BBH DR General Code

September 21, 2017

```
In [53]: #Introduction: Hello there. In this notebook, we will be examining gravitational waves
         #processing tasks to calcualte the detection range of BBH(Binary Black Hole) mergers us
         #by the LOSC (LIGO Open Science Center). Let's get right to it!
In [54]: #Setup: Installing the required packages and downloading the data:
         !wget https://losc.ligo.org/s/events/get_datafiles.sh
         !bash get_datafiles.sh
         !pip install lal
         !pip install pycbc==1.7.5
         import numpy as np
         import pylab
         from scipy import signal
         from scipy.interpolate import interp1d
         from scipy.signal import butter, filtfilt, iirdesign, zpk2tf, freqz
         import h5py
         import json
         %matplotlib inline
         %config InlineBackend.figure_format = 'retina'
         import matplotlib.pyplot as plt
         import matplotlib.mlab as mlab
         import readligo as rl
         from pycbc.frame import read_frame
         from pycbc.filter import highpass_fir, matched_filter
         from pycbc.waveform import get_td_waveform, get_fd_waveform
         from pycbc.waveform import td_approximants, fd_approximants
         from pycbc.psd import welch, interpolate
        print("Download complete!")
--2017-09-21 17:27:57-- https://losc.ligo.org/s/events/get_datafiles.sh
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | :3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1029 (1.0K) [application/x-sh]
Saving to: 'get_datafiles.sh.4'
get_datafiles.sh.4 100%[===========] 1.00K --.-KB/s
2017-09-21 17:27:57 (44.8 MB/s) - 'get_datafiles.sh.4' saved [1029/1029]
```

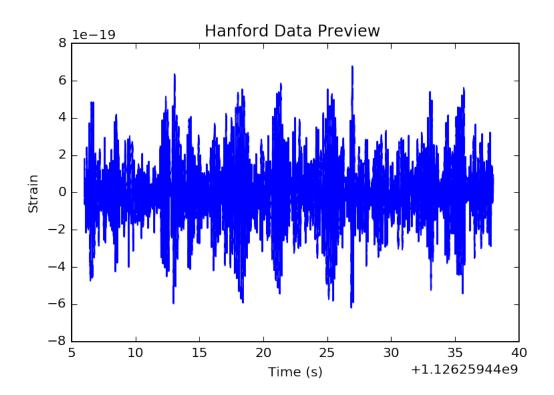
```
--2017-09-21 17:27:57-- https://losc.ligo.org/s/events/BBH_events_v3.json
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 2202 (2.2K) [application/json]
Saving to: 'BBH_events_v3.json.4'
BBH_events_v3.json. 100%[===========] 2.15K --.-KB/s
2017-09-21 17:27:58 (86.8 MB/s) - 'BBH_events_v3.json.4' saved [2202/2202]
--2017-09-21 17:27:58-- https://losc.ligo.org/s/sample_code/readligo.py
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 17238 (17K) [text/plain]
Saving to: 'readligo.py.5'
readligo.py.5
                  2017-09-21 17:27:58 (474 KB/s) - 'readligo.py.5' saved [17238/17238]
--2017-09-21 17:27:58-- https://losc.ligo.org/s/events/GW150914/H-H1_LOSC_4_V2-1126259446-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | :3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1040592 (1016K)
Saving to: 'H-H1_LOSC_4_V2-1126259446-32.hdf5.4'
in 0.3s
2017-09-21 17:27:59 (3.12 MB/s) - 'H-H1_LOSC_4_V2-1126259446-32.hdf5.4' saved [1040592/1040592]
--2017-09-21 17:27:59-- https://losc.ligo.org/s/events/GW150914/L-L1_LOSC_4_V2-1126259446-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | :3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1007420 (984K)
Saving to: 'L-L1_LOSC_4_V2-1126259446-32.hdf5.4'
2017-09-21 17:28:00 (3.22 MB/s) - 'L-L1_LOSC_4_V2-1126259446-32.hdf5.4' saved [1007420/1007420]
--2017-09-21 17:28:00-- https://losc.ligo.org/s/events/GW150914/GW150914_4_template.hdf5
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
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Proxy request sent, awaiting response... 200 OK
Length: 1056864 (1.0M)
Saving to: 'GW150914_4_template.hdf5.4'
in 0.3s
2017-09-21 17:28:00 (2.91 MB/s) - 'GW150914_4_template.hdf5.4' saved [1056864/1056864]
--2017-09-21 17:28:00-- https://losc.ligo.org/s/events/LVT151012/H-H1_LOSC_4_V2-1128678884-32.h
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1039648 (1015K)
Saving to: 'H-H1_LOSC_4_V2-1128678884-32.hdf5.4'
in 0.3s
2017-09-21 17:28:01 (3.31 MB/s) - 'H-H1_LOSC_4_V2-1128678884-32.hdf5.4' saved [1039648/1039648]
--2017-09-21 17:28:01-- https://losc.ligo.org/s/events/LVT151012/L-L1_LOSC_4_V2-1128678884-32.h
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1018496 (995K)
Saving to: 'L-L1_LOSC_4_V2-1128678884-32.hdf5.4'
in 0.3s
2017-09-21 17:28:02 (3.15 MB/s) - 'L-L1_LOSC_4_V2-1128678884-32.hdf5.4' saved [1018496/1018496]
--2017-09-21 17:28:02-- https://losc.ligo.org/s/events/LVT151012/LVT151012_4_template.hdf5
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1056864 (1.0M)
Saving to: 'LVT151012_4_template.hdf5.5'
LVT151012_4_templat 100%[============] 1.01M 3.50MB/s
2017-09-21 17:28:03 (3.50 MB/s) - 'LVT151012_4_template.hdf5.5' saved [1056864/1056864]
--2017-09-21 17:28:03-- https://losc.ligo.org/s/events/GW151226/H-H1_LOSC_4_V2-1135136334-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1040336 (1016K)
Saving to: 'H-H1_LOSC_4_V2-1135136334-32.hdf5.4'
```

```
H-H1 LOSC 4 V2-1135 100%[============] 1016K 3.28MB/s
                                                            in 0.3s
2017-09-21 17:28:03 (3.28 MB/s) - 'H-H1_LOSC_4_V2-1135136334-32.hdf5.4' saved [1040336/1040336]
--2017-09-21 17:28:03-- https://losc.ligo.org/s/events/GW151226/L-L1_LOSC_4_V2-1135136334-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1022324 (998K)
Saving to: 'L-L1_LOSC_4_V2-1135136334-32.hdf5.4'
in 0.3s
2017-09-21 17:28:04 (3.28 MB/s) - 'L-L1_LOSC_4_V2-1135136334-32.hdf5.4' saved [1022324/1022324]
--2017-09-21 17:28:04-- https://losc.ligo.org/s/events/GW151226/GW151226_4_template.hdf5
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1056864 (1.0M)
Saving to: 'GW151226_4_template.hdf5.4'
GW151226_4_template 100%[=============] 1.01M 3.41MB/s
                                                              in 0.3s
2017-09-21 17:28:05 (3.41 MB/s) - 'GW151226_4_template.hdf5.4' saved [1056864/1056864]
--2017-09-21 17:28:05-- https://losc.ligo.org/s/events/GW170104/H-H1_LOSC_4_V1-1167559920-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1033609 (1009K)
Saving to: 'H-H1_LOSC_4_V1-1167559920-32.hdf5.5'
in 0.3s
2017-09-21 17:28:05 (3.13 MB/s) - 'H-H1_LOSC_4_V1-1167559920-32.hdf5.5' saved [1033609/1033609]
--2017-09-21 17:28:05-- https://losc.ligo.org/s/events/GW170104/L-L1_LOSC_4_V1-1167559920-32.hd
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | :3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1005007 (981K)
Saving to: 'L-L1_LOSC_4_V1-1167559920-32.hdf5.5'
2017-09-21 17:28:06 (3.21 MB/s) - 'L-L1_LOSC_4_V1-1167559920-32.hdf5.5' saved [1005007/1005007]
```

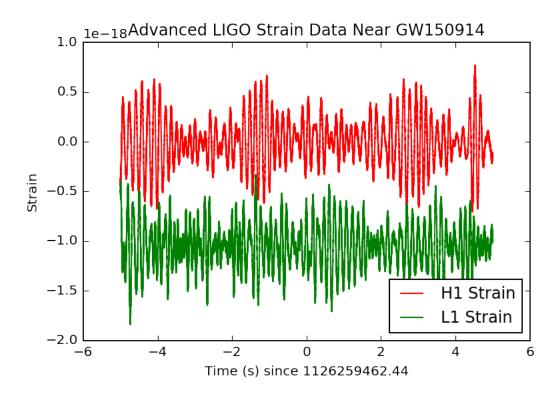
```
--2017-09-21 17:28:06-- https://losc.ligo.org/s/events/GW170104/GW170104_4_template.hdf5
Resolving webproxy (webproxy)... 100.112.158.176
Connecting to webproxy (webproxy) | 100.112.158.176 | : 3128... connected.
Proxy request sent, awaiting response... 200 OK
Length: 1056864 (1.0M)
Saving to: 'GW170104_4_template.hdf5.5'
GW170104_4_template 100%[=========>]
                                                                             1.01M 3.38MB/s
                                                                                                           in 0.3s
2017-09-21 17:28:07 (3.38 MB/s) - 'GW170104_4_template.hdf5.5' saved [1056864/1056864]
Requirement already satisfied: lal in /home/nbcommon/anaconda2_410/lib/python2.7/site-packages
Requirement already satisfied: numpy==1.13.0 in /home/nbcommon/anaconda2_410/lib/python2.7/site-
Requirement already satisfied: pycbc==1.7.5 in /home/nbcommon/anaconda2_410/lib/python2.7/site-p
Requirement already satisfied: decorator>=3.4.2 in /home/nbcommon/anaconda2_410/lib/python2.7/si
Requirement already satisfied: unittest2 in /home/nbcommon/anaconda2_410/lib/python2.7/site-pack
Requirement already satisfied: kombine==0.8.1 in /home/nbcommon/anaconda2_410/lib/python2.7/site
Requirement already satisfied: Mako>=1.0.1 in /home/nbcommon/anaconda2_410/lib/python2.7/site-page 1.0.1 in /home/nbcommon/a
Requirement already satisfied: emcee>=2.2.0 in /home/nbcommon/anaconda2_410/lib/python2.7/site-p
Requirement already satisfied: argparse>=1.3.0 in /home/nbcommon/anaconda2_410/lib/python2.7/sit
Requirement already satisfied: matplotlib>=1.3.1 in /home/nbcommon/anaconda2_410/lib/python2.7/s
Requirement already satisfied: corner>=2.0.1 in /home/nbcommon/anaconda2_410/lib/python2.7/site-
Requirement already satisfied: pyRXP>=2.1.0 in /home/nbcommon/anaconda2_410/lib/python2.7/site-p
Requirement already satisfied: beautifulsoup4>=4.6.0 in /home/nbcommon/anaconda2_410/lib/python2
Requirement already satisfied: pillow in /home/nbcommon/anaconda2_410/lib/python2.7/site-package
Requirement already satisfied: pycbc-glue-obsolete==1.1.0 in /home/nbcommon/anaconda2_410/lib/py
Requirement already satisfied: h5py>=2.5 in /home/nbcommon/anaconda2_410/lib/python2.7/site-pack
Requirement already satisfied: requests>=1.2.1 in /home/nbcommon/anaconda2_410/lib/python2.7/sit
Requirement already satisfied: numpy>=1.6.4 in /home/nbcommon/anaconda2_410/lib/python2.7/site-p
Requirement already satisfied: scipy>=0.13.0 in /home/nbcommon/anaconda2_410/lib/python2.7/site-
Requirement already satisfied: jinja2 in /home/nbcommon/anaconda2_410/lib/python2.7/site-package
Requirement already satisfied: weave>=0.16.0 in /home/nbcommon/anaconda2_410/lib/python2.7/site-
Requirement already satisfied: mpld3>=0.3 in /home/nbcommon/anaconda2_410/lib/python2.7/site-pace
Requirement already satisfied: traceback2 in /home/nbcommon/anaconda2_410/lib/python2.7/site-pac
Requirement already satisfied: six>=1.4 in /home/nbcommon/anaconda2_410/lib/python2.7/site-packa
Requirement already satisfied: MarkupSafe>=0.9.2 in /home/nbcommon/anaconda2_410/lib/python2.7/s
Requirement already satisfied: python-dateutil in /home/nbcommon/anaconda2_410/lib/python2.7/sit
Requirement already satisfied: pytz in /home/nbcommon/anaconda2_410/lib/python2.7/site-packages
Requirement already satisfied: cycler in /home/nbcommon/anaconda2_410/lib/python2.7/site-package
Requirement already satisfied: pyparsing!=2.0.4,>=1.5.6 in /home/nbcommon/anaconda2_410/lib/pyth
Requirement already satisfied: linecache2 in /home/nbcommon/anaconda2_410/lib/python2.7/site-pac
Download complete!
```

```
#eventname = 'LVT151012'
                           #eventname = 'GW170104'
                           make_plots = 1
                           plottype = "png"
                           \#plottype = "pdf"
In [56]: #Error Check: Reading the event properties from a local json file and printing an error
                           fnjson = "BBH_events_v3.json"
                                        events = json.load(open(fnjson,"r"))
                           except IOError:
                                       print("Cannot find resource file "+fnjson)
                                       print("You can download it from https://losc.ligo.org/s/events/"+fnjson)
                                       print("Quitting.")
                                       quit()
                           try:
                                        events[eventname]
                           except:
                                        print('You must select an eventname that is in '+fnjson+'! Quitting.')
                                       quit()
In [57]: #Preview of Data: Reading the Hanford data from one of the files we downloaded
                          {\tt h1 = read\_frame('H-H1\_LOSC\_4\_V2-1126259446-32.gwf', 'H1:LOSC\_STRAIN')} ~ \textit{\#Reading the filed the filed for t
                           h1 = highpass_fir(h1, 15, 16) #Filtering the data, getting rid of low frequency data
                           pylab.plot(h1.sample_times, h1)#Plotting the data
                           plt.title('Hanford Data Preview ')
                           plt.ylabel('Strain')
                           plt.xlabel('Time (s)')
Out[57]: <matplotlib.text.Text at 0x7fcb02551750>
```



```
In [58]: #Learn more about the data: Extract and print parameters for the desired event and read
         event = events[eventname]
         fn_H1 = event['fn_H1']
                                             # File name for H1 data
                                             # File name for L1 data
         fn_L1 = event['fn_L1']
         fn_template = event['fn_template'] # File name for template waveform
         fs = event['fs']
                                             # Set sampling rate
         tevent = event['tevent']
                                             # Set approximate event GPS time
         fband = event['fband']
                                             # Frequency band for bandpassing signal
         print("Reading in parameters for event " + event["name"])
         print(event)
         try:
             strain_H1, time_H1, chan_dict_H1 = rl.loaddata(fn_H1, 'H1')
             strain_L1, time_L1, chan_dict_L1 = rl.loaddata(fn_L1, 'L1')
         except:
             print("Cannot find data files!")
             print("You can download them from https://losc.ligo.org/s/events/"+eventname)
             print("Quitting.")
             quit()
         time = time H1
         dt = time[1] - time[0]
         #Printing properties of time and strain values:
         print('time_H1: len, min, mean, max = ', \
             len(time_H1), time_H1.min(), time_H1.mean(), time_H1.max() )
```

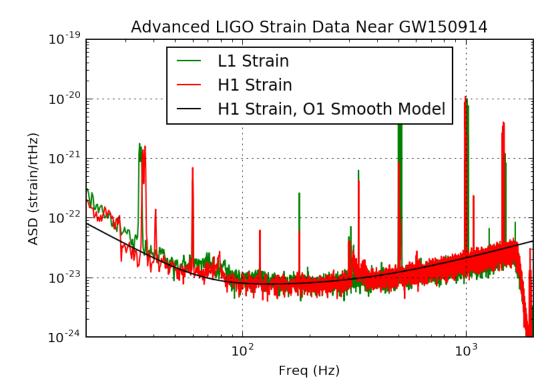
```
print('strain_H1: len, min, mean, max = ', \
             len(strain_H1), strain_H1.min(),strain_H1.mean(),strain_H1.max())
         print( 'strain_L1: len, min, mean, max = ', \
             len(strain_L1), strain_L1.min(),strain_L1.mean(),strain_L1.max())
         bits = chan_dict_H1['DATA']
         print("For H1, {0} out of {1} seconds contain usable DATA".format(bits.sum(), len(bits)
         bits = chan_dict_L1['DATA']
         print("For L1, {0} out of {1} seconds contain usable DATA".format(bits.sum(), len(bits)
Reading in parameters for event GW150914
{u'fband': [43.0, 300.0], u'approx': u'lalsim.SEOBNRv2', u'fs': 4096, u'name': u'GW150914', u'ut
('time_H1: len, min, mean, max = ', 131072, 1126259446.0, 1126259461.9998779, 1126259477.9997559
('strain_H1: len, min, mean, max = ', 131072, -7.0446659431560669e-19, 5.8955225092464373e-23, 7
('strain_L1: len, min, mean, max = ', 131072, -1.8697138664279764e-18, -1.0522332249909908e-18,
For H1, 32 out of 32 seconds contain usable DATA
For L1, 32 out of 32 seconds contain usable DATA
In [59]: # Previewing event data: Here we plot data 5 seconds around the event:
         deltat = 5 #Setting the time domain
         indxt = np.where((time >= tevent-deltat) & (time < tevent+deltat)) #Indexing into the s
         print'GPS time of event: ',tevent #Printing GPS time of event
         if make_plots:
             plt.figure()
             plt.plot(time[indxt]-tevent,strain_H1[indxt],'r',label='H1 Strain')
             plt.plot(time[indxt]-tevent,strain_L1[indxt],'g',label='L1 Strain')
             plt.xlabel('Time (s) since '+str(tevent))
             plt.ylabel('Strain')
             plt.legend(loc='lower right')
             plt.title('Advanced LIGO Strain Data Near '+eventname)
             plt.savefig(eventname+'_strain.'+plottype)
```



```
In [60]: # Using the data: Plotting the data in the Fourier domain and as ASD.
                         make_psds = 1
                         if make_psds:
                                     {	t NFFT} = 4*{	t fs} #Calculating nonequispaced fast Fourier transform using the sampling re
                                    Pxx_H1, freqs = mlab.psd(strain_H1, Fs = fs, NFFT = NFFT)
                                    Pxx_L1, freqs = mlab.psd(strain_L1, Fs = fs, NFFT = NFFT)
                                     psd_H1 = interp1d(freqs, Pxx_H1) #Use interpolations of the PSDs computed above for
                                     psd_L1 = interp1d(freqs, Pxx_L1) #Use interpolations of the PSDs computed above for
                                    Pxx = (1.e-22*(18./(0.1+freqs))**2)**2+0.7e-23**2+((freqs/2000.)*4.e-23)**2 #Smooth(freqs/2000.)*4.e-23)**2 #Smooth(freqs/2000.)*4 #Sm
                                     psd_smooth = interp1d(freqs, Pxx)
                                     print"Min frequency of the PSD",min(freqs)
                                     print"Max frequency of the PSD", max(freqs)
                         # Plotting the ASD vs Frequency:
                         if make_plots:
                                     f_min = 20.
                                    f_max = 2000.
                                     plt.figure(figsize=(6,4))
                                     plt.loglog(freqs, np.sqrt(Pxx_L1), 'g', label='L1 Strain') #Plotting ASD for L1
                                    plt.loglog(freqs, np.sqrt(Pxx_H1), 'r', label='H1 Strain') #Plotting ASD for H1
                                     plt.loglog(freqs, np.sqrt(Pxx),'k',label='H1 Strain, O1 Smooth Model')#Plotting ASI
                                    plt.axis([f_min, f_max, 1e-24, 1e-19])
                                    plt.grid('on')
                                    plt.ylabel('ASD (strain/rtHz)')
```

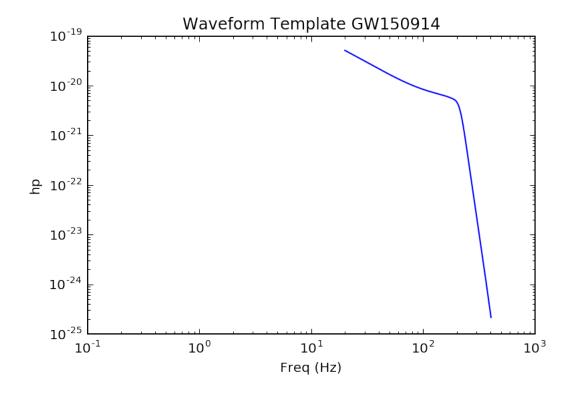
```
plt.xlabel('Freq (Hz)')
    plt.legend(loc='upper center')
    plt.title('Advanced LIGO Strain Data Near '+eventname)
    plt.savefig(eventname+'_ASDs.'+plottype)

Min frequency of the PSD 0.0
Max frequency of the PSD 2048.0
```



```
b=np.abs(hp)
totalmass=m1+m2 #Total mass of the system
print "The total mass of the BBHs is:",totalmass
print "The sampling rate of the Waveform template is:", dfWaveform
pylab.loglog(hp.sample_frequencies, np.abs(hp), label=apx)
plt.ylabel('hp')
plt.xlabel('Freq (Hz)')
plt.title('Waveform Template '+eventname)
```

The total mass of the BBHs is: 100
The sampling rate of the Waveform template is: 0.25



```
In [62]: #Computing BBH Mergers detection range:

f = freqs.copy() #Choosing a detector noise power spectrum

df = f[2]-f[1] #Choosing frequency step size

#Printing some information about the waveform and PSD:

print "The sampling rate of the PSD is: " ,df

print "The total mass of the BBHs is:",totalmass

print "The sampling rate of the Waveform template is:", dfWaveform

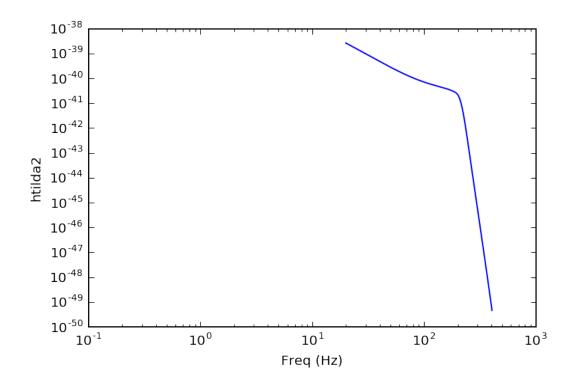
print"For accurate data the maximum frequency of the waveform template should not alway

SNRdet = 8. #Signal-to-noise ratio

Favg = 2.2648 #Conversion constant between maximum amplitude and average horizion

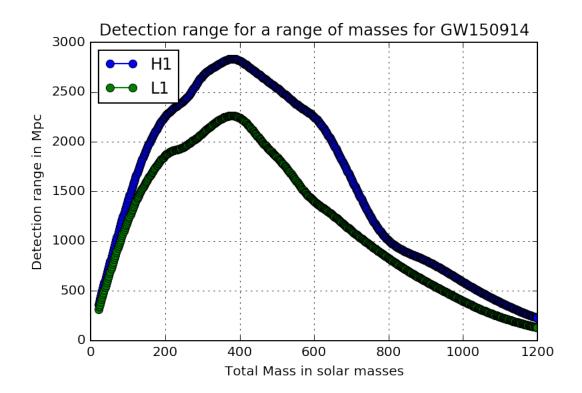
#Restricting the maximum and minimum frequency for the waveform tempelate:
```

```
f_waveform_min = min(hp.sample_frequencies) #Hz
         f_waveform_max=max(hp.sample_frequencies) #Hz
         print"Minimum frequency of the waveform template is: ",min(hp.sample_frequencies), "Hz"
         print "Maximum frequency of the waveform template is:", max(hp.sample_frequencies), "Hz"
         print "Maximum frequency of the PSD is: 2048 Hz"
         fr = np.nonzero(np.logical_and(f >= f_waveform_min , f <= f_waveform_max)) #Constructing</pre>
         ffr = f[fr] #Applying the frequency domain to the detector noise power spectrum
         #Calculation:
         # Calcualting Htilda and plotting it:
         htilda=b
         htilda2=np.power(htilda,2)
         pylab.loglog(hp.sample_frequencies, htilda2, label=apx)
         plt.ylabel('htilda2')
         plt.xlabel('Freq (Hz)')
         #Calculating the BBH detection horizion and range over both detectors:
         dets = ['H1', 'L1']
         for det in dets:
             if det is 'L1': sspec = Pxx_L1.copy() #PSD Data for L1
                             sspec = Pxx_H1.copy() #PSD Data for H1
             sspecfr = sspec[fr] #Applying frequency domain to the PSD Data
             D_BNS = np.sqrt(4.*np.sum(htilda2/sspecfr)*df)/SNRdet #Calculating horizion range
             R_BNS = D_BNS/Favg #Calculating detection range from horizion distance and converse
             print(det+' BBH inspiral horizon = {0:.1f} Mpc, BBH inspiral range = {1:.1f} Mpc'
The sampling rate of the PSD is: 0.25
The total mass of the BBHs is: 100
The sampling rate of the Waveform template is: 0.25
For accurate data the maximum frequency of the waveform template should not always be less than
Minimum frequency of the waveform template is: 0.0 Hz
Maximum frequency of the waveform template is: 512.0 Hz
Maximum frequency of the PSD is: 2048 Hz
H1 BBH inspiral horizon = 3202.6 Mpc, BBH inspiral range = 1414.1 Mpc
L1 BBH inspiral horizon = 2748.8 Mpc, BBH inspiral range = 1213.7 Mpc
```



```
In [63]: #Calcualting the BBH detection range for a range of masses: Choosing the range of masses
         #To avoid problems make sure your the total mass of the BBH merger is no less than 20 %
         #the sampling rate matches that of the PSD
         m1=10
         m2 = 10
         TMass_H1=[] #Creating arrays for Masses for H1
         DRange_H1=[] #Creating arrays for detection ranges for H1
         TMass_L1=[] #Creating arrays for Masses for L1
         DRange_L1=[] #Creating arrays for detection range for L1
         while m1<600 and m2<600:
             dfWaveform=0.25
             for apx in ['IMRPhenomPv2']:
                 hp, hc = get_fd_waveform(approximant=apx,
                                           {\tt mass1=m1},
                                           mass2=m2,
                                           spin1z=1.0,
                                           delta_f=dfWaveform,
                                           f_lower=10.)
                 a=hp.sample_frequencies
                 b=np.abs(hp)
                 totalmass=m1+m2 #Total mass of the system
             f = freqs.copy() #Choosing a detector noise power spectrum
             df = f[2]-f[1] #Choosing frequency step size
             SNRdet = 8. #Signal to noise ratio
```

```
Favg = 2.2648 #Conversion constant between maximum amplitude and average horizion
#The maximum and minimum frequency for the waveform tempelate:
    f_waveform_min = min(hp.sample_frequencies) #Hz
    f_waveform_max=max(hp.sample_frequencies) #Hz
    fr = np.nonzero(np.logical_and(f >= f_waveform_min , f <= f_waveform_max)) #Construc
    ffr = f[fr] #Applying the frequency domain to the detector noise power spectrum
#Calculating the BBH detection horizion and range over both detectors looping over a ro
    htilda=b
    htilda2=np.power(htilda,2)
    sspec = Pxx_H1.copy() #PSD Data for H1
    sspecfr = sspec[fr] #Applying frequency domain to the PSD Data for H1
    D_BBH = np.sqrt(4.*np.sum(htilda2/sspecfr)*df)/SNRdet #Calculating horizion range
    R_BBH = D_BBH/Favg #Calculating detection range from horizion distance and converse
    TMass_H1.append(totalmass) #Adding the mass to the H1 array
    DRange_H1.append(R_BBH) #Adding the detection range to the H1 array
    sspec = Pxx_L1.copy() #PSD Data for L1
    sspecfr = sspec[fr] #Applying frequency domain to the PSD Data for L1
    D_BBH = np.sqrt(4.*np.sum(htilda2/sspecfr)*df)/SNRdet #Calculating horizion range
    R_BBH = D_BBH/Favg #Calculating detection range from horizion distance and converse
    TMass_L1.append(totalmass) #Adding the mass to the L1 array
    DRange_L1.append(R_BBH) #Adding the detection range to the L1 array
    m1 += 1
    m2+=1
plt.plot(TMass_H1,DRange_H1,'-0',label='H1')
plt.plot(TMass_L1,DRange_L1,'-0',label='L1')
plt.ylabel('Detection range in Mpc')
plt.xlabel('Total Mass in solar masses')
plt.title('Detection range for a range of masses for '+eventname)
plt.legend(loc='upper left')
plt.grid('on')
```



```
In [64]: #References:
```

```
#M Vallisneri et al. "The LIGO Open Science Center", proceedings of the 10th LISA Sympole #https://github.com/ligo-cbc/binder/blob/master/Make_waveform.ipynb #https://notebooks.azure.com/nitz/libraries/pycbc #https://dcc.ligo.org/LIGO-T1100338/public #https://arxiv.org/abs/1003.2480 #https://arxiv.org/abs/gr-qc/0509116 #https://arxiv.org/abs/1203.2674 #https://losc.ligo.org/s/events/GW150914/LOSC_Event_tutorial_GW150914.html #"This research has made use of data, software and/or web tools obtained from the LIGO #(https://losc.ligo.org), a service of LIGO Laboratory and the LIGO Scientific Collaboratory
```