

A Book of Abstract Algebra | (2nd Edition)



Chapter 29, Problem 7EA



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Problem

Name an extension of \mathbb{Q} over which π is algebraic of degree 3.

Step-by-step solution

Step 1 of 2

The objective is to name an extension of \mathbb{Q} over which π is algebraic of degree 3.

[Comment](#)

Step 2 of 2

Now, π is algebraic over $\mathbb{Q}(\pi^3)$ of degree 3.

It is not in $\mathbb{Q}(\pi^3)$ as x is not a polynomial in x^3 but it is a zero of $x^3 - \pi^3$ in $\mathbb{Q}(\pi^3)[x]$.

Therefore, the extension of \mathbb{Q} over which π is algebraic of degree 3 is $\mathbb{Q}(\pi^3)$.

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