

Macroeconomics I: Report

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Question 1

The code for question 1 is available at https://github.com/basm92/macroeconomics_i/blob/master/assignment_1/question1_main.ipynb. This is both downloadable and can then be run via Jupyter notebooks, but Github also renders the output of the code and creation of the figure. No additional Python libraries are required other than the standard libraries that come with e.g. the Conda implementation of Python.

1. Include the plot and Carefully discuss the economic intuition for the differences between the time paths for $\sigma = 1$ and $\sigma = 5$.

Test

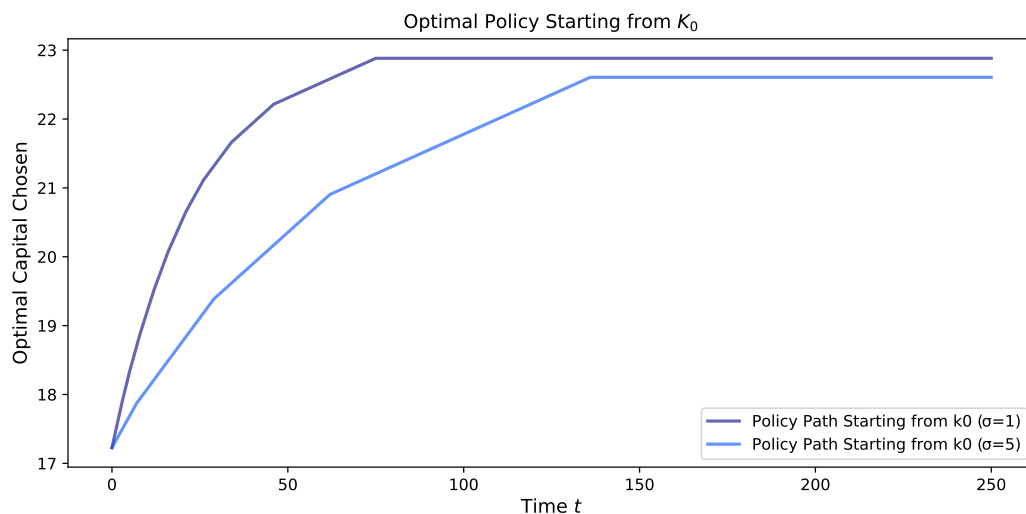


Figure 1: Plot for Question 1

Question 2

The code for question 1 is available at https://github.com/basm92/macroeconomics_i/blob/master/assignment_1/question2_main.ipynb. This is both downloadable and can then be run via Jupyter notebooks, but Github also renders the output of the code and creation of the figure. No additional Python libraries are required other than the standard libraries that come with e.g. the Conda implementation of Python.

1. Solve equation (2) for $\mu(t)$ and substitute the result in equation (1). Use the result to write down the Bellman equation with both control variables eliminated.

We find that:

$$\mu(t) = \frac{(1 - \phi)M(t) - M(t + 1)}{\gamma K(t)^\alpha} + 1$$

Substituting that in the definition for $c(t)$ gives us an expression for $c(t)$ that depends only on the state variables $M(t), M(t + 1), K(t), K(t + 1)$. The Bellman equation in terms of consumption choices is:

$$V(c(t)) = \max_{c(t)} \{U(c(t) + V(c(t + 1)))\}$$

After substituting in relevant definitions for $c(t)$ and $c(t+1)$ in terms of the state variables, we can numerically solve for V while controlling $K(t+1), M(t+1)$, starting from K_0 and M_0 , with an initial guess that $V(\cdot) = 0$. We have to satisfy two feasibility constraints: $c(t) > 0$ for all t and $0 \leq \mu(t) \leq 1$.

2. Plot the paths of $K(t), M(t), c(t)$ and $\mu(t)$ for 100 periods. In the plot for a given variable, include both the path induced by $\beta = 0.75$ and the path induced by $\beta = 0.85$ for easy comparison.

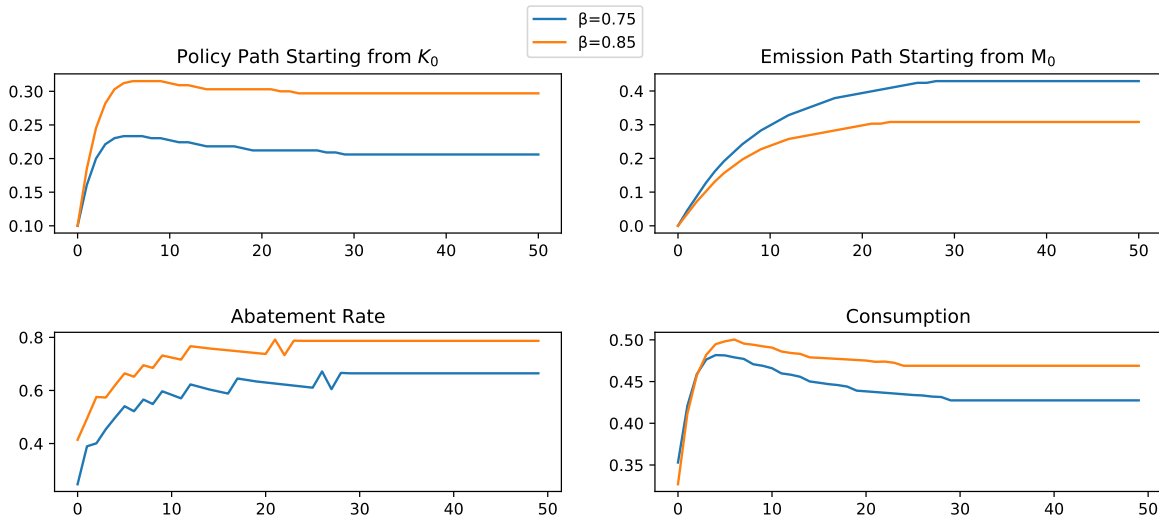


Figure 2: Plot for Question 1

3. Explain the overall qualitative pattern of the plots. Do capital and carbon converge to steady-state values? If so, is convergence monotone? Provide an intuitive economic story that accounts for this pattern.

In the plots we can clearly see that after approximately 30 periods we have that all variables (policy path, emission, abatement rate and consumption) converge to steady state values. Interestingly, we observe a non-monotone convergence for the policy path and consumption. That is, before the steady state is achieved, K and consumption first peak and afterwards slowly depreciate to their steady states. An intuitive economic story that could explain this result is the fact that when decisions on climate change policies have been made, governments and individuals (or firms) need to invest first to make sure that there are enough resources to decrease or stabilize emissions. As an example, suppose the world leaders agree on the idea that we can

only use renewable energy in 30 years. Then, we need additional capital to do research and to invest in new technologies. Also, households will consume more, by buying for instance solar panels or to insulate their houses. Therefore, it makes sense that we observe a peak in capital and consumption before we reach steady state.

4. Discuss the differences between the plots for $\beta = 0.75$ and $\beta = 0.85$. Provide an intuitive economic story that accounts for these differences.

β represents the discounting of the future. That is, lower β implies that the future is less important for the model. Therefore, in expectation, the steady state emissions should be higher for lower β . Intuitively, suppose an agent who discounts the future with a value of 0.99 (i.e. there is only little discounting). Then the agent cares a lot about the future and therefore also about future externalities of climate change. Therefore, the agent is willing to invest a lot at $t = 0$ in order to prevent the negative externalities from occurring. On the other hand, suppose an agent discounts with $\beta = 0.5$. Then the agent values next period with only half of the value of the current period. Therefore, future negative externalities are less important and the agent will invest less in emission reducing technologies.

If we look at the emission path for M_0 , we indeed observe this pattern. For $\beta = 0.75$, one can clearly see that the emissions will be higher compared to the path for $\beta = 0.85$.