A Book of Abstract Algebra (2nd Edition)

Chapter 24, Problem 2ED

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Problem

In each of the following, let A be an integral domain:

Use part 1 to give an example of an infinite integral domain with finite characteristic.

Step-by-step solution

Step 1 of 1

Let $A = {}_{5}$, ${}_{5}$ is an integral domain and has characteristic 5, then ${}_{5}[x]$ has characteristic 5. ${}_{5}[x]$ is an infinite integral domain because the elements ${}_{1}, x, x^{2}, x^{3}, \ldots$ are all distinct and any element $a_{0} + xa_{1} + \ldots + a_{n}x^{n} \in {}_{5}[x]$ where $a_{0}, a_{1}, \ldots, a_{n} \in {}_{5}$

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