3D Gaussian Splatting for Real-Time Radiance Field Rendering

Algorithm

Input – set of images of static scene

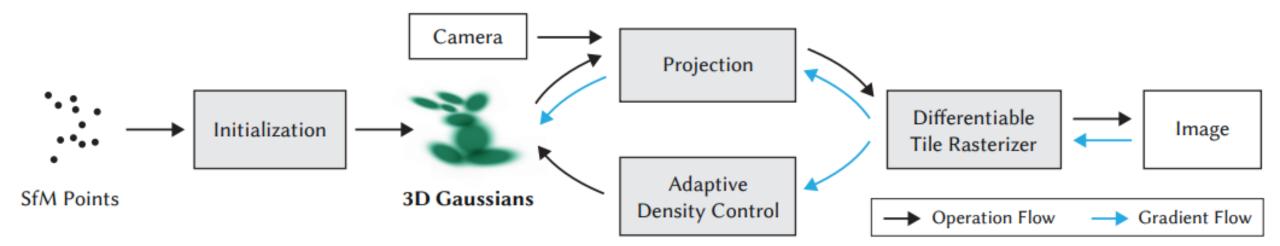
- 1. Get sparse point cloud by SfM
- 2. Create a set of 3D Gaussians
- 3. Optimize parameters of Gaussians with gradient descent
- 4. Render an image

Sparse point cloud



Pipeline

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Parameters of a Gaussian

• Position (mean)

$$G(x) = e^{-\frac{1}{2}(x)^T \Sigma^{-1}(x)}$$

 Covariance matrix (3x3)

$$\Sigma = RSS^TR^T$$
 - should be positive semi-definite

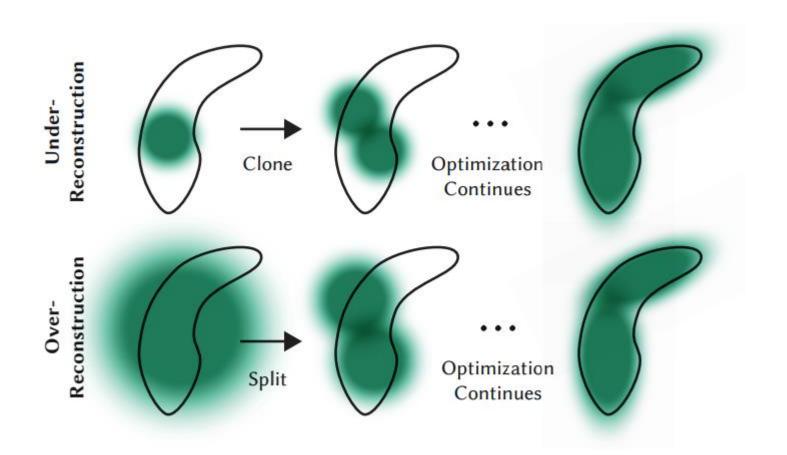
• Color (RGB)

R – rotation matrix

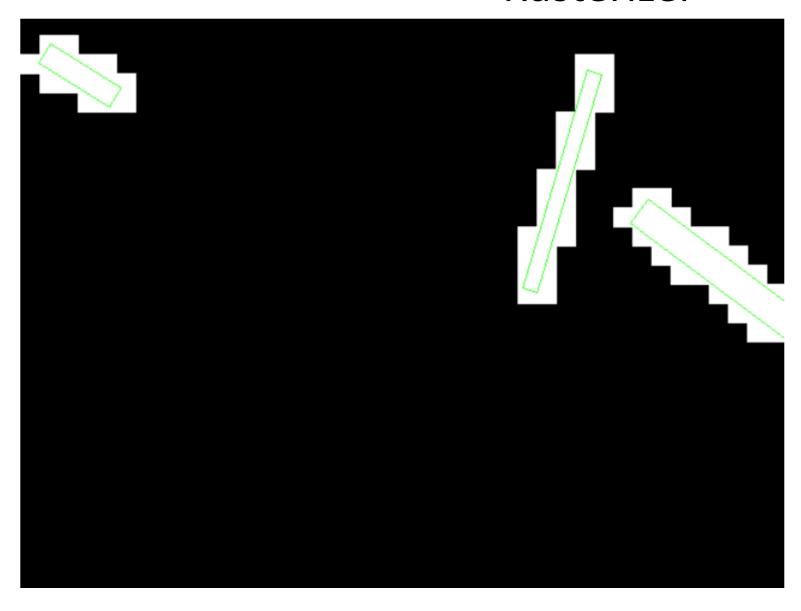
• Opacity ([0, 1])

S – scale matrix

Gaussian control



Rasterizer



$$C = \sum_{i \in \mathcal{N}} c_i \alpha_i \prod_{j=1}^{i-1} (1 - \alpha_j)$$

 $lpha_i$ - opacity of i-th point

 c_i - color of i-th point

Algorithm 1 Optimization and Densification *w*, *h*: width and height of the training images

```
M \leftarrow SfM Points
                                                                     ▶ Positions
S, C, A \leftarrow InitAttributes()
                                         ▶ Covariances, Colors, Opacities
                                                             ▶ Iteration Count
i \leftarrow 0
while not converged do
     V, \hat{I} \leftarrow \text{SampleTrainingView}()
                                                     ▶ Camera V and Image
     I \leftarrow \text{Rasterize}(M, S, C, A, V)
                                                                         ▶ Alg. 2
     L \leftarrow Loss(I, \hat{I})
                                                                           ▶ Loss
    M, S, C, A \leftarrow \operatorname{Adam}(\nabla L)
                                                           ▶ Backprop & Step
     if IsRefinementIteration(i) then
         for all Gaussians (\mu, \Sigma, c, \alpha) in (M, S, C, A) do
              if \alpha < \epsilon or IsTooLarge(\mu, \Sigma) then
                                                                      ▶ Pruning
                   RemoveGaussian()
              end if
              if \nabla_{\mathcal{D}} L > \tau_{\mathcal{D}} then
                                                                ▶ Densification
                   if ||S|| > \tau_S then
                                                      ▶ Over-reconstruction
                        SplitGaussian(\mu, \Sigma, c, \alpha)
                                                     ▶ Under-reconstruction
                   else
                        CloneGaussian(\mu, \Sigma, c, \alpha)
                   end if
              end if
         end for
     end if
     i \leftarrow i + 1
end while
```

```
w, h: width and height of the image to rasterize
M, S: Gaussian means and covariances in world space
C, A: Gaussian colors and opacities
V: view configuration of current camera
  function RASTERIZE(w, h, M, S, C, A, V)
                                                       ▶ Frustum Culling
      CullGaussian(p, V)
      M', S' \leftarrow \text{ScreenspaceGaussians}(M, S, V)
                                                             ▶ Transform
      T \leftarrow \text{CreateTiles}(w, h)
      L, K \leftarrow \text{DuplicateWithKeys}(M', T)
                                                      ▶ Indices and Keys
      SortByKeys(K, L)
                                                           ▶ Globally Sort
      R \leftarrow IdentifyTileRanges(T, K)
      I \leftarrow \mathbf{0}
                                                            ▶ Init Canvas
      for all Tiles t in I do
           for all Pixels i in t do
               r \leftarrow \text{GetTileRange}(R, t)
               I[i] \leftarrow \text{BlendInOrder}(i, L, r, K, M', S', C, A)
           end for
      end for
        return I
```

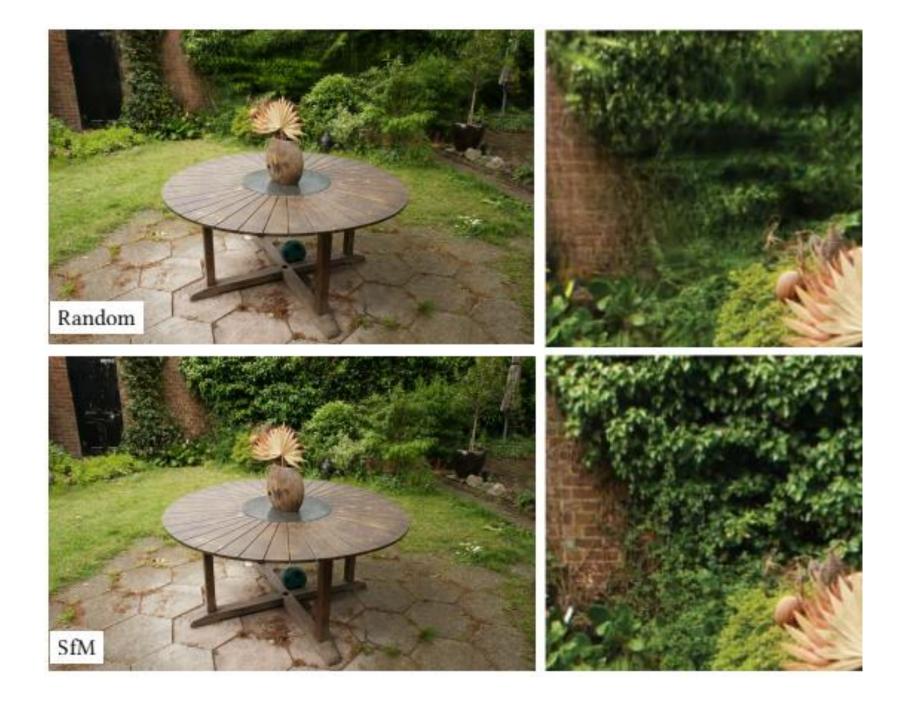
end function

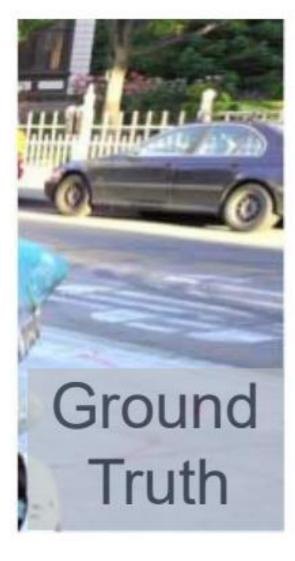
Algorithm 2 GPU software rasterization of 3D Gaussians

Metrics

Dataset	Mip-NeRF360					Tanks&Temples					Deep Blending							
Method Metric	SSIM [↑]	$PSNR^{\uparrow}$	$LPIPS^{\downarrow}$	Train	FPS	Mem	SSIM [↑]	$PSNR^{\uparrow}$	$LPIPS^{\downarrow}$	Train	FPS	Mem	SSIM [↑]	$PSNR^{\uparrow}$	$LPIPS^{\downarrow}$	Train	FPS	Mem
Plenoxels	0.626	23.08	0.463	25m49s	6.79	2.1GB	0.719	21.08	0.379	25m5s	13.0	2.3GB	0.795	23.06	0.510	27m49s	11.2	2.7GB
INGP-Base	0.671	25.30	0.371	5m37s	11.7	13MB	0.723	21.72	0.330	5m26s	17.1	13MB	0.797	23.62	0.423	6m31s	3.26	13MB
INGP-Big	0.699	25.59	0.331	7m30s	9.43	48MB	0.745	21.92	0.305	6m59s	14.4	48MB	0.817	24.96	0.390	8m	2.79	48MB
M-NeRF360	0.792^{\dagger}	27.69^{\dagger}	0.237^{\dagger}	48h	0.06	8.6MB	0.759	22.22	0.257	48h	0.14	8.6MB	0.901	29.40	0.245	48h	0.09	8.6MB
Ours-7K	0.770	25.60	0.279	6m25s	160	523MB	0.767	21.20	0.280	6m55s	197	270MB	0.875	27.78	0.317	4m35s	172	386MB
Ours-30K	0.815	27.21	0.214	41m33s	134	734MB	0.841	23.14	0.183	26m54s	154	411MB	0.903	29.41	0.243	36m2s	137	676MB

	Truck-5K	Garden-5K	Bicycle-5K	Truck-30K	Garden-30K	Bicycle-30K	Average-5K	Average-30K
Limited-BW	14.66	22.07	20.77	13.84	22.88	20.87	19.16	19.19
Random Init	16.75	20.90	19.86	18.02	22.19	21.05	19.17	20.42
No-Split	18.31	23.98	22.21	20.59	26.11	25.02	21.50	23.90
No-SH	22.36	25.22	22.88	24.39	26.59	25.08	23.48	25.35
No-Clone	22.29	25.61	22.15	24.82	27.47	25.46	23.35	25.91
Isotropic	22.40	25.49	22.81	23.89	27.00	24.81	23.56	25.23
Full	22.71	25.82	23.18	24.81	27.70	25.65	23.90	26.05









Problems

Artifacts in regions where the scene is not well observed

Memory consumption

References

- https://arxiv.org/abs/2308.04079v1 main article
- https://github.com/graphdeco-inria/gaussian-splatting implementation
- https://github.com/joeyan/gaussian_splatting/blob/main/MATH.md math of gaussian splatting
- https://huggingface.co/blog/gaussian-splatting hugging-face review
- https://habr.com/ru/articles/768590/ habr review