

## Temporal blockmodeling

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Clustering of TQs

Example: Terror news

Block mode

Conclusions

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## Toward an indirect approach for blockmodeling temporal networks

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XXXX Sunbelt Social Networks Conference on Zoom, July 13-17, 2020



## Outline

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Current version of slides (July 11, 2020 at 23:02): slides PDF

https://github.com/bavla/TQ/blob/master/docs/clusTQsunbelt.pdf



## Blockmodeling temporal networks

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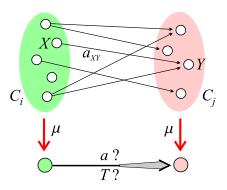
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To the traditional blockmodeling (BM) scheme we add the time dimension. We assume that the network is described using temporal quantities [6] for nodes/links activity/presence, nodes properties and links weights. Then also the BM partition  $\pi$  can be described for each node v with a temporal quantity  $\pi(v,t)$  with the meaning:

 $\pi(v,t)=i$  means that in time t node v belongs to cluster i. The clusters  $C_i(t)=\{v:\pi(v,t)=i\}$  structure and activity can change through time, but they preserve their identity.



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For the BM  $\mu$  the clusters are maped into BM nodes  $\mu: C_i \to [i]$ . To determine the BM we still have to specify how the links from  $C_i$  to  $C_j$  are represented in the BM – in general, for the model arc ([i],[j]), we have to specify two temporal quantities: its value  $a_{ij}(t)$  and, in the case of generalized BM, its type  $T_{ij}(t)$ . In general the value can be an object of different type than the values of the links in the original temporal network.

To develop a BM method we specify a criterion function  $P(\mu)$  measuring the "error" of the BM  $\mu$ . We can introduce additional knowledge by constraining the partitions to a set  $\Phi$  of feasible partitions. We are searching for a partition  $\pi^* \in \Phi$  such that the corresponding BM  $\mu^*$  minimizes the criterion function  $P(\mu)$ .



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This is a general framework. In the following years we intend to develop methods case by case.

- constant partition nodes stay in the same cluster all the time
  - indirect approach based on clustering of temporal quantities
  - temporal version of clustering with relation constraint
  - local optimization of the criterion function P over  $\Phi$
- dynamic partition nodes can move between clusters through time. The details are still to be elaborated.



## Clustering of temporal quantities

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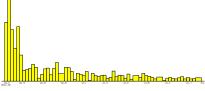
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A temporal quantity is described by a sequence

$$\mathbf{a} = [(s_r, f_r, v_r) : r = 1, 2, \dots, k]$$

where  $[s_r, f_r)$  determines a time interval and  $v_r$  is the value of variable on this interval.

We adapted traditional leaders and agglomerative hierarchical clustering methods for clustering units described by

variables that have for their values temporal quantities [2, 5].

ClusTQ at https://github.com/bavla/TQ .





## Clustering of temporal quantities

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For a unit  $X_i$ , each variable  $V_j$  is described with a weight  $h_{ij}$  and a temporal quantity  $\mathbf{x}_{ij}$ 

$$X_{ij}=(h_{ij},\mathbf{x}_{ij})$$

In our algorithms we use *normalized* values of temporal variables  $V'=(h,\mathbf{p})$  where

$$\mathbf{p} = [(s_r, f_r, p_r) : r = 1, 2, \dots, k]$$
 and  $p_r = \frac{v_r}{h}$ 

In the case, when  $h = \text{tot}(\mathbf{x}) = \sum v_r$ , the normalized TQ **p** is essentially a probability distribution.

Both methods create cluster representatives that are represented in the same way.



## September 11th Reuters terror news

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(Centering Resonance Analysis) networks produced by Steve Corman and Kevin Dooley at Arizona State University. The network is based on all the stories released during 66 consecutive days by the news agency Reuters concerning the September 11 attack on the U.S., beginning at 9:00 AM EST 9/11/01.

The Reuters terror news network was obtained from the CRA

The nodes of this network are important words (terms). There is an edge between two words iff they appear in the same utterance (for details see the paper [7]). The weight of an edge is its frequency. The network has n=13332 nodes (different words in the news) and m=243447 edges, 50859 with value larger than 1. There are no loops in the network.

The Reuters terror news network was used as a case network for the Viszards visualization session on the Sunbelt XXII International Sunbelt Social Network Conference, New Orleans, USA, 13-17. February 2002.



### **Details**

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We transformed the Pajek version of the network into NetsJSON format used in  $\mathsf{TQ}$  and Nets.

For a temporal description of each node/word for clustering we took its activity = sum of all TQs on edges adjacent to a given node.

Our leaders and hierarchical clustering methods are compatible. They are based on the same clustering error criterion function.

Usually the leaders method is used to reduce the problem to up to some hundred units. With hierarchical clustering of the leaders of the obtained clusters we afterward determine the "right" number of clusters and their representatives.



### Leaders method

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To cluster all 13332 words (nodes) in Terror news we used the adapted leaders method searching for 100 clusters.

After 50 steps we stopped the search.

$$P_1 = 41012.94, P_{50} = 23897.74$$

```
{74: 716, 43: 535, 82: 378, 2: 372, 9: 338, 69: 325, 96: 307, 46: 307, 100: 291, 26: 275, 62: 257, 13: 241, 85: 238, 81: 237, 34: 233, 98: 229, 27: 228, 29: 222, 19: 203, 22: 199, 10: 196, 88: 195, 37: 192, 12: 191, 30: 186, 54: 183, 72: 180, 66: 177, 14: 175, 33: 172, 25: 162, 23: 162, 92: 156, 71: 155, 93: 153, 87: 152, 51: 151, 24: 150, 16: 148, 58: 146, 59: 146, 47: 145, 63: 143, 61: 141, 4: 139, 45: 132, 89: 130, 8: 128, 17: 126, 56: 114, 50: 105, 77: 102, 42: 101, 1: 96, 55: 96, 97: 95, 53: 91, 94: 89, 5: 87, 70: 83, 90: 81, 44: 76, 3: 75, 60: 74, 40: 73, 52: 64, 15: 63, 84: 56, 20: 51, 57: 45, 64: 44, 67: 44, 65: 43, 21: 39, 31: 37, 11: 37, 39: 36, 79: 35, 38: 35, 36: 34, 76: 32, 91: 32, 99: 32, 80: 31, 73: 31, 68: 31, 7: 29, 6: 29, 35: 29, 28: 28, 49: 27, 86: 26, 78: 23, 83: 18, 41: 18, 32: 18, 95: 15, 18: 14, 48: 13, 75: 12}
```

We continued with hierarchical clustering of the obtained leaders.



## Hierarchical clustering

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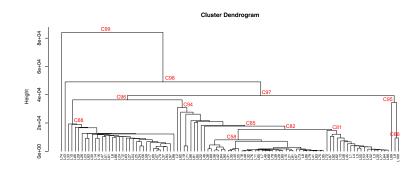
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## Word clouds for L74 and L43

 $|L74| = 716, \quad |L43| = 535$ 

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## Word clouds for L46 and C46 |L46| = 307, |C46| = 358

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## Word clouds for C88, C95 $|C88| = 5109, \quad |C95| = 954$

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## Word clouds for C58 and C81

 $|C58| = 1396, \quad |C81| = 2226$ 

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### Word cloud for C94

|C94| = 6018,  $C58, C81 \subset C94$ 

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# Comparisons of leaders and cluster representatives L74:C98, L43:C97, C96:C95, C88:C94

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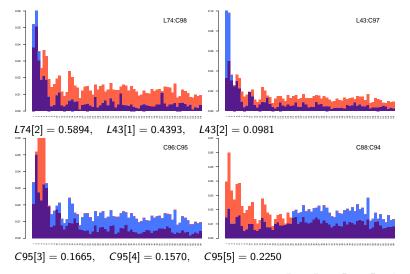
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## Comparisons of leaders and cluster representatives C58:C81, L96:C66, C46:C955, C46

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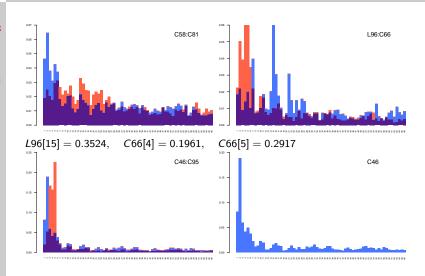
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## Block model

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To produce a block model we have to specify the values on its links. Because the original network is undirected, so is the BM. There are different options.

### Temporal quantities:

$$\mathbf{a}(([i]:[j])) = \mathsf{activity}(C_i,C_j) = \sum_{u \in C_i, v \in C_j} \mathbf{a}(u:v), \quad \mathsf{for} \ i \neq j$$

and 
$$\mathbf{a}(([i]:[i])) = \frac{1}{2} \operatorname{activity}(C_i, C_i)$$
.

Total intensities: 
$$a(([i]:[j])) = tot(a(([i]:[j])))$$
.

Geometric average intensities: 
$$g(([i]:[j])) = \frac{a(([i]:[j]))}{\sqrt{|C_i| \cdot |C_j|}}$$
.



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### **Total intensities:**

| i | cluster | size | 1      | 2     | 3    | 4    | 5    |
|---|---------|------|--------|-------|------|------|------|
| 1 | C94     | 6018 | 143549 | 67801 | 5422 | 2816 | 2939 |
| 2 | C88     | 5109 | 0      | 18288 | 739  | 357  | 357  |
| 3 | C95     | 954  | 0      | 0     | 535  | 53   | 54   |
| 4 | L43     | 535  | 0      | 0     | 0    | 205  | 51   |
| 5 | L74     | 716  | 0      | 0     | 0    | 0    | 281  |

### Geometric average intensities:

| i | cluster | 1     | 2     | 3    | 4    | 5    |
|---|---------|-------|-------|------|------|------|
| 1 | C94     | 23.85 | 12.23 | 2.26 | 1.57 | 1.42 |
| 2 | C88     | 0     | 3.58  | 0.33 | 0.22 | 0.19 |
| 3 | C95     | 0     | 0     | 0.56 | 0.07 | 0.07 |
| 4 | L43     | 0     | 0     | 0    | 0.38 | 0.08 |
| 5 | L74     | 0     | 0     | 0    | 0    | 0.39 |



## Block model Geometric average intensities, cut at level 0.3

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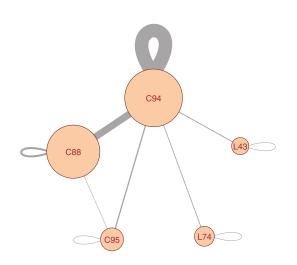
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## Hierarchical clustering of Franzosi's violence network

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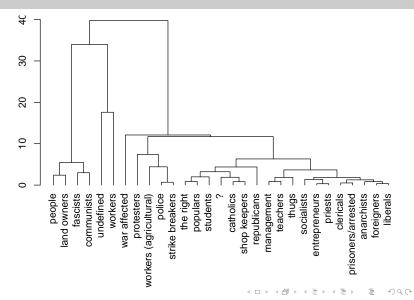
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- only started
- how to present/display the temporal BMs?
- $\bullet$  compatibilty of clustering criterion function P and BM  $\mu$



## Acknowledgments

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### References I

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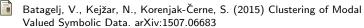
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### References II

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