transverse shear terms are under-integrated against shear locking.

### **Geometry and Nodes**

Element has quadrilateral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

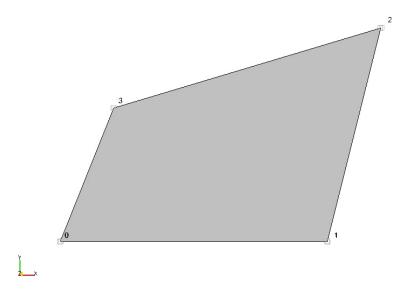


Figure - Element 16

### Interpolation

Element has bilinear-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

- $\varepsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- $\sigma_{11}$  normal stress
- σ<sub>22</sub> normal stress
- $\sigma_{33}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 17 - Eight-node Thick Shell Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, flat, shear deformable (Mindlin-Reissner) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction while the transverse shear terms are under-integrated against shear locking.

# **Geometry and Nodes**

Element has quadrilateral geometry and eight nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

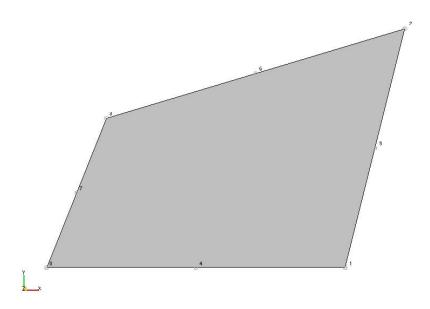


Figure – Element 17

## Interpolation

Element has biquadratic-Serendipity interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

# Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Strains**

- $\varepsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- σ<sub>11</sub> normal stress
- σ<sub>22</sub> normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 18 - Six-node Thick Shell Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, triangular, flat, shear deformable (Mindlin-Reissner) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by seven-point Gaussian integration while the transverse shear terms are under-integrated against shear locking.

# **Geometry and Nodes**

Element has triangular geometry and six nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

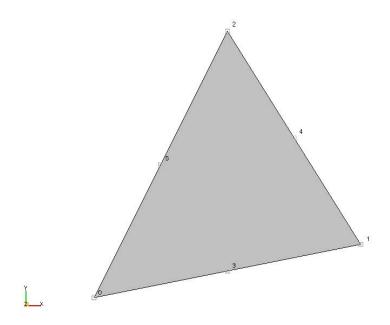


Figure – Element 18

# Interpolation

Element has linear-Lagrange interpolation functions.

# **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- $r_x$  rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

# Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

- $\varepsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- σ<sub>11</sub> normal stress
- σ<sub>22</sub> normal stress
- $\sigma_{33}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 19 - Four-node Doubly Curved Thick Shell Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, doubly curved, shear deformable (Sander) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction while the transverse shear and membrane-bending coupling terms are under-integrated against shear and membrane locking.

## **Geometry and Nodes**

Element has quadrilateral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, radii of curvatures in each local direction and a constant thickness are given as input.

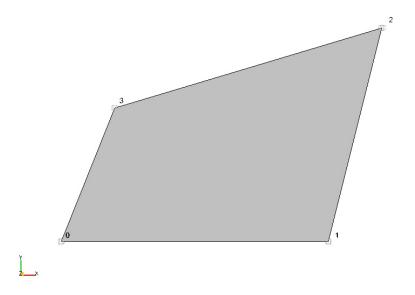


Figure – Element 19

### Interpolation

Element has bilinear-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

# Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- σ<sub>11</sub> normal stress
- σ<sub>22</sub> normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 20 - Eight-node Doubly Curved Thick Shell Element

## **Element Characteristics**

# **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, doubly curved, shear deformable (Sander) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction while the transverse shear and membrane-bending coupling terms are under-integrated against shear and membrane locking.

## **Geometry and Nodes**

Element has quadrilateral geometry and eight nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, radii of curvatures in each local direction and a constant thickness are given as input.

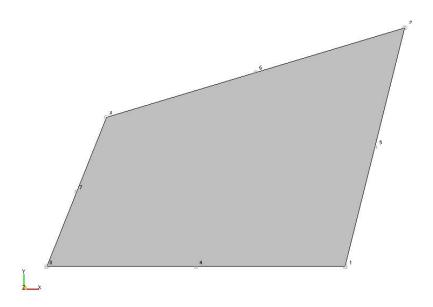


Figure – Element 20

## Interpolation

Element has biquadratic-Serendipity interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- $r_x$  rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

# Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

- $\varepsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- σ<sub>11</sub> normal stress
- σ<sub>22</sub> normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# Element 21 - Six-node Doubly Curved Thick Shell Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, triangular, doubly curved, shear deformable (Sander) shell element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by seven-point Gaussian integration while the transverse shear and membrane-bending coupling terms are underintegrated against shear and membrane locking.

# **Geometry and Nodes**

Element has triangular geometry and six nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, radii of curvatures in each local direction and a constant thickness are given as input.

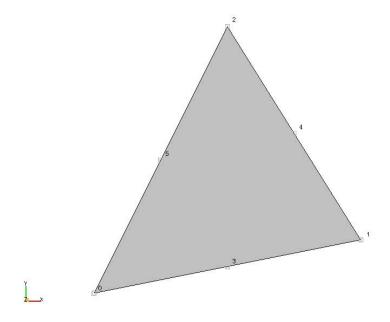


Figure – Element 21

## Interpolation

Element has linear-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

# Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit area (uniform or bilinear)
- f<sub>2</sub> force per unit area (uniform or bilinear)

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area

- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- σ<sub>11</sub> normal stress
- $\sigma_{22}$  normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

Element output internal forces are:

- P<sub>11</sub> membrane force
- N<sub>22</sub> membrane force
- Q<sub>12</sub> membrane shearing force
- F<sub>13</sub> shear force
- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 22 - Eight-node Solid Element

# **Element Characteristics**

### **Mechanics**

This is a three dimensional, hexahedral, solid element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction.

# **Geometry and Nodes**

Element has hexahedral geometry and eight nodes with counterclockwise order starting from the top side. Three coordinates per node in global x, y and z direction are given as input.

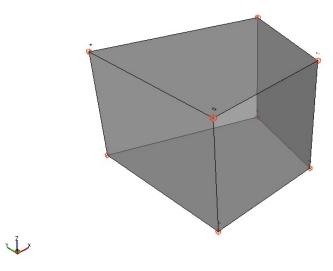


Figure – Element 22

## Interpolation

Element has trilinear-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit volume (uniform)
- f<sub>v</sub> force per unit volume (uniform)
- f<sub>z</sub> force per unit volume (uniform)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit volume (uniform)
- f<sub>2</sub> force per unit volume (uniform)
- f<sub>3</sub> force per unit volume (uniform)
- Gravity loading in local 1, 2 or 3 direction

# **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit volume
- mu<sub>v</sub> translational mass per unit volume
- mu<sub>z</sub> translational mass per unit volume

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit volume
- mu<sub>2</sub> translational mass per unit volume

• mu<sub>3</sub> translational mass per unit volume

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit volume
- su<sub>v</sub> translational stiffness per unit volume
- su<sub>z</sub> translational stiffness per unit volume

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit volume
- su<sub>2</sub> translational stiffness per unit volume
- su<sub>3</sub> translational stiffness per unit volume

# **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

## **Strains**

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{33}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\bullet \quad \sigma_{22} \ normal \ stress$
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

# **Forces**

No internal element forces are available for this element.

# ■ Element 23 - Twenty-node Solid Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, hexahedral, solid element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction.

# **Geometry and Nodes**

Element has hexahedral geometry and twenty nodes with counterclockwise order starting from the top side and vertex nodes. Three coordinates for each vertex node in global x, y and z direction are given as input.

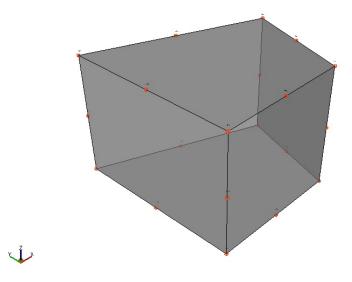


Figure – Element 23

# Interpolation

Element has triquadratic-Serendipity interpolation functions.

# **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

# **Element Assignments**

# **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit volume (uniform)
- f<sub>v</sub> force per unit volume (uniform)
- f<sub>z</sub> force per unit volume (uniform)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit volume (uniform)
- f<sub>2</sub> force per unit volume (uniform)
- f<sub>3</sub> force per unit volume (uniform)
- Gravity loading in local 1, 2 or 3 direction

## **Temperature Loading**

Element can be loaded with constant temperature.

# **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit volume
- mu<sub>v</sub> translational mass per unit volume
- mu<sub>z</sub> translational mass per unit volume

Local additional element masses can be applied as follows:

• mu<sub>1</sub> translational mass per unit volume

- mu<sub>2</sub> translational mass per unit volume
- mu<sub>3</sub> translational mass per unit volume

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit volume
- su<sub>v</sub> translational stiffness per unit volume
- suz translational stiffness per unit volume

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit volume
- su<sub>2</sub> translational stiffness per unit volume
- su<sub>3</sub> translational stiffness per unit volume

# **Element Output**

# **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

#### **Strains**

- $\varepsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\varepsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\bullet \quad \sigma_{22} \ normal \ stress$
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

# **Forces**

No internal element forces are available for this element.

## ■ Element 24 - Four-node Thick Plate Element

### **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, shear deformable (Mindlin-Reissner) plate element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction while the transverse shear terms are under-integrated against shear locking.

### **Geometry and Nodes**

Element has quadrilateral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction, and a constant thickness are given as input.

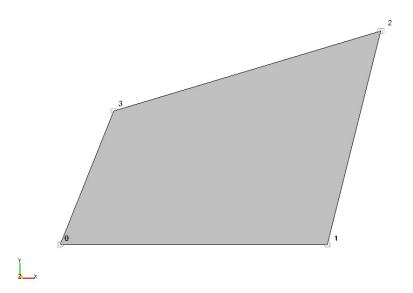


Figure - Element 24

### Interpolation

Element has bilinear-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 3 direction

### **Temperature Loading**

No temperature loading is available for this element.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>y</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>y</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area

• sr<sub>2</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\epsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress
- $\sigma_{33}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

### **Forces**

Element output internal forces are:

• F<sub>13</sub> shear force

- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# Element 25 - Eight-node Thick Plate Element

### **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, quadrilateral, shear deformable (Mindlin-Reissner) plate element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by three-point Gaussian integration in each local direction while the transverse shear terms are under-integrated against shear locking.

### **Geometry and Nodes**

Element has quadrilateral geometry and eight nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

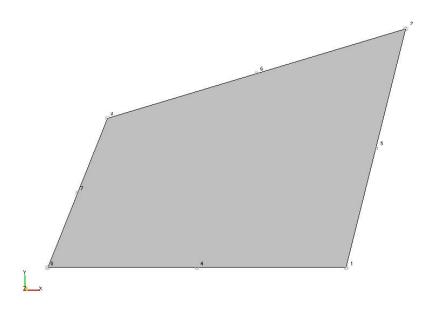


Figure – Element 25

### Interpolation

Element has biquadratic-Serendipity interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 3 direction

### **Temperature Loading**

No temperature loading is available for this element.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area

• sr<sub>2</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\epsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- σ<sub>22</sub> normal stress
- $\sigma_{33}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

### **Forces**

Element output internal forces are:

• F<sub>13</sub> shear force

- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 26 - Six-node Thick Plate Element

### **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant thickness, triangular, shear deformable (Mindlin-Reissner) plate element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by seven-point Gaussian integration while the transverse shear terms are under-integrated against shear locking.

### **Geometry and Nodes**

Element has triangular geometry and six nodes with counterclockwise order starting from the corner nodes. Three coordinates for each corner node in global x, y and z direction, and a constant thickness are given as input.

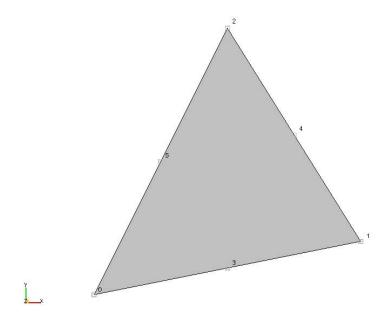


Figure – Element 26

## Interpolation

Element has quadratic-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit area (uniform or bilinear)
- f<sub>v</sub> force per unit area (uniform or bilinear)
- f<sub>z</sub> force per unit area (uniform or bilinear)
- m<sub>x</sub> moment per unit area (uniform or bilinear)
- m<sub>v</sub> moment per unit area (uniform or bilinear)
- m<sub>z</sub> moment per unit area (uniform or bilinear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>3</sub> force per unit area (uniform or bilinear)
- m<sub>1</sub> moment per unit area (uniform or bilinear)
- m<sub>2</sub> moment per unit area (uniform or bilinear)
- Gravity loading in local 3 direction

### **Temperature Loading**

No temperature loading is available for this element.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>y</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area
- su<sub>z</sub> translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area

• sr<sub>2</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\epsilon_{12}$  shear strain
- $\epsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

### **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- σ<sub>22</sub> normal stress
- $\sigma_{33}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

### **Forces**

Element output internal forces are:

• F<sub>13</sub> shear force

- H<sub>23</sub> shear force
- K<sub>22</sub> bending moment
- M<sub>11</sub> bending moment
- T<sub>12</sub> twisting moment

# ■ Element 27 - Two-node Curved Thick Beam Element

### **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant cross section, curved, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness and mass matrices are evaluated analytically except for the transverse shear terms which are under-integrated against shear locking. Element stability matrix is evaluated by one-point Gaussian integration.

### **Geometry and Nodes**

Element has two nodes. Three coordinates per node in global x, y and z direction, radius of curvature and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

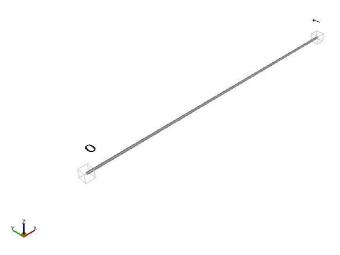


Figure – Element 27

## Interpolation

Element has linear-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

• u<sub>x</sub> displacement

- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)

- f<sub>3</sub> force per unit length (uniform or linear)
- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit area

- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain

•  $\varepsilon_{13}$  shear strain

## **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

## **Forces**

Element output internal forces are:

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

# Element 28 - Three-node Curved Thick Beam Element

### **Element Characteristics**

## **Mechanics**

This is a three dimensional, constant cross section, curved, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness and mass matrices are evaluated analytically except for the transverse shear terms which are under-integrated against shear locking. Element stability matrix is evaluated by two-point Gaussian integration.

### **Geometry and Nodes**

Element has three nodes with the order starting from end nodes. Three coordinates for each end node in global x, y and z direction, radius of curvature and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

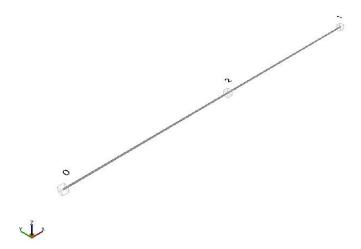


Figure - Element 28

## Interpolation

Element has quadratic-Lagrange interpolation functions.

## **Degrees of Freedom**

Global dofs (per node) are:

• u<sub>x</sub> displacement

- u<sub>v</sub> displacement
- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- r<sub>z</sub> rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- $f_x$  force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- $f_z$  force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)

- f<sub>3</sub> force per unit length (uniform or linear)
- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

## **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

• su<sub>x</sub> translational stiffness per unit area

- su<sub>v</sub> translational stiffness per unit area
- suz translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>v</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain

•  $\epsilon_{13}$  shear strain

## **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

## **Forces**

Element output internal forces are:

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

## Element 29 - Four-node Curved Thick Beam Element

### **Element Characteristics**

### **Mechanics**

This is a three dimensional, constant cross section, curved, shear deformable (Timoshenko) beam element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness and mass matrices are evaluated analytically. Element stability matrix is evaluated by three-point Gaussian integration.

### **Geometry and Nodes**

Element has four nodes with the order starting from end nodes. Three coordinates for each end node in global x, y and z direction, radius of curvature and a constant cross section are given as input. Axial rotation can be assigned as user-defined local axes.

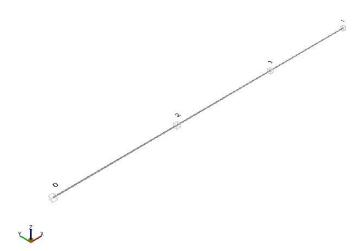


Figure – Element 29

### Interpolation

Element has cubic-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement

- u<sub>z</sub> displacement
- r<sub>x</sub> rotation
- r<sub>v</sub> rotation
- $r_z$  rotation

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit length (uniform or linear)
- f<sub>v</sub> force per unit length (uniform or linear)
- f<sub>z</sub> force per unit length (uniform or linear)
- m<sub>x</sub> moment per unit length (uniform or linear)
- m<sub>v</sub> moment per unit length (uniform or linear)
- m<sub>z</sub> moment per unit length (uniform or linear)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit length (uniform or linear)
- f<sub>2</sub> force per unit length (uniform or linear)
- f<sub>3</sub> force per unit length (uniform or linear)

- m<sub>1</sub> moment per unit length (uniform or linear)
- m<sub>2</sub> moment per unit length (uniform or linear)
- m<sub>3</sub> moment per unit length (uniform or linear)
- Gravity loading in local 1, 2 or 3 direction

## **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit area
- mu<sub>v</sub> translational mass per unit area
- mu<sub>z</sub> translational mass per unit area
- mr<sub>x</sub> rotational mass per unit area
- mr<sub>v</sub> rotational mass per unit area
- mr<sub>z</sub> rotational mass per unit area

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit area
- mu<sub>2</sub> translational mass per unit area
- mu<sub>3</sub> translational mass per unit area
- mr<sub>1</sub> rotational mass per unit area
- mr<sub>2</sub> rotational mass per unit area
- mr<sub>3</sub> rotational mass per unit area

#### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit area
- su<sub>v</sub> translational stiffness per unit area

- suz translational stiffness per unit area
- sr<sub>x</sub> rotational stiffness per unit area
- sr<sub>y</sub> rotational stiffness per unit area
- sr<sub>z</sub> rotational stiffness per unit area

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit area
- su<sub>2</sub> translational stiffness per unit area
- su<sub>3</sub> translational stiffness per unit area
- sr<sub>1</sub> rotational stiffness per unit area
- sr<sub>2</sub> rotational stiffness per unit area
- sr<sub>3</sub> rotational stiffness per unit area

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement
- r<sub>1</sub> rotation
- r<sub>2</sub> rotation
- r<sub>3</sub> rotation

### **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\epsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain

## **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress

## **Forces**

Element output internal forces are:

- N<sub>1</sub> normal force
- V<sub>2</sub> shear force
- V<sub>3</sub> shear force
- T<sub>1</sub> twisting moment
- M<sub>2</sub> bending moment
- M<sub>3</sub> bending moment

## Element 30 - Four-node Solid Element

## **Element Characteristics**

### **Mechanics**

This is a three dimensional, tetrahedral, solid element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by two-point Gaussian integration in each local direction.

## **Geometry and Nodes**

Element has tetrahedral geometry and four nodes with counterclockwise order. Three coordinates per node in global x, y and z direction are given as input.

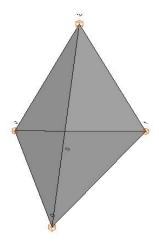




Figure – Element 30

## Interpolation

Element has trilinear-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

Local dofs (per node) are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

## **Element Assignments**

### **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit volume (uniform)
- f<sub>v</sub> force per unit volume (uniform)
- f<sub>z</sub> force per unit volume (uniform)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit volume (uniform)
- f<sub>2</sub> force per unit volume (uniform)
- f<sub>3</sub> force per unit volume (uniform)
- Gravity loading in local 1, 2 or 3 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

#### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit volume
- mu<sub>v</sub> translational mass per unit volume
- mu<sub>z</sub> translational mass per unit volume

Local additional element masses can be applied as follows:

- mu<sub>1</sub> translational mass per unit volume
- mu<sub>2</sub> translational mass per unit volume

• mu<sub>3</sub> translational mass per unit volume

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit volume
- su<sub>v</sub> translational stiffness per unit volume
- su<sub>z</sub> translational stiffness per unit volume

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit volume
- su<sub>2</sub> translational stiffness per unit volume
- su<sub>3</sub> translational stiffness per unit volume

## **Element Output**

### **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

## **Strains**

Element output strains are:

- $\epsilon_{11}$  normal strain
- $\varepsilon_{22}$  normal strain
- $\epsilon_{33}$  normal strain
- $\varepsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

## **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

No internal element forces are available for this element.

## Element 31 - Ten-node Solid Element

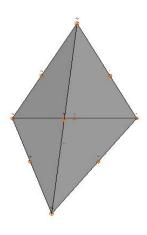
## **Element Characteristics**

### **Mechanics**

This is a three dimensional, tetrahedral, solid element. Isotropic or Orthotropic linear material models can be used with this element. Element stiffness, mass and stability matrices are evaluated by four-point Gaussian integration in each local direction.

### **Geometry and Nodes**

Element has tetrahedral geometry and ten nodes with counterclockwise order starting from the vertex nodes. Three coordinates for each vertex node in global x, y and z direction are given as input.



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Figure – Element 31

### Interpolation

Element has triquadratic-Lagrange interpolation functions.

### **Degrees of Freedom**

Global dofs (per node) are:

- u<sub>x</sub> displacement
- u<sub>v</sub> displacement
- u<sub>z</sub> displacement

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

## **Element Assignments**

## **Mechanical Loading**

Distributed global loads can be applied as follows:

- f<sub>x</sub> force per unit volume (uniform)
- f<sub>v</sub> force per unit volume (uniform)
- f<sub>z</sub> force per unit volume (uniform)
- Gravity loading in global x, y or z direction

Distributed local loads can be applied as follows:

- f<sub>1</sub> force per unit volume (uniform)
- f<sub>2</sub> force per unit volume (uniform)
- f<sub>3</sub> force per unit volume (uniform)
- Gravity loading in local 1, 2 or 3 direction

### **Temperature Loading**

Element can be loaded with constant temperature.

### **Additional Mass**

Global additional element masses can be applied as follows:

- mu<sub>x</sub> translational mass per unit volume
- mu<sub>y</sub> translational mass per unit volume
- mu<sub>z</sub> translational mass per unit volume

Local additional element masses can be applied as follows:

• mu<sub>1</sub> translational mass per unit volume

- mu<sub>2</sub> translational mass per unit volume
- mu<sub>3</sub> translational mass per unit volume

### **Additional Stiffness**

Global additional element stiffness can be applied as follows:

- su<sub>x</sub> translational stiffness per unit volume
- su<sub>v</sub> translational stiffness per unit volume
- suz translational stiffness per unit volume

Local additional element stiffness can be applied as follows:

- su<sub>1</sub> translational stiffness per unit volume
- su<sub>2</sub> translational stiffness per unit volume
- su<sub>3</sub> translational stiffness per unit volume

## **Element Output**

## **Displacements**

Element output displacements are:

- u<sub>1</sub> displacement
- u<sub>2</sub> displacement
- u<sub>3</sub> displacement

#### **Strains**

Element output strains are:

- $\varepsilon_{11}$  normal strain
- $\epsilon_{22}$  normal strain
- $\varepsilon_{33}$  normal strain
- $\varepsilon_{12}$  shear strain
- $\varepsilon_{13}$  shear strain
- $\varepsilon_{23}$  shear strain

## **Stresses**

Element output stresses are:

- $\sigma_{11}$  normal stress
- $\sigma_{22}$  normal stress
- σ<sub>33</sub> normal stress
- $\sigma_{12}$  shear stress
- $\sigma_{13}$  shear stress
- $\sigma_{23}$  shear stress

## **Forces**

No internal element forces are available for this element.