

# Remote Examination 2021-22

## PH100: Mechanics and Thermodynamics

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Marks: 20

Time: 40 Minutes

- All questions are compulsory and their marks is indicated in square bracket.
- All questions needs to be answered sequentially without fail. Non-compliance of instruction will invite deduction in marks.
- In case you feel any question/s is/are incorrect or have insufficient instruction then write in the answer book with your justification without wasting any time
- Except question number 8, all other questions are of 2 marks.

- ✖ 1. Two non-interacting particles  $m_1$  and  $m_2$  move toward each other with velocities  $v_1$  and  $v_2$ . Their paths are offset by distance  $b$ , ~~as shown in the sketch~~. Let us investigate the equivalent one body description of this system.
- ✓ 2. Compare the spectral energy density curve w.r.t frequency using Rayleigh Jean and Planck's radiation laws.
- ✓ 3. Write down two phenomenon's which shows the particle properties of waves and wave properties of particle.
- ? 4. How many photons/s are contained in a beam of electromagnetic radiation of total power 180 W if the source is (a) an AM radio station of 1100 kHz, (b) 8.0-nm x rays, and (c) 4.0-MeV gamma rays?
- ✓ 5. A proton in a one-dimensional box has an energy of 400 keV in its first excited state. How wide is the box?
- ✓ 6. What do you understand from thermal equilibrium?
- ? 7. Write down the time-dependent and independent forms of Schrodinger's equation.
- ? 8. A particle is in a cubic box with infinitely hard walls whose edges are  $L$  long. The wave functions of the particle are given by

$$\psi = A \sin \frac{n_x \pi x}{L} \sin \frac{n_y \pi y}{L} \sin \frac{n_z \pi z}{L}$$

$$\begin{aligned} n_x &= 1, 2, 3, \dots \\ n_y &= 1, 2, 3, \dots \\ n_z &= 1, 2, 3, \dots \end{aligned}$$

Find the value of the normalization constant  $A$ . Find the possible energies of the particle in the box by substituting above wave function in 3D Schrödinger's equation and solving for  $E$ . Compare the ground-state energy of a particle in a one-dimensional box of length  $L$  with that of a particle in the three-dimensional box. [4 Marks]

✓ 9.

The equation of state of an ideal gas is  $PV = nRT$ , where  $n$  and  $R$  are constants.

- Show that the volume expansivity  $\beta$  is equal to  $1/T$ .
- Show that the isothermal compressibility  $\kappa$  is equal to  $1/P$ .

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