### Convolutional Neural Networks

We now apply the MLP to MNIST (handwritten digits). First, we use densely connected networks, as done with non-image data.

Then, we look into using convolutional layers designed for images. Note that because MNIST is an easy data set to classify, the overall performances may be similar.

But there are many benefits of using CNN in images, over densely-connected networks, such as spatial understanding, less parameters, non-diminishing gradients, and others.

```
import numpy as np
import torch
import torch.nn as nn
import torch.optim as optim
# PyTorch TensorBoard support
# from torch.utils.tensorboard import SummaryWriter
# import torchvision
# import torchvision.transforms as transforms
from datetime import datetime
import torchvision
import torchvision.transforms as transforms
from torchvision.datasets import FashionMNIST
import matplotlib.pyplot as plt
%matplotlib inline
from torch.utils.data import random_split
from torch.utils.data import DataLoader
import torch.nn.functional as F
from PIL import Image
#import torchvision.transforms as T
```

# load the dataset
mnist\_dataset = FashionMNIST(root = 'data/', download=True, train = True, trans
print(mnist\_dataset)

100% | 26.4M/26.4M [00:01<00:00, 21.4MB/s] 100% | 29.5k/29.5k [00:00<00:00, 340kB/s] 100% | 4.42M/4.42M [00:00<00:00, 6.26MB/s] 100% | 5.15k/5.15k [00:00<00:00, 8.81MB/s] Dataset FashionMNIST

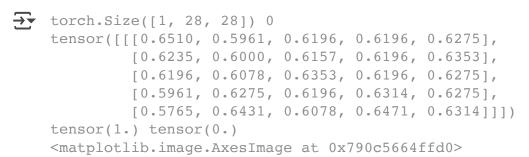
Number of datapoints: 60000

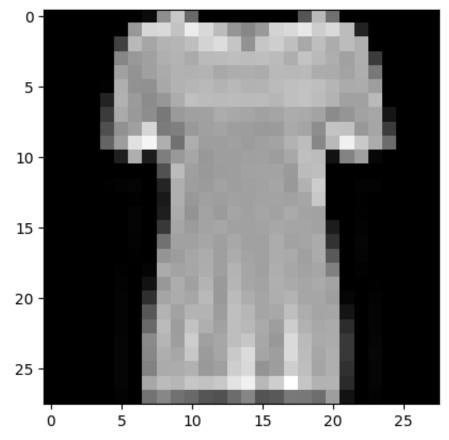
Root location: data/

Split: Train
 StandardTransform
Transform: ToTensor()

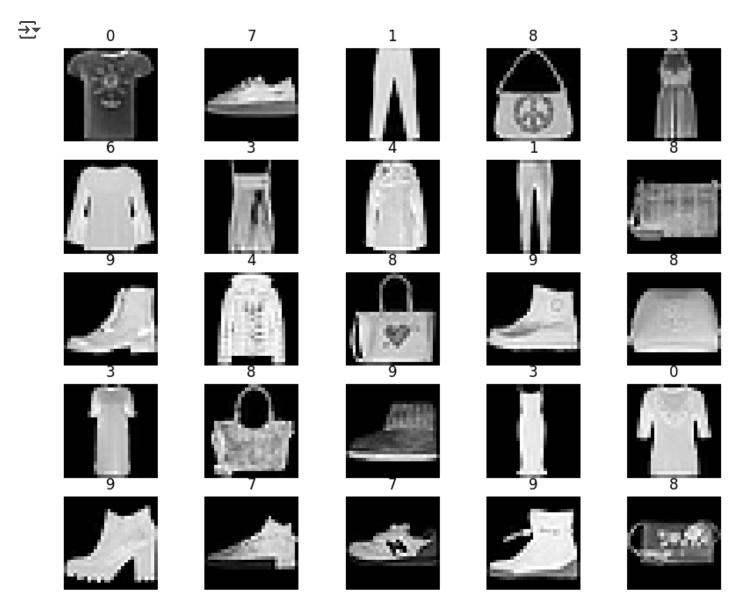
```
# mnist_dataset has 'images as tensors' so that they can't be displayed directl
sampleTensor, label = mnist_dataset[10]
print(sampleTensor.shape, label)
tpil = transforms.ToPILImage() # using the __call__ to
image = tpil(sampleTensor)
image.show()

# The image is now convert to a 28 X 28 tensor.
# The first dimension is used to keep track of the color channels.
# Since images in the MNIST dataset are grayscale, there's just one channel.
# The values range from 0 to 1, with 0 representing black, 1 white and the value print(sampleTensor[:,10:15,10:15])
print(torch.max(sampleTensor), torch.min(sampleTensor))
plt.imshow(sampleTensor[0,:,:],cmap = 'gray')
```

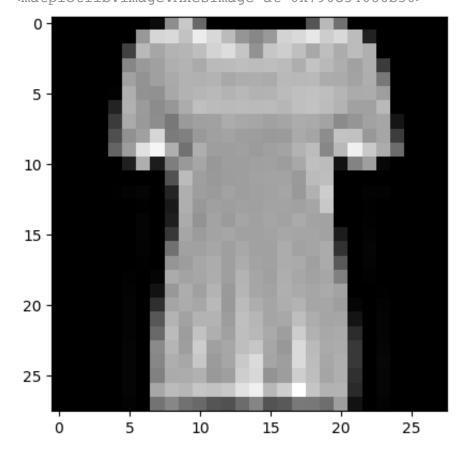




```
# Print multiple images at once
figure = plt.figure(figsize=(10, 8))
cols, rows = 5, 5
for i in range(1, cols * rows + 1):
    sample_idx = torch.randint(len(mnist_dataset), size=(1,)).item()
    img, label = mnist_dataset[sample_idx]
    figure.add_subplot(rows, cols, i)
    plt.title(label)
    plt.axis("off")
    plt.imshow(img.squeeze(), cmap="gray")
plt.show()
```



```
# The image is now convert to a 28 X 28 tensor.
# The first dimension is used to keep track of the color channels.
# Since images in the MNIST dataset are grayscale, there's just one channel.
# The values range from 0 to 1, with 0 representing black, 1 white and the value print(sampleTensor[:,10:15,10:15])
print(torch.max(sampleTensor), torch.min(sampleTensor))
plt.imshow(sampleTensor[0,:,:],cmap = 'gray')
```



## Training and validation data

While building a ML/DP models, it is common to split the dataset into 3 parts:

- Training set to train the model,c ompute the loss and adjust the weights of the model using gradient descent.
- Validation set to evalute the traing model, adjusting the hyperparameters and pick the best version of the model.
- Test set to final check the model predictions on the new unseen data to evaluate how well the model is performing.

Quite often, validation and test sets are interchanged (i.e., the validation set is used to final check the model predictions...). Read carefully of the setup.

Following adapted from Kaggle notebook

```
train_data, validation_data = random_split(mnist_dataset, [50000, 10000])
## Print the length of train and validation datasets
print("length of Train Datasets: ", len(train_data))
print("length of Validation Datasets: ", len(validation_data))

batch_size = 128
train_loader = DataLoader(train_data, batch_size, shuffle = True)
val_loader = DataLoader(validation_data, batch_size, shuffle = False)
## MNIST data from pytorch already provides held-out test set!

→ length of Train Datasets: 50000
length of Validation Datasets: 10000
```

## Multi-class Logistic Regression (a building block of DNN)

Since nn.Linear expects the each training example to a vector, each 1 X 28 X 28 image tensor needs to be flattened out into a vector of size 784(28 X 28), before being passed into the model.

The output for each image is vector of size 10, with each element of the vector signifying the probability a particular target label (i.e 0 to 9). The predicted label for an image is simply the one with the highest probability.

```
## Basic set up for a logistic regression model (won't be used in practice or f
input_size = 28 * 28
num_classes = 10

# we gradually build on this inherited class from pytorch
model = nn.Linear(input_size, num_classes)
```

We define the class with multiple methods so that we can train, evaluate, and do many other routine tasks with the model.

Particularly, we are looking at multi-class logistic regression (a generalization of one-class logistic regression) using the softmax function (more about this in a few cells down)

```
# Slowly build the model, first with basic
class MnistModel(nn.Module):
    def __init__(self):
        super().__init__()
        self.linear = nn.Linear(input size, num classes)
    def forward(self, xb):
        # view xb with two dimensions, 28 \times 28 (i.e 784)
        # One argument to .reshape can be set to -1(in this case the first dime
        # to let PyTorch figure it out automatically based on the shape of the
        xb = xb.reshape(-1, 784)
        print(xb)
        out = self.linear(xb)
        print(out)
        return(out)
model = MnistModel()
print(model.linear.weight.shape, model.linear.bias.shape)
list(model.parameters())
→ torch.Size([10, 784]) torch.Size([10])
    [Parameter containing:
     tensor([[ 2.0907e-02, 2.7459e-02, -1.4845e-02, ..., -1.7609e-02,
              -2.2391e-02, 2.1963e-02],
              [-8.0819e-03, 2.4515e-05, -3.3890e-02, ..., 1.3287e-02,
              -2.2234e-02, 3.2460e-02],
              [-2.3208e-02, -1.6071e-03, -3.0139e-02, ..., 2.1160e-02,
              -3.6655e-03, -6.7761e-03],
              [ 7.5451e-03, 1.2244e-02, 2.3981e-02, ..., 1.5644e-02,
               1.5831e-02, -1.5363e-03],
              [ 3.4407e-02, -3.5048e-03, 3.3605e-04, ..., 3.4028e-02,
               2.0446e-02, -3.4489e-02],
              [-2.1184e-02, -3.0666e-02, -1.6693e-02, ..., 8.1354e-03,
              -1.8302e-02, -3.3419e-02]], requires_grad=True),
     Parameter containing:
     tensor([-0.0244, 0.0245, -0.0346, 0.0199, -0.0297, -0.0021, 0.0165,
    -0.0319,
              0.0347, 0.0131], requires grad=True)]
```

```
# Alway check the dimensions and sample data/image
for images, labels in train_loader:
    outputs = model(images)
    break
print('Outputs shape: ', outputs.shape) # torch.Size([128, 10])
print('Sample outputs: \n', outputs[:2].data) # example outputs
→ tensor([[0., 0., 0., ..., 0., 0., 0.],
            [0., 0., 0., ..., 0., 0., 0.]
            [0., 0., 0., \ldots, 0., 0., 0.]
            [0., 0., 0., ..., 0., 0., 0.]
            [0., 0., 0., ..., 0., 0., 0.]
            [0., 0., 0., ..., 0., 0., 0.]])
    tensor([[ 0.0182, 0.2751, -0.1472, ..., -0.0385, 0.1367, 0.1214],
            [-0.1486, 0.1062, -0.1046, ..., -0.1610, 0.0119, -0.0697],
            [-0.3764, 0.0882, -0.1604, ..., -0.1429, -0.0489, -0.2043],
            [-0.0113, 0.0607, -0.0438, \ldots, -0.0642, -0.0405, -0.1512],
            [-0.1826, -0.2300, 0.1216, \dots, 0.2772, 0.1210, 0.0545],
            [-0.2659, 0.0113, 0.0558, \dots, 0.3705, -0.2021, 0.0633]],
           grad fn=<AddmmBackward0>)
    Outputs shape: torch.Size([128, 10])
    Sample outputs:
     tensor([[ 0.0182,  0.2751, -0.1472,  0.2251, -0.0220, -0.3688, -0.1669, -0
              0.1367, 0.1214],
            [-0.1486, 0.1062, -0.1046, 0.1274, -0.0118, -0.1053, 0.0188, -0.1053]
              0.0119, -0.0697]
```

### Softmax function

The softmax formula is as follows:

$$\sigma(\vec{z})_i = \frac{e^{z_i}}{\sum_{j=1}^K e^{z_j}}$$

### Mathematical definition of the softmax function

where all the zi values are the elements of the input vector and can take any real value. The term on the bottom of the formula is the normalization term which ensures that all the output values of the function will sum to 1, thus constituting a valid probability distribution.

The softmax function is a function that turns a vector of K real values into a vector of K real values that sum to 1. The input values can be positive, negative, zero, or greater than one, but the softmax transforms them into values between 0 and 1, so that they can be interpreted as probabilities. If one of the inputs is small or negative, the softmax turns it into a small probability, and if an input is large, then it turns it into a large probability, but it will always remain between 0 and 1.

The softmax function is sometimes called the softargmax function, or multi-class logistic regression. This is because the softmax is a generalization of logistic regression that can be used for multi-class classification, and its formula is very similar to the sigmoid function which is used for logistic regression. The softmax function can be used in a classifier only when the classes are mutually exclusive.

Many multi-layer neural networks end in a penultimate layer which outputs real-valued scores that are not conveniently scaled and which may be difficult to work with. Here the softmax is very useful because it converts the scores to a normalized probability distribution, which can be displayed to a user or used as input to other systems. For this reason it is usual to append a softmax function as the final layer of the neural network.

### Softmax Activation Function

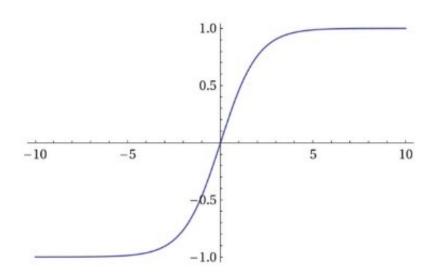


Image from <a href="https://insideaiml.com/blog/SoftMaxActivation-Function-1034">https://insideaiml.com/blog/SoftMaxActivation-Function-1034</a>

### Evaluation Metric and Loss Function

Here we evaluate our model by finding the percentage of labels that were predicted correctly i.e. the accuracy of the predictions. We can simply find the label with maximum value (before OR after the softmax layer).

NOTE that while accuracy is a great way to evluate the model, it can't be used as a loss function for optimizing our model using gradient descent, because it does not take into account the actual probabilities predicted by the model, so it can't provide sufficient feedback for increemental improvements.

Due to this reason accuracy is a great evaluation metric (and human-understanble) for classification metric, but not a good loss function. A commonly used loss function for classification problems is the Cross Entropy (implemented directly, no extra coding required).

```
# accuracy calculation
def accuracy(outputs, labels):
    _, preds = torch.max(outputs, dim = 1)
    return(torch.tensor(torch.sum(preds == labels).item()/ len(preds)))

print("Accuracy: ", accuracy(outputs, labels))
print("\n")
loss_fn = F.cross_entropy
print("Loss Function: ",loss_fn)
print("\n")
## Loss for the current batch
loss = loss_fn(outputs, labels)
print(loss)

Accuracy: tensor(0.0234)

Loss Function: <function cross_entropy at 0x790d3c34a5c0>
tensor(2.3646, grad_fn=<NllLossBackward0>)
```

## Cross-Entropy

Cross-entropy is commonly used to quantify the difference between two probabilities distribution. Usually the "True" distribution is expressed in terms of a one-hot distribution.

#### Read more on:

- https://en.wikipedia.org/wiki/Cross\_entropy
- <a href="https://machinelearningmastery.com/cross-entropy-for-machine-learning/">https://machinelearningmastery.com/cross-entropy-for-machine-learning/</a>
- https://stackoverflow.com/questions/41990250/what-is-cross-entropy

```
# We put all of the above:
class MnistModel(nn.Module):
    def __init__(self):
        super().__init__()
        self.linear = nn.Linear(input_size, num_classes)
    def forward(self, xb):
        xb = xb.reshape(-1, 784)
        out = self.linear(xb)
        return(out)
    # We add extra methods
    def training step(self, batch):
        # when training, we compute the cross entropy, which help us update wei
        images, labels = batch
        out = self(images) ## Generate predictions
        loss = F.cross_entropy(out, labels) ## Calculate the loss
        return(loss)
    def validation_step(self, batch):
        images, labels = batch
        out = self(images) ## Generate predictions
        loss = F.cross_entropy(out, labels) ## Calculate the loss
        # in validation, we want to also look at the accuracy
        # idealy, we would like to save the model when the accuracy is the high
        acc = accuracy(out, labels) ## calculate metrics/accuracy
        return({'val_loss':loss, 'val_acc': acc})
    def validation_epoch_end(self, outputs):
        # at the end of epoch (after running through all the batches)
        batch_losses = [x['val_loss'] for x in outputs]
        epoch_loss = torch.stack(batch_losses).mean()
        batch_accs = [x['val_acc'] for x in outputs]
        epoch_acc = torch.stack(batch_accs).mean()
```

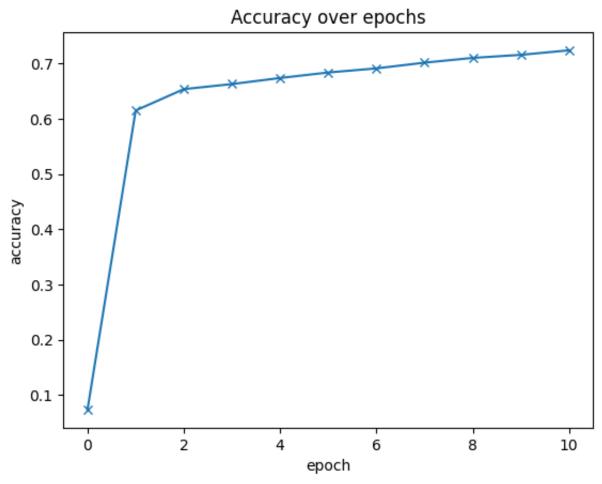
```
return({'val_loss': epoch_loss.item(), 'val_acc' : epoch_acc.item()})
    def epoch_end(self, epoch,result):
        # log epoch, loss, metrics
        print("Epoch [{}], val_loss: {:.4f}, val_acc: {:.4f}".format(epoch, res
# we instantiate the model
model = MnistModel()
# a simple helper function to evaluate
def evaluate(model, data_loader):
    # for batch in data loader, run validation step
    outputs = [model.validation_step(batch) for batch in data_loader]
    return(model.validation epoch end(outputs))
# actually training
def fit(epochs, lr, model, train_loader, val_loader, opt_func = torch.optim.SGD
    history = []
    optimizer = opt_func(model.parameters(), lr)
    for epoch in range(epochs):
        ## Training Phase
        for batch in train loader:
            loss = model.training_step(batch)
            loss.backward() ## backpropagation starts at the loss and goes thro
            optimizer.step() ## the optimizer iterate over all parameters (tens
            optimizer.zero_grad() ## reset gradients
        ## Validation phase
        result = evaluate(model, val loader)
        model.epoch_end(epoch, result)
        history.append(result)
    return(history)
# test the functions, with a randomly initialized model (weights are random, e.
result0 = evaluate(model, val_loader)
result0
→ {'val_loss': 2.3714499473571777, 'val_acc': 0.07337816804647446}
```

```
# let's train for 10 epochs
history1 = fit(10, 0.001, model, train_loader, val_loader)

Epoch [0], val_loss: 1.7310, val_acc: 0.6149
Epoch [1], val_loss: 1.4329, val_acc: 0.6536
Epoch [2], val_loss: 1.2623, val_acc: 0.6628
Epoch [3], val_loss: 1.1527, val_acc: 0.6738
Epoch [4], val_loss: 1.0764, val_acc: 0.6837
Epoch [5], val_loss: 1.0195, val_acc: 0.6912
Epoch [6], val_loss: 0.9754, val_acc: 0.7015
Epoch [7], val_loss: 0.9400, val_acc: 0.7101
Epoch [8], val_loss: 0.9109, val_acc: 0.7157
Epoch [9], val_loss: 0.8858, val_acc: 0.7239
```

```
# we combine the first result (no training) and the training results of 5 epoch
# plotting accuracy
history = [result0] + history1
accuracies = [result['val_acc'] for result in history]
plt.plot(accuracies, '-x')
plt.xlabel('epoch')
plt.ylabel('accuracy')
plt.title('Accuracy over epochs')
```

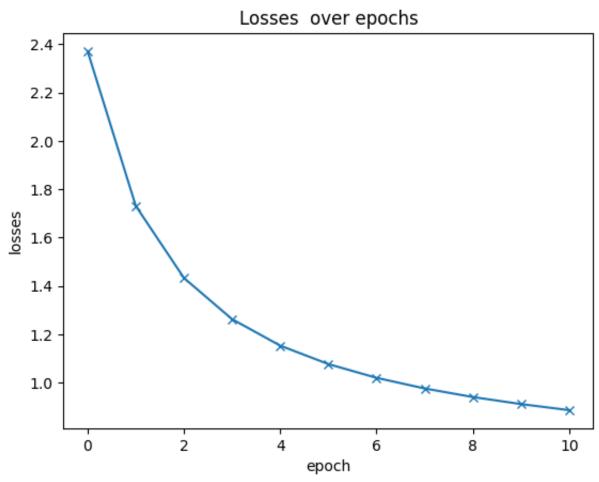




```
# plotting losses
history = [result0] + history1
losses = [result['val_loss'] for result in history]
plt.plot(losses, '-x')
plt.xlabel('epoch')
plt.ylabel('losses')
plt.title('Losses over epochs')
```

<del>⋽</del>₹

Text(0.5, 1.0, 'Losses over epochs')

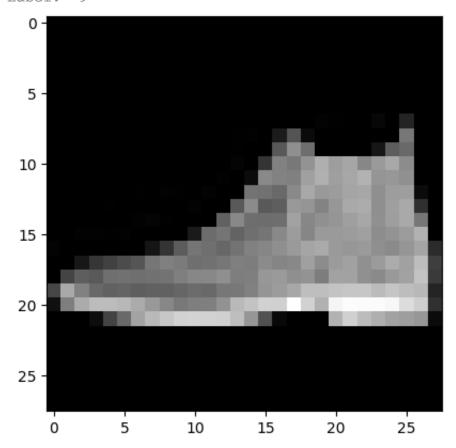


# Final check using the (held-out) test dataset.

We will first load the test dataset (from MNIST) and individually check the prediction made by the model. And then, we will put through all images in the test dataset to obtain the final accuracy

```
# Testing with individual images
## Define the test dataset
test_dataset = FashionMNIST(root = 'data/', train = False, transform = transfor
print("Length of Test Datasets: ", len(test_dataset))
img, label = test_dataset[0]
plt.imshow(img[0], cmap = 'gray')
print("Shape: ", img.shape)
print('Label: ', label)
```

Length of Test Datasets: 10000 Shape: torch.Size([1, 28, 28]) Label: 9



```
def predict_image(img, model):
    xb = img.unsqueeze(0)
    yb = model(xb)
    _, preds = torch.max(yb, dim = 1)
    return(preds[0].item())

img, label = test_dataset[0]
print('Label:', label, ', Predicted :', predict_image(img, model))

The Label: 9 , Predicted : 9
```

# Convolutional Neural Network (CNN)

So far we treated the MNIST data by flatting each image into a vector. However, there's a lot of information embedded in spatial information. In order to fully `understand' the image, we need to consider its 2 or more dimensions. Convolutional layers help us in this regard. In most of cases, CNN outperforms densely connected networks and is the most popular architecture for imaging analysis.

CNN is the main force behind revolutionizing the AI or deep learning in the recent decade. Deep neural networks using CNN has shown unprecedented performances when they were first introduced at many competitions (e.g., the ImageNet) by large margins. For imaging analysis, CNN remains the mainstay.

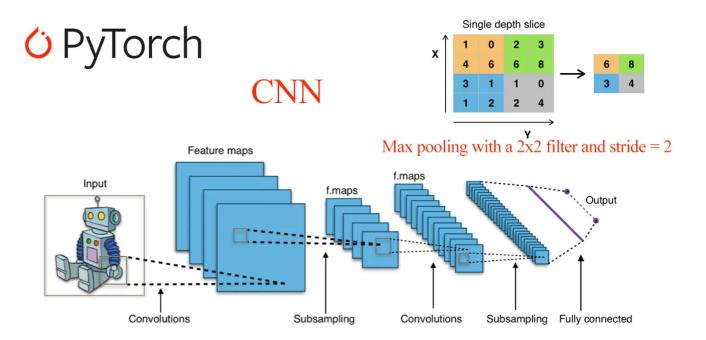
Looking ahead, there are more recent architectures such as the transformer and the diffusion model. We won't be convering them in this course;)

Convolutional layer is implemented in pytorch as **nn.Conv2d**. As you can see, it is essentially a drop in replacement for nn.Linear and other classes.

The explanation for the pytorch class **nn.Conv2d**.

in\_channels (int) — Number of channels in the input image, 1 for a grayscale image out\_channels (int) — Number of channels produced by the convolution kernel\_size (int or tuple) — Size of the convolving kernel stride (int or tuple, optional) — Stride of the convolution. Default: 1 padding (int or tuple, optional) — Zero-padding added to both sides of the input. Default: 0 padding\_mode (string, optional) — 'zeros', 'reflect', 'replicate' or 'circular'. Default: 'zeros' dilation (int or tuple, optional) — Spacing between kernel elements. Default: 1 groups (int, optional) — Number of blocked connections from input channels to output channels. Default: 1

bias (bool, optional) — If True, adds a learnable bias to the output. Default: True Adapted from <a href="mailto:onuntanbhogendrasharma">onuntanbhogendrasharma</a>



```
# We construct a fundamental CNN class.
class CNN(nn.Module):
    def __init__(self):
        super(CNN, self).__init__()
        self.conv1 = nn.Sequential(
            nn.Conv2d(
                in_channels=1,
                out channels=16,
                kernel_size=5,
                stride=1.
                padding=2,
            ),
            nn.ReLU(),
            nn.MaxPool2d(kernel_size=2),
        self.conv2 = nn.Sequential(
            nn.Conv2d(16, 32, 5, 1, 2),
            nn.ReLU(),
            nn.MaxPool2d(2),
        )
        # fully connected layer, output 10 classes
        self.out = nn.Linear(32 * 7 * 7, 10)
    def forward(self, x):
        x = self.conv1(x)
        x = self.conv2(x)
        # flatten the output of conv2 to (batch_size, 32 * 7 * 7)
        x = x.view(x.size(0), -1)
        output = self.out(x)
        return output, x # return x for visualization
cnn = CNN()
print(cnn)
    CNN (
       (conv1): Sequential(
         (0): Conv2d(1, 16, kernel size=(5, 5), stride=(1, 1), padding=(2, 2))
         (1): ReLU()
         (2): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mod
       (conv2): Sequential(
         (0): Conv2d(16, 32, kernel size=(5, 5), stride=(1, 1), padding=(2, 2))
         (1): ReLU()
         (2): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mod
      (out): Linear(in_features=1568, out_features=10, bias=True)
```

```
loss_func = nn.CrossEntropyLoss()
loss_func
# unlike earlier example using optim.SGD, we use optim.Adam as the optimizer
# lr(Learning Rate): Rate at which our model updates the weights in the cells \epsilon
optimizer = optim.Adam(cnn.parameters(), lr = 0.01)
optimizer
    Adam (
    Parameter Group 0
         amsgrad: False
         betas: (0.9, 0.999)
         capturable: False
         differentiable: False
         eps: 1e-08
         foreach: None
         fused: None
         lr: 0.01
         maximize: False
         weight_decay: 0
     )
```

```
# train_data, validation_data = random_split(mnist_dataset, [50000, 10000])
# ## Print the length of train and validation datasets
# print("length of Train Datasets: ", len(train_data))
# print("length of Validation Datasets: ", len(validation_data))
# batch size = 128
# train_loader = DataLoader(train_data, batch_size, shuffle = True)
# val loader = DataLoader(validation data, batch size, shuffle = False)
from torch.autograd import Variable
def train(num_epochs, cnn, loaders):
    cnn.train()
    optimizer = optim.Adam(cnn.parameters(), lr = 0.01)
    loss_func = nn.CrossEntropyLoss()
    # Train the model
    total step = len(loaders)
    for epoch in range(num_epochs):
        for i, (images, labels) in enumerate(loaders):
            # gives batch data, normalize x when iterate train_loader
            b_x = Variable(images)
                                     # batch x
            b_y = Variable(labels)
                                     # batch v
            output = cnn(b_x)[0]
            loss = loss_func(output, b_y)
            # clear gradients for this training step
            optimizer.zero_grad()
            # backpropagation, compute gradients
            loss.backward()
            # apply gradients
            optimizer.step()
            if (i+1) % 100 == 0:
                print ('Epoch [{}/{}], Step [{}/{}], Loss: {:.4f}'.format(epoch
                pass
        pass
    pass
```

```
# instiate the CNN model
cnn = CNN()
# for testing purpose, we calculate the accuracy of the initial
with torch.no grad():
    correct = 0
    total = 0
    for images, labels in train loader:
        test_output, last_layer = cnn(images)
        pred_y = torch.max(test_output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
        pass
print('Accuracy of the model on the 10000 test images: %.2f' % accuracy)
Accuracy of the model on the 10000 test images: 0.10
train(num epochs=5, cnn=cnn, loaders=train loader)
    Epoch [1/5], Step [100/391], Loss: 0.6000
    Epoch [1/5], Step [200/391], Loss: 0.4482
    Epoch [1/5], Step [300/391], Loss: 0.3724
    Epoch [2/5], Step [100/391], Loss: 0.3143
    Epoch [2/5], Step [200/391], Loss: 0.2415
    Epoch [2/5], Step [300/391], Loss: 0.2864
    Epoch [3/5], Step [100/391], Loss: 0.3050
    Epoch [3/5], Step [200/391], Loss: 0.3437
    Epoch [3/5], Step [300/391], Loss: 0.3125
    Epoch [4/5], Step [100/391], Loss: 0.2782
    Epoch [4/5], Step [200/391], Loss: 0.3053
    Epoch [4/5], Step [300/391], Loss: 0.1805
    Epoch [5/5], Step [100/391], Loss: 0.2349
    Epoch [5/5], Step [200/391], Loss: 0.1802
    Epoch [5/5], Step [300/391], Loss: 0.2750
```

## Evaluate the model on test data

We must call model.eval() to set dropout and batch normalization layers to evaluation mode before running inference. model.train() set layers like dropout, batchnorm etc. to behave for training.

You can call either model.eval() or model.train(mode=False) to tell that you are testing the model.

```
# Test the model, after the training
cnn.eval()
with torch.no_grad():
    correct = 0
    total = 0
    for images, labels in train_loader:
        test_output, last_layer = cnn(images)
        pred y = torch.max(test output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
print('Test Accuracy of the model on the 10000 test images: %.2f' % accuracy)
Test Accuracy of the model on the 10000 test images: 0.94
# Test the model, after the training
cnn.eval()
with torch.no grad():
    correct = 0
    total = 0
    for images, labels in test_loader:
        test_output, last_layer = cnn(images)
        pred y = torch.max(test output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
        pass
print('Test Accuracy of the model on the 10000 test images: %.2f' % accuracy)
Test Accuracy of the model on the 10000 test images: 0.88
Run inference on individual images
sample = next(iter(test_loader))
imgs, lbls = sample
actual number = lbls[:10].numpy()
actual number
test_output, last_layer = cnn(imgs[:10])
pred_y = torch.max(test_output, 1)[1].data.numpy().squeeze()
print(f'Prediction number: {pred_y}')
print(f'Actual number: {actual_number}')
→ Prediction number: [9 2 1 1 6 1 4 6 5 7]
    Actual number: [9 2 1 1 6 1 4 6 5 7]
```

# Fashion MNIST (Homework dataset)

The MNIST dataset is not too demanding, let's try something a little more difficult - Fashion MNIST.

#### LINK TO IMAGE

Check out labels on GitHub:

```
Start coding or generate with AI.
```

## HOMEWORK 1

Build a classifier for fashion MNIST.

- 1. Use exactly the same architectures (both densely connected layers and from convolutional layers) as the above MNIST e.g., replace the dataset. Save the Jupyter Notebook in its original format and output a PDF file after training, testing, and validation. Make sure to write down how do they perform (training accuracy), testing accuracy).
- 2. Improve the architecture. Experiment with different numbers of layers, size of layers, number of filters, size of filters. You are required to make those adjustment to get the highest accuracy. Watch out for overfitting -- we want the highest testing accuracy! Please provide a PDF file of the result, the best test accuracy and the architecture (different numbers of layers, size of layers, number of filters, size of filters)

```
self.conv2 = nn.Sequential(
            nn.Conv2d(32, 64, 5, 1, 2),
            nn.BatchNorm2d(64),
            nn.ReLU(),
            nn.MaxPool2d(2),
        )
        self.conv3 = nn.Sequential(
            nn.Conv2d(64, 128, 3, 1, 1),
            nn.BatchNorm2d(128),
            nn.ReLU(),
            nn.MaxPool2d(2),
        )
         # fully connected layer, output 10 classes
        self.dropout = nn.Dropout(0.5)
        self.out = nn.Linear(128 * 3 * 3, 10)
    def forward(self, x):
        x = self.conv1(x)
        x = self.conv2(x)
        x = self.conv3(x)
        x = x.view(x.size(0), -1)
        x = self.dropout(x)
        output = self.out(x)
        return output, x
cnn = CNN()
print(cnn)
```

```
→ CNN (
       (conv1): Sequential(
         (0): Conv2d(1, 32, kernel size=(5, 5), stride=(1, 1), padding=(2, 2))
         (1): ReLU()
         (2): MaxPool2d(kernel size=2, stride=2, padding=0, dilation=1, ceil mod
       (conv2): Sequential(
         (0): Conv2d(32, 64, kernel_size=(5, 5), stride=(1, 1), padding=(2, 2))
         (1): BatchNorm2d(64, eps=1e-05, momentum=0.1, affine=True, track_runnin
         (2): ReLU()
         (3): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mod
       )
       (conv3): Sequential(
         (0): Conv2d(64, 128, kernel\_size=(3, 3), stride=(1, 1), padding=(1, 1))
         (1): BatchNorm2d(128, eps=1e-05, momentum=0.1, affine=True, track_runni
         (2): ReLU()
         (3): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mod
       (dropout): Dropout(p=0.5, inplace=False)
       (out): Linear(in_features=1152, out_features=10, bias=True)
     )
loss func = nn.CrossEntropyLoss()
loss_func
# unlike earlier example using optim.SGD, we use optim.Adam as the optimizer
# lr(Learning Rate): Rate at which our model updates the weights in the cells \epsilon
optimizer = optim.Adam(cnn.parameters(), lr = 0.001)
optimizer
    Adam (
    Parameter Group 0
         amsgrad: False
         betas: (0.9, 0.999)
         capturable: False
         differentiable: False
         eps: 1e-08
         foreach: None
         fused: None
         lr: 0.001
         maximize: False
        weight_decay: 0
     )
```

```
# train_data, validation_data = random_split(mnist_dataset, [50000, 10000])
# ## Print the length of train and validation datasets
# print("length of Train Datasets: ", len(train_data))
# print("length of Validation Datasets: ", len(validation_data))
# batch size = 128
# train_loader = DataLoader(train_data, batch_size, shuffle = True)
# val loader = DataLoader(validation data, batch size, shuffle = False)
from torch.autograd import Variable
def train(num_epochs, cnn, loaders):
    cnn.train()
    optimizer = optim.Adam(cnn.parameters(), lr = 0.001)
    loss_func = nn.CrossEntropyLoss()
    # Train the model
    total step = len(loaders)
    for epoch in range(num_epochs):
        for i, (images, labels) in enumerate(loaders):
            # gives batch data, normalize x when iterate train_loader
            b_x = Variable(images)
                                     # batch x
            b_y = Variable(labels)
                                     # batch v
            output = cnn(b_x)[0]
            loss = loss_func(output, b_y)
            # clear gradients for this training step
            optimizer.zero_grad()
            # backpropagation, compute gradients
            loss.backward()
            # apply gradients
            optimizer.step()
            if (i+1) % 100 == 0:
                print ('Epoch [{}/{}], Step [{}/{}], Loss: {:.4f}'.format(epoch
                pass
        pass
    pass
```

```
# instiate the CNN model
cnn = CNN()
# for testing purpose, we calculate the accuracy of the initial
cnn.eval()
with torch.no_grad():
    correct = 0
    total = 0
    for images, labels in train_loader:
        test_output, last_layer = cnn(images)
        pred_y = torch.max(test_output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
        pass
print('Accuracy of the model on the 10000 test images: %.2f' % accuracy)
```

Accuracy of the model on the 10000 test images: 0.07

#### train(num epochs=15, cnn=cnn, loaders=train loader)

```
Epoch [1/15], Step [100/391], Loss: 0.3381
Epoch [1/15], Step [200/391], Loss: 0.4306
Epoch [1/15], Step [300/391], Loss: 0.2697
Epoch [2/15], Step [100/391], Loss: 0.3284
Epoch [2/15], Step [200/391], Loss: 0.3872
Epoch [2/15], Step [300/391], Loss: 0.2838
Epoch [3/15], Step [100/391], Loss: 0.2822
Epoch [3/15], Step [200/391], Loss: 0.1569
Epoch [3/15], Step [300/391], Loss: 0.2902
Epoch [4/15], Step [100/391], Loss: 0.3591
Epoch [4/15], Step [200/391], Loss: 0.2058
Epoch [4/15], Step [300/391], Loss: 0.2580
Epoch [5/15], Step [100/391], Loss: 0.1563
Epoch [5/15], Step [200/391], Loss: 0.2188
Epoch [5/15], Step [300/391], Loss: 0.1739
Epoch [6/15], Step [100/391], Loss: 0.2508
Epoch [6/15], Step [200/391], Loss: 0.2612
Epoch [6/15], Step [300/391], Loss: 0.2151
Epoch [7/15], Step [100/391], Loss: 0.2580
Epoch [7/15], Step [200/391], Loss: 0.2317
Epoch [7/15], Step [300/391], Loss: 0.1819
Epoch [8/15], Step [100/391], Loss: 0.2024
Epoch [8/15], Step [200/391], Loss: 0.1288
Epoch [8/15], Step [300/391], Loss: 0.1056
Epoch [9/15], Step [100/391], Loss: 0.2760
Epoch [9/15], Step [200/391], Loss: 0.2494
Epoch [9/15], Step [300/391], Loss: 0.2407
Epoch [10/15], Step [100/391], Loss: 0.1204
Epoch [10/15], Step [200/391], Loss: 0.1939
Epoch [10/15], Step [300/391], Loss: 0.1982
Epoch [11/15], Step [100/391], Loss: 0.1412
Epoch [11/15], Step [200/391], Loss: 0.1153
Epoch [11/15], Step [300/391], Loss: 0.1413
Epoch [12/15], Step [100/391], Loss: 0.1875
Epoch [12/15], Step [200/391], Loss: 0.2065
Epoch [12/15], Step [300/391], Loss: 0.1518
Epoch [13/15], Step [100/391], Loss: 0.1022
Epoch [13/15], Step [200/391], Loss: 0.1487
Epoch [13/15], Step [300/391], Loss: 0.1300
Epoch [14/15], Step [100/391], Loss: 0.1634
Epoch [14/15], Step [200/391], Loss: 0.1388
Epoch [14/15], Step [300/391], Loss: 0.1624
Epoch [15/15], Step [100/391], Loss: 0.1376
Epoch [15/15], Step [200/391], Loss: 0.0750
Epoch [15/15], Step [300/391], Loss: 0.1229
```

```
# Test the model, after the training
cnn.eval()
with torch.no_grad():
    correct = 0
    total = 0
    for images, labels in train_loader:
        test_output, last_layer = cnn(images)
        pred y = torch.max(test output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
print('Test Accuracy of the model on the 10000 test images: %.2f' % accuracy)
Test Accuracy of the model on the 10000 test images: 1.00
# Test the model, after the training
cnn.eval()
with torch.no grad():
    correct = 0
    total = 0
    for images, labels in test_loader:
        test_output, last_layer = cnn(images)
        pred y = torch.max(test output, 1)[1].data.squeeze()
        accuracy = (pred_y == labels).sum().item() / float(labels.size(0))
        pass
print('Test Accuracy of the model on the 10000 test images: %.2f' % accuracy)
Test Accuracy of the model on the 10000 test images: 0.94
sample = next(iter(test_loader))
imgs, lbls = sample
actual_number = lbls[:10].numpy()
actual_number
test_output, last_layer = cnn(imgs[:10])
pred_y = torch.max(test_output, 1)[1].data.numpy().squeeze()
print(f'Prediction number: {pred_y}')
print(f'Actual number: {actual number}')
→ Prediction number: [9 2 1 1 6 1 4 6 5 7]
    Actual number: [9 2 1 1 6 1 4 6 5 7]
```