

## MECHATRONICS ENGINEERING GRADUATION PROJECT CODES

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Some of the codes which we used them to implement our algorithmic categories and control scenarios of robot manipulator consists of both Arduino, and python scratch codes.

We expressed them as will be shown in the following sections .

### 1-Trajectory generation task

This algorithm has been created to be used in trajectory generation for all manipulators and it can be change instantly by manipulation just with end effector position and orientation desired values.

```
import sys                                ###main code for trajectory generation
import time
import numpy as np
import math as m
import matplotlib.pyplot as plt
from pylab import *
import time
import serial
import sympy
a2=230;b2=230;TH2F1=(1214-1172); TH2F2=(1228-1158);
XE2=b2*m.cos((TH2F1+TH2F2)*m.pi/180)+a2*m.cos(TH2F1*m.pi/180);
YE2=b2*m.sin((TH2F1+TH2F2)*m.pi/180)+a2*m.sin(TH2F1*m.pi/180);
print(XE2,YE2)                            ##THE END OF FORWARD
tf21=8;tf22=8 #time period definition
t=np.arange(0,8,1);# path in between points
```

```

#x2=80;y2=200 #second station of end effector

a2=230;b2=230 #links length

#algorithm to obtain via point and end effector positions

x22, y22 = sympy.symbols("x22 y22", real=True) #to solve system equation


x21=XE2;x23=0;y21=YE2;y23=321;#position w.r.t manipulator itself

#print(x21,x23,y21,y23)

WW2=m.sqrt((y23-y21)**2+(x23-x21)**2)

#print(WW2)

THE2=30    ##bending angle (it can be change)

QQ21=(x22-x21)**2+(y22-y21)**2 ##first circle equ
QQ22=(x22-x23)**2+(y22-y23)**2 ##second circle equ
L2=(WW2/2)/(m.cos(THE2*m.pi/180)) ##midpoint of distance
CC21=L2**2 ##radius of 1st circle
CC22=L2**2 ##radius for 2nd circle
eq21 = sympy.Eq(QQ21, CC21)
eq22 = sympy.Eq(QQ22, CC22)
solution2=sympy.solve([eq21, eq22]) ##system equations solution
print(solution2)
S21=solution2[0]
S22=solution2[1]
VI2=[list(S21.values()),list(S22.values())]##values for both solution
##first solution
print(VI2)
x22=VI2[0][0]
y22=VI2[0][1]

#####via point has finish###

###INVERSE K FOR INTIAL POINT

A2O =-2*a2*x21;

```

```

B2O = -2*a2*y21;
C2O = x21**2 + a2**2 + y21**2 - b2**2;
th210 = 2*m.atan2((-B2O - m.sqrt(B2O**2 + A2O**2 - C2O**2)), (C2O - A2O))*(180/m.pi);
th220 = (m.atan2(y21 - a2*m.sin(th210*m.pi/180), x21 - a2*m.cos(th210*m.pi/180))*180/m.pi) - th210;
#INVERSE K FOR via POINT
AM2 = -2*a2*x22;
BM2 = -2*a2*y22;
CM2 = x22**2 + a2**2 + y22**2 - b2**2;
th211 = 2*m.atan2((-BM2 - m.sqrt(BM2**2 + AM2**2 - CM2**2)), (CM2 - AM2))*(180/m.pi);
th221 = (m.atan2(y22 - a2*m.sin(th211*m.pi/180), x22 - a2*m.cos(th211*m.pi/180))*180/m.pi) - th211;
#INVERSE K FOR FINAL POINT
AF2 = -2*a2*x23;
BF2 = -2*a2*y23;
CF2 = x23**2 + a2**2 + y23**2 - b2**2;
th212 = 2*m.atan2((-BF2 - m.sqrt(BF2**2 + AF2**2 - CF2**2)), (CF2 - AF2))*(180/m.pi);
th222 = (m.atan2(y23 - a2*m.sin(th212*m.pi/180), x23 - a2*m.cos(th212*m.pi/180))*180/m.pi) - th212;
#8 by 8 matrices FOR FIRST ACTUATOR (parameters coefficients)
B21 = np.array([[th210], [th211], [th211], [th212], [0], [0], [0], [0]]) #values of angles obtained from inverse
kinematic 1.st actuator
A21 = np.array([[1, 0, 0, 0, 0, 0, 0, 0], [1, tf21, tf21*tf21, tf21*tf21*tf21, 0, 0, 0, 0],
[0, 0, 0, 0, 1, 0, 0, 0], [0, 0, 0, 0, 1, tf22, tf22*tf22, tf22*tf22*tf22],
[0, 1, 0, 0, 0, 0, 0, 0], [0, 0, 0, 0, 0, 1, 2*tf22, 3*tf22*tf22],
[0, 1, 2*tf21+3*tf21*tf21, 0, 0, -1, 0, 0], [0, 0, 2, 6*tf21, 0, 0, -2, 0]])
A21N = np.linalg.inv(A21)
C21 = np.matmul(A21N, B21)
print(C21)
#print(th10, th11, th12)
t21s1 = C21[0,0] + C21[1,0]*t + C21[2,0]*t**2 + C21[3,0]*t**3; #first segment equation for 1.st act
t21s2 = C21[4,0] + C21[5,0]*t + C21[6,0]*t**2 + C21[7,0]*t**3; #second segment equation for 1st act

```

#8 by 8 matrices FOR second ACTUATOR

B22=np.array([[th220],[th221],[th221],[th222],[0],[0],[0],[0]]) #values of angles obtained from inverse kinematic 1.st actuator

#8 by 8 matrices FOR second ACTUATOR (parameters coefficients)

```
A22=np.array([[1,0,0,0,0,0,0,0],[1,tf21,tf21*tf21,tf21*tf21*tf21,0,0,0,0],
              [0,0,0,0,1,0,0,0],[0,0,0,0,1,tf22,tf22*tf22,tf22*tf22*tf22],
              [0,1,0,0,0,0,0,0],[0,0,0,0,0,1,2*tf22,3*tf22*tf22],
              [0,1,2*tf21+3*tf21*tf21,0,0,-1,0,0],[0,0,2,6*tf21,0,0,-2,0]])
```

A2N=np.linalg.inv(A22)

C22=np.matmul(A2N,B22)

#print(th20,th21,th22)

t22s1=C22[0,0]+C22[1,0]\*t+C22[2,0]\*t\*\*2+C22[3,0]\*t\*\*3; #first segment equation for 1.st act

t22s2=C22[4,0]+C22[5,0]\*t+C22[6,0]\*t\*\*2+C22[7,0]\*t\*\*3; #second segment equation for

tt21=[];tt22=[];tt23=[];tt24=[] #empty lists for thetas array to be send like integers

for aq21 in t21s1\*100:

bb21=('%.0f'%aq21)

#print(bb1)

tt21.append(int(bb21))

#time.sleep(1)

tm21s1=tt21 #list to be send for first segment of first motor

#print(tm21s1)

for aq22 in t21s2\*100:

bb22=('%.0f'%aq22)

#print(bb22)

tt22.append(int(bb22))

#time.sleep(1)

tm21s2=tt22 #list to be send for second segment of first motor

#print(tm21s2)

```

for aq23 in t22s1*100:
    bb23=('%.0f'%aq23)
    #print(bb23)
    tt23.append(int(bb23))
    #time.sleep(1)
tm22s1=tt23 #list to be send for first segment of second motor
#print(tm22s1)
for aq24 in t22s2*100:
    bb24=('%.0f'%aq24)
    ##print(bb4)
    tt24.append(int(bb24))
    #time.sleep(1)
tm22s2=tt24 #list to be send for second segment of second motor
#print(tm22s2)
print(tm21s1)
print(tm22s1)
print(tm21s2)
print(tm22s2)

```

## **2-Main code to communicate between Raspberry Pi and Atmega microcontroller**

In this code we design a standard algorithm that will be used in our communication between master and other slaves

### **2-a-Master code(Python)**

```

import sys
import smbus
import time
import numpy as np

```

```

import math as m
import matplotlib.pyplot as plt
from pylab import *
import time
import serial
import sympy

import RPi.GPIO as GPIO

from smbus2 import SMBus #communication protocol that used in i2c

bus = smbus.SMBus(1)

address = 0x08 #communication address

def writeNumber(a,b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,aa,bb,cc,dd,ii,jj,kk,ll,mm,nn,oo,pp,rr,ss,tt,uu):

    bus.write_i2c_block_data(address, a,[
b,c,d,e,f,g,h,i,j,k,l,m,n,o,p,aa,bb,cc,dd,ii,jj,kk,ll,mm,nn,oo,pp,rr,ss,tt,uu]) ##the total ammount of data
that will be send to atmega

    return -1

def requestreading(): ##reading function definition

    block=bus.read_i2c_block_data(address,0,3) ##to read potontimeter values that will be taken from
arduino chip

    return block

p=1
while True:

    try:

        b=requestreading() ##data requesting from arduino

        p1=int(b[0]*4.0118) #to convet analog values of potontimeter 1 to its original value 1023

        tetha11=int(p1*(5/1023)*720) ##convert analog value to angle value

        p2=int(b[2]*4.0118) #to convet analog values of potontimeter 1 to its original value 1023

        tetha12=int(p2*(5/1023)*720) ##convert analog value to angle value

        print("p1 %s p2 %s :"%(tetha11,tetha12)) ##to print those values into serial monitor

```

```

##forward kinamtic calculation

a2=230;b2=230;TH2F1=(tetha11-1172); TH2F2=(tetha12-1158);

XE2=b2*m.cos((TH2F1+TH2F2)*m.pi/180)+a2*m.cos(TH2F1*m.pi/180);
YE2=b2*m.sin((TH2F1+TH2F2)*m.pi/180)+a2*m.sin(TH2F1*m.pi/180);

#print(XE2,YE2)

    ##starting point of trajectory generation

tf21=8;tf22=8 #time period definition

t=np.arange(0,8,1); ##time sectioning slices definition for quadratic equation

#x2=80;y2=200 #second station of end effector

a2=230;b2=230 #links length

#algorithm to obtain via point and end effector positions

x22, y22 = sympy.symbols("x22 y22", real=True) #to solve system equation
x21=XE2;x23=0;y21=YE2;y23=321;#position w.r.t manipulator itself
WW2=m.sqrt((y23-y21)**2+(x23-x21)**2)

THE2=30    ##bending angle for via point inclination (it can be change)

QQ21=(x22-x21)**2+(y22-y21)**2 ##first circle equ
QQ22=(x22-x23)**2+(y22-y23)**2 ##second circle equ

L2=(WW2/2)/(m.cos(THE2*m.pi/180)) ##midpoint of distance

CC21=L2**2 ##radius of 1st circle
CC22=L2**2 ##radius for 2nd circle

eq21 = sympy.Eq(QQ21, CC21) ##first equation symboling
eq22 = sympy.Eq(QQ22, CC22) ##first equation symboling

solution2=sympy.solve([eq21, eq22]) ##system equations solution

#print(solution2)

S21=solution2[0]
S22=solution2[1]

VI2=[list(S21.values()),list(S22.values())]##values for both solution

##first solution

x22=VI2[0][0]

```

```

y22=VI2[0][1]

#####via point has finish###

###INVERSE K FOR INTIAL POINT

A2O =-2*a2*x21;

B2O =-2*a2*y21;

C2O = x21**2 +a2**2 + y21**2 -b2**2;

th210=2*m.atan2((-B2O -m.sqrt(B2O**2 + A2O**2 - C2O**2)),(C2O - A2O))*(180/m.pi); ##first
motor joint angle

th220=(m.atan2(y21-a2*m.sin(th210*m.pi/180),x21-a2*m.cos(th210*m.pi/180))*180/m.pi)-th210;
##second motor joint angle

#INVERSE K FOR via POINT

AM2=-2*a2*x22;

BM2=-2*a2*y22;

CM2=x22**2 +a2**2 + y22**2 -b2**2;

th211=2*m.atan2((-BM2 -m.sqrt(BM2**2 + AM2**2 - CM2**2)),(CM2 - AM2))*(180/m.pi);

th221=(m.atan2(y22-a2*m.sin(th211*m.pi/180),x22-a2*m.cos(th211*m.pi/180))*180/m.pi)-th211;

#INVERSE K FOR FINAL POINT

AF2=-2*a2*x23;

BF2=-2*a2*y23;

CF2=x23**2 +a2**2 +y23**2-b2**2;

th212=2*m.atan2((-BF2 -m.sqrt(BF2**2 + AF2**2 - CF2**2)),(CF2 -AF2))*(180/m.pi);

th222=(m.atan2(y23-a2*m.sin(th212*m.pi/180),x23-a2*m.cos(th212*m.pi/180))*180/m.pi)-th212;

#8 by 8 matrices FOR FIRST ACTUATOR that contains coefficients of parameters

B21=np.array([[th210],[th211],[th211],[th212],[0],[0],[0],[0]]) #values of abgles obtained from
inverse kinematic 1.st actuator

A21=np.array([[1,0,0,0,0,0,0,0],[1,tf21,tf21*tf21,tf21*tf21*tf21,0,0,0,0],
[0,0,0,0,1,0,0,0],[0,0,0,0,1,tf22,tf22*tf22,tf22*tf22*tf22],
[0,1,0,0,0,0,0,0],[0,0,0,0,0,1,2*tf22,3*tf22*tf22],
[0,1,2*tf21+3*tf21*tf21,0,0,-1,0,0],[0,0,2,6*tf21,0,0,-2,0]])

A21N= np.linalg.inv(A21)

```



```

C21=np.matmul(A21N,B21)

#print(th10,th11,th12)

t21s1=C21[0,0]+C21[1,0]*t+C21[2,0]*t**2+C21[3,0]*t**3; #first segment equation for 1.st act
t21s2=C21[4,0]+C21[5,0]*t+C21[6,0]*t**2+C21[7,0]*t**3; #second segment equation for 1st act

#8 by 8 matrices FOR second ACTUATOR

B22=np.array([[th220],[th221],[th221],[th222],[0],[0],[0],[0]]) #values of angles obtained from
inverse kinematic 1.st actuator

A22=np.array([[1,0,0,0,0,0,0,0],[1,tf21,tf21*tf21,tf21*tf21*tf21,0,0,0,0],
[0,0,0,0,1,0,0,0],[0,0,0,0,1,tf22,tf22*tf22,tf22*tf22*tf22],
[0,1,0,0,0,0,0,0],[0,0,0,0,0,1,2*tf22,3*tf22*tf22],
[0,1,2*tf21+3*tf21*tf21,0,0,-1,0,0],[0,0,2,6*tf21,0,0,-2,0]])

A2N=np.linalg.inv(A22)

C22=np.matmul(A2N,B22)

#print(th20,th21,th22)

t22s1=C22[0,0]+C22[1,0]*t+C22[2,0]*t**2+C22[3,0]*t**3; #first segment equation for 1.st act
t22s2=C22[4,0]+C22[5,0]*t+C22[6,0]*t**2+C22[7,0]*t**3; #second segment equation for

tt21=[];tt22=[];tt23=[];tt24=[] #empty lists for thetas array

for aq21 in t21s1*100:

    bb21=('%.0f'%aq21)

    #print(bb1)

    tt21.append(int(bb21))

    #tt1.append(int(bb21)/100)

    #time.sleep(1)

tm21s1=tt21 #list to be send for first segment of first motor

#print(tm21s1)

for aq22 in t21s2*100:

    bb22=('%.0f'%aq22)

    #print(bb22)

```

```

    tt22.append(int(bb22))

    #time.sleep(1)

tm21s2=tt22 #list to be send for second segment of first motor

#print(tm21s2)

for aq23 in t22s1*100:

    bb23=('%0.0f'%aq23)

    #print(bb23)

    tt23.append(int(bb23))

    #time.sleep(1)

tm22s1=tt23 #list to be send for first segment of second motor

#print(tm22s1)

for aq24 in t22s2*100:

    bb24=('%0.0f'%aq24)

    ##print(bb4)

    tt24.append(int(bb24))

    #time.sleep(1)

tm22s2=tt24 #list to be send for second segment of second motor

#print(tm22s2)

```

##data that will be send toward atmega

```

TK=[tm21s1[0]//255,tm21s1[1]//255,tm21s1[2]//255,tm21s1[3]//255,tm21s1[4]//255,tm21s1[5]//255,tm21s1[6]//255,tm21s1[7]//255,tm22s1[0]//255,tm22s1[1]//255,tm22s1[2]//255,tm22s1[3]//255,tm22s1[4]//255,tm22s1[5]//255,tm22s1[6]//255,tm22s1[7]//255]
TM=[tm21s1[0]%255,tm21s1[1]%255,tm21s1[2]%255,tm21s1[3]%255,tm21s1[4]%255,tm21s1[5]%255,tm21s1[6]%255,tm21s1[7]%255,tm22s1[0]%255,tm22s1[1]%255,tm22s1[2]%255,tm22s1[3]%255,tm22s1[4]%255,tm22s1[5]%255,tm22s1[6]%255,tm22s1[7]%255]
TK2=[tm21s2[0]//255,tm21s2[1]//255,tm21s2[2]//255,tm21s2[3]//255,tm21s2[4]//255,tm21s2[5]//255,tm21s2[6]//255,tm21s2[7]//255,tm22s2[0]//255,tm22s2[1]//255,tm22s2[2]//255,tm22s2[3]//255,tm22s2[4]//255,tm22s2[5]//255,tm22s2[6]//255,tm22s2[7]//255]
TM2=[tm21s2[0]%255,tm21s2[1]%255,tm21s2[2]%255,tm21s2[3]%255,tm21s2[4]%255,tm21s2[5]%255,tm21s2[6]%255,tm21s2[7]%255,tm22s2[0]%255,tm22s2[1]%255,tm22s2[2]%255,tm22s2[3]%255,tm22s2[4]%255,tm22s2[5]%255,tm22s2[6]%255,tm22s2[7]%255]
writeNumber(TK[0],TK2[0],TK[1],TK2[1],TK[2],TK2[2],TK[3],TK2[3],TK[4],TK2[4],TK[5],TK2[5],TK[6],TK2[6])

```

```
,TK[7],TK2[7],TK[8],TK2[8],TK[9],TK2[9],TK[10],TK2[10],TK[11],TK2[11],TK[12],TK2[12],TK[13],TK2[13],TK[
14],TK2[14],TK[15],TK2[15])
writeNumber(TM[0],TM2[0],TM[1],TM2[1],TM[2],TM2[2],TM[3],TM2[3],TM[4],TM2[4],TM[5],TM2[5],T
M[6],TM2[6],TM[7],TM2[7],TM[8],TM2[8],TM[9],TM2[9],TM[10],TM2[10],TM[11],TM2[11],TM[12],TM2[
12],TM[13],TM2[13],TM[14],TM2[14],TM[15],TM2[15])

    print(tm21s1)

    print(tm22s1)

    print(tm21s2)

    print(tm22s2)

    time.sleep(0.5)          #delay one second

    if p>0:

        break

except KeyboardInterrupt:

    quit()
```

## 2-b-Slave code (Arduino Atmega)

This code has been created as slave code that will be impeded into Arduino microcontrollers so that we can receive and send data in order to implement the goal which we aim to do .

```
//HABERLESME TANIMLAMALARI

#include <Wire.h>

#define SLAVE_ADDRESS 0x08

int data [32];

int data11 [32];

int datanew[16];

int datanew11[16];

int x = 0;

int y = 0;

volatile int16_t data1[2];

volatile int16_t datanew1[2];

//PATHDEN GELEN TANIMLAMALAR

//link lenght constant
```

```

float a =230.0;

float b = 230.0;

//İnital positions of the our robot arms end effector CONSTANT

float A1x, A1y;

//forward kinematics Angle of manipulator1

float tetha12 ; //pottan alınacak

float tetha11 ;

//global point that will be taken from user

float Ax=0;

float Ay=0;

//end effector position defining

float Axx;

float Ayy;

//inital distance(offsets)

float x1 = 0;   //IT WILL CHANGE FOR EACH MANİPULATOR THESE ONE FOR 1.ST MANİPULATOR

float y1 =-325.0 ; //IT WILL CHANGE FOR EACH MANİPULATOR THESE ONE FOR 1.ST MANİPULATOR

//inverse kinematics angle of link1

float th12, th11;

//inverse kinematics angle of link1 to origin

float tht12, tht11;

//Saranın tanımlamaları

float Kp =10.0;

float Kp2=0.8;

int i = 0, sum = 0;

float angle, angle2, voltage, voltage2, pot1, pot2, reftheta, reftheta2, error, error2, pwm, pwm2;

int p=1;

void setup() {

Serial.begin(9600);

Wire.begin(SLAVE_ADDRESS);

```

```

Wire.onReceive(receiveData);

Wire.onRequest(sendAnalogReading);

}

void loop() {

    for( int l = 0; l<2; l++)
    {
        data1[l] = analogRead( A4 + l);
        delay(50);
        datanew1[l]=map(data1[l],0,1023,0,255);
        //Serial.println(datanew1[l]);
    }
    /*for( int p = 0; p<16; p++)
    {
        Serial.print(datanew[p]);
        Serial.print("\t");
        Serial.println(datanew11[p]);

        delay(50);
    }*/
    for(int m=0;m<8;m++)
    {
        pot1 = analogRead( A4);
        pot2=analogRead( A5);
        voltage = pot1 * (5.0 / 1023);
        tetha11 = voltage * 720.0 ; //initial angle of link1
        voltage2 = pot2 * (5.0 / 1023);
    }
}

```

```

tetha12 = voltage2 * 720.0 ; //initial angle link2
//Serial.println(tetha11);
/*Serial.print(tetha11);
Serial.print("\t");
Serial.println(tetha12);*/

th11=datanew[m];
th12=datanew[m+8];
delay(100);

//SARANIN KODU BURDA OLACAK

error = (tetha11)-(th11+1172.0); //675 FOR FIRST MANIPULATOR FIRST MOTOR REFERENCE ANGLE.IT
WILL CAHANGE FOR EACH MANIPULATOR

error2 = (tetha12)-(th12+1158.0); //418 FOR FIRST MANIPULATOR SECOND MOTOR REFERENCE
ANGLE.IT WILL CAHANGE FOR EACH MANIPULATOR

/*Serial.print(error);
Serial.print("\t");
Serial.println(error2);*/

if (error > 0)
{
    pwm = (Kp) * error;
    if (pwm > 255)
    {
        pwm = 255;
    }
    analogWrite(8, pwm); //ccw
    analogWrite(9, 0);

}

if (error < 0)
{

```

```

pwm = -(Kp * error); // pwm can not be negative
if (pwm > 255)
{
    pwm = 255;
}
analogWrite(9, pwm); //cc
analogWrite(8, 0);

}

if (error2 > 0)
{
    pwm2 = (Kp2) * error2;
    if (pwm2 > 255)
    {
        pwm2 = 255;
    }
    analogWrite(5, pwm2); //ccw
    analogWrite(7, 0);

}

if (error2 < 0)
{
    pwm2 = -(Kp2 * error2); // pwm can not be negative
    if (pwm2 > 255)
    {
        pwm2 = 255;
    }
    analogWrite(7, pwm2); //cc

```

```

    analogWrite(5, 0);

}

Serial.print(pwm);

Serial.print("\t");

Serial.println(pwm2);

}

Serial.println("-----");

delay(1000);

for(int n=0;n<8;n++)
{
    pot1 = analogRead(A4);
    pot2 = analogRead(A5);
    voltage = pot1 * (5.0 / 1023);
    tetha11 = voltage * 720.0 ; //initial angle of link1
    voltage2 = pot2 * (5.0 / 1023);
    tetha12 = voltage2 * 720.0 ; //initial angle link2

    /*Serial.print(tetha11);

    Serial.print("\t");

    Serial.print(tetha12);

    Serial.println();*/

    th11=datanew11[n];
    th12=datanew11[n+8];
    delay(100);

    /*Serial.print(th12);

    Serial.print("\t");

    Serial.println(th11);*/

    //SARANIN KODU BURDA OLACAK

```



error = (tetha11)-(th11+1172.0); //675 FOR FIRST MANIPULATOR FIRST MOTOR REFERENCE ANGLE.IT  
WILL CAHANGE FOR EACH MANIPULATOR

error2 = (tetha12)-(th12+1158.0); //418 FOR FIRST MANIPULATOR SECOND MOTOR REFERENCE  
ANGLE.IT WILL CAHANGE FOR EACH MANIPULATOR

```
/* Serial.print(error);  
Serial.print("\t");  
Serial.println(error2);*/  
if (error > 0)  
{  
    pwm = (Kp) * error;  
    if (pwm > 255)  
    {  
        pwm = 255;  
    }  
    analogWrite(8, pwm); //ccw  
    analogWrite(9, 0);  
  
}  
if (error < 0)  
{  
    pwm = -(Kp * error); // pwm can not be negative  
    if (pwm > 255)  
    {  
        pwm = 255;  
    }  
    analogWrite(9, pwm); //cc  
    analogWrite(8, 0);  
  
}
```

```

if (error2 > 0)
{
    pwm2 = (Kp2) * error2;
    if (pwm2 > 255)
    {
        pwm2 = 255;
    }
    analogWrite(5, pwm2); //ccw
    analogWrite(7, 0);

}

if (error2 < 0)
{
    pwm2 = -(Kp2 * error2); // pwm can not be negative
    if (pwm2 > 255)
    {
        pwm2 = 255;
    }
    analogWrite(7, pwm2); //cc
    analogWrite(5, 0);

}

Serial.print(pwm);
Serial.print("\t");
Serial.println(pwm2);
}
}

void receiveData(int byteCount) {

```

while(Wire.available()) { //Wire.available() returns the number of bytes available for retrieval with Wire.read(). Or it returns TRUE for values >0.

```
    data[x]=Wire.read();
```

```
    data11[y]=Wire.read();
```

```
    x++;
```

```
    y++;
```

```
}
```

```
for(int i=0;i<16;i++)
```

```
{
```

```
//Serial.println((data[i]*(255)+data[i+16]));
```

```
datanew[i]=((data[i]*(255)+data[i+16])/100;
```

```
datanew11[i]=((data11[i]*(255)+data11[i+16])/100;
```

```
}
```

```
for(int k=0;k<16;k++)
```

```
{
```

```
if(datanew[k]<0)
```

```
{
```

```
    datanew[k]=datanew[k]+256;
```

```
}
```

```
if(datanew11[k]<0)
```

```
{
```

```
    datanew11[k]=datanew11[k]+256;
```

```
}
```

```
}
```

```
}
```

```
void sendAnalogReading(){
```

```
Wire.write( (uint8_t *) datanew1, sizeof( datanew1));
```

```
}
```

### 3-Pure rotation task (just to rotate platform with zero translation)

This code is specified for attaching and detaching task so that by doing pure rotation we can configure all end effector operation with respect to rotation needs .

```
import numpy as np
import sympy
import math as m
import matplotlib.pyplot as plt
from pylab import *
import time
import serial
import Rpi.GPIO as GPIO
import smbus

bus = smbus.SMBus(1)
address = 0x04 #ADRESS CAN BE CHANGE
GPIO.setmode(GPIO.BCM)
GPIO.setwarnings(False)

sevo1=17
servo2=18
servo3=19

        ##HEXAGONAL CORNERS CORDINATIONS FINDING START

GPIO.setup(servo1, GPIO.OUT) # setting servo pin for first manipulator(gripper1)
GPIO.setup(servo2, GPIO.OUT) # setting servo pin for second manipulator(gripper2)
GPIO.setup(servo3, GPIO.OUT) # setting servo pin for third manipulator(gripper3)
def setServoAngle(servo, angle):

    pwm.start(8)

    dutyCycle = angle / 18. + 2.

    pwm.ChangeDutyCycle(dutyCycle)
```

```

        sleep(0.3)

        pwm.stop()

def writeNumber(a,b):

    bus.write_i2c_block_data(address, a, [b])

    return -1

#####HEXAGONAL CODE START HERE##

##CENTER AND FIRST CIRCLE

xc1, yc1 = sympy.symbols("xc1 yc1", real=True)

xx1=140;yy1=80;xx2=80;yy2=80

C1E=(xc1-xx1)**2+(yc1-yy1)**2

C2E=(xc1-xx2)**2+(yc1-yy2)**2

RR=60**2

E1Q1=sympy.Eq(C1E,RR)

E1Q2=sympy.Eq(C2E,RR)

SOLUTION1=sympy.solve([E1Q1,E1Q2])

print(SOLUTION1)

SS1=SOLUTION1[0]

SS2=SOLUTION1[1]

VV1I=[list(SS1.values()),list(SS2.values())]##values for both solution

xc10=float(VV1I[0][0]) ##X-FIRST CORDINATE

yc10=float(VV1I[0][1]) ##Y-FIRST CORDINATE

xc20=float(VV1I[1][0]) ##X-SECOND CORDINATE

yc20=float(VV1I[1][1]) ##Y-SECOND CORDINATE

print(xc10,yc10,xc20,yc20)

##CENTER AND SECOND CIRCLE

xc2, yc2 = sympy.symbols("xc2 yc2", real=True)

xx12=140;yy12=80;xx22=200;yy22=80

C1E2=(xc2-xx12)**2+(yc2-yy12)**2

C2E2=(xc2-xx22)**2+(yc2-yy22)**2

```

```

RR=60**2

E2Q1=sympy.Eq(C1E2,RR)
E2Q2=sympy.Eq(C2E2,RR)
SOLUTION2=sympy.solve([E2Q1,E2Q2])
print(SOLUTION2)
S2S1=SOLUTION2[0]
S2S2=SOLUTION2[1]
VV2I=[list(S2S1.values()),list(S2S2.values())]##values for both solution
xc11=float(VV2I[0][0]) ##X-THIRD CORDINATE
yc11=float(VV2I[0][1]) ##Y-THIRD CORDINATE
xc21=float(VV2I[1][0]) ##X-FOURTH CORDINATE
yc21=float(VV2I[1][1]) ##Y-FOURTH CORDINATE
print(xc11,yc11,xc21,yc21)

xx1c=xx1-60
yy1c=yy1
xx2c=xx1+60
yy2c=yy1
print(xx1c,yy1c)
print(xx2c,yy2c)

#####HEXAGONAL CODE FINISH HERE##

#####FORWARD KINEMATIC CODE START HERE##

##forward kinametic for FIRST MANIPULATOR
a1=230;b1=230;XF1=50;YF1=40;TH1F1=20;TH1F2=330
XE1=XF1+b1*m.cos((TH1F1+TH1F2)*m.pi/180)+a1*m.cos(TH1F1*m.pi/180); #tethas coming from Pic
YE1=YF1+b1*m.sin((TH1F1+TH1F2)*m.pi/180)+a1*m.sin(TH1F1*m.pi/180);

##forward kinametic for SECOND MANIPULATOR
a2=230;b2=230;XF2=10;YF2=10;TH2F1=20;TH2F2=330
XE2=XF2+b2*m.cos((TH2F1+TH2F2)*m.pi/180)+a2*m.cos(TH2F1*m.pi/180);
YE2=YF2+b2*m.sin((TH2F1+TH2F2)*m.pi/180)+a2*m.sin(TH2F1*m.pi/180);

```

```

##forward kinametic for THIRD MANIPULATOR
a3=230;b3=230;XF3=-50;YF3=100;TH3F1=20;TH3F2=330

XE3=XF3+b3*m.cos((TH3F1+TH3F2)*m.pi/180)+a3*m.cos(TH3F1*m.pi/180);
YE3=YF3+b3*m.sin((TH3F1+TH3F2)*m.pi/180)+a3*m.sin(TH3F1*m.pi/180);
print(XE3,YE3)

        ##THE END OF FORWARD

        ###ROTATION TASK CODE START HERE##

for x in range(6):
#INVERSE FOR FINAL POINT OF FIRST MANIPULATOR

    aa=230;bb=230 #links length

    AFM =-2*aa*xc11;
    BFM =-2*aa*yc11;
    CFM= xc11**2 +aa**2 + yc11**2 -bb**2;
    th10h=2*m.atan2((-BFM -m.sqrt(BFM**2 + AFM**2 - CFM**2)),(CFM -AFM))*(180/m.pi);
    th20h=(m.atan2(yc11-aa*m.sin(th10h*m.pi/180),xc11-aa*m.cos(th10h*m.pi/180))*180/m.pi)-th10h;
    #th10h ve th20h Pic'e yollanacak raspberryden !!!!
    while True:
        try:
            writeNumber(th10h,th20h)
            time.sleep(1)          #delay one second

        except KeyboardInterrupt:
            quit()

#INVERSE kinematic FOR FINAL POINT OF SECOND MANIPULATOR

aa=230;bb=230 #links length

ASM =-2*aa*xc21;
BSM =-2*aa*yc21;
CSM= xc21**2 +aa**2 + yc21**2 -bb**2;

```

```

th11h=2*m.atan2((-BSM -m.sqrt(BSM**2 + ASM**2 - CSM**2)),(CSM -ASM))*(180/m.pi);
th21h=(m.atan2(yc11-aa*m.sin(th11h*m.pi/180),xc21-aa*m.cos(th11h*m.pi/180))*180/m.pi)-th11h;
#th11h ve th21h Pic'e yollanacak raspberryden

while True:

    try:

        writeNumber(th11h,th21h)

        time.sleep(1)          #delay one second


    except KeyboardInterrupt:

        quit()


#INVERSE FOR FINAL POINT OF THIRD MANIPULATOR
aa=230;bb=230 #links length
ATM =-2*aa*xc20;
BTM =-2*aa*yc20;
CTM= xc20**2 +aa**2 + yc20**2 -bb**2;
th12h=2*m.atan2((-BTM -m.sqrt(BTM**2 + ATM**2 - CTM**2)),(CTM -ATM))*(180/m.pi);
th22h=(m.atan2(yc20-aa*m.sin(th12h*m.pi/180),xc20-aa*m.cos(th12h*m.pi/180))*180/m.pi)-th12h;
#th12h ve th22h Pic'e yollanacak raspberryden !!!!

while True:

    try:

        writeNumber(th12h,th22h)

        time.sleep(1)          #delay one second


    except KeyboardInterrupt:

        quit()

if __name__ == '__main__':

    setServoAngle(servo3, 180) #180 degree suppose gripper is closing at that angle

```



```
GPIO.cleanup()
```

```
#INVERSE FOR FINAL POINT OF FIRST MANIPULATOR GOING BACK
```

```
if __name__ == '__main__':
```

```
    setServoAngle(servo1, 0) #0 degree suppose gripper is opening at that angle
```

```
GPIO.cleanup()
```

```
aa=230;bb=230 #links length
```

```
AFM =-2*aa*xc10;
```

```
BFM =-2*aa*yc10;
```

```
CFM= xc10**2 +aa**2 + yc10**2 -bb**2;
```

```
th10h=2*m.atan2((-BFM -m.sqrt(BFM**2 + AFM**2 - CFM**2)),(CFM -AFM))*(180/m.pi);
```

```
th20h=(m.atan2(yc10-aa*m.sin(th10h*m.pi/180),xc10-aa*m.cos(th10h*m.pi/180))*180/m.pi)-th10h;
```

```
#th10h ve th20h Pic'e yollanacak raspberryden!!!!
```

```
while True:
```

```
    try:
```

```
        writeNumber(th10h,th20h)
```

```
        time.sleep(1)          #delay one second
```

```
    except KeyboardInterrupt:
```

```
        quit()
```

```
if __name__ == '__main__':
```

```
    setServoAngle(servo1, 180) #180 degree suppose gripper is closing at that angle
```

```
GPIO.cleanup()
```

```
#INVERSE FOR FINAL POINT OF SECOND MANIPULATOR GOING BACK
```

```
if __name__ == '__main__':
```

```
    setServoAngle(servo2, 0) #0 degree suppose gripper is opening at that angle
```

```
GPIO.cleanup()
```

```

aa=230;bb=230 #links length

ASM =-2*aa*xx2c;

BSM =-2*aa*yy2c;

CSM= xx2c**2 +aa**2 + yy2c**2 -bb**2;

th11h=2*m.atan2((-BSM -m.sqrt(BSM**2 + ASM**2 - CSM**2)),(CSM -ASM))*(180/m.pi);

th21h=(m.atan2(yy2c-aa*m.sin(th11h*m.pi/180),xx2c-aa*m.cos(th11h*m.pi/180))*180/m.pi)-th11h;

#th11h ve th21h Pic'e yollanacak raspberryden !!!!

while True:

    try:

        writeNumber(th11h,th21h)

        time.sleep(1)          #delay one second

    except KeyboardInterrupt:

        quit()

if __name__ == '__main__':

    setServoAngle(servo2, 180) #180 degree suppose gripper is closing at that angle

GPIO.cleanup()

#INVERSE FOR FINAL POINT OF THİRD MANİPULATOR

if __name__ == '__main__':

    setServoAngle(servo3, 0) #0 degree suppose gripper is opening at that angle

GPIO.cleanup()

aa=230;bb=230 #links length

ATM =-2*aa*XE3;

BTM =-2*aa*YE3;

CTM= XE3**2 +aa**2 + YE3**2 -bb**2;

th12h=2*m.atan2((-BTM -m.sqrt(BTM**2 + ATM**2 - CTM**2)),(CTM -ATM))*(180/m.pi);

```

```
th22h=(m.atan2(YE3-aa*m.sin(th12h*m.pi/180),XE3-aa*m.cos(th12h*m.pi/180))*180/m.pi)-th12h;
```

```
#th12h ve th22h Pic'e yollanacak raspberryden !!!!!
```

```
while True:
```

```
    try:
```

```
        writeNumber(th12h,th22h)
```

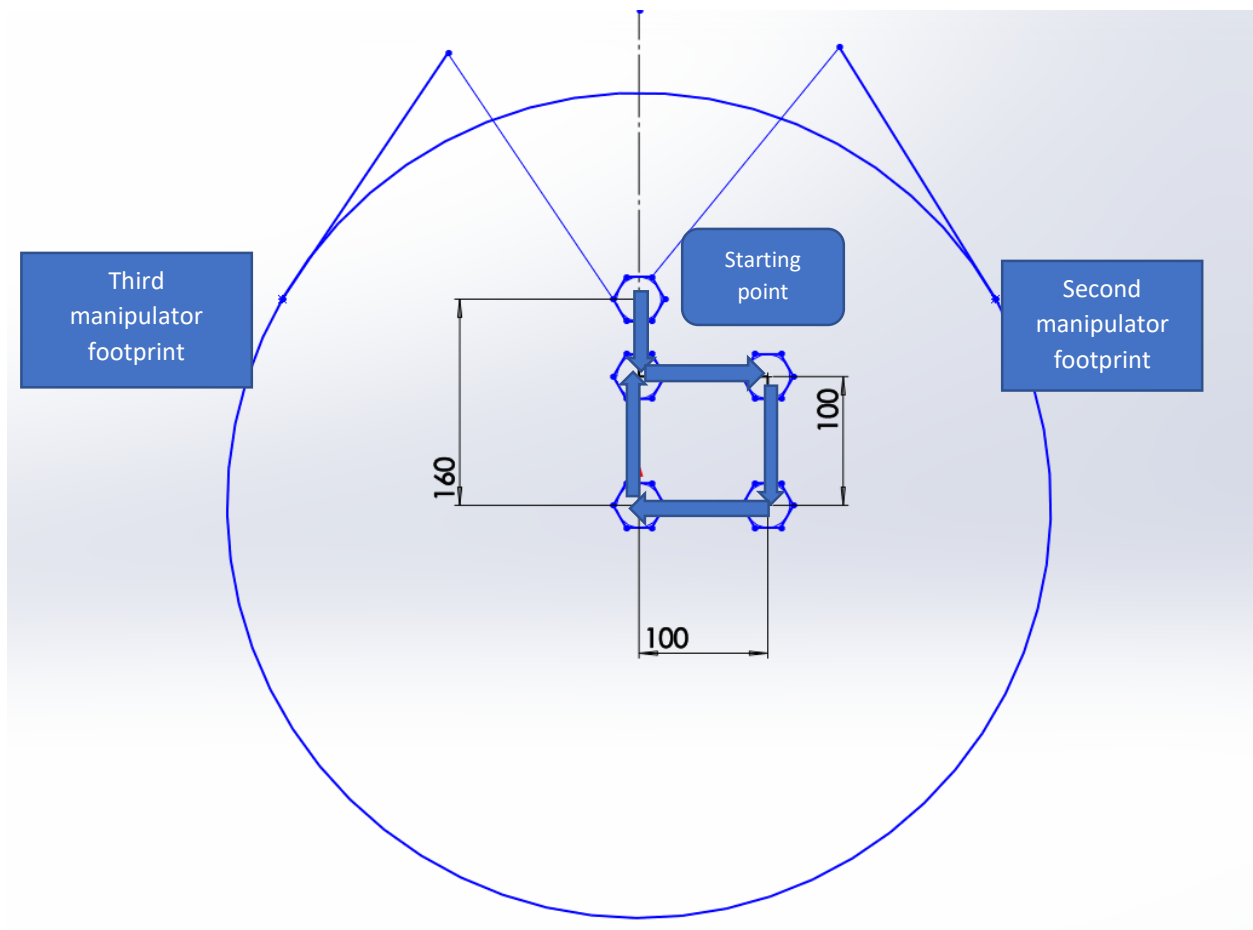
```
        time.sleep(1)           #delay one second
```

```
    except KeyboardInterrupt:
```

```
        quit()
```

#### **4-Drawing square task(pure translation)**

In this task we used just second and third manipulator without any attaching and detaching operation so that it can go segment by segment until we reach to the final position of platform center .This task can be configure and apply into laser cutting job which we chose it to be our main task configuration.



#Note:to move indentations or dedent press ctr+] or ctr+[

#just second and third manipulator will be implemented

```
import numpy as np
import sympy
import math as m
import matplotlib.pyplot as plt
from pylab import *
import time
import serial

def f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33): #DEFING function for instantly chanegable variables
    #####second manipulator code start here

    tf21=10;tf22=10 #time period definition

    t=np.arange(0,10,0.5);
```

```

#x2=80;y2=200 #second station of end effector

a2=230;b2=230 #links length

#algorithm to obtain via point and end effector positions

x22, y22 = sympy.symbols("x22 y22", real=True) #to solve system equation

x21=-(277.13-xg21); x23=-(277.13-xg23); y21=-(160-yg21); y23=-(160-yg23);#position w.r.t
manipulator itself

WW2=m.sqrt((y23-y21)**2+(x23-x21)**2)

THE2=30 ##bending angle (it can be change)

QQ21=(x22-x21)**2+(y22-y21)**2 ##first circle equ
QQ22=(x22-x23)**2+(y22-y23)**2 ##second circle equ

L2=(WW2/2)/(m.cos(THE2*m.pi/180)) ##midpoint of distance

CC21=L2**2 ##radius of 1st circle
CC22=L2**2 ##radius for 2nd circle

eq21 = sympy.Eq(QQ21, CC21)
eq22 = sympy.Eq(QQ22, CC22)

solution2=sympy.solve([eq21, eq22]) ##system equations solution

print(solution2)

S21=solution2[0]
S22=solution2[1]

VI2=[list(S21.values()),list(S22.values())]##values for both solution

##first solution

x22=VI2[0][0]
y22=VI2[0][1]

#####via point has finish###

###INVERSE K FOR INTIAL POINT

A2O =-2*a2*x21;
B2O =-2*a2*y21;
C2O = x21**2 +a2**2 + y21**2 -b2**2;

th210=2*m.atan2((-B2O -m.sqrt(B2O**2 + A2O**2 - C2O**2)),(C2O - A2O))*(180/m.pi);

```

```

th220=(m.atan2(y21-a2*m.sin(th210*m.pi/180),x21-a2*m.cos(th210*m.pi/180))*180/m.pi)-th210;
#INVERSE K FOR via POINT
AM2=-2*a2*x22;
BM2=-2*a2*y22;
CM2=x22**2 +a2**2 + y22**2 -b2**2;
th211=2*m.atan2((-BM2 -m.sqrt(BM2**2 + AM2**2 - CM2**2)),(CM2 - AM2))*(180/m.pi);
th221=(m.atan2(y22-a2*m.sin(th211*m.pi/180),x22-a2*m.cos(th211*m.pi/180))*180/m.pi)-th211;
#INVERSE K FOR FINAL POINT
AF2=-2*a2*x23;
BF2=-2*a2*y23;
CF2=x23**2 +a2**2 +y23**2-b2**2;
th212=2*m.atan2((-BF2 -m.sqrt(BF2**2 + AF2**2 - CF2**2)),(CF2 -AF2))*(180/m.pi);
th222=(m.atan2(y23-a2*m.sin(th212*m.pi/180),x23-a2*m.cos(th212*m.pi/180))*180/m.pi)-th212;
#8 by 8 matrices FOR FIRST ACTUATOR
B21=np.array([[th210],[th211],[th211],[th212],[0],[0],[0],[0]]) #values of abgles obtained from inverse
kinematic 1.st actuator
A21=np.array([[1 ,0 ,0 ,0 ,0 ,0 ,0 ,0],[1 ,tf21, tf21*tf21, tf21*tf21*tf21, 0, 0, 0 ,0],
[0 ,0 ,0 ,0 ,1 ,0 ,0 ,0 ],[0 ,0 ,0 ,0 ,1, tf22, tf22*tf22, tf22*tf22*tf22],
[0 ,1 ,0 ,0 ,0 ,0 ,0 ,0 ],[0 ,0 ,0 ,0 ,0 ,1, 2*tf22, 3*tf22*tf22],
[0 ,1 ,2*tf21+3*tf21*tf21, 0, 0, -1, 0 ,0,],[0 ,0 ,2, 6*tf21, 0 ,0 ,-2, 0 ]])
A21N= np.linalg.inv(A21)
C21=np.matmul(A21N,B21)
#print(th10,th11,th12)
t21s1=C21[0,0]+C21[1,0]*t+C21[2,0]*t**2+C21[3,0]*t**3; #first segment equation for 1.st act
t21s2=C21[4,0]+C21[5,0]*t+C21[6,0]*t**2+C21[7,0]*t**3; #second segment equation for 1st act
#8 by 8 matrices FOR second ACTUATOR
B22=np.array([[th220],[th221],[th221],[th222],[0],[0],[0],[0]]) #values of angles obtained from inverse
kinematic 1.st actuator
A22=np.array([[1 ,0 ,0 ,0 ,0 ,0 ,0 ,0],[1 ,tf21, tf21*tf21, tf21*tf21*tf21, 0, 0, 0 ,0],

```

```

[0,0,0,0,1,0,0,0],[0,0,0,0,1,tf22,tf22*tf22,tf22*tf22*tf22],
[0,1,0,0,0,0,0,0],[0,0,0,0,0,1,2*tf22,3*tf22*tf22],
[0,1,2*tf21+3*tf21*tf21,0,0,-1,0,0],[0,0,2,6*tf21,0,0,-2,0]])
A2N=np.linalg.inv(A22)
C22=np.matmul(A2N,B22)
#print(th20,th21,th22)
t22s1=C22[0,0]+C22[1,0]*t+C22[2,0]*t**2+C22[3,0]*t**3; #first segment equation for 1.st act
t22s2=C22[4,0]+C22[5,0]*t+C22[6,0]*t**2+C22[7,0]*t**3; #second segment equation for 1.st act
tt21=[];tt22=[];tt23=[];tt24=[] #empty lists for thetas array
for aq21 in t21s1*100:
    bb21=('%.0f'%aq21)
    #print(bb1)
    tt21.append(int(bb21))
    #tt1.append(int(bb21)/100)
    #time.sleep(1)
tm21s1=tt21 #list to be send for first segment of first motor
print(tm21s1)
for aq22 in t21s2*100:
    bb22=('%.0f'%aq22)
    #print(bb22)
    tt22.append(int(bb22))
    #time.sleep(1)
tm21s2=tt22 #list to be send for second segment of first motor
print(tm21s2)
for aq23 in t22s1*100:
    bb23=('%.0f'%aq23)
    #print(bb23)
    tt23.append(int(bb23))

```

```

#time.sleep(1)
tm22s1=tt23 #list to be send for first segment of second motor
print(tm22s1)
for aq24 in t22s2*100:
    bb24=('%.0f'%aq24)
    ##print(bb4)
    tt24.append(int(bb24))
    #time.sleep(1)
tm22s2=tt24 #list to be send for second segment of second motor
print(tm22s2)
print('Second manipulator data')

    ##second manipulator code end point

                                #####thid manipulator code start here

tf31=10;tf32=10 #time period definition
t=np.arange(0,10,0.5);
#x2=80;y2=200 #second station of end effector
a3=230;b3=230 #links length
#algorithm to obtain via point start
x32, y32 = sympy.symbols("x32 y32", real=True) #to solve system equation
x31=-(-277.13-xg31);    x33=-(-277.13-xg33);    y31=-(160-yg31);    y33=-(-160-yg33);#first and last
station of end effector

WW3=m.sqrt((y33-y31)**2+(x33-x31)**2)
THE3=30    ##bending angle (it can be change)
QQ31=(x32-x31)**2+(y32-y31)**2 ##first circle equ
QQ32=(x32-x33)**2+(y32-y33)**2 ##second circle equ
L3=(WW3/2)/(m.cos(THE3*m.pi/180)) ##midpoint of distance
CC31=L3**2 ##radius of 1st circle
CC32=L3**2 ##radius for 2nd circle
eq31 = sympy.Eq(QQ31, CC31)

```



```

eq32 = sympy.Eq(QQ32, CC32)
solution3=sympy.solve([eq31, eq32]) ##system equations solution
print(solution3)
S31=solution3[0]
S32=solution3[1]
VI3=[list(S31.values()),list(S32.values())]##values for both solution
##first solution
x32=VI3[0][0]
y32=VI3[0][1]
#####via point has finish###
###INVERSE K FOR INTIAL POINT
A3O =-2*a3*x31;
B3O =-2*a3*y31;
C3O = x31**2 +a3**2 + y31**2 -b3**2;
th310=2*m.atan2((-B3O -m.sqrt(B3O**2 + A3O**2 - C3O**2)),(C3O - A3O))*(180/m.pi);
th320=(m.atan2(y31-a3*m.sin(th310*m.pi/180),x31-a3*m.cos(th310*m.pi/180))*180/m.pi)-th310;
#INVERSE K FOR via POINT
AM3=-2*a3*x32;
BM3=-2*a3*y32;
CM3=x32**2 +a3**2 + y32**2 -b3**2;
th311=2*m.atan2((-BM3 -m.sqrt(BM3**2 + AM3**2 - CM3**2)),(CM3 - AM3))*(180/m.pi);
th321=(m.atan2(y32-a3*m.sin(th311*m.pi/180),x32-a3*m.cos(th311*m.pi/180))*180/m.pi)-th311;
#INVERSE K FOR FINAL POINT
AF3=-2*a3*x33;
BF3=-2*a3*y33;
CF3=x33**2 +a3**2 +y33**2-b3**2;
th312=2*m.atan2((-BF3 -m.sqrt(BF3**2 + AF3**2 - CF3**2)),(CF3 -AF3))*(180/m.pi);
th322=(m.atan2(y33-a3*m.sin(th312*m.pi/180),x33-a3*m.cos(th312*m.pi/180))*180/m.pi)-th312;
#8 by 8 matrices FOR FIRST ACTUATOR

```

```
B31=np.array([[th310],[th311],[th311],[th312],[0],[0],[0],[0]]) #values of abgles obtained from inverse kinematic 1.st actuator
```

```
A31=np.array([[1,0,0,0,0,0,0,0],[1,tf31, tf31*tf31, tf31*tf31*tf31, 0, 0, 0,0],  
[0,0,0,0,1,0,0,0],[0,0,0,0,1, tf32, tf32*tf32, tf32*tf32*tf32],  
[0,1,0,0,0,0,0,0],[0,0,0,0,0,1, 2*tf32, 3*tf32*tf32],  
[0,1,2*tf31+3*tf31*tf31, 0,0, -1, 0,0],[0,0,2, 6*tf31, 0,0,-2, 0]])
```

```
A31N= np.linalg.inv(A31)
```

```
C31=np.matmul(A31N,B31)
```

```
#print(th30,th31,th12)
```

```
t31s1=C31[0,0]+C31[1,0]*t+C31[2,0]*t**2+C31[3,0]*t**3; #first segment equation for 1.st act
```

```
t31s2=C31[4,0]+C31[5,0]*t+C31[6,0]*t**2+C31[7,0]*t**3; #second segment equation for 1st act
```

```
#8 by 8 matrices FOR second ACTUATOR
```

```
B32=np.array([[th320],[th321],[th321],[th322],[0],[0],[0],[0]]) #values of angles obtained from inverse kinematic 1.st actuator
```

```
A32=np.array([[1,0,0,0,0,0,0,0],[1,tf31, tf31*tf31, tf31*tf31*tf31, 0, 0, 0,0],  
[0,0,0,0,1,0,0,0],[0,0,0,0,1, tf32, tf32*tf32, tf32*tf32*tf32],  
[0,1,0,0,0,0,0,0],[0,0,0,0,0,1, 2*tf32, 3*tf32*tf32],  
[0,1,2*tf31+3*tf31*tf31, 0,0, -1, 0,0],[0,0,2, 6*tf31, 0,0,-2, 0]])
```

```
A3N=np.linalg.inv(A32)
```

```
C32=np.matmul(A3N,B32)
```

```
#print(th20,th21,th22)
```

```
t32s1=C32[0,0]+C32[1,0]*t+C32[2,0]*t**2+C32[3,0]*t**3; #first segment equation for 1.st act
```

```
t32s2=C32[4,0]+C32[5,0]*t+C32[6,0]*t**2+C32[7,0]*t**3; #second segment equation for
```

```
tt31=[];tt32=[];tt33=[];tt34=[] #empty lists for thetas array
```

```
for aq31 in t31s1*100:
```

```
bb31=('%.0f'%aq31)
```

```
#print(bb3)
```

```
tt31.append(int(bb31))
```

```
#time.sleep(1)
```

```
tm31s1=tt31 #list to be send for first segment of first motor
```

```
print(tm31s1)
```

```
for aq32 in t31s2*100:
```

```
    bb32=('%.0f'%aq32)
```

```
    #print(bb22)
```

```
    tt32.append(int(bb32))
```

```
    #time.sleep(1)
```

```
tm31s2=tt32 #list to be send for second segment of first motor
```

```
print(tm31s2)
```

```
for aq33 in t32s1*100:
```

```
    bb33=('%.0f'%aq33)
```

```
    #print(bb23)
```

```
    tt33.append(int(bb33))
```

```
    #time.sleep(1)
```

```
tm32s1=tt33 #list to be send for first segment of second motor
```

```
print(tm32s1)
```

```
for aq34 in t32s2*100:
```

```
    bb34=('%.0f'%aq34)
```

```
    ##print(bb4)
```

```
    tt34.append(int(bb34))
```

```
    #time.sleep(1)
```

```
tm32s2=tt34 #list to be send for second segment of second motor
```

```
print(tm32s2)
```

```
print('Third manipulator data')
```

```
#print("verification done")
```

```
for i in [0,1,2,3,4]: ##slicing operation into five segment
```

```

if i==0: #first segment will be run from stationary point of end effector to first corner of square

    xg21=60*m.cos(60*m.pi/180); xg23=60*m.cos(60*m.pi/180); yg21=160+60*m.sin(60*m.pi/180);
    yg23=100+60*m.sin(60*m.pi/180); ##position w.r.t global frame(2nd manipulator)

    xg31=-60;      xg33=-60;   yg31=160;    yg33=100; ##position w.r.t global frame (third
manipulator)

    f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33)##calling function to evaluate suitable condition
    print("stationary line^^^^^^ ")

    print("-----")
    print("----- ")

    time.sleep(1)

if i==1: #second segment will be run from first to second corner of square

    xg21=60*m.cos(60*m.pi/180); xg23=130; yg21=100+60*m.sin(60*m.pi/180);
    yg23=100+60*m.sin(60*m.pi/180); ##position w.r.t global frame(2nd manipulator)

    xg31=-60;      xg33=40;   yg31=100;    yg33=100; ##position w.r.t global frame (third
manipulator)

    f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33)##calling function to evaluate suitable condition
    print("square first line CCW^^^^^^ ")

    print("-----")
    print("----- ")

    time.sleep(1)

if i==2: #third segment will be run from second to third corner of square

    xg21=130; xg23=130; yg21=151.96; yg23=51.96 ##position w.r.t global frame(2nd manipulator)

    xg31=40; xg33=40; yg31=100; yg33=0; ##position w.r.t global frame (third manipulator)

    f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33)##calling function to evaluate suitable condition
    print("square second line CCW^^^^^^ ")

    print("-----")
    print("----- ")

    time.sleep(1)

if i==3: #fourth segment will be run from third to fourth corner of square

    xg21=100+60*m.cos(60*m.pi/180); xg23=30; yg21=60*m.sin(60*m.pi/180);
    yg23=60*m.sin(60*m.pi/180); ##position w.r.t global frame(2nd manipulator)

```

```

    xg31=40;      xg33=-60;   yg31=0;    yg33=0;##position w.r.t global frame (third
manipulator)

    f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33)##calling function to evaluate suitable condition

    print("square third line CCW^^^^^^")

    print("-----")
    print("-----")

    time.sleep(1)

    if i==4:#fifth segment will be run from fourth to first corner of square

        xg21=60*m.cos(60*m.pi/180); xg23=60*m.cos(60*m.pi/180); yg21=60*m.sin(60*m.pi/180);
        yg23=100+60*m.sin(60*m.pi/180);##position w.r.t global frame(2nd manipulator)

        xg31=-60;      xg33=-60;   yg31=0;    yg33=100;##position w.r.t global frame (third
manipulator)

        f(xg21,xg23,yg21,yg23,xg31,xg33,yg31,yg33)##calling function to evaluate suitable condition

        print("square fourth line CCW ^^^^^^^^^")

        print("-----")
        print("-----")

        time.sleep(1)

```