

**Basma El Shenawy**

**900150283**

Assignment 1 report

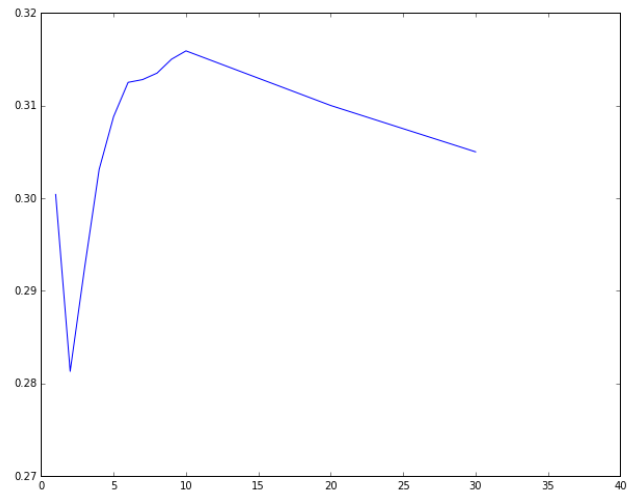
March 3rd, 2018

## Part 1

The aim of my training and validation was to find the K that produces the best accuracy and standard deviation. I started by getting the accuracies of a wide set of data to find where this best K might fall. See the results below.

```
for k= 1
Got 968 / 3330 correct => accuracy: 0.290691
Got 1002 / 3330 correct => accuracy: 0.300901
Got 1031 / 3330 correct => accuracy: 0.309610
average accuracy: 0.3004004004
for k= 2
Got 908 / 3330 correct => accuracy: 0.272673
Got 938 / 3330 correct => accuracy: 0.281682
Got 964 / 3330 correct => accuracy: 0.289489
average accuracy: 0.281281281281
for k= 3
Got 928 / 3330 correct => accuracy: 0.278679
Got 987 / 3330 correct => accuracy: 0.296396
Got 1007 / 3330 correct => accuracy: 0.302402
average accuracy: 0.292492492492
for k= 4
Got 962 / 3330 correct => accuracy: 0.288889
Got 1026 / 3330 correct => accuracy: 0.308108
Got 1040 / 3330 correct => accuracy: 0.312312
average accuracy: 0.303103103103
for k= 5
Got 975 / 3330 correct => accuracy: 0.292793
Got 1046 / 3330 correct => accuracy: 0.314114
Got 1064 / 3330 correct => accuracy: 0.319520
average accuracy: 0.308808808809
for k= 6
Got 982 / 3330 correct => accuracy: 0.294895
Got 1055 / 3330 correct => accuracy: 0.316817
Got 1085 / 3330 correct => accuracy: 0.325826
average accuracy: 0.312512512513
for k= 7
Got 989 / 3330 correct => accuracy: 0.296997
Got 1058 / 3330 correct => accuracy: 0.317718
Got 1078 / 3330 correct => accuracy: 0.323724
average accuracy: 0.312812812813
for k= 8
Got 989 / 3330 correct => accuracy: 0.296997
Got 1059 / 3330 correct => accuracy: 0.318018
Got 1084 / 3330 correct => accuracy: 0.325526
average accuracy: 0.313513513514
for k= 9
Got 999 / 3330 correct => accuracy: 0.300000
Got 1065 / 3330 correct => accuracy: 0.319820
Got 1083 / 3330 correct => accuracy: 0.325225
average accuracy: 0.315015015015
for k= 10
Got 1007 / 3330 correct => accuracy: 0.302402
Got 1066 / 3330 correct => accuracy: 0.320120
Got 1083 / 3330 correct => accuracy: 0.325225
average accuracy: 0.315915915916
for k= 20
Got 1005 / 3330 correct => accuracy: 0.301802
Got 1035 / 3330 correct => accuracy: 0.310811
Got 1057 / 3330 correct => accuracy: 0.317417
average accuracy: 0.31001001001
for k= 30
Got 993 / 3330 correct => accuracy: 0.298198
Got 1013 / 3330 correct => accuracy: 0.304204
Got 1041 / 3330 correct => accuracy: 0.312613
average accuracy: 0.305005005005
```

best k: 10 value: 0.315915915916



I then tried testing the bigger numbers just to ensure that I got the best K. The average accuracy is less than that of the smaller values as we see in the following results.

```
for k= 50
Got 955 / 3330 correct => accuracy: 0.286787
Got 1005 / 3330 correct => accuracy: 0.301802
Got 1041 / 3330 correct => accuracy: 0.312613
average accuracy: 0.3004004004
for k= 100
Got 928 / 3330 correct => accuracy: 0.278679
Got 962 / 3330 correct => accuracy: 0.288889
Got 979 / 3330 correct => accuracy: 0.293994
average accuracy: 0.287187187187
for k= 150
Got 906 / 3330 correct => accuracy: 0.272072
Got 931 / 3330 correct => accuracy: 0.279580
Got 958 / 3330 correct => accuracy: 0.287688
average accuracy: 0.27977977978
for k= 200
Got 884 / 3330 correct => accuracy: 0.265465
Got 914 / 3330 correct => accuracy: 0.274474
Got 916 / 3330 correct => accuracy: 0.275075
average accuracy: 0.271671671672
```

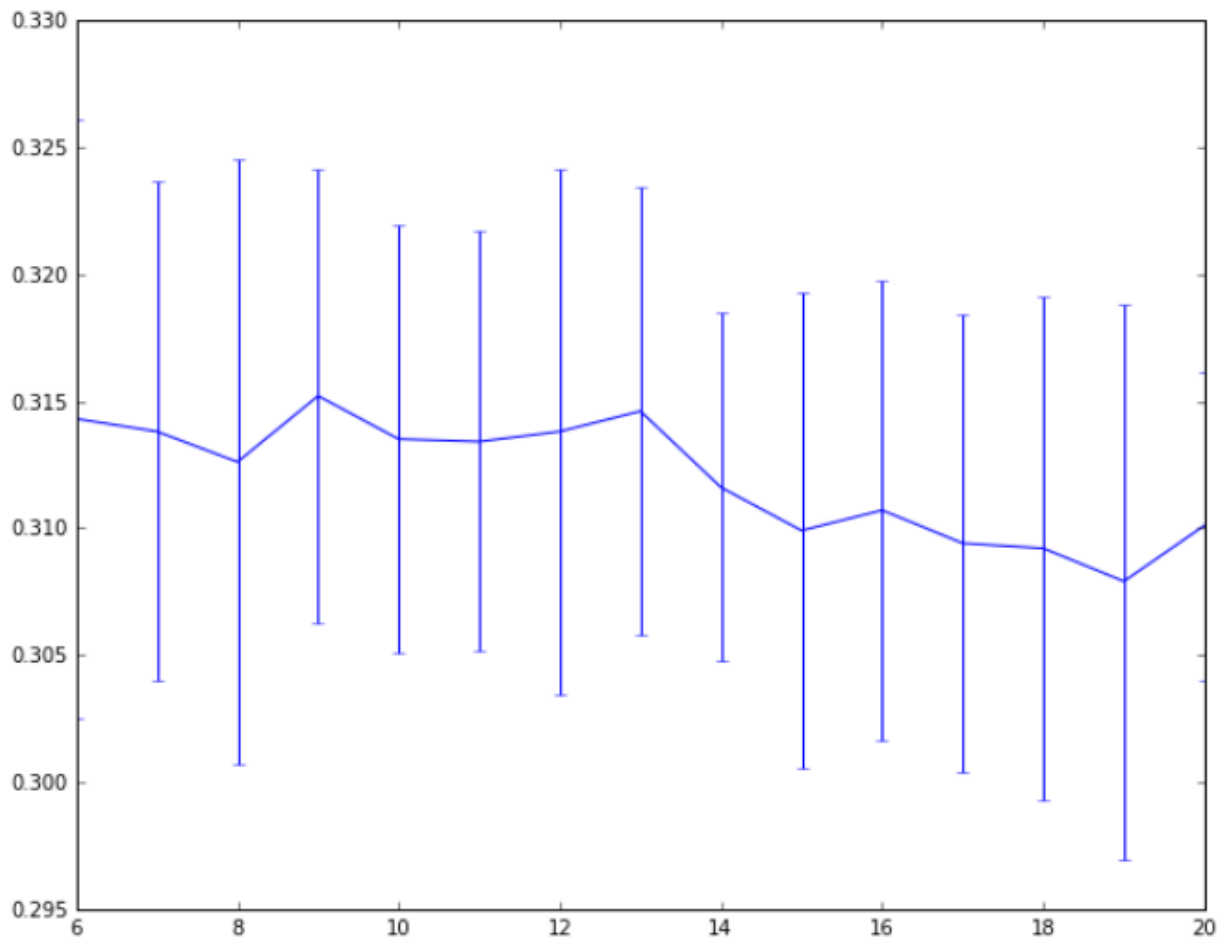
As we can see from the previous data, the maximums occur somewhere between k=6 and k=20. Therefore, I repeated the results whose average accuracy is between 0.31 and 0.32 (k=6 till k=20) but calculated the standard deviation as well in order to find the best K. see result below.

---

```
for k= 6
Got 993 / 3330 correct => accuracy: 0.298198
Got 1061 / 3330 correct => accuracy: 0.318619
Got 1086 / 3330 correct => accuracy: 0.326126
average accuracy: 0.314314314314
for k= 7
Got 1000 / 3330 correct => accuracy: 0.300300
Got 1058 / 3330 correct => accuracy: 0.317718
Got 1077 / 3330 correct => accuracy: 0.323423
average accuracy: 0.313813813814
for k= 8
Got 987 / 3330 correct => accuracy: 0.296396
Got 1055 / 3330 correct => accuracy: 0.316817
Got 1081 / 3330 correct => accuracy: 0.324625
average accuracy: 0.312612612613
for k= 9
Got 1008 / 3330 correct => accuracy: 0.302703
Got 1066 / 3330 correct => accuracy: 0.320120
Got 1075 / 3330 correct => accuracy: 0.322823
average accuracy: 0.315215215215
for k= 10
Got 1005 / 3330 correct => accuracy: 0.301802
Got 1057 / 3330 correct => accuracy: 0.317417
Got 1070 / 3330 correct => accuracy: 0.321321
average accuracy: 0.313513513514
for k= 11
Got 1005 / 3330 correct => accuracy: 0.301802
Got 1059 / 3330 correct => accuracy: 0.318018
Got 1067 / 3330 correct => accuracy: 0.320420
average accuracy: 0.313413413413
for k= 12
Got 997 / 3330 correct => accuracy: 0.299399
Got 1062 / 3330 correct => accuracy: 0.318919
Got 1076 / 3330 correct => accuracy: 0.323123
average accuracy: 0.313813813814
for k= 13
Got 1012 / 3330 correct => accuracy: 0.303904
Got 1047 / 3330 correct => accuracy: 0.314414
Got 1084 / 3330 correct => accuracy: 0.325526
average accuracy: 0.314614614615
```

```
for k= 14
Got 1006 / 3330 correct => accuracy: 0.302102
Got 1048 / 3330 correct => accuracy: 0.314715
Got 1059 / 3330 correct => accuracy: 0.318018
average accuracy: 0.311611611612
for k= 15
Got 988 / 3330 correct => accuracy: 0.296697
Got 1055 / 3330 correct => accuracy: 0.316817
Got 1053 / 3330 correct => accuracy: 0.316216
average accuracy: 0.309909990991
for k= 16
Got 992 / 3330 correct => accuracy: 0.297898
Got 1057 / 3330 correct => accuracy: 0.317417
Got 1055 / 3330 correct => accuracy: 0.316817
average accuracy: 0.310710710711
for k= 17
Got 989 / 3330 correct => accuracy: 0.296697
Got 1042 / 3330 correct => accuracy: 0.312913
Got 1060 / 3330 correct => accuracy: 0.318318
average accuracy: 0.309409409409
for k= 18
Got 984 / 3330 correct => accuracy: 0.295495
Got 1044 / 3330 correct => accuracy: 0.313514
Got 1061 / 3330 correct => accuracy: 0.318619
average accuracy: 0.309209209209
for k= 19
Got 976 / 3330 correct => accuracy: 0.293093
Got 1037 / 3330 correct => accuracy: 0.311411
Got 1063 / 3330 correct => accuracy: 0.319219
average accuracy: 0.307907907908
for k= 20
Got 1006 / 3330 correct => accuracy: 0.302102
Got 1037 / 3330 correct => accuracy: 0.311411
Got 1055 / 3330 correct => accuracy: 0.316817
average accuracy: 0.310110110111
```

---



As we can see from the data, the best K is =9 with validation accuracy of 0.315215215215.. So, I used the entire 10000 dataset as training data and tested using the testing batch. I got the overall accuracy and the accuracy of each class See the results below.

**Got 3241 / 9990 correct => accuracy: 0.324424**

The average accuracy of each of the 10 classes:

```

CCRN is: 0.542000 for class: plane
CCRN is: 0.166000 for class: car
CCRN is: 0.443000 for class: bird
CCRN is: 0.144000 for class: cat
CCRN is: 0.422000 for class: deer
CCRN is: 0.191000 for class: dog
CCRN is: 0.271000 for class: frog
CCRN is: 0.197000 for class: horse
CCRN is: 0.657000 for class: ship
CCRN is: 0.208000 for class: truck

```

## Part 2

How do I get the  $w$ ?

$$E(w) = \sum_{i=1}^N (t_i - w^T x_i)^2 = (t - Xw)^T (t - Xw)$$

$\uparrow$  labels = 10000       $\uparrow$  weights       $\uparrow$  training point

$$x = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ 1 \end{bmatrix} \rightarrow X = \begin{bmatrix} x_{11} & x_{12} & x_{13} & \dots & 1 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ x_{n1} & x_{n2} & \dots & \dots & 1 \end{bmatrix}$$

$\uparrow$  one training pt.       $n = 10000$

$$w = \begin{bmatrix} w_1 \\ w_2 \\ \vdots \\ w_n \end{bmatrix} \quad t = \begin{bmatrix} t_1 \\ t_2 \\ \vdots \\ t_n \end{bmatrix}$$

$\uparrow$  no longer scalars, but vectors       $n = 10000$

To get min. residual sum, we differentiate wrt  $w$

$$X^T (t - Xw) = 0 \rightarrow (X^T X)^{-1} X^T t$$

To get the prediction:

$$y(x) = w^T x$$

$\uparrow$  where  $x$  here is the testing pt.

Accuracy of the training:

0.50944

Accuracy of testing:

ACCR for testing data is : 0.363700

The average accuracy of each of the 10 classes:

CCRN is:	0.469000	for class: plane
CCRN is:	0.445000	for class: car
CCRN is:	0.207000	for class: bird
CCRN is:	0.177000	for class: cat
CCRN is:	0.243000	for class: deer
CCRN is:	0.285000	for class: dog
CCRN is:	0.449000	for class: frog
CCRN is:	0.426000	for class: horse
CCRN is:	0.508000	for class: ship
CCRN is:	0.428000	for class: truck

I believe that no overfitting occurred because the difference between the accuracy of the testing and the accuracy of the training is very small. (about 1.5)