Applied Microeconometrics - Assignment 2

Walter Verwer (589962) & Bas Machielsen (590049)

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1. Compute the average probability to receive benefits 10 and 30 weeks after application for applicants that had a search period and applicants that did not have a search period.

```
dataset %>%
  group_by(searchperiod) %>%
  summarize(prob_10weeks = mean(benefits_week10), prob_30weeks = mean(benefits_week30)) %>%
  knitr::kable()
```

searchperiod	prob_10weeks	prob_30weeks
0	0.7359116	0.5403315
1	0.5723684	0.4144737

It seems that there is a large difference in unconditional means in the outcome variable among treated and controlled groups. Individuals exposed to the treatment (a search period) have much lower probabilities of ultimately receiving benefits, whether this is after 10 weeks, or after 30 weeks. This could be a potential indication of the presence of a treatment effect, but a more rigorous examination should ensue.

2. Make a balancing table in which you compare characteristics of applicants with and without a search period.

	With Search (N=760)		Without Search (N=905)			
	Mean	Std. Dev.	Mean	Std. Dev.	Diff. in Means	p
sumincome12monthsbefore	1.259	1.099	1.296	1.052	0.037	0.485
sumincome 24 months before	2.689	2.125	2.785	2.054	0.096	0.352
age	37.259	8.657	39.926	9.031	2.667	0.000
female	0.372	0.484	0.397	0.490	0.025	0.301
children	0.114	0.319	0.164	0.370	0.049	0.004
partner	0.107	0.309	0.126	0.332	0.019	0.218
period1	0.222	0.416	0.264	0.441	0.042	0.048
period2	0.233	0.423	0.256	0.437	0.023	0.267
period3	0.286	0.452	0.265	0.442	-0.020	0.356
period4	0.259	0.438	0.214	0.411	-0.045	0.033
location1	0.113	0.317	0.177	0.382	0.064	0.000
location2	0.232	0.422	0.182	0.386	-0.049	0.014
location3	0.300	0.459	0.373	0.484	0.073	0.002
location4	0.222	0.416	0.101	0.301	-0.122	0.000
location5	0.133	0.340	0.167	0.373	0.034	0.052
educbachelormaster	0.267	0.443	0.264	0.441	-0.003	0.890
educprepvocational	0.200	0.400	0.218	0.413	0.018	0.376
educprimaryorless	0.149	0.356	0.130	0.337	-0.018	0.285
educunknown	0.050	0.218	0.014	0.119	-0.036	0.000
educvocational	0.334	0.472	0.373	0.484	0.039	0.095

It seems that all covariates are rather balanced, indicated by the absence of significant differences in means among the treated and the control group. Of course, because we are dealing with a large number of joint null-hypotheses, we should only reject the null hypothesis according to a Bonferroni-corrected p-value. If our regular p-value criterion would be p < 0.05, in this case, we reject the null hypothesis when $p < \frac{0.05}{20} = 0.0025$. Even with this criterion, most of the location dummies are still significantly different in treatment and control groups, indicating that perhaps the treatment was administered in different regions, but was stratified according to all other observables. Adding region-specific fixed effects to the regression specifications should solve this problem. Another variable that differs significantly is age. We observe that older individuals are assigned to the no search group more often than younger individuals.

3. Regress the outcome variables first only on whether or not a search period was applied (which should give the difference-in-means estimate) and next include other covariates in the regression.

```
model1 <- lm(data = dataset, formula = benefits_week10 ~ searchperiod)</pre>
model2 <- lm(data = dataset, formula = benefits_week30 ~ searchperiod)</pre>
model3 <- update(model1, . ~ . + period1 + period2 + period3 + period4 +</pre>
                      location1 + location2 + location3 + location4)
model4 <- update(model2, . ~ . + period1 + period2 + period3 + period4 +</pre>
                      location1 + location2 + location3 + location4)
model5 <- update(model3, . ~ . + sumincome_12monthsbefore +</pre>
                      sumincome_24monthsbefore + age + female + children +
                     partner + educ_bachelormaster + educ_prepvocational +
                      educ_primaryorless + educ_unknown + educ_vocational)
model6 <- update(model4, . ~ . + sumincome_12monthsbefore +</pre>
                      sumincome_24monthsbefore + age + female + children +
                      partner + educ_bachelormaster + educ_prepvocational +
                      educ_primaryorless + educ_unknown + educ_vocational)
models <- list(model1, model2, model3, model4, model5, model6)</pre>
stargazer(models, title = "Estimations of the Effect of Search on P(Benefits)",
          label = "tab:reg", header=FALSE, model.names = FALSE,
```

Table 2: Estimations of the Effect of Search on P(Benefits)

	Dependent variable:						
	Benefits 10 Weeks	Benefits 30 Weeks	Benefits 10 Weeks	Benefits 30 Weeks	Benefits 10 Weeks	Benefits 30 Weeks	
	(1)	(2)	(3)	(4)	(5)	(6)	
searchperiod	-0.164^{***} (0.023)	-0.126^{***} (0.024)	-0.157^{***} (0.023)	-0.121^{***} (0.025)	-0.143^{***} (0.024)	-0.099^{***} (0.025)	
$sumincome_12 months before$					0.0004 (0.027)	-0.022 (0.028)	
$sumincome_24months before$					-0.009 (0.014)	-0.005 (0.014)	
age					0.001 (0.001)	0.004*** (0.001)	
female					-0.010 (0.024)	-0.028 (0.026)	
children					-0.037 (0.037)	0.002 (0.040)	
partner					0.056 (0.040)	0.078* (0.043)	
$educ_bachelormaster$					-0.092*** (0.029)	-0.116*** (0.031)	
educ_prepvocational					0.013 (0.032)	0.022 (0.033)	
educ_primaryorless					-0.034 (0.037)	0.033 (0.039)	
educ_unknown					-0.381^{***} (0.068)	-0.270^{***} (0.072)	
educ_vocational							
Constant	0.736*** (0.016)	0.540*** (0.016)	0.682*** (0.038)	0.404*** (0.040)	0.723*** (0.068)	0.326*** (0.072)	
Period Dummies Region Dummies Observations Adjusted R ² F Statistic	No No 1,665 0.029 50.771***	No No 1,665 0.015 26.592***	Yes Yes 1,665 0.034 8.301***	Yes Yes 1,665 0.020 5.298***	Yes Yes 1,663 0.057 6.565***	Yes Yes 1,663 0.054 6.304***	

Note: *p<0.1; **p<0.05; ***p<0.01

The results imply that the treatment is effective in reducing the probability of receiving benefits on the long-term (30 weeks) by 10-percentage points, and slightly higher (15 percentage points) on the short-term

(10-weeks). If there is no selection on unobservables, these estimates give a good estimate of the ATE. But to what extent can these estimates be trusted?

4. Compute the no-assumption bounds for the treatment effects.

```
# Implement the no assumption bounds
no_assumption_bounds <- function(dataset, y_min, y_max, treatmentvar, depvar){</pre>
  depvar <- dplyr::enquo(depvar)</pre>
  treatmentvar <- dplyr::enquo(treatmentvar)</pre>
  pr_treated <- dataset %>%
    summarize(mean = mean(UQ(treatmentvar), na.rm = TRUE)) %>%
    pull()
  pr_untreated <- 1-pr_treated</pre>
  expected_y_given_deq1 <- dataset %>%
    dplyr::filter(UQ(treatmentvar) == 1) %>%
             summarize(mean = mean(UQ(depvar), na.rm = TRUE)) %>%
             pull()
  expected_y_given_deq0 <- dataset%>%
    dplyr::filter(UQ(treatmentvar) == 0) %>%
             summarize(mean = mean(UQ(depvar), na.rm = TRUE)) %>%
             pull()
  # bounds on y^*_1:
  lower_bound_y1 <- expected_y_given_deq1 * pr_treated + y_min * pr_untreated</pre>
  upper_bound_y1 <- expected_y_given_deq1 * pr_treated + y_max * pr_untreated</pre>
  # bounds on u^* 0:
  lower_bound_y0 <- expected_y_given_deq0 * pr_untreated + y_min * pr_treated</pre>
  upper_bound_y0 <- expected_y_given_deq0 * pr_untreated + y_max * pr_treated
  # bounds on the ATE:
  lower_bound_ate <- expected_y_given_deq1*pr_treated - expected_y_given_deq0*pr_untreated +</pre>
    (y_min + y_max)*pr_untreated - y_max
  upper_bound_ate <- expected_y_given_deq1*pr_treated - expected_y_given_deq0*pr_untreated +
    (y_min + y_max)*pr_untreated - y_min
  out <- tribble(~"lower_bound_y1", ~"upper_bound_y1", ~"lower_bound_y0",</pre>
                  ~"upper_bound_y0", ~"lower_bound_ate", ~"upper_bound_ate",
          lower_bound_y1, upper_bound_y1, lower_bound_y0, upper_bound_y0, lower_bound_ate, upper_bound_ate)
  return(out)
}
no_assumption_bounds(dataset, 0,1,searchperiod, benefits_week10) %>%
  knitr::kable(booktabs=T) %>%
    kableExtra::kable_styling(font_size = 7, latex_options = "hold_position")
                      upper\_bound\_y1
                                                          upper\_bound\_y0
                                                                                               upper_bound_ate
    lower_bound_y1
                                        lower_bound_y0
                                                                            lower_bound_ate
          0.2612613
                             0.8048048
                                                                                   -0.5951952
                                                                                                      0.4048048
                                                     0.4
                                                                 0.8564565
no_assumption_bounds(dataset, 0,1,searchperiod, benefits_week30) %>%
  knitr::kable(booktabs=T) %>%
    kableExtra::kable_styling(font_size = 7, latex_options = "hold_position")
                                        lower_bound_y0
                                                          upper\_bound\_y0
    lower bound v1
                      upper\_bound\_y1
                                                                            lower bound ate
                                                                                               upper\_bound\_ate
          0.1891892
                             0.7327327
                                               0.2936937
                                                                 0.7501502
                                                                                    -0.560961
                                                                                                       0.439039
```

5. Assume that caseworkers only apply search periods to applicants who benefit from it. How does this affects the bounds.

If people only select into the treatment if it works (meaning, decreasing the probability of benefits), we have:

$$\mathbb{E}[Y_1^*|D=1] \leq \mathbb{E}[Y_0^*|D=1]$$
 and $\mathbb{E}[Y_0^*|D=0] \leq \mathbb{E}[Y_1^*|D=0]$

Since the case is the opposite of the case that is worked out on the lecture slides, we cannot blindly apply the formulate, but realizing that:

 $y_{min} \leq \mathbb{E}[Y_1^*|D=1] \leq \mathbb{E}[Y_0^*|D=1] \leq y_{max} \text{ and} y_{min} \leq \mathbb{E}[Y_0^*|D=0] \leq \mathbb{E}[Y_1^*|D=0] \leq y_{max}$ We can evaluate $\mathbb{E}[Y_1^*]$, and we get:

 $\mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + \Pr[D=0] * \mathbb{E}[Y_0^*|D=0] \le \mathbb{E}[Y_1^*] \le \mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + y_{max} * \Pr[D=0]$ And for $\mathbb{E}[Y_0^*]$, we get:

$$\mathbb{E}[Y_0^*|D=0] * \Pr[D=0] + \Pr[D=1] * \mathbb{E}[Y_1^*|D=1] \leq \mathbb{E}[Y_0^*] \leq \mathbb{E}[Y_0^*|D=0] * \Pr[D=0] + \Pr[D=1] * y_{max} = 0$$

Then, realizing that the lower bound of $\mathbb{E}[Y_1^* - Y_0^*]$ is the lower bound of $\mathbb{E}[Y_1^*]$ minus the upper bound of $\mathbb{E}[Y_0^*]$, and *mutatis mutandis* for the upper bound of $\mathbb{E}[Y_1^* - Y_0^*]$, after rewriting, we find:

$$-\Pr(D=1) \cdot (y_{max} - \mathbb{E}[Y_1^*|D=1]) \le \mathbb{E}[Y_1^* - Y_0^*] \le \Pr(D=0) \cdot (y_{max} - \mathbb{E}[Y_0^*|D=0])$$

Which corresponds to the same properties as found in the lecture slides (i.e. narrower bounds, but without ever excluding zero). Implementing these bounds gives the following:

- [1] "For the 10-weeks outcome, the lower bound for $\mathrm{E}[Y_1^*-Y_0^*]=-0.195195195195195$ " paste('For the 10-weeks outcome, the upper bound for $\mathrm{E}[Y_1^*-Y_0^*]=-0.195195195195195$ ") paste('For the 10-weeks outcome, the upper bound for $\mathrm{E}[Y_1^*-Y_0^*]=-0.195195195195195$ ")

```
upper_bound30 <- bounds_info$pr_untreated * (bounds_info$y_max - expected_y_given_deq0)

paste('For the 30-weeks outcome, the lower bound for E[Y^*_1 - Y^*_0] = ', lower_bound30)
```

- [1] "For the 30-weeks outcome, the lower bound for $E[Y^*_1 Y^*_0] = -0.267267267267267$ " paste('For the 30-weeks outcome, the upper bound for $E[Y^*_1 Y^*_0] = '$, upper_bound30)
- [1] "For the 30-weeks outcome, the upper bound for $E[Y^*_1 Y^*_0] = 0.24984984984985$ "
 - 6. Next, imposed the monotone treatment response and the monotone treatment selection assumption separately and also jointly.
 - (i) First, we work out the case for our data, in which a favorable outcome is no benefits. Then, the MTS assumption becomes:

$$y_{min} \le \mathbb{E}[Y_1^*|D=1] \le \mathbb{E}[Y_1^*|D=0] \le y_{max}$$

 $y_{min} \le \mathbb{E}[Y_0^*|D=1] \le \mathbb{E}[Y_0^*|D=0] \le y_{max}$

This means that individuals who are or would have been assigned to the treatment group would have more favorable outcomes than non-treated subjects, whatever their treatment status. Bounding $\mathbb{E}[Y_1^*]$ gives:

$$\mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + \mathbb{E}[Y_1^*|D=1] * \Pr[D=0] \le \mathbb{E}[Y_1^*] \le \mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + y_{max} * \Pr[D=0]$$

And bounding $\mathbb{E}[Y_0^*]$ gives:

$$\mathbb{E}[Y_0^*|D=0]*\Pr[D=0] + y_{min}*\Pr[D=1] \leq \mathbb{E}[Y_0^*] \leq \mathbb{E}[Y_0^*|D=0]*\Pr[D=0] + \mathbb{E}[Y_0^*|D=0]*\Pr[D=1]$$

Simplifying both bounds, and realizing that the lower bound for $\mathbb{E}[Y_1^* - Y_0^*]$ equals the lower bound for Y_1^* minus the upper bound for Y_0^* , and the upper bound for $\mathbb{E}[Y_1^* - Y_0^*]$ equals the upper bound for Y_1^* minus the lower bound for Y_0^* , we find that the MTS bounds are:*

$$\mathbb{E}[Y_1^*|D=1] - \mathbb{E}[Y_0^*|D=0] \le \mathbb{E}[Y_1^* - Y_0^*] \le \Pr[D=1] * \mathbb{E}[Y_1^*|D=1] + \Pr[D=0] * y_{max} - \Pr[D=0] * \mathbb{E}[Y_0^*|D=0] - \Pr[D=1] * y_{min} \quad (1)$$

```
expected_y_given_deq1_10 <- dataset %>%
   dplyr::filter(searchperiod == 1) %>%
             summarize(mean = mean(benefits_week10, na.rm = TRUE)) %>%
             pull()
expected_y_given_deq0_10 <- dataset%>%
    dplyr::filter(searchperiod == 0) %>%
             summarize(mean = mean(benefits_week10, na.rm = TRUE)) %>%
             pull()
expected_y_given_deq1_30 <- dataset %>%
   dplyr::filter(searchperiod == 1) %>%
             summarize(mean = mean(benefits_week30, na.rm = TRUE)) %>%
             pull()
expected_y_given_deq0_30 <- dataset%>%
   dplyr::filter(searchperiod == 0) %>%
             summarize(mean = mean(benefits_week30, na.rm = TRUE)) %>%
             pull()
```

[1] "The lower bound for $E[Y_1^* - Y_0^*]$, for 10 weeks is -0.163543181157313"

[1] "The upper bound for $E[Y_1^* - Y_0^*]$, for 10 weeks is 0.404804804804805"

```
paste("The lower bound for $E[Y^*_1 - Y^*_0]$, for 30 weeks is", expected_y_given_deq1_30 - expected_y_given_deq0_30)
```

[1] "The lower bound for $E[Y_1^* - Y_0^*]$, for 30 weeks is -0.125857807502181"

```
paste("The upper bound for $E[Y^**_1 - Y^**_0]$, for 30 weeks is",
    pr_treated*expected_y_given_deq1_30 +
        pr_untreated * y_max -
        pr_untreated * expected_y_given_deq0_30 -
        pr_treated * y_min)
```

[1] "The upper bound for $E[Y_1^* - Y_0^*]$, for 30 weeks is 0.439039039039039"

After some rewriting, this result is a nice "mirror case" of the results on the slides, as it should be.

(ii) Imposing the MTR means in our case: $y_{min} \le Y_1^* \le Y_0^* \le y_{max}$. We then again proceed to analyse the bounds for Y_1^* and Y_0^* :

$$\mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + \Pr[D=0] * y_{min} \leq \mathbb{E}[Y_1^*| \leq \mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + \mathbb{E}[Y_0^*|D=0] * \Pr[D=0]$$

$$\mathbb{E}[Y_0^*|D=0] * \Pr[D=0] + \mathbb{E}[Y_1^*|D=1] * \Pr[D=1] \le \mathbb{E}[Y_0^*] \le \mathbb{E}[Y_0^*|D=0] * \Pr[D=0] + y_{max} * \Pr[D=1] = \mathbb{E}[Y_0^*|D=0] = \mathbb{E}$$

Then, applying the same procedure as before, we find that $\mathbb{E}[Y_1^* - Y_0^*]$ is bounded as follows:

$$\begin{split} \mathbb{E}[Y_1^*|D=1] * \Pr[D=1] + \Pr[D=0] * y_{min} \\ - \mathbb{E}[Y_0^*|D=0] * \Pr[D=0] - \Pr[D=1] * y_{max} \leq \mathbb{E}[Y_1^* - Y_0^*] \leq 0 \end{split}$$

We observe that we have again a mirror case compared to the lecture slides: the upper bound is now 0, instead of the lower bound.

[1] "The lower bound for $E[Y_1^* - Y_0^*]$, for 10 weeks is -0.595195195195195"

```
paste("The upper bound for $E[Y^*_1 - Y^*_0]$, for 10 weeks is", 0)
```

- [1] "The upper bound for $E[Y_1^* Y_0^*]$, for 10 weeks is 0" paste("The lower bound for $E[Y_1^* Y_0^*]$, for 30 weeks is", expected_y_given_deq1_30 * pr_treated + pr_untreated * y_min expected_y_given_deq0_30 * pr_untreated pr_treated*y_max)
- [1] "The lower bound for $E[Y_1^* Y_0^*]$, for 30 weeks is -0.560960960960961" paste("The upper bound for $E[Y_1^* Y_0^*]$, for 30 weeks is", 0)
- [1] "The upper bound for $E[Y_1^* Y_0^*]$, for 30 weeks is 0"
- (iii) Applying MTS and MTR together simply yields the most strict bounds from both sides. After some simplifying, we find that it reduces to:

$$\mathbb{E}[Y_1^*|D=1] - \mathbb{E}[Y_0^*|D=0] \leq \mathbb{E}[Y_1^* - Y_0^*] \leq 0$$

- [1] "The lower bound for $E[Y_1^* Y_0^*]$, for 10 weeks is -0.163543181157313" paste("The upper bound for $E[Y_1^* Y_0^*]$, for 10 weeks is", 0)
- [1] "The upper bound for $E[Y_1^* Y_0^*]$, for 10 weeks is 0" paste("The lower bound for $E[Y^*_1 Y^*_0]$, for 30 weeks is", expected_y_given_deq1_30 expected_y_given_deq0_30)
- [1] "The lower bound for $E[Y_1^* Y_0^*]$, for 30 weeks is -0.125857807502181" paste("The upper bound for $E[Y_1^* Y_0^*]$, for 30 weeks is", 0)
- [1] "The upper bound for $E[Y_1^* Y_0^*]$, for 30 weeks is 0"
 - 7. Usually higher educated workers have more favorable labor market outcomes. Use education as monotone instrumental variable and compute the bounds.

In our case, the monotone instrumental variable assumption is that the higher the education, the lower on average the benefits, i.e.:

$$\mathbb{E}[Y_d^*|Z = \text{BachelorMaster}] \leq \mathbb{E}[Y_d^*|Z = \text{Vocational}] \leq \text{Etc.}$$

After repeating the way of thinking in the lecture slides, but omitting the algebraic "proof" for brevity, in comparison to the slides, the formula for the bounds on the expected potential outcomes, conditional on Z changes to:

$$\max_{z' \geq z} \{LB(d,z)\} \leq \mathbb{E}[Y_d^*|Z=z] \leq \min_{z' \leq z} \{UB(d,z)\}$$

And unconditionally, to:

$$\sum_{z} \Pr[Z=z] \max_{z' \geq z} LB(d,z') \leq \mathbb{E}[Y_d^*] \leq \sum_{z} \Pr[Z=z] \max_{z' \leq z} UB(d,z')$$

We now implement this in a function, after slightly modifying the data so that education is in one column, and we omit the "unknown" education from the dataset, because it is unclear where that fits in the monotonicity:

```
dataset_new <- dataset %>%
 mutate(education = dplyr::case_when(educ_bachelormaster == 1 ~ 4,
                                      educ_vocational == 1 ~ 3,
                                      educ_prepvocational == 1 ~ 2,
                                      educ_primaryorless == 1 ~ 1)) %>%
 filter(!is.na(education))
First, we conduct the analysis for the 10-weeks outcome:
# We start with calculating the original lower and upper bounds using the previous function
# no_assumption_bounds for each group separately
original_bounds <- dataset_new %>%
 group_split(education) %>%
 map_df(~ no_assumption_bounds(.x, 0, 1, searchperiod, benefits_week10)) %>%
 mutate(z = c(1,2,3,4))
# Write an empty data frame to which we will write the effective LBs and UBs
effective_bounds <- data.frame(z = rep(c(1,2,3,4),2),
                               effective_lb = rep(0,8),
                               effective_ub = rep(0,8),
                               d = c(rep(0,4), rep(1,4))) %>%
 arrange(z)
\# Then, we for each Z and d, we find the "maximum" and "minimum" bounds among the feasible z'
for(i in 1:4){
  # Find the maximum lower bound y0 and write them to the effective bounds df
  effective_bounds[2*i-1, "effective_lb"] <- original_bounds %>%
    filter(z >= i) %>%
   summarize(effective_lb = max(lower_bound_y0)) %>% pull()
  # Find the maximum lower bound y1 and write them to the effective bounds df
 effective_bounds[2*i, "effective_lb"] <- original_bounds %>%
   filter(z >= i) %>%
   summarize(effective_lb = max(lower_bound_y1)) %>% pull()
  # Find the minimum upper bound y0 ...
 effective_bounds[2*i-1, "effective_ub"] <- original_bounds %>%
   filter(z <= i) %>%
   summarize(effective_ub = min(upper_bound_y0)) %>% pull()
 \# Find the minimum upper bound y1
 effective_bounds[2*i, "effective_ub"] <- original_bounds %>%
   filter(z <= i) %>%
   summarize(effective_ub = min(upper_bound_y1)) %>% pull()
# Then, we weight average the "effective" bounds to arrive at the bounds for Y^*_1 and Y^*_0
## First, calculate the probabilities
probs <- dataset_new %>%
 group_by(education) %>%
 summarize(n = n()) \%
 mutate(freq = n/sum(n)) %>% pull()
## Lower Bound Y_0:
lb_y0 <- effective_bounds %>%
 filter(d == 0) %>%
 select(effective_lb) %>% pull()
## Upper Bound Y_0:
ub_y0 <- effective_bounds %>%
 filter(d == 0) %>%
```

select(effective_ub) %>% pull()

select(effective_lb) %>% pull()

lb_y1 <- effective_bounds %>%
filter(d == 1) %>%

Lower Bound Y_1:

lower_bound_y0	upper_bound_y0	lower_bound_y1	upper_bound_y1	lower_bound_ate	upper_bound_ate
0.4165238	0.8568773	0.2639405	0.7877742	-0.5929368	0.3712504

We repeat the above exercise again for the 30-weeks outcome:

```
# We start with calculating the original lower and upper bounds using the previous function
# no_assumption_bounds for each group separately
original_bounds <- dataset_new %>%
 group_split(education) %>%
 map_df(~ no_assumption_bounds(.x, 0, 1, searchperiod, benefits_week30)) %>%
 mutate(z = c(1,2,3,4))
# Write an empty data frame to which we will write the effective LBs and UBs
effective_bounds <- data.frame(z = rep(c(1,2,3,4),2),
                               effective_lb = rep(0,8),
                               effective_ub = rep(0,8),
                               d = c(rep(0,4), rep(1,4))) \%
 arrange(z)
\# Then, we for each Z and d, we find the "maximum" and "minimum" bounds among the feasible z'
for(i in 1:4){
  # Find the maximum lower bound y0 and write them to the effective bounds df
 effective_bounds[2*i-1, "effective_lb"] <- original_bounds %>%
   filter(z >= i) %>%
    summarize(effective_lb = max(lower_bound_y0)) %>% pull()
  # Find the maximum lower bound y1 and write them to the effective bounds df
 effective_bounds[2*i, "effective_lb"] <- original_bounds %>%
   filter(z >= i) %>%
   summarize(effective_lb = max(lower_bound_y1)) %>% pull()
  \# Find the minimum upper bound y0 ...
 effective_bounds[2*i-1, "effective_ub"] <- original_bounds %>%
   filter(z <= i) %>%
   summarize(effective_ub = min(upper_bound_y0)) %>% pull()
  # Find the minimum upper bound y1
 effective_bounds[2*i, "effective_ub"] <- original_bounds %>%
   filter(z <= i) %>%
   summarize(effective_ub = min(upper_bound_y1)) %>% pull()
# Then, we weight average the "effective" bounds to arrive at the bounds for Y^*_1 and Y^*_2
## First, calculate the probabilities
probs <- dataset_new %>%
 group_by(education) %>%
 summarize(n = n()) \%
 mutate(freq = n/sum(n)) %>% pull()
## Lower Bound Y_0:
lb_y0 <- effective_bounds %>%
 filter(d == 0) %>%
```

```
select(effective_lb) %>% pull()
## Upper Bound Y_0:
ub_y0 <- effective_bounds %>%
 filter(d == 0) %>%
  select(effective_ub) %>% pull()
## Lower Bound Y_1:
lb_y1 <- effective_bounds %>%
 filter(d == 1) %>%
  select(effective_lb) %>% pull()
## Upper Bound Y_1:
ub_y1 <- effective_bounds %>%
 filter(d == 1) %>%
  select(effective_ub) %>% pull()
## Summarize in data.frame
data.frame(lower_bound_y0 = sum(probs*lb_y0), upper_bound_y0 = sum(probs*ub_y0),
          lower_bound_y1 = sum(probs*lb_y1), upper_bound_y1 = sum(probs*ub_y1)) %>%
  mutate(lower_bound_ate = lower_bound_y1 - upper_bound_y0,
  upper_bound_ate = upper_bound_y1 - lower_bound_y0) %>%
knitr::kable(booktabs=T) %>%
  kableExtra::kable_styling(font_size = 7, latex_options = "hold_position")
```

lower_	bound_y0	$upper_bound_y0$	$lower_bound_y1$	$upper_bound_y1$	$lower_bound_ate$	upper_bound_ate
	0.3040764	0.7484511	0.1908302	0.7404126	-0.5576208	0.4363362