

Interquartile Range (IQR) Calculation and Outlier Detection

Day Data

- **Minimum:** 32
- **Q1:** 56
- **Median:** 74.5
- **Q3:** 82.5
- **Maximum:** 99

Night Data

- **Minimum:** 25.5
- **Q1:** 78
- **Median:** 81
- **Q3:** 89
- **Maximum:** 98

Step 1: Calculate IQR for Day and Night

Day IQR

$$\text{IQR}_{\text{Day}} = \text{Q3}_{\text{Day}} - \text{Q1}_{\text{Day}} \quad \text{IQR}_{\text{Day}} = 82.5 - 56 = 26.5$$

Night IQR

$$\text{IQR}_{\text{Night}} = \text{Q3}_{\text{Night}} - \text{Q1}_{\text{Night}} \quad \text{IQR}_{\text{Night}} = 89 - 78 = 11$$

Step 2: Compare the IQRs

- The IQR for the Day data is 26.5
- The IQR for the Night data is 11

Comparison:

- The IQR for Day data (26.5) is significantly larger than the IQR for Night data (11). This indicates that the daytime temperatures have a wider spread or more variability compared to the nighttime temperatures.

Step 3: Identify Outliers

Day Outliers

$$\text{Using the } 1.5 * \text{IQR rule: Lower Bound}_{\text{Day}} = \text{Q1}_{\text{Day}} - 1.5 * \text{IQR}_{\text{Day}} \quad \text{Lower Bound}_{\text{Day}} = 56 - 1.5 * 26.5 = 56 - 39.75 = 16.25$$

$$\text{Upper Bound}_{\text{Day}} = \text{Q3}_{\text{Day}} + 1.5 * \text{IQR}_{\text{Day}} \quad \text{Upper Bound}_{\text{Day}} = 82.5 + 1.5 * 26.5 = 82.5 + 39.75 = 122.25$$

Outliers in Day Data:

- Any data points below 16.25 or above 122.25 are considered outliers.
- Given the range of the data (32 to 99), there are no outliers in the Day data.

Night Outliers

Using the 1.5 * IQR rule: Lower Bound_Night = $Q1_Night - 1.5 * IQR_Night$
Lower Bound_Night = $78 - 1.5 * 11 = 78 - 16.5 = 61.5$

Upper Bound_Night = $Q3_Night + 1.5 * IQR_Night$
Upper Bound_Night = $89 + 1.5 * 11 = 89 + 16.5 = 105.5$

Outliers in Night Data:

- Any data points below 61.5 or above 105.5 are considered outliers.
- Given the range of the data (25.5 to 98), the data point 25.5 is an outlier in the Night data.

Summary

- **Day Data:**
 - **IQR:** 26.5
 - **Outliers:** None
- **Night Data:**
 - **IQR:** 11
 - **Outliers:** 25.5

Conclusion: The daytime temperatures have greater variability compared to nighttime temperatures. There are no outliers in the Day data, while the Night data has one outlier (25.5).