

$$\vec{M} = \vec{m} / V$$

Magnetostatics

Magnetization Eqn of Continuity.

$$\vec{J}_b = \vec{\nabla} \times \vec{M}$$

$$\vec{K}_b = \vec{M} \times \hat{n}$$

$$\boxed{\nabla \cdot \vec{J} + \frac{\partial P}{\partial t} = 0}$$

$$\nabla \cdot \vec{B} = 0$$

$$\oint \vec{B} \cdot d\vec{l} = M_0 I$$

$$\nabla \times \vec{B} = M_0 \vec{J}$$

Electrostatics

$$\nabla \cdot E = P / \epsilon_0$$

$$\nabla \times E = 0$$

$$\boxed{I = \vec{P} \times \vec{E}}$$

$$\vec{D} = \epsilon \vec{E} + \vec{P}$$

$$\vec{\nabla} \cdot \vec{D} = P_{\text{free}}$$

$$\sigma_b = \vec{P} \cdot \hat{n}$$

$$P_b = - \nabla \cdot \vec{P}$$

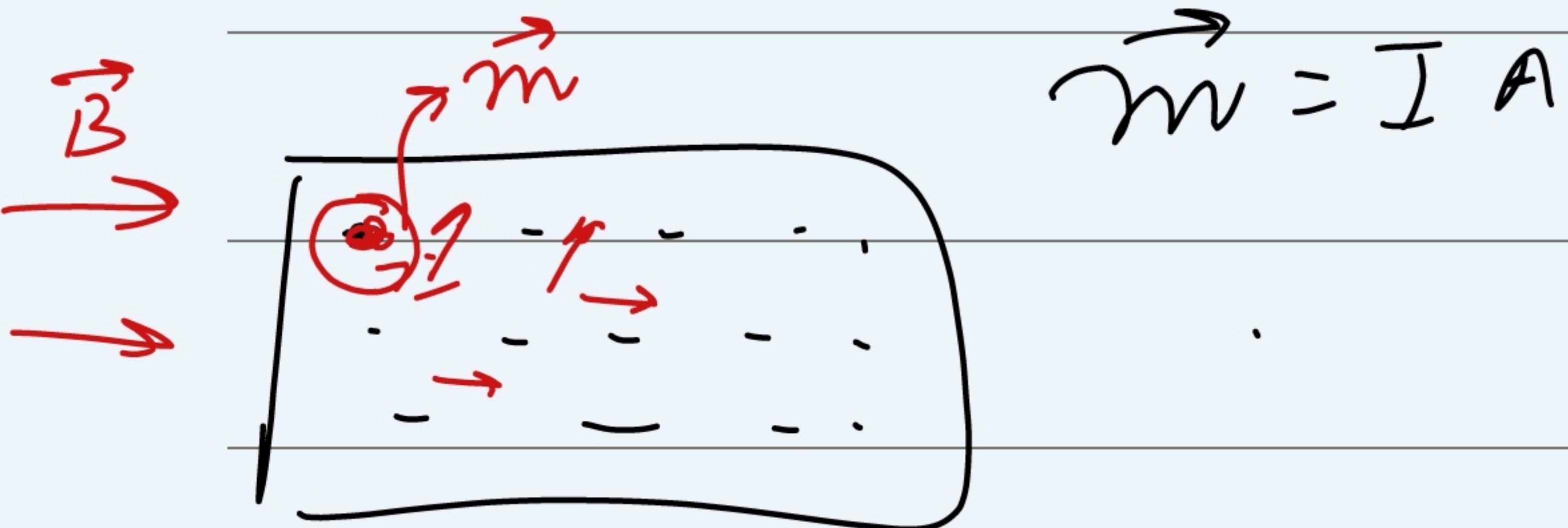
$$\vec{P} = \frac{\vec{P}}{r}$$

Matter

Magnetostatics in Matter



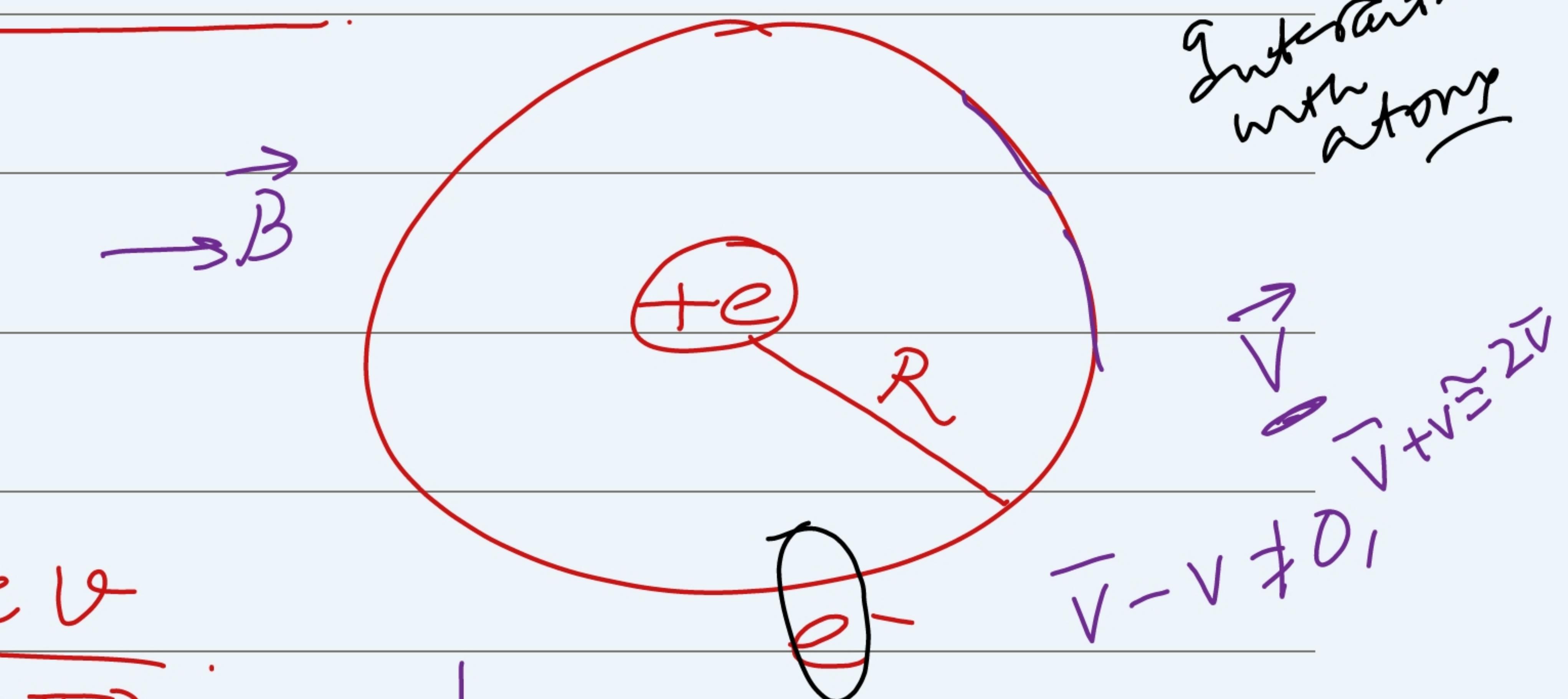
$$\text{Red circled } T = \vec{m} \times \vec{B}$$



Effect of Magnetic field on Atomic Orbits

R = circular
interaction
with atoms

$$T = \frac{2\pi R}{v} \Rightarrow v = \frac{2\pi R}{T}$$



$$\vec{m} = IA$$

$$= (-) \frac{ev}{2\pi R} \pi R^2$$

$$I = -\frac{e}{T} = -\frac{ev}{2\pi R}$$

$$\vec{m} = -\frac{1}{2} evR \hat{\zeta}$$

$$\Delta m = -\frac{1}{2} e (\Delta v) R \propto -B$$

$$\vec{B} = 0,$$

$$-\frac{1}{4\pi\epsilon_0} \cdot \frac{e^2}{R^2} = \frac{m v^2}{R}$$

$$\vec{B} \neq 0$$

$$-\frac{1}{4\pi\epsilon_0} \cdot \frac{e^3}{R^2} + qvB = \frac{mv^2}{R}$$

$$qvB = \frac{m}{R} (\bar{v}^2 - v^2)$$

$$= \frac{m}{R} (\bar{v} - v)(\bar{v} + v)$$

$$qvB = \frac{m}{R} (\Delta v) 2\bar{v}$$

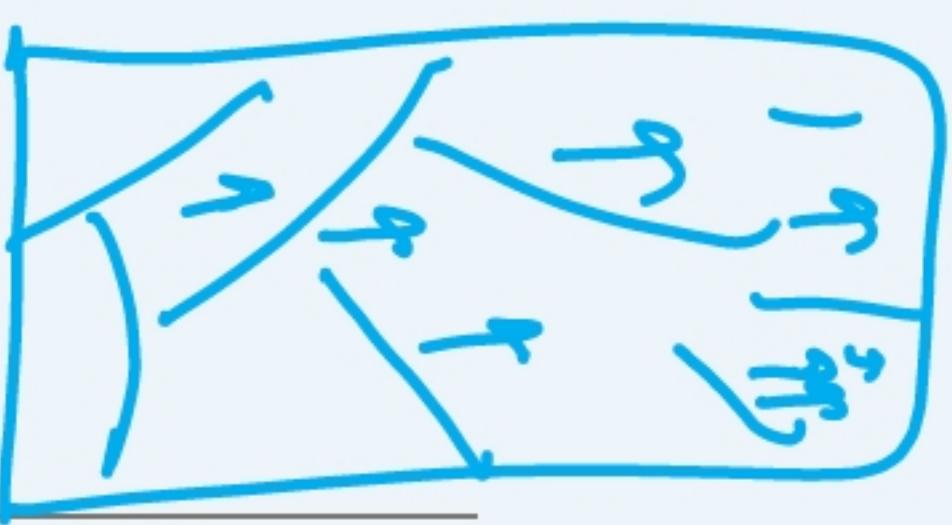
$$\Delta v = \frac{qR}{2m} B$$

$$\nabla \times \vec{B} = \mu_0 \vec{J}$$

$$\begin{aligned} \vec{J} &= \vec{J}_f + \vec{J}_M \\ &= \vec{J}_f + \nabla \times \vec{M}, \end{aligned}$$

\vec{J}_f = free current density

Ferromagnetic M



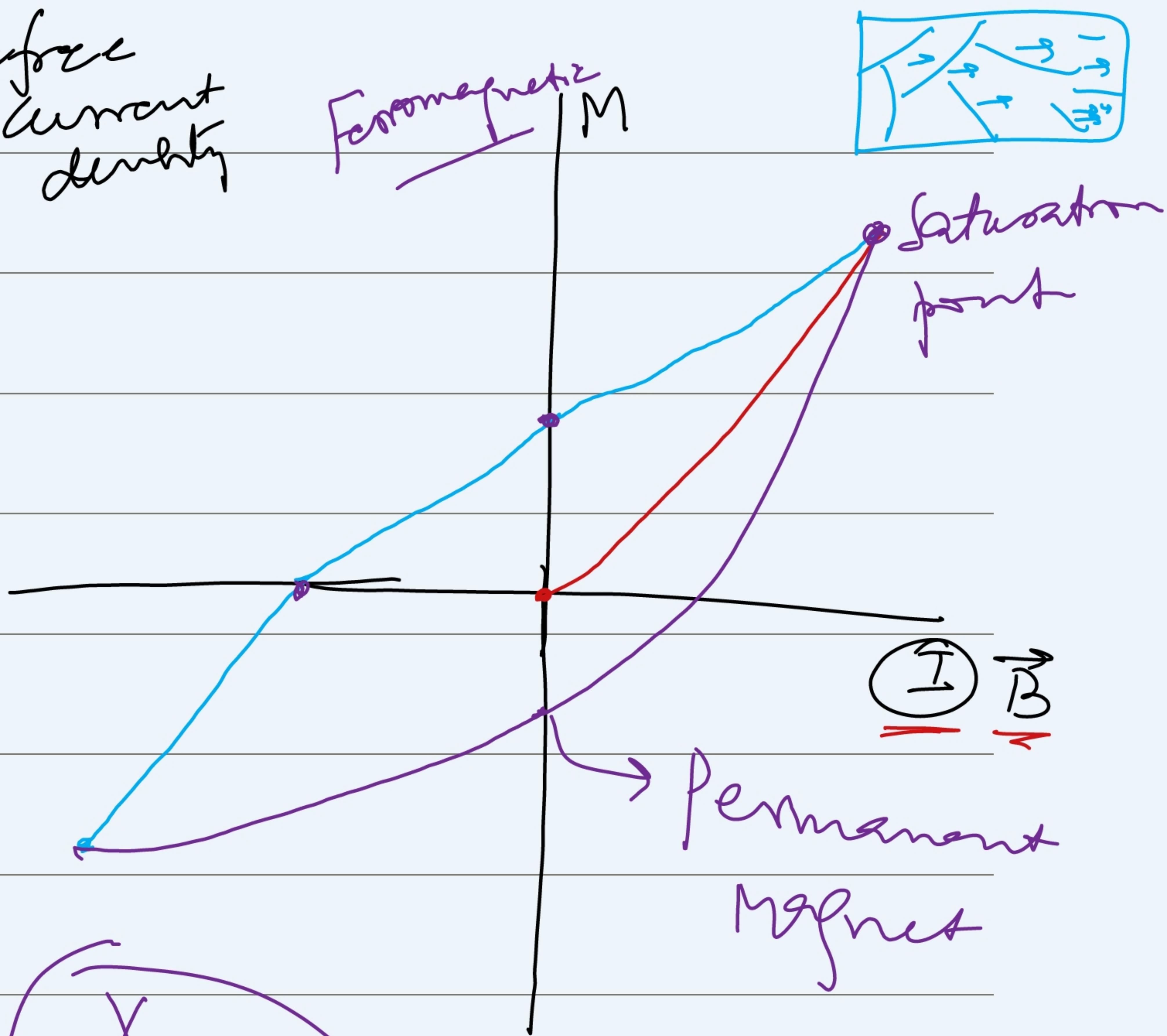
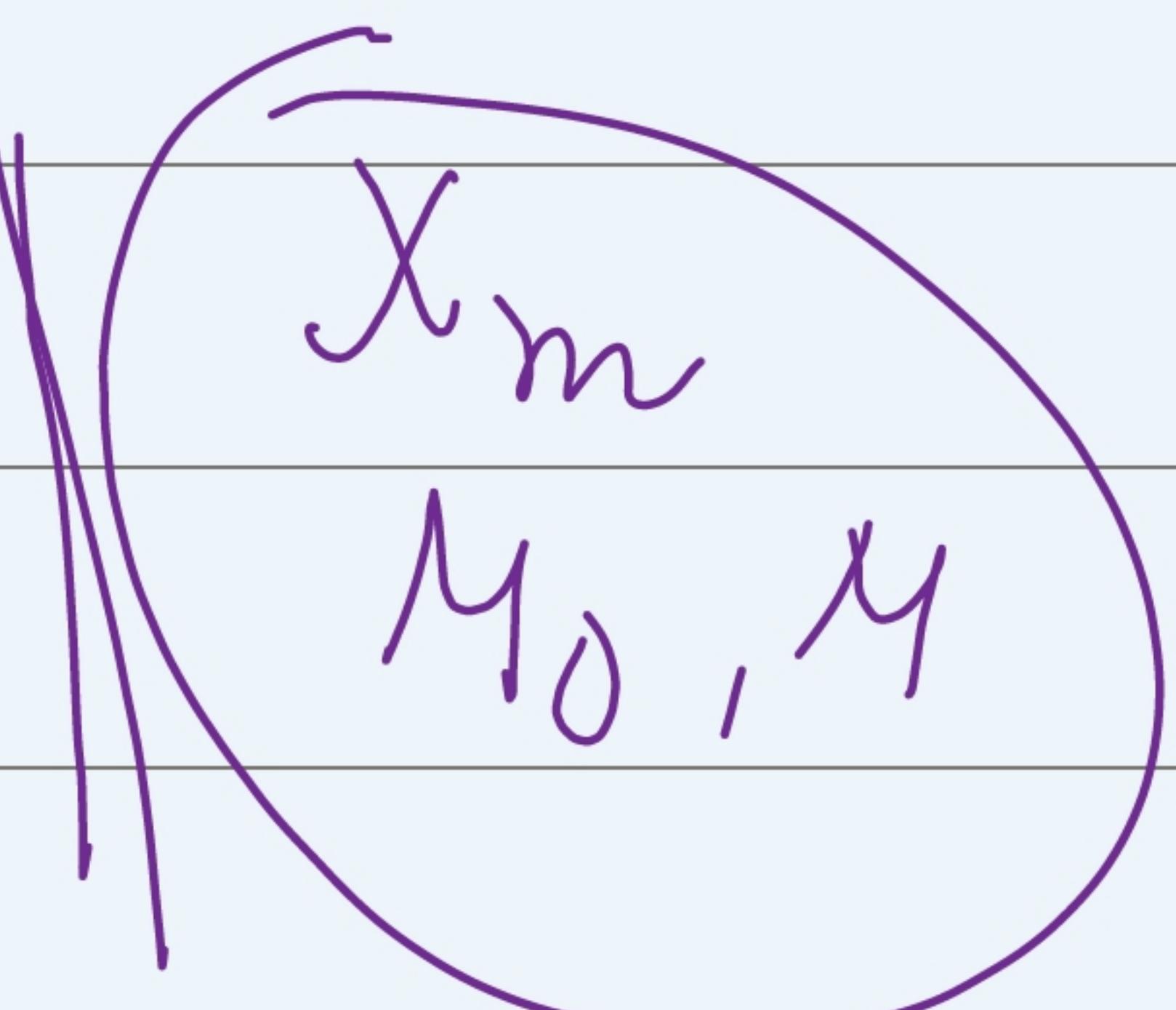
$$\frac{1}{\mu_0} [\nabla \times \vec{B}] = \vec{J}_f + \nabla \times \vec{M}$$

$$\nabla \times \left[\frac{\vec{B}}{\mu_0} - \vec{M} \right] = \vec{J}_f. \quad \vec{H} = \frac{\vec{B}}{\mu_0} - \vec{M}$$

$$\boxed{\nabla \times \vec{H} = \vec{J}_f}$$

$$\boxed{\nabla \cdot \vec{H} = -\nabla \cdot \vec{M}}$$

$$\boxed{\oint \vec{H} \cdot d\vec{l} = I_f}$$



Linear Media $\rightarrow \vec{P} \propto \epsilon_0 \chi_0 \vec{E}$

$$\vec{M} = \chi_m \vec{H}$$

$$\vec{H} = \frac{\vec{B}}{\mu_0} - \vec{M}$$

$$\vec{B} = \mu_0 [\vec{H} + \vec{M}]$$

$$\vec{B} = \mu_0 [1 + \chi_m] \vec{H}$$

$$\boxed{\vec{B} = \mu \vec{H}}$$

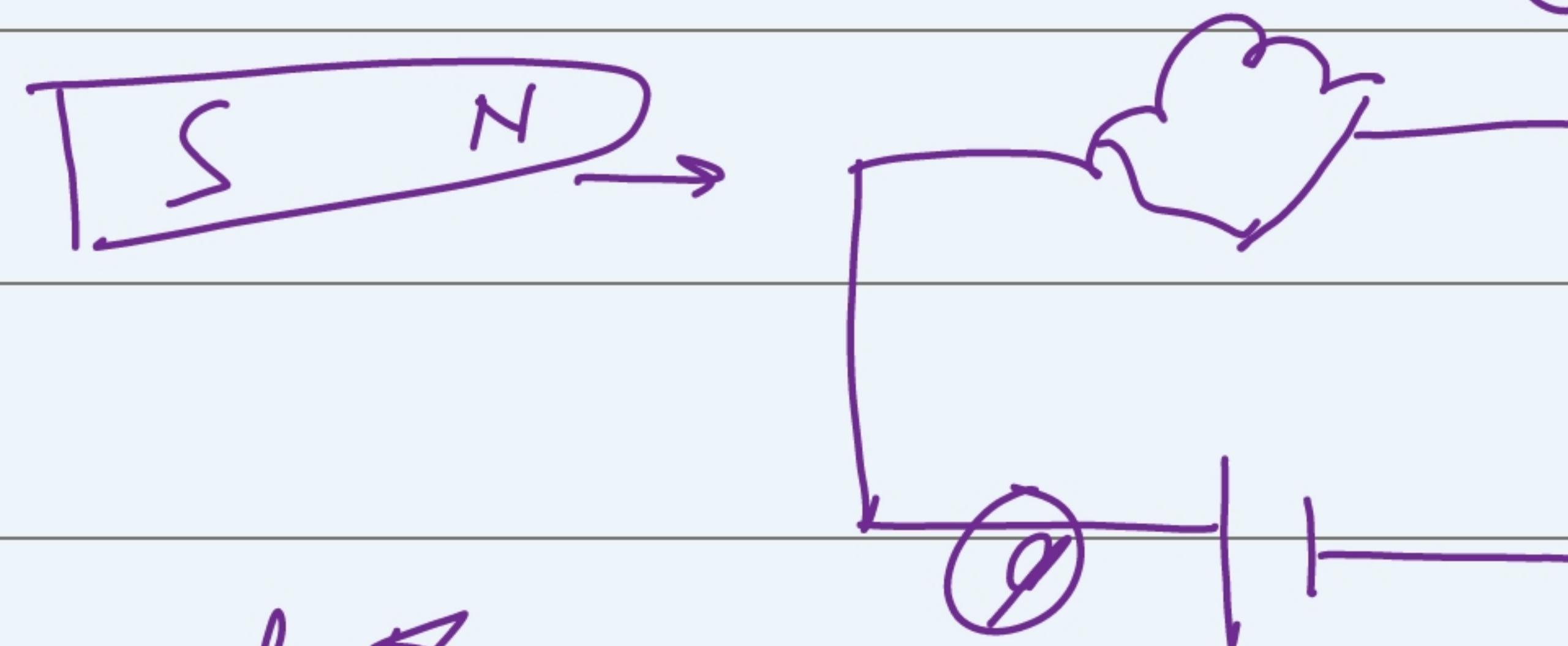
$$\mu = \mu_0 [1 + \chi_m]$$

Electrodynamics \rightarrow

Faraday Law \rightarrow

change flux & ind
emf
(of position
x time).

$$\left\{ \text{EMF} = -\frac{d\phi}{dt} \right. \quad \vec{\phi}_B = \vec{B} \cdot \vec{A}$$



$$\mathcal{E} = \oint \vec{E} \cdot d\vec{l} = - \frac{d\phi_B}{dt} = - \frac{d}{dt} \int \vec{B} \cdot d\vec{A}$$

$$\Rightarrow \boxed{\nabla \times \vec{E} = - \frac{\partial \vec{B}}{\partial t}}$$

$$- \quad \iint (\nabla \times \vec{E}) \cdot d\vec{a}$$

Changing \vec{B} will generate
 \vec{E} .

$$\Phi_2 = \int \vec{B}_1 \cdot d\vec{a}_2 = M_{21} I_1$$

$$= \int (\nabla \times \vec{A}_1) \cdot d\vec{a}_2$$

$$\Rightarrow \oint \vec{A}_1 \cdot d\vec{l}_2 = M_{21} I_1$$

$$M_{21} = \frac{\mu_0 I_1}{4\pi} \oint \left[\frac{d\vec{l}_1}{r} \right] \cdot d\vec{l}_2 = M_{21} I_1$$

$$\Phi = L I$$

$$\Sigma = -L \frac{dI}{dt}$$

Mutual Inductance

Selko

Maxwell's Eqn

$$\vec{D}$$

$$\partial \vec{E}$$

$$\frac{\partial}{\partial t}$$