Using open data to rapidly benchmark biomolecular simulations: Phospholipid internal dynamics

Hanne S. Antila,[†] Tiago Ferreira,[‡] Matti Javanainen,[¶] O. H. Samuli Ollila,[§] and Markus S. Miettinen[*,†]

†*Department of Theory and Bio-Systems, Max Planck Institute of Colloids and Interfaces, 14424 Potsdam, Germany*
‡*NMR Group — Institute for Physics, Martin-Luther University Halle–Wittenberg, 06120 Halle (Saale), Germany*
¶*Add Matti to author list?*
§*Institute of Biotechnology, University of Helsinki, 00014 Helsinki, Finland*

E-mail: markus.miettinen@iki.fi

Abstract

Molecular dynamics (MD) simulations are widely used to study the atomistic structure and dynamics of biomembranes. It remains unknown, however, how well the conformational dynamics observed in MD simulations correspond to those occurring in real life phospholipids. The accuracy of such time scales in MD can be assessed by comparing against the effective correlation times τ_e of the C-H bonds measured in nuclear magnetic resonance experiments (J. Chem. Phys. 142 044905 (2015)).

Here, we extend this previous analysis by considering carefully the error estimation of MD-determined τ_e, and analyze the conformational dynamics of phospholipids as produced by several commonly used MD models (force fields). None of the tested force fields reproduced all the effective correlation times within experimental error, much like they do not provide accurate conformational ensemble (J. Phys. Chem. B 119 15075 (2015)). However, the dynamics observed in CHARMM36 and Slipids were more realistic than those seen in the Amber Lipid14, OPLS-based MacRog, and GROMOS-based Berger force fields, where dynamics of the

glycerol backbone was unrealistically slow.

1   Introduction

Ever since the conception of Protein Data Bank (PDB)[?][?] and GenBank,[?][?] open access to standardised and searchable pools of experimental data has revolutionized research in life sciences. The databanks,[?] constantly growing and improving in fidelity[?][?] due to collaborative effort, enable scientific progress that is well beyond the resources of one single research group, giving rise to entirely new ways of doing science in the form of bio- and cheminformatics, and enabling data-driven development of characterisation techniques,[?] drugs,[?] and materials.[?] The idea of public availability and conservation of data has recently extended also to molecular dynamics (MD) simulation trajectories of biomolecules, and discussion on how and by whom these databases for dynamic information would be set up is currently active.[?][?][?][?][?]

1.Mention GPCRmd[?] ? SAMULI: I think yes.

Since 2013 the NRMlipids Project (`nmrlipids.blogspot.fi`) has promoted an open collaboration approach, where the whole research process, from the initial ideas and discussions

1

to the analysis methods, data and publications, are publicly available all the time.[?] While the main focus of the NMRlipids Project has been in conformational ensembles of lipid headgroups and ion binding to lipid membranes,[?][?][?] it has also accumulated a collection of atomistic MD simulations of lipid membranes containing hundreds of trajectories (`zenodo.org/communities/nmrlipids`). These data are also partially indexed at `www.nmrlipids.fi`. Such databanks are particularly relevant for disordered molecules, such as biological lipids composing cellular membranes, which cannot be descibed by coordinates of single structure in contrast to folded proteins or DNA strands. Realistic MD simulations can provide conformational ensemble and dynamics of such molecules as well as enable studies of their biological functions in complex biomolecules assemblies. However, current MD simulation force fields largely fail to capture conformational ensembles of lipid headgroups and disordered proteins.[?][?][?] Therefore, the quality of MD simulations in databanks and other applications must be carefully assessed against experimental data. For lipid bilayers, such evaluation is possible against NMR and scattering data.[?]

Here, we demonstrate how publicly available set of MD simulation data can be utilized to rapidly evaluate how fast individual lipid molecules sample their conformational ensemble against experimental data in different force fields with unprecedented extent. MD simulations with correct lipid dynamics are desired, for example, for the interpretation of NMR or other experiments detecting molecular dynamics and to understand dynamics of biological processes where lipid deformations have rate limiting role such as membrane fusion.[?] In addition, information on dynamics is crucial to assess if simulations have converged.

Our comprehensive comparison of dynamics between different MD models for phosphatidylcholine lipids with varying biologically relevant compositions and conditions paves the way for the development of more realistic lipid force fields. Furthermore, the analysis of extensive set of data from different models shed light on the complex dynamics lipid in their biological relevant disordered state. Our results demonstrate the power of publicly available simulation trajectories in creating new knowledge at a lowered computational cost and high potential for automation. We believe that our work paves the way for novel applications of publicly available MD simulations databanks, as well as demonstrates their usefullness not only for lipid bilayers but also for other biomolecular systems.

2 Methods

2.1 Evaluation of conformational dynamics of lipids against NMR data

We analyze lipid dynamics based on two quantities available from published ^{13}C-NMR experiments:[?][?][?] The effective C–H bond correlation time τ_e and the spin-lattice relaxation rate R_1, both directly quantifiable from atomistic MD simulations. The τ_e are effectively an average over all the time scales relevant for the lipid internal dynamics, and respond intuitively to changes in these: Increasing τ_e always signals some type of slowdown in the C–H bond dynamics.[?] The R_1 rates (or the corresponding T_1 times) have been traditionally used to assess both the conformational dynamics of lipids in experiments[?][?][?][?][?] and the dynamics produced by MD models in simulations.[?][?][?][?] In contrast to τ_e, the R_1 are sensitive to processes within a rather narrow time scale window set by the magnet frequency, and changes in R_1 are not intuitively related to changes in process speeds: A decrease in R_1 tells that the amount of processes in the sensitive time window decreases, but not if the corresponding processes become faster or slower.

^{13}C NMR experiments investigating lipid conformational dynamics take advantage of the fact that the relaxation of ^{13}C magnetization dominantly happens via the dipolar coupling of the carbon with the magnetic moments of the protons bound to it, with the symmetry axis of the interaction aligning with the C–H bond.

The spectral density depicting the ^{13}C relaxation rates (at frequency ω) is expressed as

$$j(\omega) = 2 \int_0^\infty \cos(\omega\tau)g(\tau)\mathrm{d}\tau, \qquad (1)$$

which is the Fourier transformation of the C–H bond second order autocorrelation function at time τ

$$g(\tau) = \langle P_2\left(\vec{\mu}(t) \cdot \vec{\mu}(t+\tau)\right)\rangle, \qquad (2)$$

where $\vec{\mu}(t)$ is the unit vector in the direction of the C–H bond at time t and P_2 is the second order Legendre polynomial. The angular brackets depict averaging over time. The autocorrelation function can be expressed as the product of two functions

$$g(\tau) = g_\mathrm{f}(\tau)g_\mathrm{s}(\tau), \qquad (3)$$

where $g_\mathrm{f}(\tau)$ characterizes fast decays owing to, for example, the molecular rotations, and $g_\mathrm{s}(\tau)$ describes slow decays that originate from, e.g., lipid diffusion. The two components, along with the oscillation due to magic angle spinning at the $\sim$kHz region, are depicted in Fig. **??**. Correlation time of 4.2 ms has been estimated for multilamellar POPC samples at 300 K for the slow modes, whereas in liquid crystalline lipid bilayers the faster $g_\mathrm{f}(\tau)$ decays to a plateau value S_CH^2 within a few hundred nanoseconds.[?] The C–H bond order parameters

$$S_\mathrm{CH} = \frac{1}{2}\langle 3\cos^2\theta(t) - 1\rangle, \qquad (4)$$

where $\theta(t)$ is the angle between the bond and the bilayer normal, are measured in NMR experiments from this plateau. As S_CH describes the conformational ensemble of the molecule, the fast-decaying component of the rotational correlation function intuitively depicts the time needed to sample these conformations. The characteristic time can be quantified via the effective correlation time

$$\tau_\mathrm{e} = \int_0^\infty \frac{g_\mathrm{f}(\tau) - S_\mathrm{CH}^2}{1 - S_\mathrm{CH}^2}\mathrm{d}\tau. \qquad (5)$$
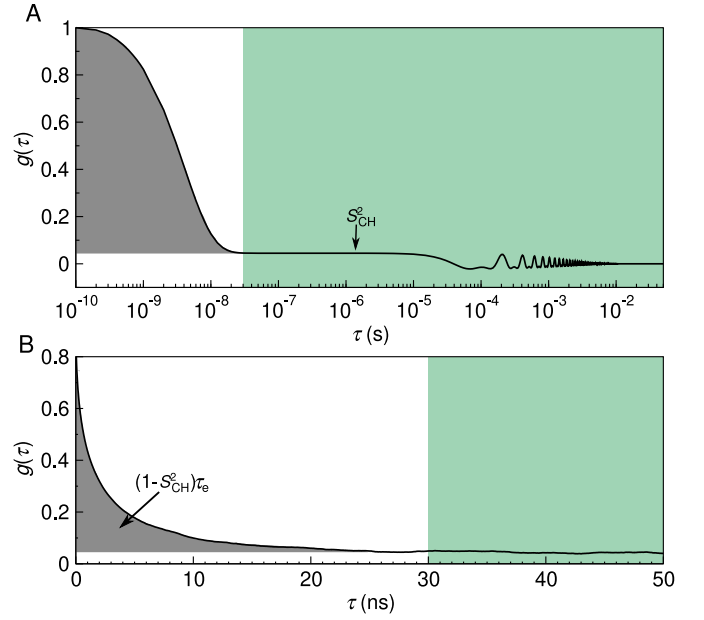
The integrand can be viewed as a reduced and

Figure 1: The autocorrelation function $g(\tau)$ a) The fast mode (white background) and the slow mode (shaded green) of the correlation function along with the oscillation owing to magic angle spinning. The fast mode decays to a plateau quantifying the S_CH while the slow mode gives the final descent to zero. b) Illustration of typical C–H bond autocorrelation function obtained from a MD simulation. The gray area under the curve gives a way of quantifying the τ_e.

normalized correlation function

$$g_\mathrm{f}'(\tau) = \frac{g_\mathrm{f}(\tau) - S_\mathrm{CH}^2}{1 - S_\mathrm{CH}^2}. \qquad (6)$$

That is, τ_e is defined as the area under $g_\mathrm{f}'(\tau)$, as graphically depicted in Fig. **??**b. **2.Maybe also add 1C that explicitly shows g_f'?** It is easily seen that in the presence of more long-lived correlations τ_e grows, signaling that more time is needed for full conformational sampling.

The spin-lattice relaxation rate R_1 defines the time-scale on which ^{13}C longitudal magnetization equilibrates. It is defined as

$$R_1 = \frac{d_\mathrm{CH}^2 N_\mathrm{H}}{20}\left[j(\omega_\mathrm{H} - \omega_\mathrm{C})\right. \\ \left. + 3j(\omega_\mathrm{C}) + 6j(\omega_\mathrm{H} + \omega_\mathrm{C})\right], \qquad (7)$$

where N_H is the number of bound hydrogens, ω_H and ω_C are the Larmor frequencies for ^{1}H

and ^{13}C, and d_{CH} is the rigid dipolar coupling constant. For the methylene bond, $d_{CH}/2\pi$ approximately equals to -22 kHz. **3.why there is a minus sign above?**

The dependency of R_1 on the spectral densities j at the Larmor frequencies means that the R_1 value depicts the relative amounts of relaxation processes with time-scales near the inverses of these frequencies. Since the Larmor frequencies depend on the field strength used in the NMR measurements, this typically makes R_1 sensitive to $\sim$1–10 ns time-scales. Importantly, a change in R_1 thus indicates a difference in the relative amounts of processes within the detection window, and therefore does not give information on the modulation of the total sampling rate.

2.2 Experimental data acquisition and analysis

All the experimental quantities were collected from the literature **4.Except are they, or mostly from Tiago and re-analysed from raw data?** sources referred at the respective figures **5.How to refer to experimental data from Tiago?**.

2.3 Simulational data acquisition and analysis

The simulation trajectories used in this work were collected from the Zenodo repository (`zenodo.org`) with majority of the data originating from the NMRlipids Project[?][?] (`nmrlipids.blogspot.fi`). Table ?? details, with references to the trajectory files, the simulations of pure POPC bilayers at/near room temperature and at full hydration, whereas Table ?? lists simulations including cholesterol; Table ?? simulations with varying hydration; and Table ?? at increasing NaCl concentration. Additional computational details for each of the simulations are available at the cited Zenodo entry.

The simulation data were analyzed using in-house scripts. These are available on GitHub[?] along with a Python notebook outlining an example analysis run. After downloading the necessary files from Zenodo, the trajectory was

Table 1: Analyzed simulations of POPC lipid bilayers at standard conditions.

force field	$N_l{}^a$	$N_w{}^b$	T^c(K)	$t_{anal}{}^d$(ns)	files^e
Berger-X[?]	256	10240	300	300	[?]
CHARMM36[?]	256	8704	300	300	[?]
MacRog[?]	128	5120	300	500	[?]
Lipid14[?]	72	2234	303	50	[?]
Slipids[?]	200	9000	310	500	[?]
ECC[?]	128	6400	300	300	[?]

^{a}Number of POPC molecules.
^{b}Number of water molecules.
^{c}Simulation temperature.
^{d}Trajectory length used for analysis.
^{e}Reference for the openly available simulation files.

Table 2: Analyzed simulations of cholesterol-containing POPC bilayers.

force field POPC/cholesterol	$c_{chol}{}^a$	$N_{chol}{}^b$	$N_l{}^c$	$N_w{}^d$	T^e(K)	$t_{anal}{}^f$(ns)	files^g
Berger-POPC-07[?]	0%	0	128	7290	298	50	[?]
/Höltje-CHOL-13[?][?]	50%	64	64	10314	298	50	[?]
CHARMM36[?]	0%	0	128	5120	303	140	[?]
/CHARMM36[?]	50%	80	80	4496	303	200	[?]
MacRog[?]	0%	0	128	6400	310	500	[?]
/MacRog[?]	50%	64	64	6400	310	500	[?]
Slipids[?]	0%	0	200	9000	310	500	[?]
/Slipids[?]	50%	200	200	18000	310	500	[?]

^{a}Bilayer cholesterol content (mol %).
^{b}Number of cholesterol molecules.
^{c}Number of POPC molecules.
^{d}Number of water molecules.
^{e}Simulation temperature.
^{f}Trajectory length used for analysis.
^{g}Reference for the openly available simulation files.

processed with Gromacs `gmx trjconv` to make the molecules whole. The C–H bond order parameters S_{CH}, see Eq. (??), were then calculated with the `calcOrderParameters.py`[?] script that uses the MDanalysis[?] Python library. The C–H bond correlation functions $g(\tau)$, see Eq. (??), were calculated with Gromacs5.1.4[?] `gmx rotacf`; note that on simulational (fast) time scales $g = g_s g_f = g_f$. To obtain the g'_f, the S_{CH} were used to normalize the g_f following Eq. (??).

The effective correlation times τ_e were then calculated by integrating $g'_f(\tau)$, see Eqs. (??) and (??), over time from $\tau = 0$ until $\tau = t_0$. Here $t_0 = \min\{t \,|\, g'(t) = 0\}$, that is, t_0 is the first time point at which g'_f reached zero. If g'_f did not reach zero within $t_{anal}/2$, the τ_e was not

Table 3: Analyzed simulations of lipid bilayers under varying hydration level.

force field	lipid	$n_{w/l}{}^a$	$N_l{}^b$	$N_w{}^c$	T^d(K)	$t_{anal}{}^e$(ns)	files^f
Berger-POPC-07[?]	POPC	57	128	7290	298	50	[?]
	POPC	7	128	896	298	60	[?]
Berger-X[?]	POPC	40	256	10240	300	300	[?]
Berger-DLPC-13[?]	DLPC^g	24	72	1728	300	80	[?]
	DLPC[??]	16	72	1152	300	80	[?]
	DLPC[??]	12	72	864	300	80	[?]
	DLPC[??]	4	72	288	300	80	[?]
CHARMM36[?]	POPC	40	128	5120	303	140	[?]
	POPC	34	128	5120	300	500	[?]
	POPC	31	72	2232	303	20	[?]
	POPC	15	72	1080	303	20	[?]
	POPC	7	72	504	303	20	[?]
MacRog[?]	POPC	50	288	14400	310	40	[?]
	POPC	25	288	7200	310	50	[?]
	POPC	15	288	4320	310	50	[?]
	POPC	10	288	2880	310	50	[?]
	POPC	5	288	1440	310	50	[?]

^{a}Water/lipid molar ratio.
^{b}Number of lipid molecules.
^{c}Number of water molecules.
^{d}Simulation temperature.
^{e}Trajectory length used for analysis.
^{f}Reference for the openly available simulation files.
^{g}1,2-didodecanoyl-sn-glycero-3-phosphocholine.

**6. The data points here do not match those in Fig. ??B.
MacRog in Fig. ??B: 50, 25, 10, 5 w/l, and C36 in
Fig. ??B: 40, 31, 15, 7 w/l.**

7. The t_{anal} for MacRog here do not match Ref. ?

$(100\,\text{ns} \rightarrow 50\,\text{ns})$?

Table 4: Analyzed simulations of POPC lipid bilayers at varying NaCl concentration.

force field POPC/ions	[NaCl]^a (mM)	$N_{Na}{}^b$	$N_l{}^c$	$N_w{}^d$	T^e(K)	$t_{anal}{}^f$(ns)	files^g
CHARMM36[?]	0	0	128	5120	303	140	[?]
/CHARMM36[?]	346	13	72	2085	303	60	[?]
	692	26	72	2085	303	60	[?]
	947	37	72	2168	303	60	[?]
MacRog[?]	0	0	128	6400	310	500	[?]
/OPLS[?]	103	27	288	14554	310	50	[?]
	207	54	288	14500	310	50	[?]
	311	81	288	14446	310	40	[?]
	416	108	288	14392	310	50	[?]
Slipids[?]	0	0	200	9000	310	500	[?]
/AMBER[?]	130	21	200	9000	310	100	[?]
	999	162	200	9000	310	200	[?]

^{a}NaCl concentration, calculated as [NaCl]= $N_{Na} \times$[water]$/N_w$, where [water] = 55.5 M.
^{b}Number of Na$^+$ ions, equal to number of Cl$^-$ ions.
^{c}Number of POPC molecules.
^{d}Number of water molecules.
^{e}Simulation temperature.
^{f}Trajectory length used for analysis.
^{g}Reference for the openly available simulation files.

determined, and we report only its upper and lower error estimates.

To quantify the error on τ_e, we first estimate the error on $g'_f(\tau)$, where we account for two sources of uncertainty, $g_f(\tau)$ and S^2_{CH}. Performing linear error propagation on Eq. (??) gives

$$\Delta g'_f(\tau) = \left| \frac{1}{1 - S^2_{CH}} \right| \Delta g_f(\tau)$$
$$+ \left| \frac{2\left(g_f(\tau) - 1\right) S_{CH}}{\left(1 - S^2_{CH}\right)^2} \right| \Delta S_{CH}. \tag{8}$$

Here the ΔS_{CH} was determined as in the NMR-lipids Project:[?] as the standard error of the mean of the S_{CH} of all the N_l individual lipids in the system. Similarly, we quantified the error on $g_f(\tau)$ by first determining an individual correlation function $g_f^m(\tau)$ for each lipid m over the whole trajectory, and then obtaining the error estimate $\Delta g_f(\tau)$ as the standard error of the mean over the N_l lipids. Importantly, this gives an uncertainty estimate at each time point τ.

To obtain the lower bound on τ_e, we integrate the function $g'_f(\tau) - \Delta g'_f(\tau)$ over time from $\tau = 0$ until $\tau = t_l$. Here

$$t_l = \min \left\{ \{t \mid g'_f(t) - \Delta g'_f(t) = 0\}, \frac{t_{anal}}{2} \right\}. \tag{9}$$

That is, t_l equals the first time point at which the lower error estimate of g'_f reached zero; or $t_l = t_{anal}/2$, if zero was not reached by that point.

To obtain the upper error estimate on τ_e, we first integrate the function $g'_f(\tau) + \Delta g'_f(\tau)$ over time from $\tau = 0$ until $t_u = \min\{t_0, t_{anal}/2\}$. Note, however, that this is not yet sufficient, because there could be slow processes that our simulation was not able to see. Although these would contribute to τ_e with a low weight, their contribution over long times could still add up to a sizable effect on τ_e. That said, it seems feasible to assume (see Fig. ??A) that there are no longer-time contributions to g_f than something that decays with a time constant of 10^{-6} s. We use this as our worst case estimate to assess the upper bound for τ_e, and assume that all the decay from the time point

$t_u = \min\{t_0, t_{\text{anal}}/2\}$ onwards comes solely from this slowest process. The additional contribution to the upper bound for τ_e then reads $\Delta g'_f(t_u) \times (\exp(-t_u/10^{-6}\,\text{s}) - \exp(-1)) \times 10^{-6}\,\text{s}$.

8.Discuss the possibility of skewed error distributions?

The R_1 rates were calculated using Eq. (**??**). The spectral density $j(\omega)$ was obtained from the normalized correlation function g'_f by fitting it with a sum of $N = 71$ exponentials

$$g'_f(\tau) \approx \sum_{i=1}^{N} \alpha_i e^{-\tau/\tau_i}, \qquad (10)$$

with logarithmically spaced time-scales τ_i ranging from 0.1 ps to 1 μs, and then calculating the spectral density of this fit based on the Fourier transformation[?]

$$j(\omega) = 2(1 - S_{\text{CH}}) \sum_{i=1}^{N} \alpha_i \frac{\tau_i}{1 + \omega\tau_i}. \qquad (11)$$

The R_1 rate of a given C–H bond was first calculated separately for each lipid m (using Eq. (**??**) with $N_H = 1$, and $j^m(\omega)$ obtained for the normalized correlation function g'^m_f). The resulting N_l measurements per bond were then assumed independent: Their mean gave the R_1 rate of the bond, and standard error of the mean its uncertainty. The total R_1 rate of a given carbon was obtained as a sum of the R_1 rates of its C–H bonds. When several carbons contribute to the experimental R_1 rate of a carbon segment, the carbon-wise R_1 rates were averaged to obtain the segment-wise R_1 rate. The segment-wise error estimates were obtained by standard error propagation, starting from the uncertainties of the R_1 rates of the C–H bonds.

To gain some qualitative insight on the time scales at which the main contributions to the (headgroup) R_1 rates arise, we also looked at 'cumulative' R_1 rates, $R_1(\tau)$. These contained just those contributions in the sum of Eq. (**??**) for which $\tau_i < \tau$. Note that here the g'_f averaged over lipids was used; therefore, the 'cumulative' $R_1(\tau \to \infty)$ does not necessarily have exactly the same numerical value as the actual R_1.

Finally, we note that the fit of Eq. (**??**) pro-vides an alternative to estimating τ_e, because

$$\tau_e = \int_0^\infty g'_f(\tau)\,\mathrm{d}\tau \approx \sum_{i=1}^{N} \alpha_i \tau_i. \qquad (12)$$

When the simulation trajectory is not long enough for the correlation function to reach the plateau, integrating g'_f gives a lower bound estimate for τ_e, while the sum of Eq. (**??**) includes also (some) contribution from the longer-time components via the fitting process. However, in practice the fit is often highly unreliable in depicting the long tails of the correlation function, and thus we chose to quantify τ_e using the area under g'_f, and estimate its uncertainty as detailed above.

3 Results and Discussion

In the following, we discuss phospholipid conformational dynamics in six different MD force fields. We do this first for standard conditions (pure POPC bilayers, full hydration, no salt; see Table **??** for simulation details and Fig. **??** for results) and then proceed to cover a wider range of experimentally, biologically, and computationally relevant conditions. We investigate how the dynamics change when cholesterol is added to the bilayer (Table **??** and Fig. **??**), when hydration level is reduced (Table **??** and Fig. **??**), and when monovalent salt is added to the solution (Table **??** and Fig. **??**).

One should keep in mind that none of the force fields we study produces all the C–H bond order parameters, S_{CH}, within experimental accuracy.[?] This means that the structural ensembles simulated do not exactly match the structural ensemble occurring in reality.Consequently, the τ_e times and R_1 rates depict the dynamics of sampling a somewhat different phase space for each model. To this end, we avoid overly detailed discussion on the models and rather concentrate on common and qualitative trends.

Effective correlation times τ_e at standard conditions.

The left panels of Fig. **??** compare the τ_e obtained for fully hydrated POPC bilayers in experiments (black) and in the six different MD force fields (color).

Qualitatively, every force field captures the general shape of the τ_e profile: Dynamics slows down towards the glycerol backbone in both the headgroup and the tails. Quantitatively, MD has a tendency towards slightly too fast dynamics in the membrane core, but at the water-facing interface MD is typically too slow. CHARMM36 and Slipids show the best overall performance—although the τ_e in Slipids exhibit a qualitatively wrong (decreasing) trend from g_3 to g_1.

The detected slow glycerol backbone dynamics in MD is consistent with previous results for the Berger model.**?** It also agrees with the insufficient conformational sampling of glycerol backbone torsions observed in 500-ns-long CHARMMc32b2**? ?** simulations of a DOPC lipid.**?**

Note that the temperature varied across these openly available simulation data. However, it was in no case lower than in the experiment. Were the simulations done at the experimental 298 K, the overestimation of τ_e at the glycerol backbone by MD would get worse as τ_e increases at decreasing temperature —as indicated by the CHARMM36 data covering several temperatures. **9.HA: add new CHARMM36 data to plot**

R_1 rates at standard conditions.

The panels on the right side of Fig. **??** compare experimental and simulated R_1 rates under the same conditions as for the τ_e on the left.

There are certain qualitative features that all force fields predict correctly (for example that g_2 has the smallest R_1 among the glycerol and C9 among the oleoyl double bond segments), and certain that they all miss (that R_1 rates for the oleoyl segments C8, C10, and C11 are all roughly equal).

Quantitatively, there are a few cases where

both R_1 and τ_e (almost) match experiments, suggesting (almost) correct rotational dynamics at all relevant time scales. For example, Slipids performs well at the β and α segments; CHARMM36 for the g_3, g_2, C2 and C3; Lipid14 and ECC for the oleoyl double bond; and MacRog for the tail end segments.

Notably, there are also instances where the R_1 comparison distinctly differs from what is seen for τ_e: Some models that do very well for τ_e, do rather poorly for R_1. Conversely, a matching R_1 can be accompanied by a larger-than-experimental τ_e. To appreciate such differences, recall that in order to capture our experimental R_1 rates (measured at 125 MHz) a force field has to have correct rotational dynamics at the $(2\pi \times 125\ \text{MHz})^{-1} \approx 1\ \text{ns}$ time scale, whereas τ_e reflects all the sub-μs time scales (Fig. **??**).

MacRog for the β, α, g_3, and g_1 segments provides a prominent example where the R_1 rates are well reproduced, but τ_e times systematically overestimated. Such a combination suggests that MD does well at the 1 ns scale, but has too slow long-time dynamics.

The opposite—where τ_e matches experiments, but R_1 does not—is demonstrated by all five all-atom force fields for the γ segment, and by CHARMM36 for β and α. Therein a cancellation of error occurs in τ_e: The wrong dynamics at the 1 ns scale are compensated by wrong dynamics at the other time scales. As CHARMM36 overall performs rather well for both R_1 and τ_e, we proceed to study this shortcoming on the headgroup R_1 rates in some more detail.

Dynamics of headgroup segments in CHARMM36.

Figure **??**A zooms in on the headgroup (γ, β, α) segments, whose τ_e were not clearly visible on the scale of Fig. **??**. For all three, CHARMM36 matches the experimental τ_e, but overestimates R_1. No other force field does any better for γ, but for β and α Slipids provides almost perfect dynamics.

To investigate where the differences between force fields arise, we visualize the 'cumulative' $R_1(\tau)$ in Fig. **??**B. It is obtained, as detailed in
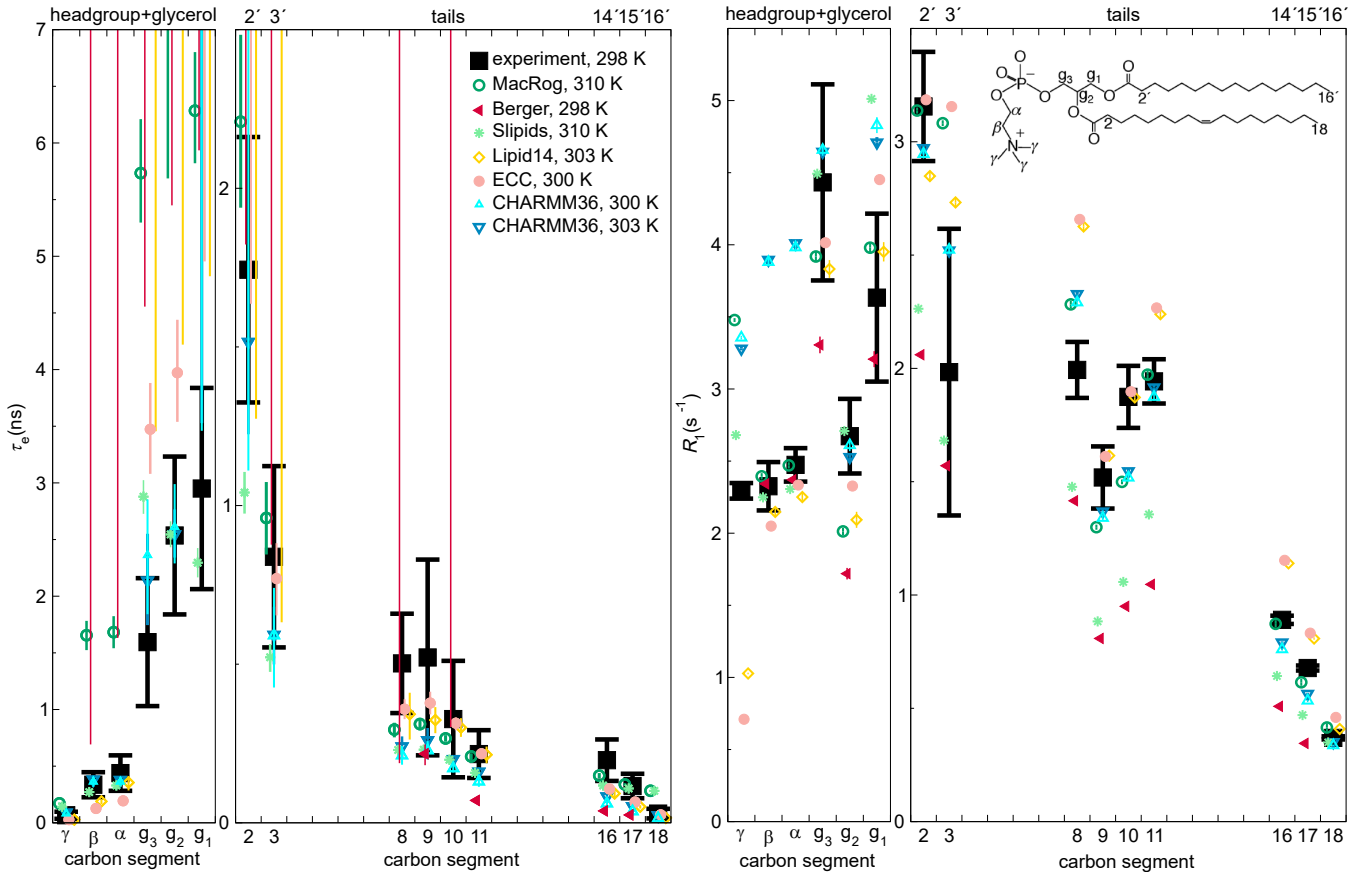
Figure 2: Effective correlation times (τ_{e}, left panels) and R_1 rates (right panels) in experiments (black) and MD simulations (colored) of POPC bilayers in L_α phase under full hydration. Inset on the right shows the POPC structure and carbon segment labeling. Each plotted value contains contributions from all the hydrogens within its carbon segment; the data for segments 8–11 are only from the sn-2 (oleoyl) chain, whereas the (experimentally non-resolved) contributions of both tails are included for segments 2–3 (2'–3' in the sn-1 chain) and 16–18 (14'–16'). Simulation data are only shown for the segments for which there exists experimental data. For τ_{e}, a simulation data point indicates the average over C–H bonds; however, if τ_{e} could not be determined for all bonds, only the error bar (extending from the mean of the lower to the mean of the upper error estimates) is shown. The Berger data for methyl segments (γ, C18, and C16') are left out, because the protonation algorithm used to construct the hydrogens post-simulation in united atom models does not preserve the methyl C–H bond dynamics. Table ?? provides further simulation details. Error bars for the experimental values reflect error estimate of XXX.

10.Experimental error estimate changed since the data were originally published; needs to be explained to the reader.

11.How to refer to the experiments? Not really from previous publication because of re-analysis.

Methods, by including in the sum of Eq. (??) only terms with $\tau_i < \tau$. Consequently, at $\tau \to \infty$ the 'cumulative' $R_1(\tau)$ approaches the actual R_1. Ranges of steepest increase therefore indicate time scales that most strongly contribute to R_1 rates.

Figure ??B shows that for models that overestimate the R_1 rate of γ (MacRog, CHARMM36, and Slipids, see Fig. ??A) the major contribu-

tion to R_1 arises at $\tau > 50\,\mathrm{ps}$, whereas those underestimating the R_1 (Lipid14 and ECC, see Fig. ??) the major contribution comes from $\tau < 50\,\mathrm{ps}$. This also manifests in the distribution of fitting weights (α_i in Eq. (??)) in Fig. ??C: The earlier the non-zero weights occur, the smaller is the resulting R_1.

For the β and α segments, Fig. ??B shows that the main contribution to R_1 rates arises

from processes between 200 ps and 2 ns. As CHARMM36 has the largest weights of all models in this window (Fig. **??**C), it overestimates R_1. In contrast, Slipids, which has simultaneously R_1 and τ_e correct, has its largest weights at $\tau < 200\,\mathrm{ps}$. Indeed, considerable weights at short time scales ($< 10\,\mathrm{ps}$ in α for Lipid14, ECC, Berger) and at long time scales ($> 10\,\mathrm{ns}$ in both β and α for MacRog and Berger) do not manifest at all in the R_1 rates. However, the latter contribute heavily on τ_e, which is thus considerably overestimated by MacRog and Berger (Fig. **??**).

What are the motions in the 0.2–2 ns window that are over-presented in CHARMM36? Identifying them and speeding them up would improve the model dynamics. However, the connection between the fitted correlation times and the correlation times of distinct motional processes, such as dihedral rotations and lipid wobbling, turns out to be highly non-trivial; we thus refrain from further analysis here.

Effect of cholesterol.

The experimental effective correlation times τ_e (Fig. **??**A, top panels) show that when cholesterol is added, the glycerol region conformational dynamics slow down markedly. The tail segments slow down too, the effect increasing towards the backbone.

In stark contrast, however, the τ_e of headgroup segments (γ, β, α) are unaffected by cholesterol. Furthermore, cholesterol induces no measurable change in the headgroup β and α segment dynamics at short ($\sim 1\,\mathrm{ns}$) time scales, as demonstrated by the experimental R_1 rates (Fig. **??**A, lower panels). That said, there is a small but measurable impact on R_1 at γ.

All the force fields investigated qualitatively reproduce the increase in τ_e (see Fig. **??**B): Slipids gives the best magnitude estimates, while CHARMM36 and MacRog clearly overestimate the changes at the glycerol, C2, and C3 carbons. Notably, MacRog **12.and Berger?** erroneously predict slow down also for the β and α carbons, for which experiments detect no change. Note that, while CHARMM36 correctly shows no chance in τ_e of the γ, β, and

α carbons, it predicts a non-zero ΔR_1 for all three, indicating some inaccuracies in the headgroup rotational dynamics. Such inaccuracies might be reflected in the recent findings**?** (obtained using CHARMM36) that the headgroups of PCs neighbouring a cholesterol (within 6.6 Å) spend more time on top of the cholesterol than elsewhere; such arrested rotations could manifest on τ_e and R_1. Interestingly, the tail ΔR_1 seem to be pretty well reproduced by all three all-atom force fields, whereas Berger fails to capture the change at the oleoyl double bond.

Effect of ~~drying~~<u>dehydration</u>.

<u>The impact of dehydration on the structure and dynamics of lipid bilayers is of considerable interest as membrane fusion is always preceeded by removal of water between the opposing membranes and therefore may affect the rate of fusion. Lipid bilayers in dehydrated states are also found, e.g., in skin tissue.</u>

Figure **??**A shows how a mild dehydration affects C–H bond dynamics in the PC headgroup and glycerol backbone; the plot compares the experimental effective correlation times τ_e measured for POPC at full hydration and for DMPC (1,2-dimyristoyl-sn-glycero-3-phosphocholine) at 13 waters per lipid.

The τ_e are the same within experimental accuracy, which suggests two conclusions. Firstly, the headgroup (γ, β, α) τ_e are unaffected by structural differences in the tails. This is analogous to what was seen experimentally when adding cholesterol (Fig. **??**): Changes in the tail and glycerol regions do not reflect to the headgroup. Secondly, a mild dehydration does not alter the τ_e in the headgroup and glycerol regions.

Figure **??**B shows the effects of dehydration in three MD models. Combination of the unrealistically slow dynamics, especially in the glycerol backbone, (Fig. **??**) and the relatively short lengths of the openly available trajectories (Table **??**) led to large uncertainty estimates. ~~However, in the γ segment there is clearly no effect above 13 w/l in CHARMM36 and MacRog, in agreement with the experiments; reducing water content further induces a slow~~

9

~~down , especially in MacRog below 10 w/l.~~
~~Similarly, the~~

Owing to the uncertainties, we only point out the qualitative trends. For all carbons in the headgroup and glycerol segments, the simulated τ_e indicates slow down upon dehydration. This is manifested in the increase in the magnitude of the error estimate (cf. the Berger data for β and α ~~segments show no detectable change above 13 w/l for CHARMM36 and Berger, in agreement with the experiments; below 10 w/l Berger exhibits a slowdown, and in CHARMM36 the slowdown manifests as an abrupt increase of the uncertainty estimate .~~

~~Owing to the large uncertainties, we only point out the qualitative trends~~) as well as in the increase of the lower ~~error estimates on the glycerol segments~~ limit of the error. For CHARMM36 ~~it stays~~ the lower error estimates almost constant all the way until 7 w/l, whereas for Berger and MacRog ~~the lower error estimate suggests~~ they indicate a retardation of the dynamics starting already from $\sim$20 w/l.

These simulational findings suggest that experiments reducing hydration levels below 10 w/l would also show an increase in τ_e. This prediction is in line with the exponential slowdown of the headgroup conformational dynamics upon dehydration that was indicated by ^{2}H-NMR R_1 measurements of DOPC bilayers: $R_1 \sim \exp(-n_{w/l}/4)$.[?] The slowdown was attributed to the reduction in the effective volume available for the headgroup[?] owing to its tilt towards the membrane upon dehydration; the tilt is observed via changes of the lipid headgroup order parameters,[?] and is qualitatively reproduced by all the simulation models.[?]

Figure ~~??~~ ??C shows a collection of experimental ^{13}C-NMR R_1 rates measured at 125 MHz for the headgroup segments at different water contents; in addition to the full hydration POPC data from Fig. ??, DMPC at 13 w/l,[?] and POPC at 20 and 5 w/l[?] are shown. An increasing trend with decreasing hydration is observed for all the segments, indicating changes of headgroup dynamics at short ($\sim$1 ns) time scales. Interestingly, only CHARMM36 captures this, whereas Berger and MacRog give decreasing R_1 rates for β and α.

The characteristics of the slow down discussed here ~~is~~ are of significance not only ~~when simulating a bilayer (stack) under low hydration, but also for~~ for computational studies of intermembrane interactions, such as membrane fusion, ~~because these naturally lead to dehydrated conditions when the lipid assemblies approach~~ but also when simulating a bilayer (stack) under low hydration. Slower dynamics imply that longer simulation times are needed for equilibration, for reliably quantifying the properties of the bilayers, and for observing rare events.

Effect of cation binding.

17.This section will (possibly) be on ECC simulations and how teff chances with (divalent?) ion binding

Finally, we comment on the response of the MD model dynamics to increasing amounts of ~~monovalent salt. To our knowledge, no experimental ^{13}C-NMR R_1 or τ_e data exists as a function of monovalent salt concentration; therefore, the following discussion is kept qualitative.~~ salt. Experimentally, the modulation of α and β carbon order parameters upon increasing ion concentration have been used to quantify ion binding to lipid bilayers (the molecular electrometer[?] [?]). The order parameters are constant for POPC bilayers under NaCl addition in experiments, indicating negligible ion binding. ~~Based on this, we anticipate the effective correlation times also to be unaffected by monovalent salt.~~, but change in the presence increasing amounts of divalent ions.

The molecular electrometer has been used to show that most molecular dynamics force fields overestimate the binding of monovalent ions to PC bilayers:[?] In the simulations the modulation of the α and β carbon order parameters by increasing NaCl concentration was overestimated compared to the experiments, and accompanied by accumulation of ions at the bilayer surface. ~~In Fig. ?? we compare three force fields, one that is known to exhibit pronounced overbinding [?] (MacRog) and two producing more realistic binding affinity (Slipids and CHARMM36). The lateral distribution of~~

Na$^+$ ions near the bilayer is quantified in Fig. ??A whereas Fig. ??B shows the chance in τ_e for increasing salt concentration. Ion accumulation results in a slow down in the effective correlation time. Correlation times extracted from CHARMM36 vary only a little (low ion binding) when ion concentration is increased, whereas a slightly more pronounced change is observed with Slipids, and MacRog exhibits a clear slow-down (significant ion binding). Here, we use existing data from a force field, the ECC model, that is know to have mostly realistic ion binding.

This indicates that, similarly to the order parameters, τ_e may be useful in investigating the ion binding affinity of lipid bilayers and experimental work exploring this avenue would be interesting.

Correlation time of S_{CH} versus τ_e.

To determine the C–H bond order parameter S_{CH} (Eq.) in MD, one first calculates an instantaneous order parameter

$$S_{CH}(t) = \frac{1}{2}\left(3\cos^2\theta(t) - 1\right),$$

where $\theta(t)$ is the angle between the C–H bond and the membrane normal at time t. As this quantity is sampled along the trajectory, its average $\langle S_{CH}(t)\rangle$ approaches S_{CH}. For reliable determination of S_{CH}, it would be of interest to know the correlation time of this relaxation, because it determines the minimum simulation length required.

To this end, it is also of interest to know how this correlation time relates to τ_e. As discussed (see Fig. ??), in a bilayer the C–H bond's second order rotational correlation function $g(\tau)$, see Eq. , approaches S_{CH}^2 with time. The speed of this approach tells how fast the C–H bond orientations are sampled. However, the correlation time of S_{CH}, which is calculated using the a prioriknowledge of the membrane normal direction (Eq.), does not need to equal τ_e. Rather, one would intuitively expect it to be shorter than τ_e, because the rotational averaging around the membrane normal direction is already implicitly taken into account in Eq. .

A further complication is that the relaxational process of the C–H bond direction (used to determine τ_e) can be single or multi-exponential. If the relaxation is single-exponential, τ_e is the relaxation time of this exponential process. If the relaxation is multi-exponential, τ_e is the weighted mean of the corresponding set of relaxation times, and it is a bit hard to say just based on τ_e how long one needs to sample to reach the S_{CH}, because this depends also on the weights of the processes.

Figure ?? shows this correlation for systems studied in this work; we see...

4   Conclusions

Open access databanks of MD trajectories enables the creation new scientific information without running a single new simulation. Here, we demonstrated this by investigating the dynamics of a wide range of phosphatidylcholine molecular dynamics models using the existing trajectories from the NMRlipids databank.

We found that MD qualitatively captures the ^{13}C-NMR effective correlation time (τ_e) profile of POPC—the slow glycerol backbone and the faster motions of the headgroup and tail regions—but most MD force fields are prone to too slow dynamics of the glycerol C–H bonds (Fig. ??). While no force field reproduces all the experimental data, CHARMM36 and Slipids have an overall impressive τ_e. This is particularly true for CHARMM36, as it is also known to well reproduce the experimental conformational ensemble.[?] That said, we find that CHARMM36 struggles with the balance of dynamics in the headgroup region: The R_1 rates, sensitive for $\sim$1-ns processes, are too high for the γ, β, and α segments (Fig. ??).

19.Make the point that the 500-ns simulations indicated by Vogel[?] are not needed for sufficient sampling?

In addition to standard conditions, we explored how the dynamics react to addition of cholesterol or NaCl, or to removal of water. MD qualitatively captures that when cholesterol is mixed into a POPC bilayer, the conformational

dynamics in the tail and glycerol regions slows down; however, some force fields predict an (erroneous) slowdown also for the headgroup (Fig. **??**). With increasing NaCl concentration, a behaviour reminiscent of the molecular electrometer was observed: Amount of ion binding to the bilayer correlated with the magnitude increase in τ_e; this could open up the possibility of using τ_e in quantifying cation binding to lipid bilayers. When reducing the water content, MD exhibits slowdown of headgroup and backbone dynamics below ~10 waters per lipid in qualitative agreement with experimental data. **20. Hydration needs some kind of statement of significance.**

By gathering a set of ^{13}C-NMR data on the phosphatidylcholine dynamics and charting the typical features of the existing MD models against it, this study lays the foundation for further improvement of the force fields. While work is still needed in capturing even the correct conformations,**?** realistic dynamics will be an essential part of developing MD into a true computational microscope.

Importantly, this work demonstrates the power of open data in creating new knowledge out of existing trajectories at a reduced computational and labor cost. If the data are well indexed and documented, this process could be automated and has the potential to facilitate faster progress, e.g., in the development of MD force fields, for example through machine learning approaches.
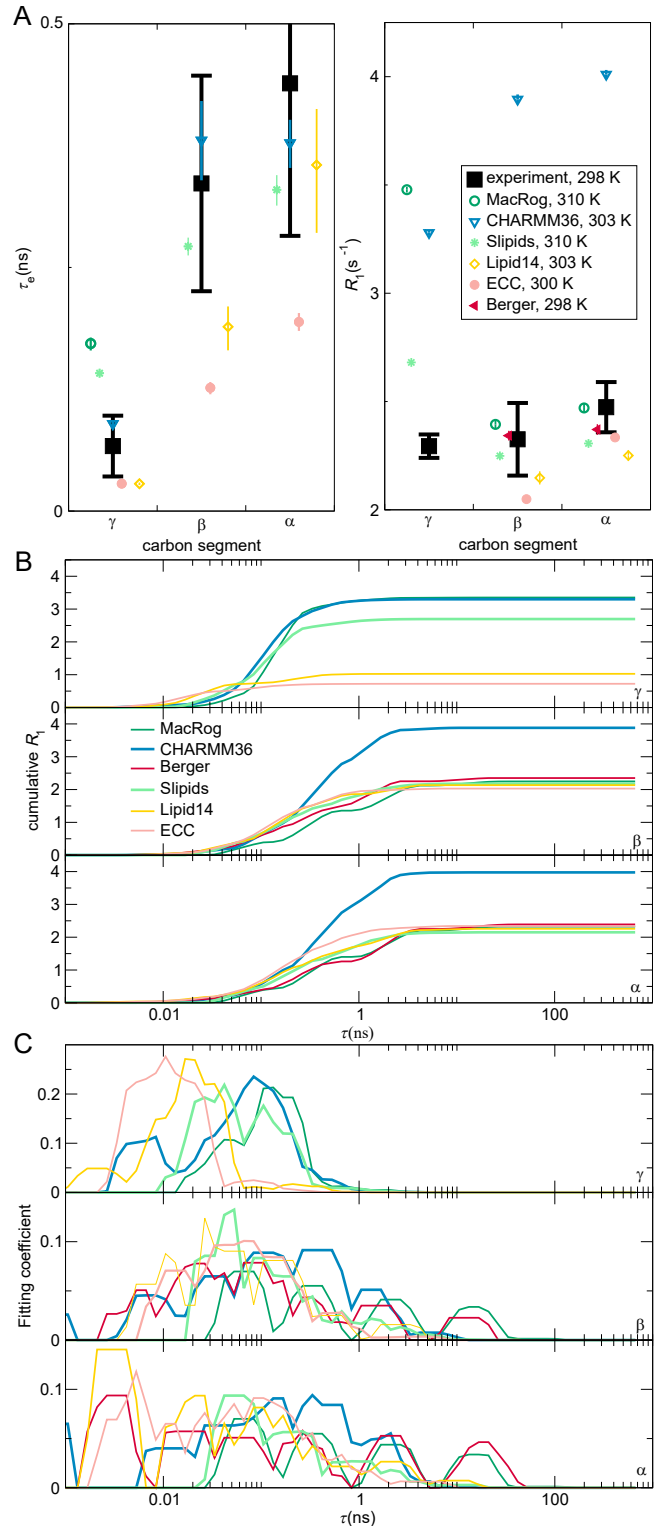
Acknowledgement

Figure 3: (A) Zoom on the headgroup τ_e (left panel) and R_1 (right). (B) 'Cumulative' R_1 (see Methods for definition) of the γ (top panel), β (middle), and α (bottom) segments. (C) Prefactor weighs α_i from Eq. (**??**) of γ (top), β (middle), and α (bottom). In B and C, a sliding average over 5 neighboring data points is shown.
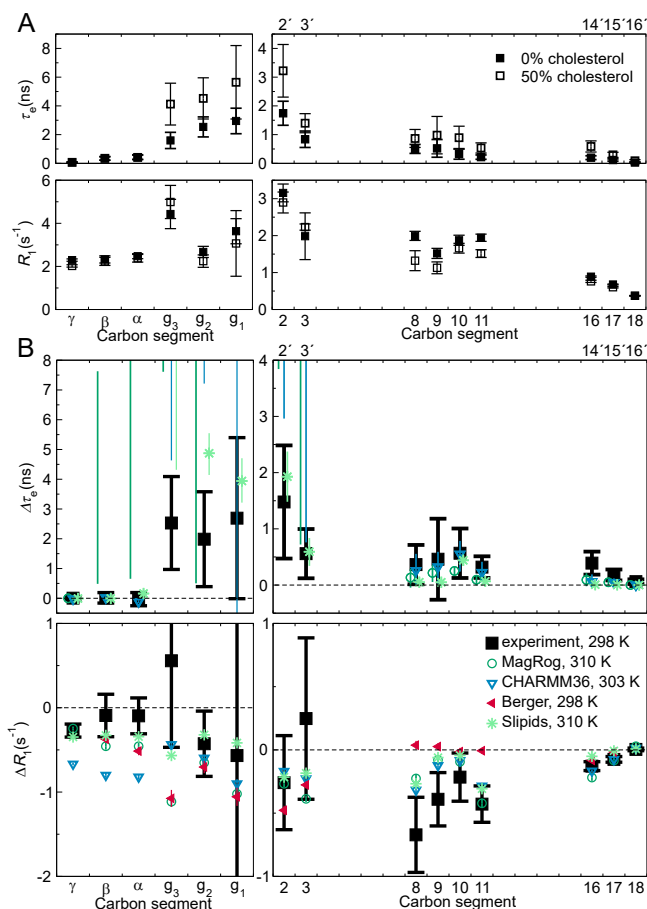
Figure 4: Effect of bilayer cholesterol content. (A) The experimental effective correlation times τ_e (top panels) and R_1 rates (bottom) in a pure POPC bilayer and in a bilayer containing 50% cholesterol. The data were measured at 298 K and full hydration. (B) The change in τ_e ($\Delta\tau_e$, top panels) and R_1 (ΔR_1, bottom), both in experiments and in MD simulations, when bilayer composition changes from pure POPC to 50% cholesterol. Berger not shown for $\Delta\tau_e$, because the open data available were insufficient to determine meaningful error estimates. Error estimates for the simulated $\Delta\tau_e$ are the maximal possible based on the errors at 0% and 50% cholesterol; for other data regular error propagation is used. Table **??** provides further simulation details; for segment labeling, see Fig. **??**.

13.@Hanne: Double check that the calculation of errors in (B) was as the caption describes. 14.Check if cholesterol data is in full hydration
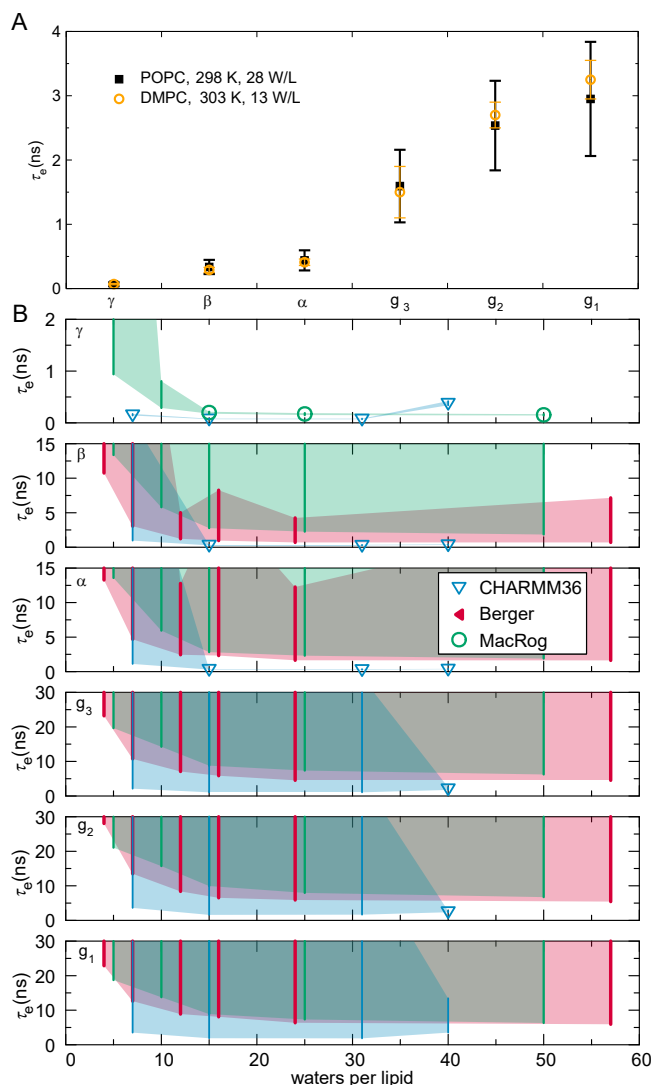

Figure 5: Effect of drying on effective correlation times in headgroup and glycerol backbone. (A) Experimental τ_e for DMPC (from Ref. **?**) at low hydration do not significantly differ from the τ_e for POPC at full hydration. (B) Calculated τ_e for POPC at decreasing hydration in three MD models. Note that three Berger data points (4, 12, 16, and 24 w/l) are from DLPC bilayers~~dashed~~. Symbols give the mean of segment hydrogens, if τ_e could be determined for all hydrogens; else only the error bar (extending from the mean of the lower to the mean of the upper uncertainty estimates) is shown; the area delimited by the error bars is shaded for visualization. See Table **??** for simulation details.
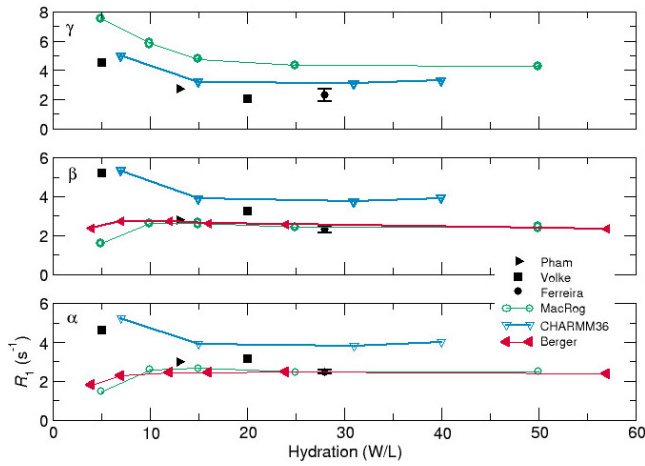
15.How to refer to full hydration POPC data?

Figure 6: Effect of drying on ^{13}C-NMR R_1 rates of the headgroup segments (at $125\,\mathrm{MHz}$) in experiments and simulations.

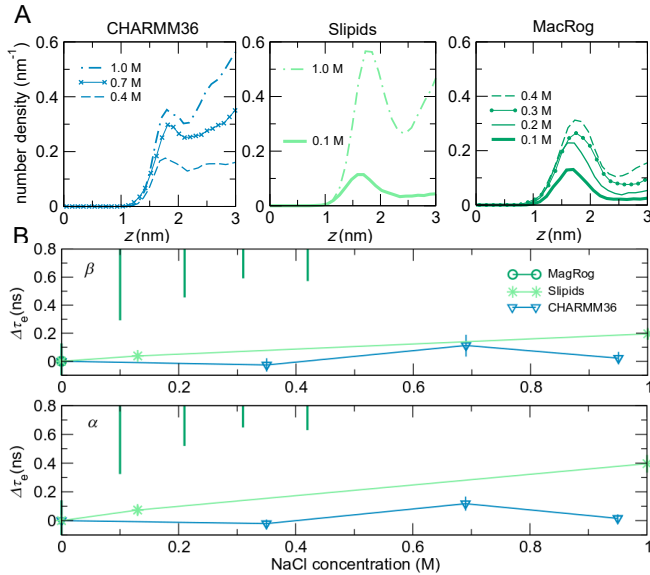**16.HA: merge this with the Fig. ??**

Figure 7: ~~The impact~~ A picture of ~~increasing ionic strength on effective correlation times. a) The density distribution (average over both leaflets) of Na$^+$~~ alpha and beta teff vs bound CA ions ~~as function of distance z from the bilayer center. The plots for each force field are presented from left to right~~ in the ~~order of increasing ion accumulation. b) Effective correlation times for α and β C-H bonds in growing NaCl concentration from CHARMM36, Slipids, MacRog POPC simulations. Details on the simulation data are provided in Table ??.~~ ECC model

18.analysis running

Graphical TOC Entry

TOC here if needed