

Thermodynamics

- ↳ Quantum computers operates in range of milli kelvins
- ↳ A mega watt of power is consumed in computer centre
- ↳ This mega watt of energy converts into heat. This heat has to be taken out otherwise temperature will keep rising and system will be melt. There should be heat removal mechanism.
- ↳ Tower has model had been adapted due to its thermal profit.

Q1. Find mass of Air in closed classroom using $pV = nRT$.

Q2. At NTP, gap between two neighbouring molecules of nitrogen (for uniformly distribution).

Q3. Specific heat of monoatomic gas, (C_p, C_v, γ, R) relation.

↳ 4 laws of thermodynamics.

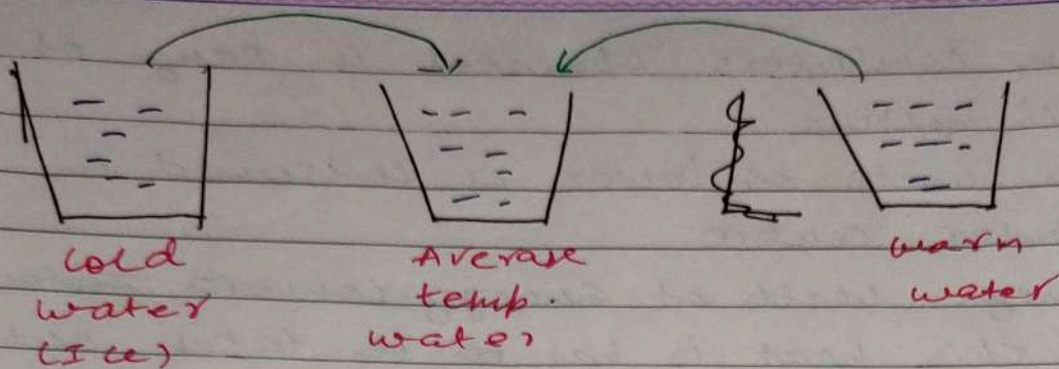
↳ Galileo (1600-1665) → had a Ambassador friend

Q.

Ambassador asked to Galileo: -

Water is cooler in summer & warmer in winter

↳ but in actually, water is warmer in summer and cooler in winter.



↳ Newton asked first ^{to} his friend to put Right hand in Ice water and Left hand in warm water and kept it for 5 minutes, after 5 minutes put your both ~~hand~~ hand in Avg. temperature water.

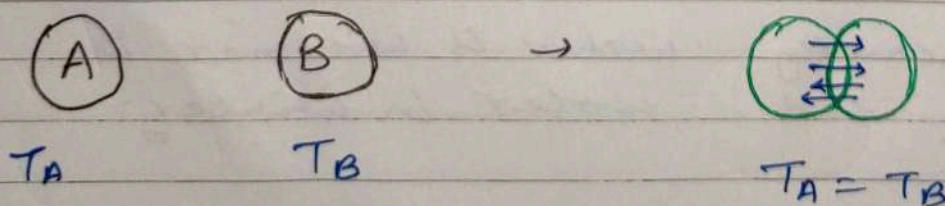
↳ Right hand feels warmer. } → Psychological perception.
 ↳ Left hand feels colder

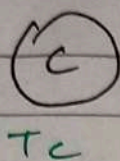
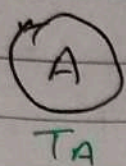
↳ but temperature should be constant for both left and right hand.

↳ from here, concept of temperature was derived.

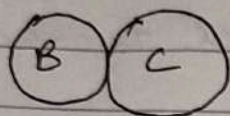
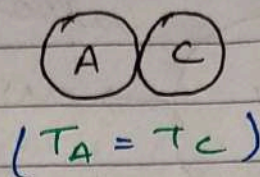
temperature ⇒ Celsius (0-100)
 Fahrenheit (32-212)
 Reaumur (0-80) } → Scaling

Zeroth Law





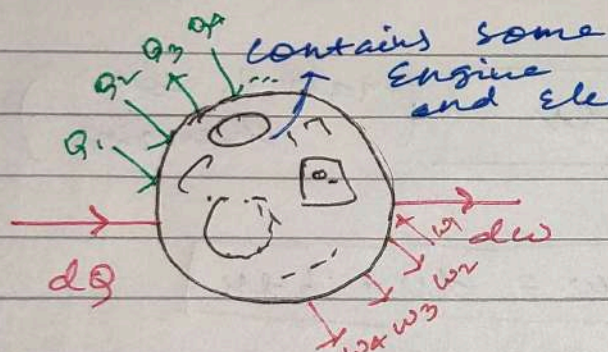
→



↳ There will be no heat flow
($T_B = T_C = T_A$)

↳ A & B, A & C, B & C are in thermal equilibrium.

First Law of Thermodynamics



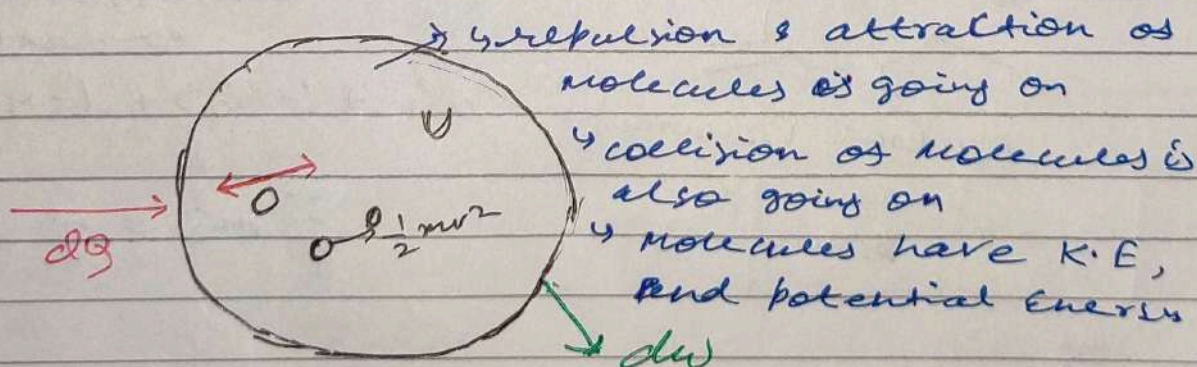
VVI

Q entering → positive
 W leaving → negative

$$dQ = (Q_1 + Q_2 - Q_3 + Q_4 - \dots)$$

$$dW = (-W_1 + W_2 + W_3 + W_4)$$

dQ, dW → all are in Joules



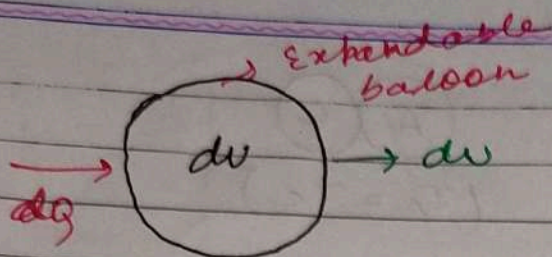
$$dQ = dW + dU$$

Heat Work Internal Energy

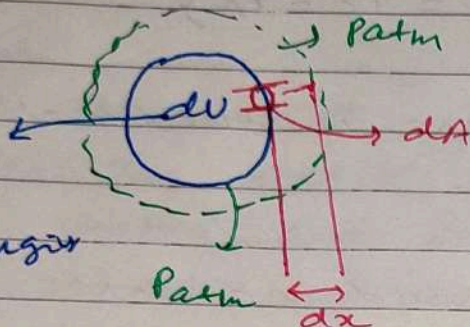
Income Expenditure assets

Internal energy:-
Sum of K.E + P.E + Rotational Energy, #

all energies ~ of all molecules.



↳ on providing dq , temperature will increase



$$F = p dA$$

$$dw = F \cdot dx = p dA dx = p dV$$

$$dw = p dV$$

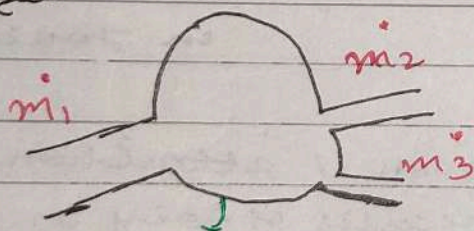
no. of molecules is not changing

$$dq = du + p \cdot dV \quad (\text{mass is not changing})$$

(in closed system)

↳ FLOT \Rightarrow $dq = du + dw = du + p dV$

conservation of matter



control volume
Imaginary boundary

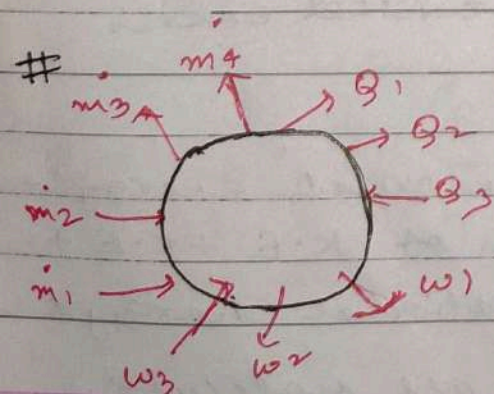
↳ After steady state,

$$m_1 = m_2 + m_3$$

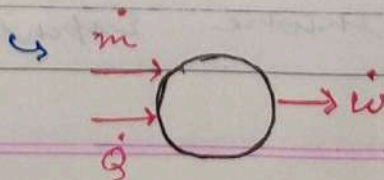
↳ conservation of matter

$$m_1 + (-m_2) + (-m_3) = 0$$

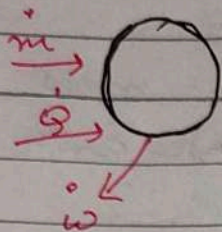
$$\sum_j m_j = 0$$



$$\dot{m} = \sum \dot{m}_i \quad \dot{Q} = \sum \dot{Q}_i \quad \dot{w} = \sum \dot{w}_i$$



Conservation of Energy :-



$$\dot{m} \left[u + p v + \frac{v^2}{2} + g z \right] + \dot{Q} - \dot{W} = 0$$

↳ 1st Law of thermodynamics

↳ $u \rightarrow$ Internal Energy (P.E + K.E + ...) of molecules

↳ $\frac{1}{2} \dot{m} v^2 \rightarrow$ K.E of \dot{m}
 \downarrow velocity

↳ $mgz \rightarrow$ P.E of \dot{m} Electric (magnetic attraction or repulsion)

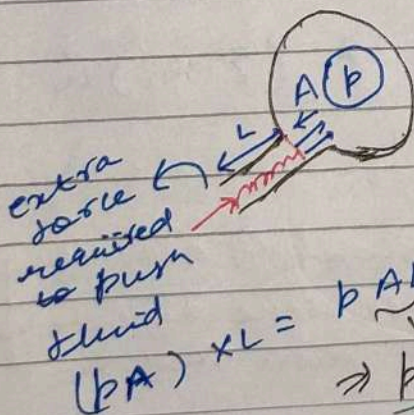
↳ $p v \rightarrow$ flow work $p =$ pressure, $\text{pascal} = \frac{\text{N}}{\text{m}^2}$

$v \rightarrow$ specific volume $= \frac{\text{m}^3}{\text{kg}}$

flow work :- work done to push this gas/liquid inside the open boundary.

*** $\nabla \cdot \mathbf{V} = 0$ FLOT (for open system)

$$\sum_{j=1}^n \dot{m} \left(u + p v + \frac{v^2}{2} + g z \right) + \dot{Q} - \dot{W} = 0$$



↳ flow work ($p v$) and work (\dot{W}) are Independent.

$p v \rightarrow$ unit $\rightarrow \frac{\text{Pa} \cdot \text{m}^3}{\text{kg}}$

$$= \frac{\text{N}}{\text{m}^2} \cdot \frac{\text{m}^3}{\text{kg}}$$

$$= \frac{\text{Nm}}{\text{kg}} = \frac{\text{J}}{\text{kg}}$$

$$(pA) \times L = p A L$$

$$\rightarrow \frac{p v}{2}$$

flow work

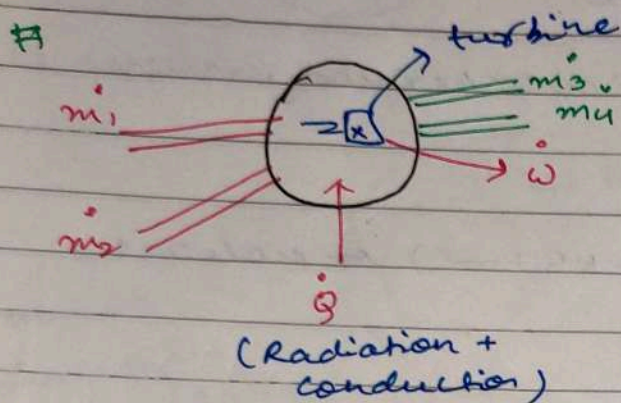
flow work

$$u + pv = H = \text{Enthalpy}$$

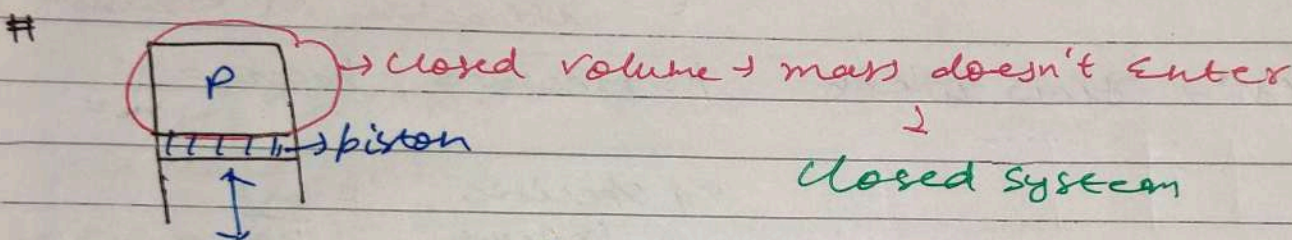
Internal energy

open system! - mass can exchange with surrounding

closed system! - mass can't exchange with surrounding.

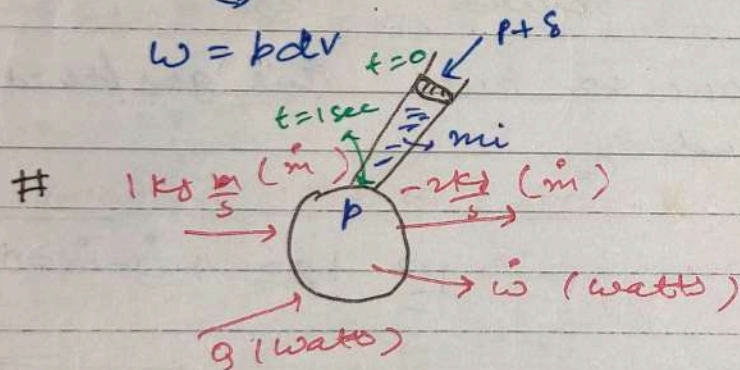


$$\dot{m} \Rightarrow \text{unit} \Rightarrow \frac{\text{kg}}{\text{s}}$$



Closed system

$$W = p dV$$



$$\sum_{i=1}^n \dot{m}_i \left(u + \frac{v^2}{2} + gz \right) + p_i v + \dot{Q} - \dot{W}$$

come to this term later.

$$= (\sum \dot{m}_i) u$$

$$\sum \dot{m}_i = \frac{\partial m}{\partial t} \rightarrow \text{kg/s}$$

physical work done (work done by external to push that gas)

$$\sum \dot{m}_i \left(u + \frac{v^2}{2} + gz \right) + \sum \dot{m}_i p v_i + \dot{Q} - \dot{W}$$

M = total inside the control volume

$$= \frac{\partial (Mu)}{\partial t} = 0$$

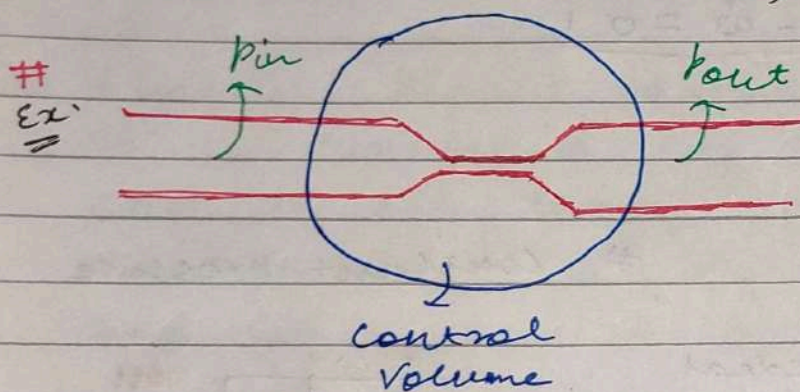
U → Internal Energy of all molecules.

↳ In steady state, $\sum \dot{m}_i = 0$

↳ $H = u + pv = \text{Enthalpy}$

$$\sum \dot{m}_i \left(h_i + \frac{v^2}{2} + gz \right) + \dot{Q} - \dot{W} = 0$$

↳ most valuable equation of first law



$$\dot{m}_{in} \left(h + \frac{v^2}{2} + gz \right)_{in} - \dot{m}_{out} \left(h + \frac{v^2}{2} + gz \right)_{out} + \dot{Q} - \dot{W} = 0$$

↳ $\dot{m}_{in} = \dot{m}_{out}$ (conservation of mass)

↳ $v_{in} \neq v_{out}$ (velocity)

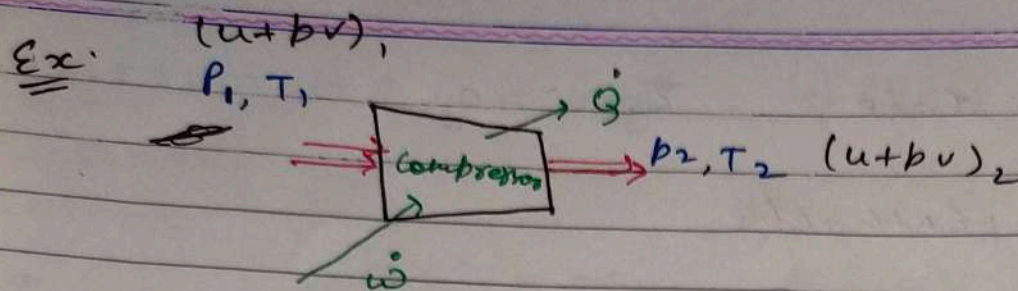
↳ but $h \gg \frac{v^2}{2}$

↳ both are at same level $z_{in} = z_{out}$

$$\dot{m} (h_{in} - h_{out}) + \dot{Q} - \dot{W} = 0$$

||,

$$\dot{m} \Delta h + \dot{Q} - \dot{W} = 0$$



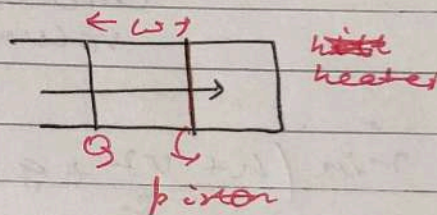
$$\dot{m}h_1 + \dot{W} = \dot{Q} + \dot{m}h_2$$

$$\dot{m}(h_2^* - h_1) + \dot{Q} - \dot{W} = 0$$

Enthalpy (h)

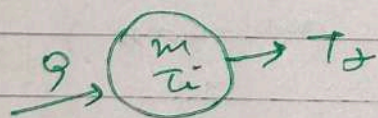
$h = u + pv = \underbrace{u + RT}_{\substack{\text{Valid for} \\ \text{all type} \\ \text{of gases}}}$ $\underbrace{\text{only Ideal gas}}$

Constant pressure



(fluids, Ideal gas, non-ideal gas, liquids, mixture)

Cv
Assuming volume is constant



$$Q = m \cdot C_v (T_+ - T_i)$$

$$C_v = \frac{Q}{m \cdot \Delta T}$$

Cp → Assuming the pressure is constant

$$Q = m C_p (T_+ - T_i)$$

$$C_p = \frac{Q}{m \cdot \Delta T}$$

$Q = m(u_+ - u_i) + p(V_+ - V_i)$
 $= m[(u + pv)_+ - (u + pv)_i]$
 $= m[h_+ - h_i]$

$$= m \Delta h = m C_p \Delta T$$

$$\Delta h = C_p \Delta T$$

$h = u + RT$ (for Ideal gas)

$$\frac{dh}{dT} = \frac{du}{dT} + R$$

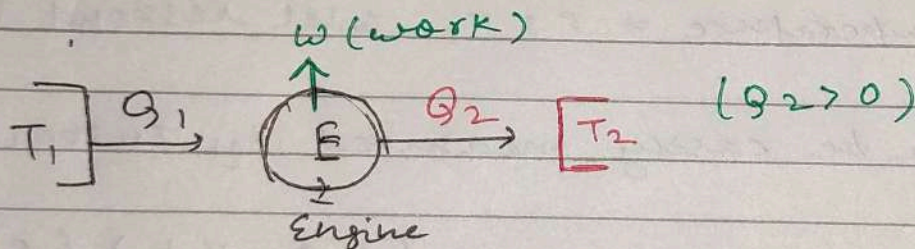
$$C_p = \frac{dh}{dT}, \quad C_v = \frac{du}{dT}$$

↳ $C_p = C_v + R$ $\overset{VVT}{=}$

Second law of thermodynamics (SLOT)

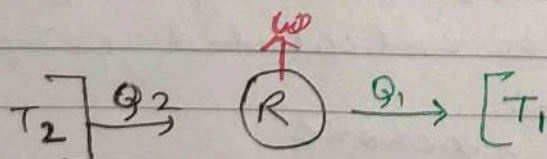
(i) Kelvin - Planck statement

↳ If u running a engine in closed cycle, and u are taking heat from higher temperature T_1 and amount of Q_1 and you expect to get work out from engine, atmospheric T_2 and amount of Q_2 should be positive ($Q_2 > 0$).



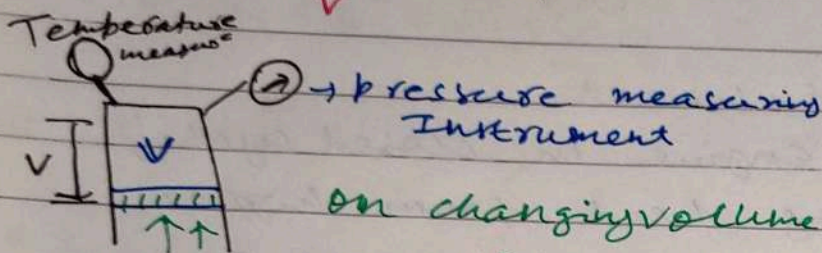
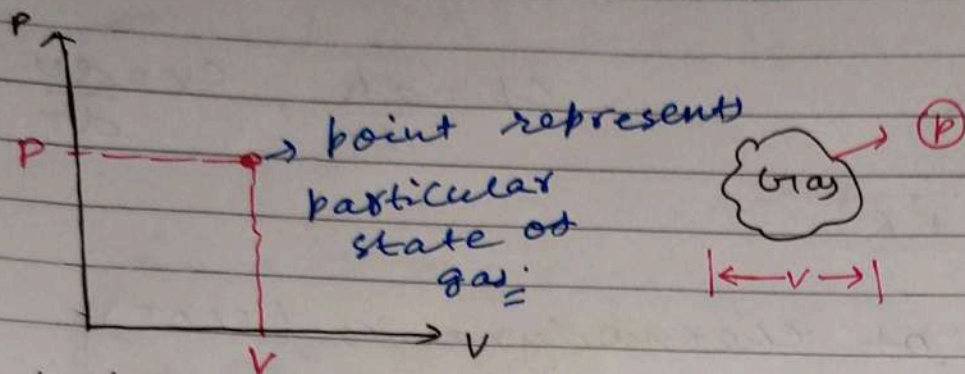
↳ 100% of heat is not converted into work. Some amount of heat is lost in atmosphere.

(ii) Clausius statement



↳ 100% of heat is not converted into heat. (from T_2 to T_1). Some amount of work done should be there.

Carnot, Sadi



on changing volume, we get different value of pressure.

~~Temperature~~

- (i) change volume \Rightarrow P & T will respond
- (ii) change temperature \Rightarrow P & V will respond

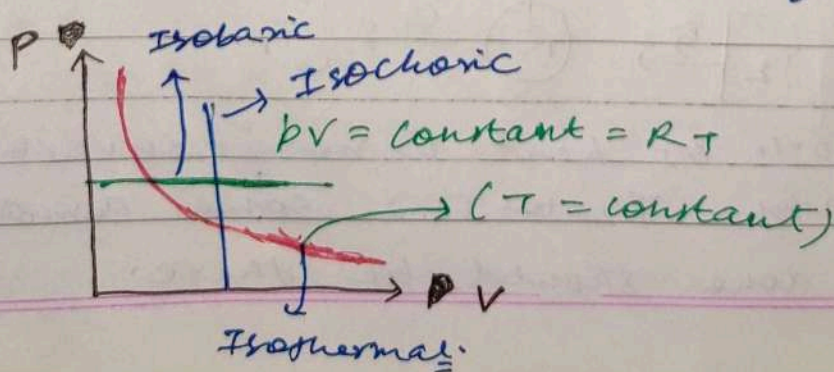
\hookrightarrow P, V, T \rightarrow can be easily measured by instruments

- # Isothermal $\Rightarrow T = \text{constant}$ ($P \uparrow, V \downarrow$) ($P \downarrow, V \uparrow$)
- # Isochoric $\Rightarrow V = \text{constant}$ ($P \uparrow, T \uparrow$) ($P \downarrow, T \downarrow$)
- # Isobaric $\Rightarrow P = \text{constant}$ ($V \uparrow, T \uparrow$) ($V \downarrow, T \downarrow$)

Ex: If P, V are given, then $T = ?$ (Ideal gas)
 $T = \frac{PV}{nR}$ \Rightarrow H, W, Q \Rightarrow many things can be calculated using

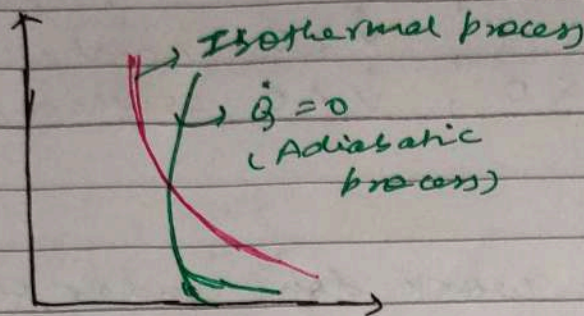
$T = \text{constant}$

- (PV) curve is hyperbola



Adiabatic process $\Rightarrow Q = \text{constant}$

$(p v^{\gamma} = \text{constant})$



$$\gamma = \frac{C_p}{C_v}$$

$\gamma > 1$

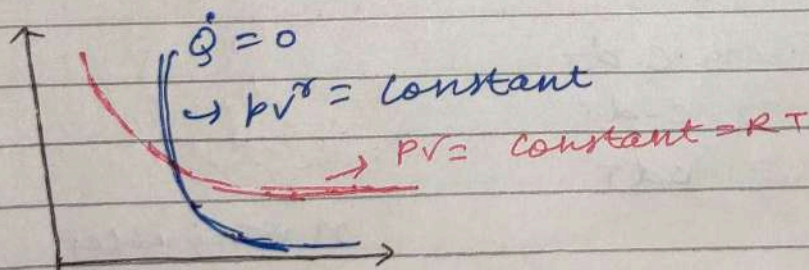
$\Delta T / V = \text{constant} \Rightarrow \frac{Q}{C_v \cdot m}$

old	T	p	V
new	γT	$\gamma^{\gamma} p$	$\frac{V}{\gamma}$
$(Q=0)$			

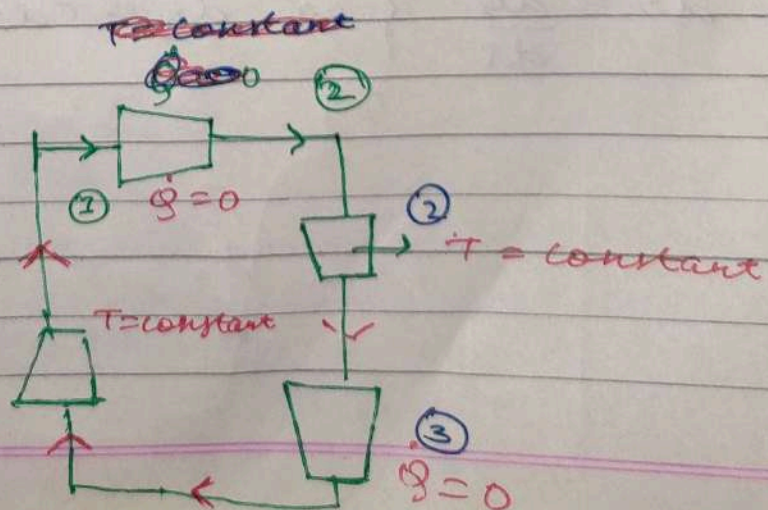
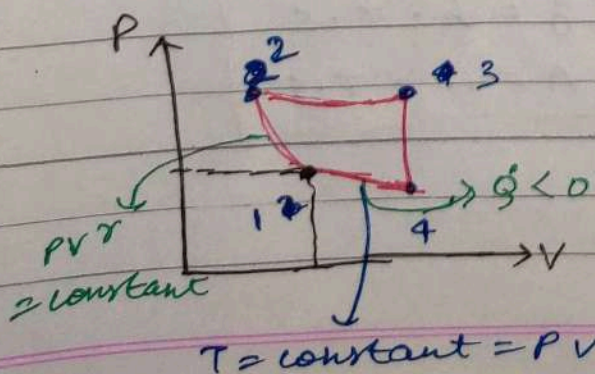
$C_p - C_v = R$

$\Rightarrow \gamma - 1 = \frac{R}{C_v} \Rightarrow \gamma = 1 + \left(\frac{R}{C_v}\right) \Rightarrow \text{positive} \Rightarrow \gamma > 1$

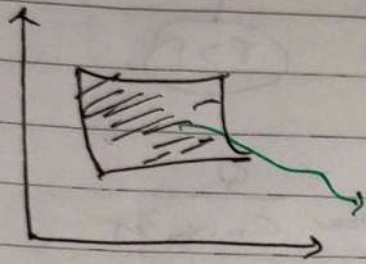
$C_v = \frac{R}{\gamma - 1} \quad C_p = \frac{\gamma R}{\gamma - 1}$



Carnot cycle



1-2	, $\dot{Q}=0$, $\dot{W}<0$, $\dot{V}<0$	Adiabatic
2-3	, $\dot{Q}>0$, $\dot{W}>0$, $\dot{V}>0$	Isothermal
3-4	, $\dot{Q}=0$, $\dot{W}>0$, $\dot{V}>0$	Adiabatic
4-1	, $\dot{Q}<0$, $\dot{W}<0$, $\dot{V}<0$	Isothermal



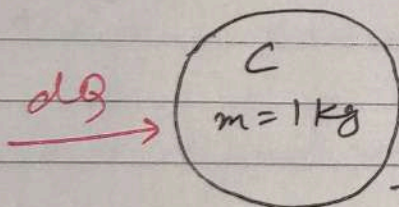
\dot{W}_{total} = work done under the p-v curve

Area = net work output

$$\eta_{carnot} = 1 - \frac{T_L}{T_H}$$

Entropy (S): -

$$dQ = c dT$$

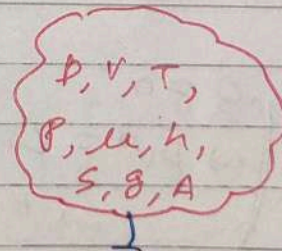


$$T \rightarrow T + dt$$

$$dQ = m \cdot c dT$$

$$= 1 \cdot c \cdot dT$$

$$= c dT$$



n variables

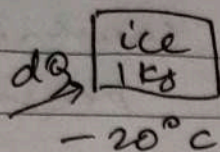
\downarrow
n-2 eqns

$$ds = \frac{dQ}{dT} \quad \} \quad \text{or} \quad dQ = T ds$$

$$g = h \cdot T \cdot s$$

$$A = u \cdot T \cdot s$$

Ex:



$$dQ = mc dT$$

$$dQ = T ds$$

$$c dT = T ds$$

$$ds = \int \frac{c dT}{T}$$

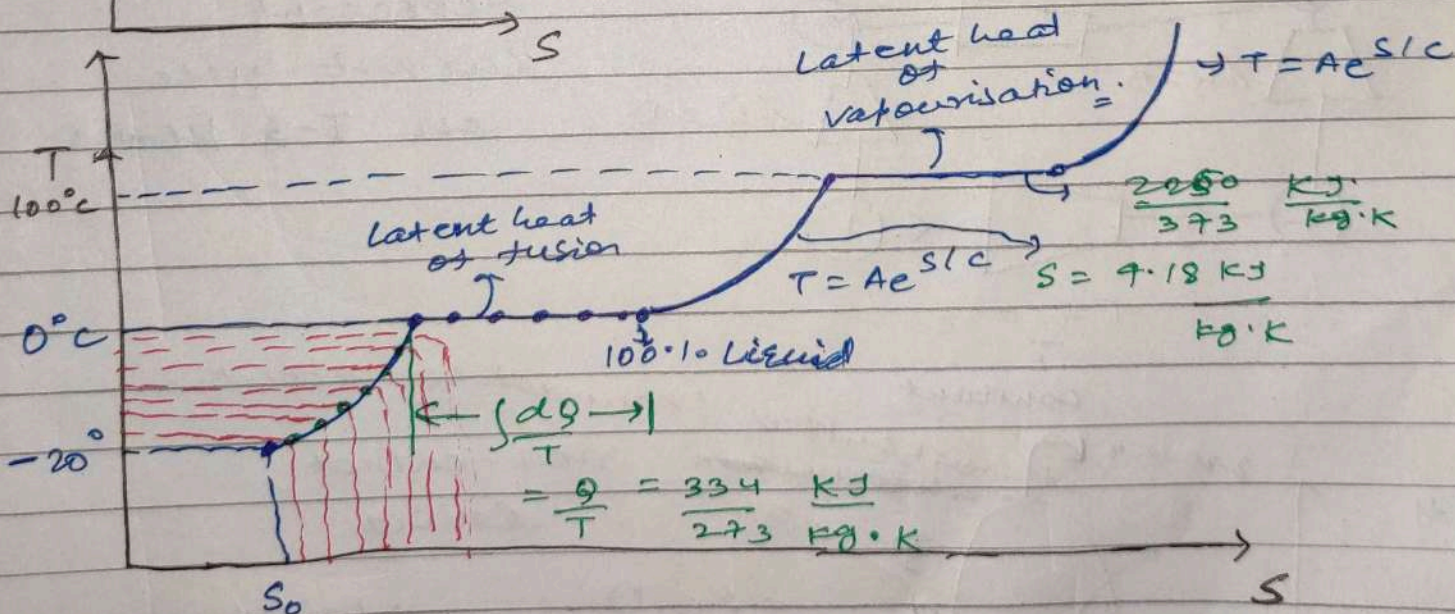
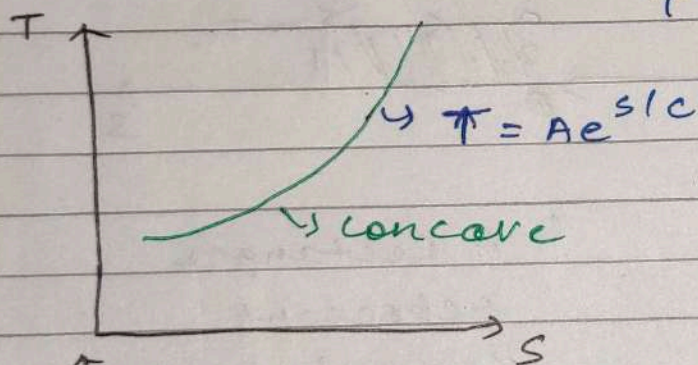
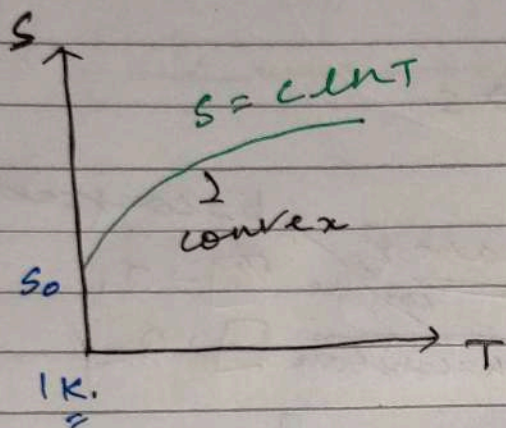
$$S = c \cdot \ln T + S_0$$

$$S - S_0 = c \cdot \ln T$$

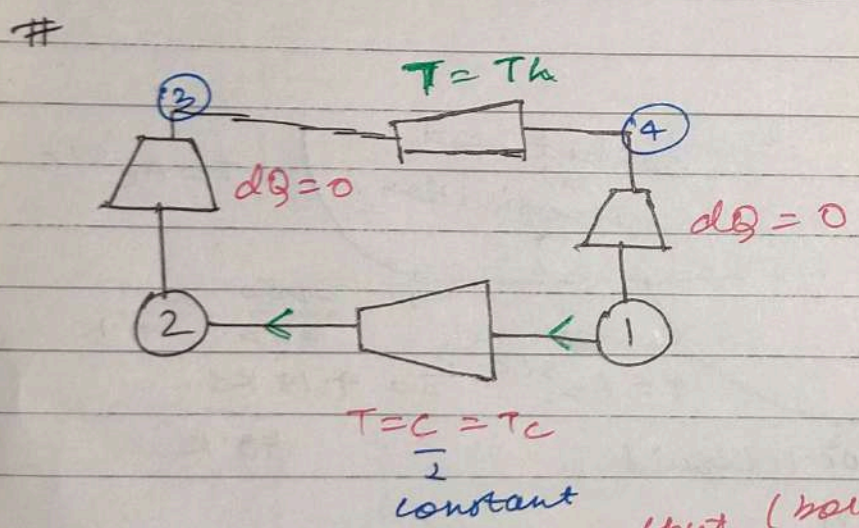
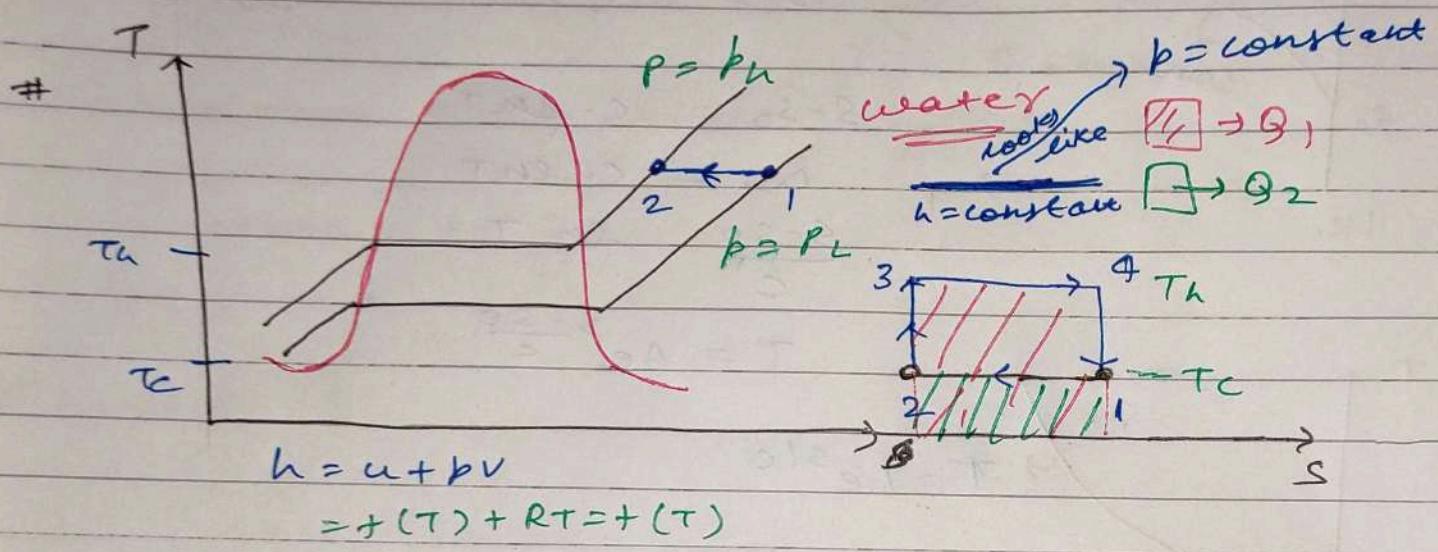
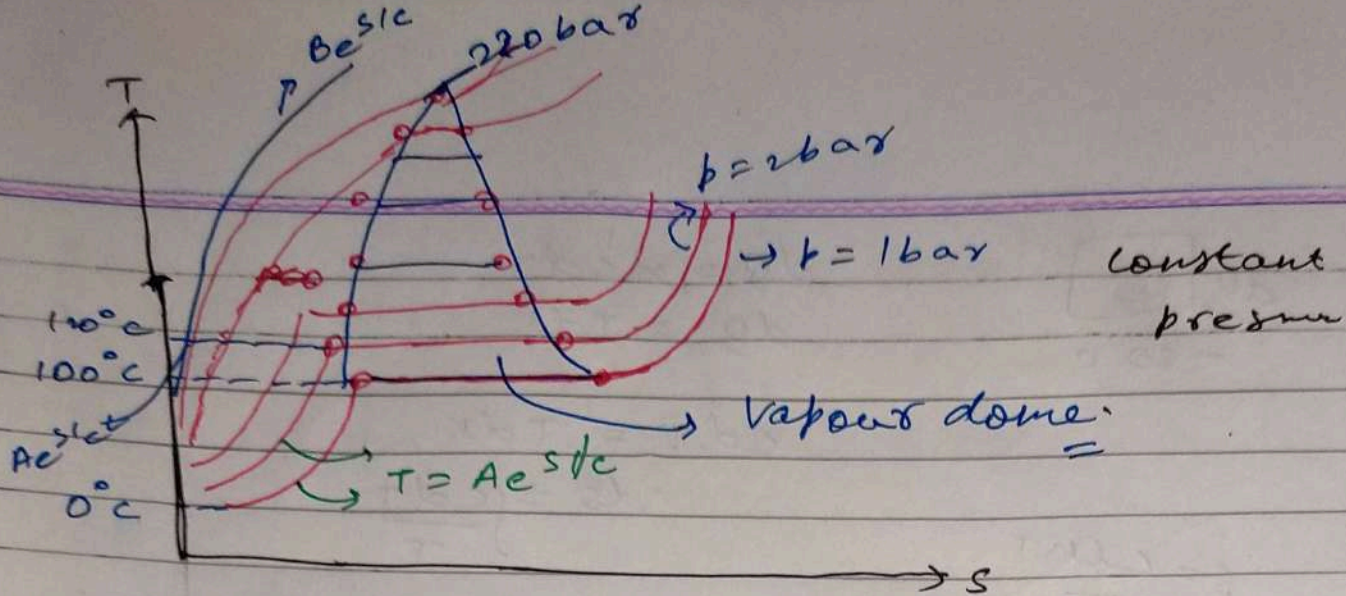
$$\Delta S = c \cdot \ln T$$

$$\frac{S - S_0}{c} = \ln T$$

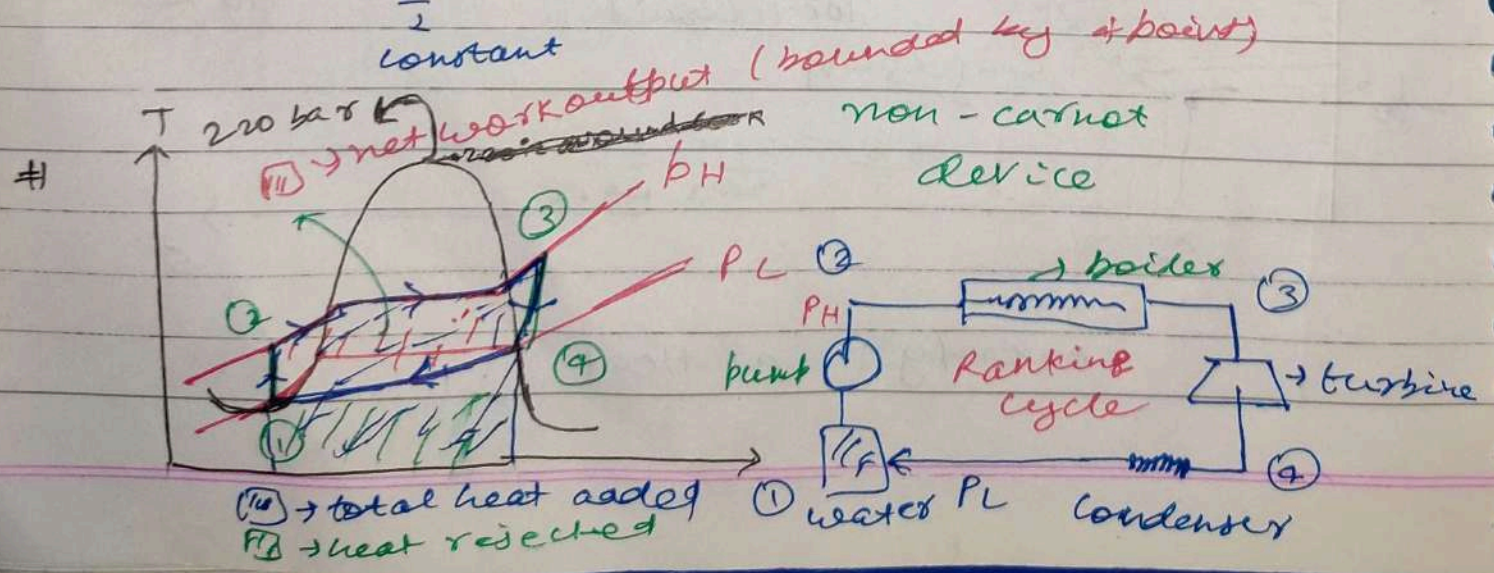
$$T = A e^{\frac{S - S_0}{c}}$$



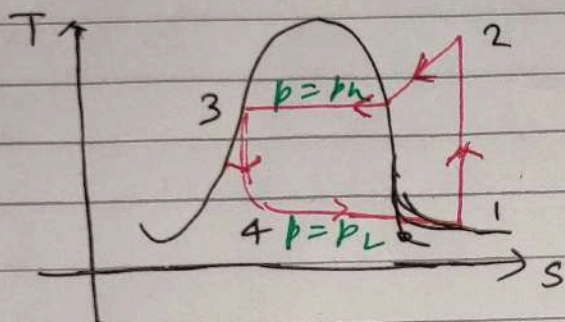
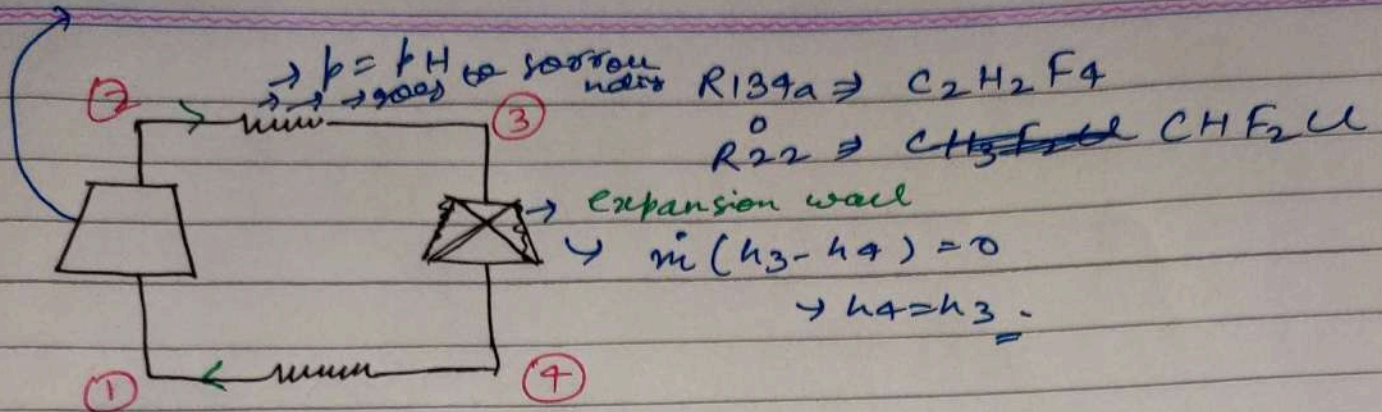
entropy T , as Heat T .

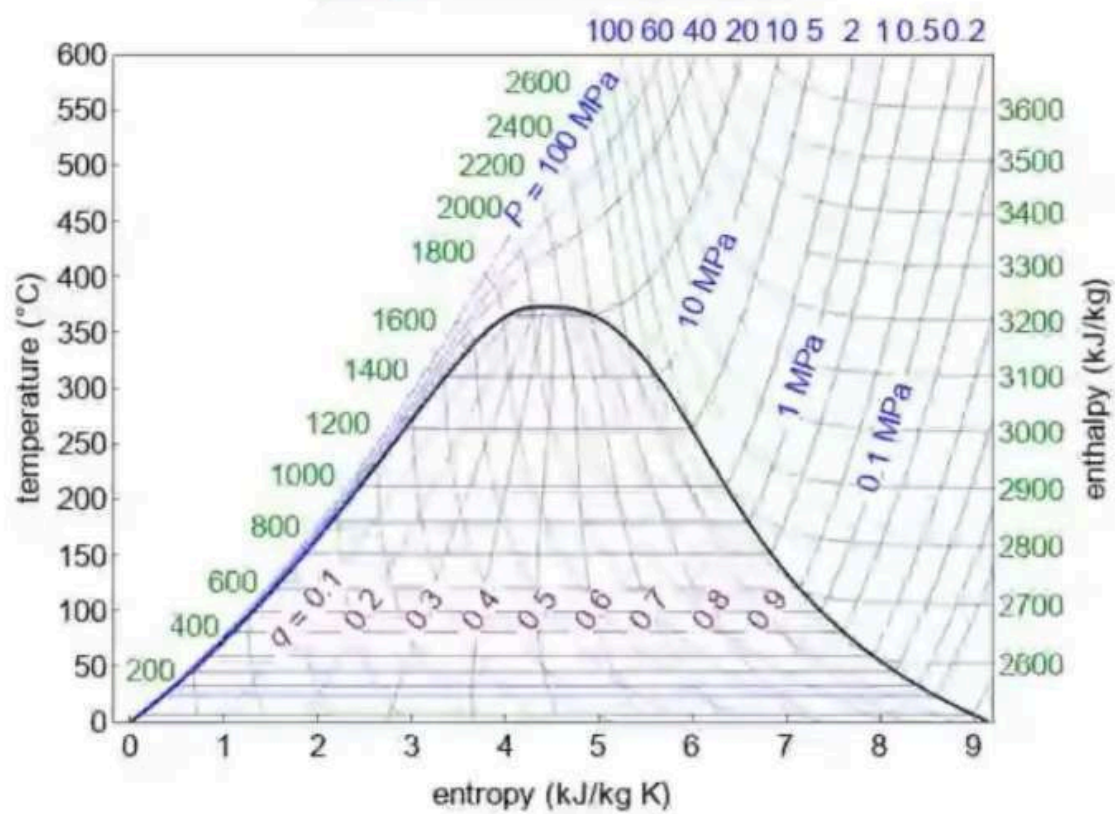


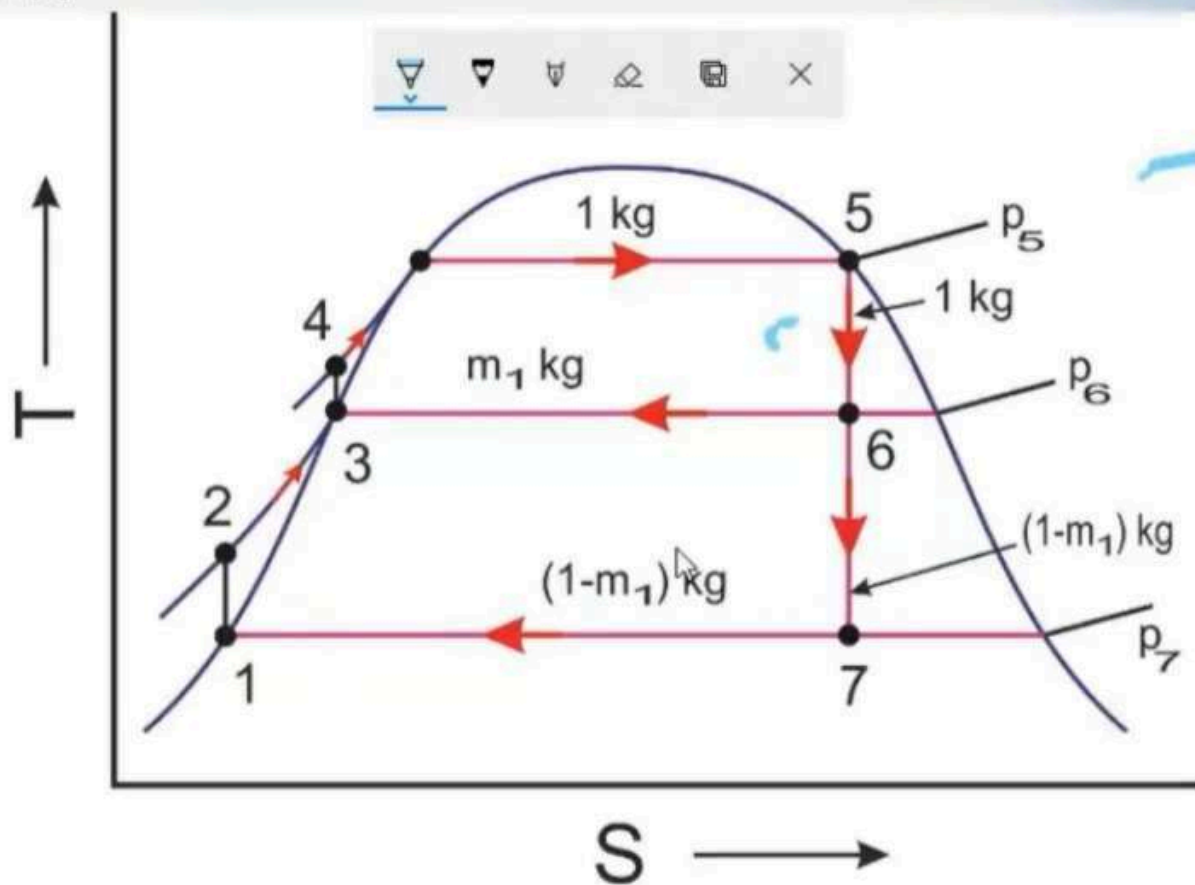
A Rectangle represent Carnot cycle on T-s plane



Adiabatic compressor ($s = \text{constant}$)







R134a

