

CS6745: Mining Massive DataSets

Tutorial 9

November 13, 2019

- Write your name and roll number in the space provided
- Be neat, and use the space judiciously.
- **Rough sheets won't be evaluated.**

1. Suppose there are 100 items, numbered 1 to 100, and also 100 baskets, also numbered 1 to 100. Item i is in basket b if and only if i divides b with no remainder. Thus, item 1 is in all the baskets, item 2 is in all fifty of the even-numbered baskets, and so on. Basket 12 consists of items 1, 2, 3, 4, 6, 12, since these are all the integers that divide 12. Answer the following questions,

- (a) (2 marks) If the support threshold is 5, which items are frequent?

Ans: Items $\{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20\}$ appears in at-least 5 buckets.
So, If the support threshold is 5, frequent items are:
 $\{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20\}$.

- (b) (3 marks) If the support threshold is 5, which pairs of items are frequent?

Ans: For the set $\{1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20\}$ in Q1.

Pairs which will appear in at-least 5 buckets and hence frequents items pairs if support threshold is 5 are:

$\{(1,2),(1,3),(1,4),(1,5),(1,6),(1,7),(1,8),(1,9),(1,10),(1,11),(1,12),(1,13),(1,14),(1,15),(1,16),$
 $(1,17),(1,18), (1,19),(1,20),(2,4),(2,6),(2,8),(2,10),(2,12),(2,14),(2,16),(2,18),(2,20),(3,6),$
 $(3,9),(3,12),(3,15),(3,18),(4,8), (4,12),(4,16),(4,20),(5,10),(5,15),(5,20),(6,12),(6,18),(7,14),$
 $(8,16),(9,18),(10,20)\}$

2. (5 marks) Apply the A-Priori Algorithm with support threshold 5 to the data present in Q1.

Ans:

Possible items set of size 1:

1,2,3,...,100

Actual frequent items set of size 1 with support threshold of 5 are:

1,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20

Possible items set of size 2:

Any two elements pairs from 1 element frequent size elements.

Actual frequent items set of size 2 with support threshold of 5 are:

{(1,2),(1,3),(1,4),(1,5),(1,6),(1,7),(1,8),(1,9),(1,10),(1,11),(1,12),(1,13),(1,14),(1,15), (1,16), (1,17), (1,18), (1,19),(1,20),(2,4),(2,6),(2,8),(2,10),(2,12),(2,14),(2,16),(2,18), (2,20),(3,6), (3,9),(3,12), (3,15),(3,18),(4,8), (4,12),(4,16),(4,20),(5,10),(5,15),(5,20), (6,12),(6,18),(7,14), (8,16),(9,18), (10,20)}

Possible items set of size 3:

Any three elements sets formed from elements of sets in two items set.

Actual frequent items set of size 3 with support threshold of 5 are:

{(1, 2, 3), (1, 2, 4), (1, 2, 5), (1, 2, 6), (1, 2, 7), (1, 2, 8), (1, 2, 9), (1, 2, 10), (1, 2, 12), (1, 2, 14), (1, 2, 16), (1, 2, 18), (1, 2, 20), (1, 3, 4), (1, 3, 5), (1, 3, 6), (1, 3, 9), (1, 3, 12), (1, 3, 15), (1, 3, 18), (1, 4, 5), (1, 4, 6), (1, 4, 8), (1, 4, 10), (1, 4, 12), (1, 4, 16), (1, 4, 20), (1, 5, 10), (1, 5, 15), (1, 5, 20), (1, 6, 9), (1, 6, 12), (1, 6, 18), (1, 7, 14), (1, 8, 16), (1, 9, 18), (1, 10, 20), (2, 3, 4), (2, 3, 6), (2, 3, 9), (2, 3, 12), (2, 3, 18), (2, 4, 5), (2, 4, 6), (2, 4, 8), (2, 4, 10), (2, 4, 12), (2, 4, 16), (2, 4, 20), (2, 5, 10), (2, 5, 20), (2, 6, 9), (2, 6, 12), (2, 6, 18), (2, 7, 14), (2, 8, 16), (2, 9, 18), (2, 10, 20), (3, 4, 12), (3, 5, 15), (4, 5, 10), (4, 5, 20), (4, 6, 12), (5, 10, 20), (6, 9, 18)}

Possible items set of size 4:

Any 4 elements set formed from elements of 3 elements sets.

Actual frequent items set of size 4 with support threshold of 5 are:

{(1, 2, 3, 4), (1, 2, 3, 6), (1, 2, 3, 9), (1, 2, 3, 12), (1, 2, 3, 18), (1, 2, 4, 5), (1, 2, 4, 6), (1, 2, 4, 8), (1, 2, 4, 10), (1, 2, 4, 12), (1, 2, 4, 16), (1, 2, 4, 20), (1, 2, 5, 10), (1, 2, 5, 20), (1, 2, 6, 9), (1, 2, 6, 12), (1, 2, 6, 18), (1, 2, 7, 14), (1, 2, 8, 16), (1, 2, 9, 18), (1, 2, 10, 20), (1, 3, 4, 12), (1, 3, 5, 15), (1, 4, 5, 10), (1, 4, 5, 20), (1, 4, 6, 12), (1, 5, 10, 20), (1, 6, 9, 18), (2, 3, 4, 12), (2, 4, 5, 10), (2, 4, 5, 20), (2, 4, 6, 12), (2, 5, 10, 20), (2, 6, 9, 18), (4, 5, 10, 20)}

Possible items set of size 5:

Any 5 elements set formed from elements of 4 elements sets.

Actual frequent items set of size 5 with support threshold of 5 are:

{(1, 2, 3, 4, 12), (1, 2, 4, 5, 10), (1, 2, 4, 5, 20), (1, 2, 4, 6, 12), (1, 2, 5, 10, 20), (1, 2, 6, 9, 18), (1, 4, 5, 10, 20), (2, 4, 5, 10, 20)}

Possible items set of size 6:

Any 6 elements set formed from elements of 5 elements sets.

Actual frequent items set of size 6 with support threshold of 5 are:

{1, 2, 4, 5, 10, 20}

Since there is only one frequent items set, we can stop here.