

Common Mathematical Subjects

Trigonometry

Identities

$$\cos^2(\theta) + \sin^2(\theta) = 1$$

$$1 + \tan^2(\theta) = \sec^2(\theta)$$

$$1 + \cot^2(\theta) = \csc^2(\theta)$$

Addition Formulas

$$\cos(A + B) = \cos(A) \cdot \cos(B) - \sin(A) \cdot \sin(B)$$

$$\sin(A + B) = \sin(A) \cdot \cos(B) + \cos(A) \cdot \sin(B)$$

Double Angle Formulas

$$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta)$$

$$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$$

Half-Angle Formulas

$$\cos^2(\theta) = \frac{1 + \cos(2\theta)}{2}$$

$$\sin^2(\theta) = \frac{1 - \cos(2\theta)}{2}$$

Hyperbolic Function

$$\sinh(x) = \frac{e^x - e^{-x}}{2}$$

$$\cosh(x) = \frac{e^x + e^{-x}}{2}$$

$$\tanh(x) = \frac{\sinh(x)}{\cosh(x)} = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

$$\coth(x) = \frac{\cosh(x)}{\sinh(x)} = \frac{e^x + e^{-x}}{e^x - e^{-x}}$$

$$\operatorname{sech}(x) = \frac{1}{\cosh(x)}$$

$$\operatorname{cosech}(x) = \frac{1}{\sinh(x)}$$

Eular Formulas

$$e^{ix} = \cos(x) + i \sin(x)$$

$$e^{-ix} = \cos(x) - i \sin(x)$$

$$\sin(x) = \frac{e^{ix} - e^{-ix}}{2i}$$

$$\cos(x) = \frac{e^{ix} + e^{-ix}}{2}$$

$$\tan(x) = \frac{1}{i} \frac{e^{ix} - e^{-ix}}{e^{ix} + e^{-ix}}$$

Limit

$$\lim_{x \rightarrow c} f(x) = L$$

and

$$\lim_{x \rightarrow c} g(x) = M$$

1. Summation Rule: $\lim_{x \rightarrow c} (f(x) + g(x)) = L + M$

2. Difference Rule: $\lim_{x \rightarrow c} (f(x) - g(x)) = L - M$

3. Product Rule: $\lim_{x \rightarrow c} (f(x) \cdot g(x)) = L \cdot M$

4. Constant Multiplication Rule: $\lim_{x \rightarrow c} k \cdot f(x) = k \cdot L$

5. Quotient Rule: $\lim_{x \rightarrow c} \left(\frac{f(x)}{g(x)} \right) = \frac{L}{M}$

