

BIG-OH

$$\begin{aligned}
 5n + \lg(n) - 12 &\leq 5n + \lg(n) - 12 \\
 5n + \lg(n) - 12 &\leq 5n + \lg(n) \\
 5n + \lg(n) - 12 &\leq 5n + 10n & n \geq 0 \\
 5n + \lg(n) - 12 &\leq 15n & n \geq 0 \\
 && n0 = 0 & c = 15 \\
 && & O(n)
 \end{aligned}$$

OMEGA

$$\begin{aligned}
 5n + \lg(n) - 12 &\geq 5n + \lg(n) - 12 \\
 5n + \lg(n) - 12 &\geq 5n - 12 & n \geq 1 \\
 5n + \lg(n) - 12 &\geq 5n & n \geq 12 \\
 && n0 = 12 & c = 5 \\
 && & O(n)
 \end{aligned}$$

RECURRENCE RELATION

$$\begin{aligned}
 T(1) &= 1 \\
 T(0) &= 1 \\
 T(n) &= T(n-1) + 1 \\
 &= T(n-1-1) + 1 + 1 \\
 &= T(n-2) + 2 \\
 &= T(n-2-1) + 2 + 1 \\
 &= T(n-3) + 3 \\
 &= T(n-3-1) + 3 + 1 \\
 &= T(n-4) + 4 \\
 &= T(n-i) + i \\
 n - i &= \text{base case (aka 0 or 1)} \Rightarrow i = n \\
 &= T(n-n) + n \\
 &= 1 + n \\
 &= O(n)
 \end{aligned}$$

RECURRENCE RELATION #2

$$\begin{aligned}
 T(1) &= 1 \\
 T(n) &= T(n-1) + T(1) + T(n-1) \\
 &= 2T(n-1) + 1 \\
 &= 2(2T(n-1-1) + 1) + 1 \\
 &= 4T(n-2) + 2 + 1 \\
 &= 4(2T(n-2-1) + 1) + 2 + 1 \\
 &= 8T(n-3) + 4 + 2 + 1 \\
 &= 2^i T(n-i) + 2^i - 1 \\
 n - i &= \text{base case (aka 1)} \Rightarrow i = n - 1 \\
 &= 2^{n-1} T(n-(n-1)) + 2^{n-1} - 1 \\
 &= 2^n n - 1 \\
 &= O(2^n)
 \end{aligned}$$