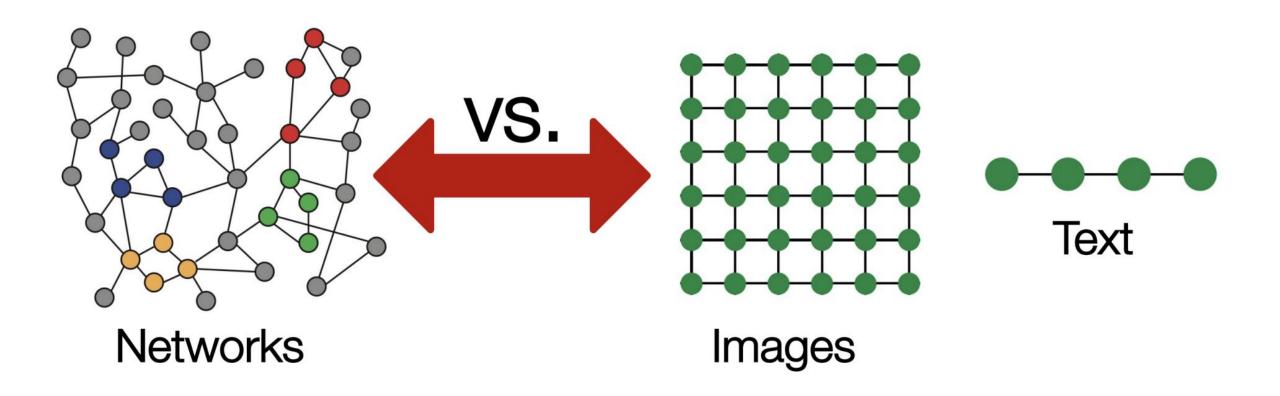
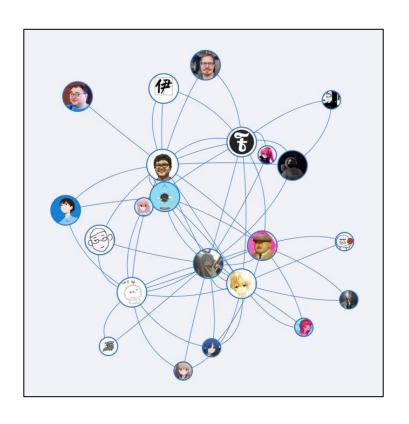
Нейросетевые методы для работы с графами

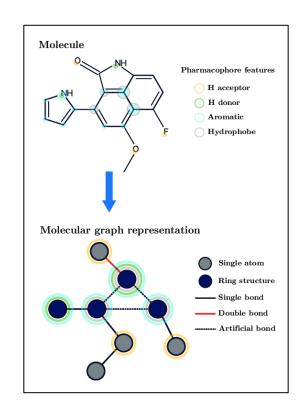
Пономарчук Аня

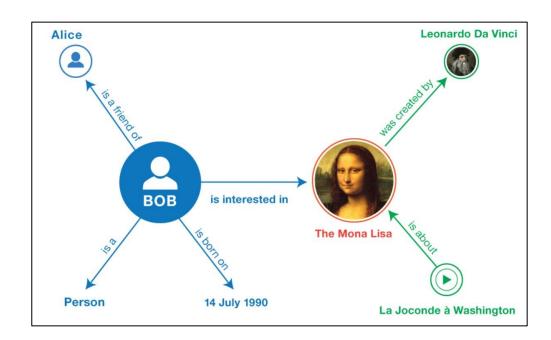
Data structures



Graph examples





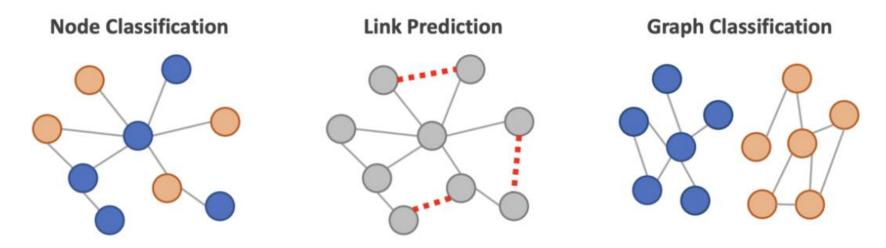


Graph analysis tasks

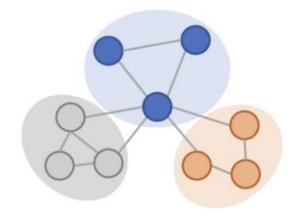
➤ Node-level

>Edge-level

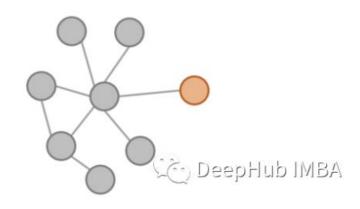
➤ Graph-level



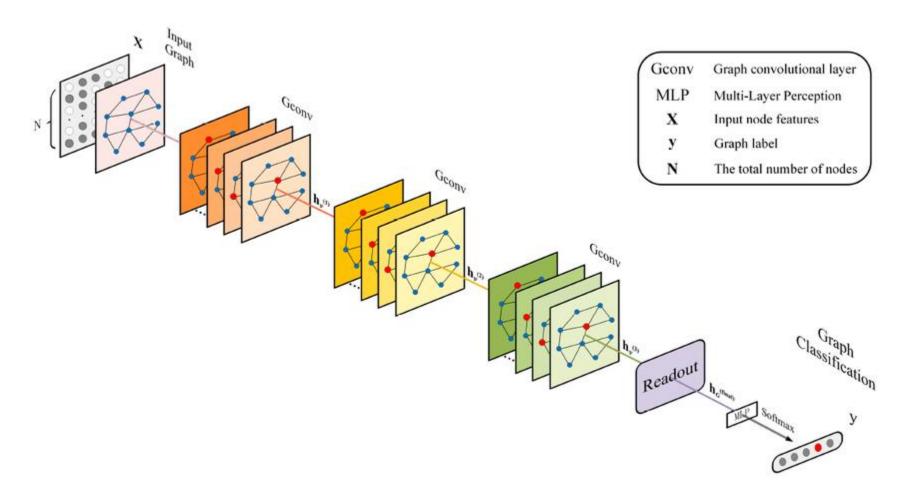
Community Detection



Anomaly Detection

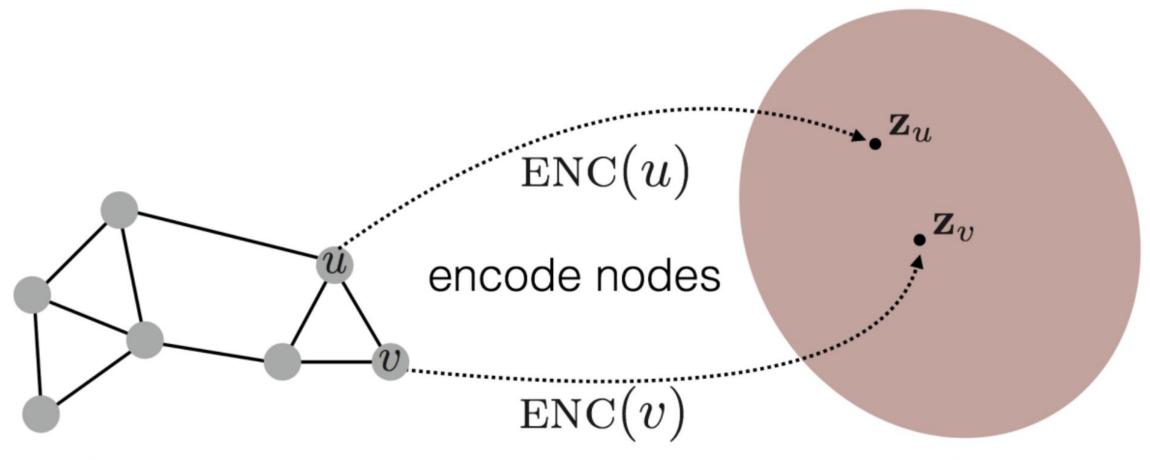


Visualization of general convolutional GNN architecture



Embedding Nodes

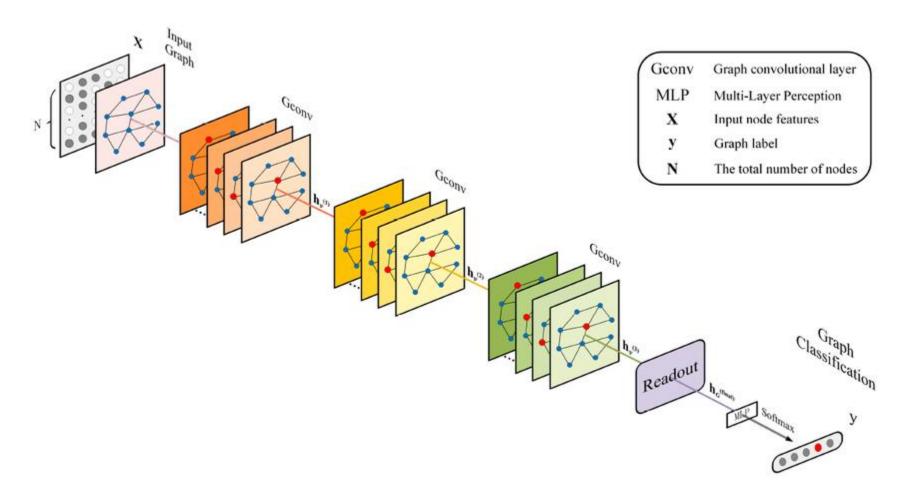
 $ext{similarity}(u,v) pprox z_v^T z_u, z \in \mathbb{R}^d$



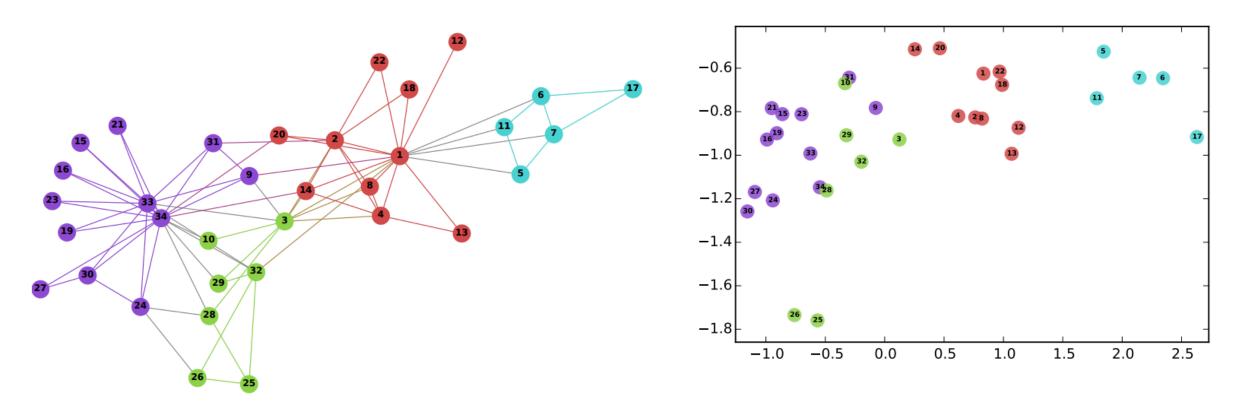
original network

embedding space

Visualization of general convolutional GNN architecture



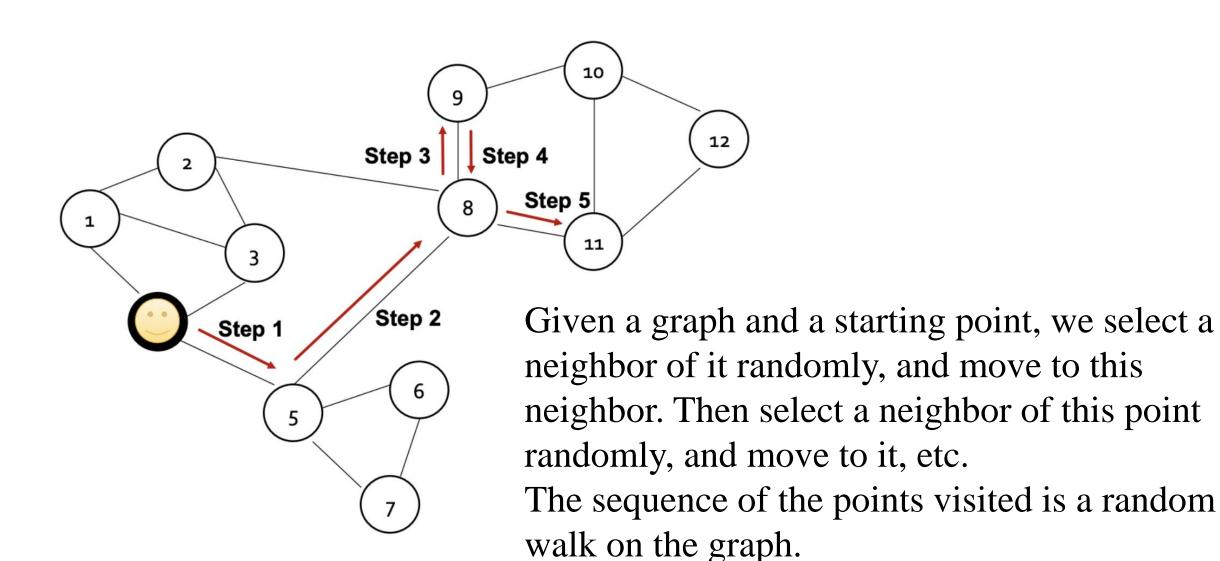
DeepWalk problem definition



(a) Input: Karate Graph

(b) Output: Representation

Random Walks



Power law

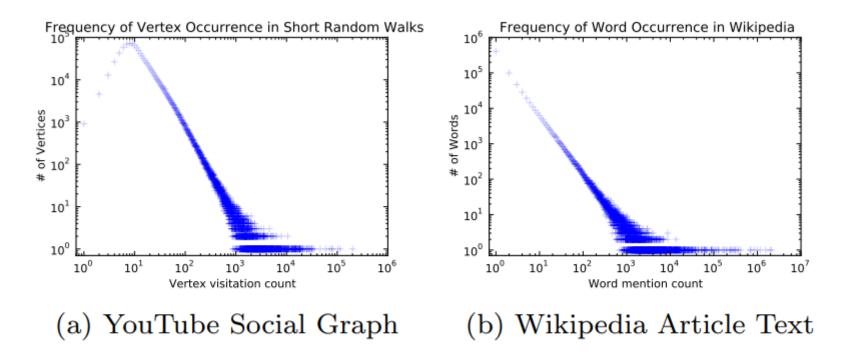


Figure 2: The power-law distribution of vertices appearing in short random walks (2a) follows a power-law, much like the distribution of words in natural language (2b).

DeepWalk

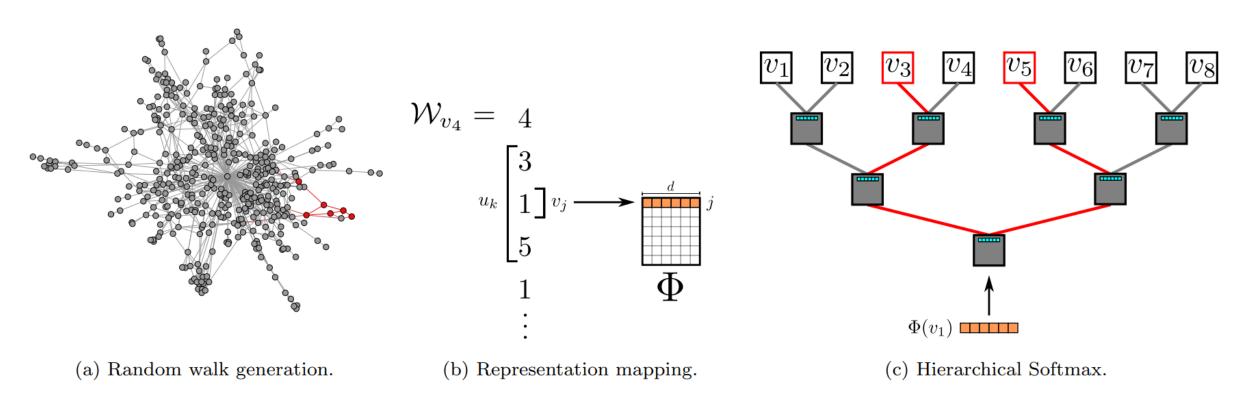


Figure 3: Overview of DEEPWALK. We slide a window of length 2w + 1 over the random walk W_{v_4} , mapping the central vertex v_1 to its representation $\Phi(v_1)$. Hierarchical Softmax factors out $\Pr(v_3 \mid \Phi(v_1))$ and $\Pr(v_5 \mid \Phi(v_1))$ over sequences of probability distributions corresponding to the paths starting at the root and ending at v_3 and v_5 . The representation Φ is updated to maximize the probability of v_1 co-occurring with its context $\{v_3, v_5\}$.

DeepWalk

6: end for

```
Algorithm 1 DEEPWALK(G, w, d, \gamma, t)
Input: graph G(V, E)
    window size w
    embedding size d
    walks per vertex \gamma
    walk length t
Output: matrix of vertex representations \Phi \in \mathbb{R}^{|V| \times d}
 1: Initialization: Sample \Phi from \mathcal{U}^{|V| \times d}
 2: Build a binary Tree T from V
 3: for i = 0 to \gamma do
       \mathcal{O} = \text{Shuffle}(V)
       for each v_i \in \mathcal{O} do
        W_{v_i} = RandomWalk(G, v_i, t)
         SkipGram(\Phi, W_{v_i}, w)
       end for
9: end for
```

```
Algorithm 2 SkipGram(\Phi, W_{v_i}, w)
```

```
1: for each v_j \in \mathcal{W}_{v_i} do

2: for each u_k \in \mathcal{W}_{v_i}[j-w:j+w] do

3: J(\Phi) = -\log \Pr(u_k \mid \Phi(v_j))

4: \Phi = \Phi - \alpha * \frac{\partial J}{\partial \Phi}

5: end for
```

Parallelizability

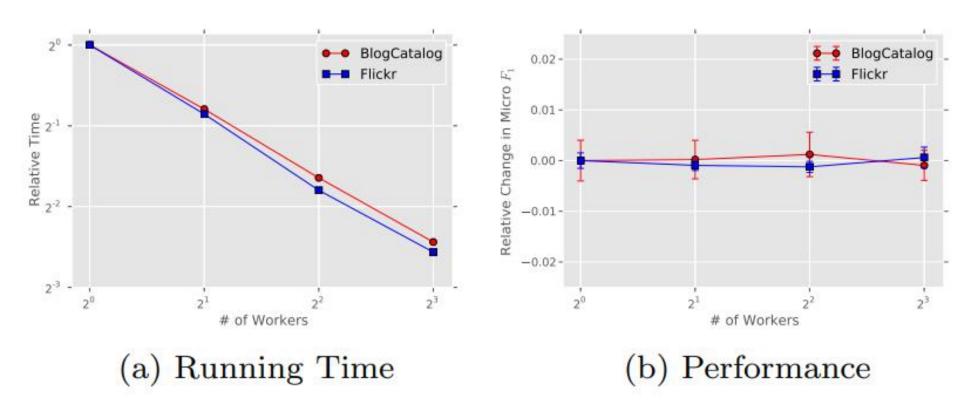


Figure 4: Effects of parallelizing DeepWalk

Experiments

Name	BlogCatalog	FLICKR	YouTube
V	10,312	80,513	1,138,499
E	$333,\!983$	5,899,882	2,990,443
$ \mathcal{Y} $	39	195	47
Labels	Interests	Groups	Groups

- ➤ BlogCatalog is a network of social relationships provided by blogger authors. The labels represent the topic categories provided by the authors.
- Flickr is a network of the contacts between users of the photo sharing website. The labels represent the interest groups of the users such as 'black and white photos'.
- ➤ YouTube is a social network between users of the popular video sharing website. The labels here represent groups of viewers that enjoy common video genres (e.g. anime and wrestling).

BlogCatalog results

	% Labeled Nodes	10%	20%	30%	40%	50%	60%	70%	80%	90%
	DeepWalk	36.00	38.20	39.60	40.30	41.00	41.30	41.50	41.50	42.00
	SpectralClustering	31.06	34.95	37.27	38.93	39.97	40.99	41.66	42.42	42.62
	EdgeCluster	27.94	30.76	31.85	32.99	34.12	35.00	34.63	35.99	36.29
Micro-F1(%)	Modularity	27.35	30.74	31.77	32.97	34.09	36.13	36.08	37.23	38.18
	wvRN	19.51	24.34	25.62	28.82	30.37	31.81	32.19	33.33	34.28
	Majority	16.51	16.66	16.61	16.70	16.91	16.99	16.92	16.49	17.26
	DeepWalk	21.30	23.80	25.30	26.30	27.30	27.60	27.90	28.20	28.90
	SpectralClustering	19.14	23.57	25.97	27.46	28.31	29.46	30.13	31.38	31.78
	EdgeCluster	16.16	19.16	20.48	22.00	23.00	23.64	23.82	24.61	24.92
Macro-F1(%)	Modularity	17.36	20.00	20.80	21.85	22.65	23.41	23.89	24.20	24.97
	wvRN	6.25	10.13	11.64	14.24	15.86	17.18	17.98	18.86	19.57
	Majority	2.52	2.55	2.52	2.58	2.58	2.63	2.61	2.48	2.62

Flickr results

	% Labeled Nodes	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
	DeepWalk	32.4	34.6	35.9	36.7	37.2	37.7	38.1	38.3	38.5	38.7
	SpectralClustering	27.43	30.11	31.63	32.69	33.31	33.95	34.46	34.81	35.14	35.41
Micro-F1(%)	EdgeCluster	25.75	28.53	29.14	30.31	30.85	31.53	31.75	31.76	32.19	32.84
	Modularity	22.75	25.29	27.3	27.6	28.05	29.33	29.43	28.89	29.17	29.2
	wvRN	17.7	14.43	15.72	20.97	19.83	19.42	19.22	21.25	22.51	22.73
	Majority	16.34	16.31	16.34	16.46	16.65	16.44	16.38	16.62	16.67	16.71
	DeepWalk	14.0	17.3	19.6	21.1	22.1	22.9	23.6	24.1	24.6	25.0
	SpectralClustering	13.84	17.49	19.44	20.75	21.60	22.36	23.01	23.36	23.82	24.05
Macro-F1(%)	EdgeCluster	10.52	14.10	15.91	16.72	18.01	18.54	19.54	20.18	20.78	20.85
	Modularity	10.21	13.37	15.24	15.11	16.14	16.64	17.02	17.1	17.14	17.12
	wvRN	1.53	2.46	2.91	3.47	4.95	5.56	5.82	6.59	8.00	7.26
	Majority	0.45	0.44	0.45	0.46	0.47	0.44	0.45	0.47	0.47	0.47

YouTube results

	% Labeled Nodes	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
	DEEPWALK	37.95	39.28	40.08	40.78	41.32	41.72	42.12	42.48	42.78	43.05
	SpectralClustering										
Micro-F1(%)	EdgeCluster	23.90	31.68	35.53	36.76	37.81	38.63	38.94	39.46	39.92	40.07
, ,	Modularity		_								
	wvRN	26.79	29.18	33.1	32.88	35.76	37.38	38.21	37.75	38.68	39.42
	Majority	24.90	24.84	25.25	25.23	25.22	25.33	25.31	25.34	25.38	25.38
	DeepWalk	29.22	31.83	33.06	33.90	34.35	34.66	34.96	35.22	35.42	35.67
	SpectralClustering										
Macro-F1(%)	EdgeCluster	19.48	25.01	28.15	29.17	29.82	30.65	30.75	31.23	31.45	31.54
	Modularity		_								
	wvRN	13.15	15.78	19.66	20.9	23.31	25.43	27.08	26.48	28.33	28.89
	Majority	6.12	5.86	6.21	6.1	6.07	6.19	6.17	6.16	6.18	6.19

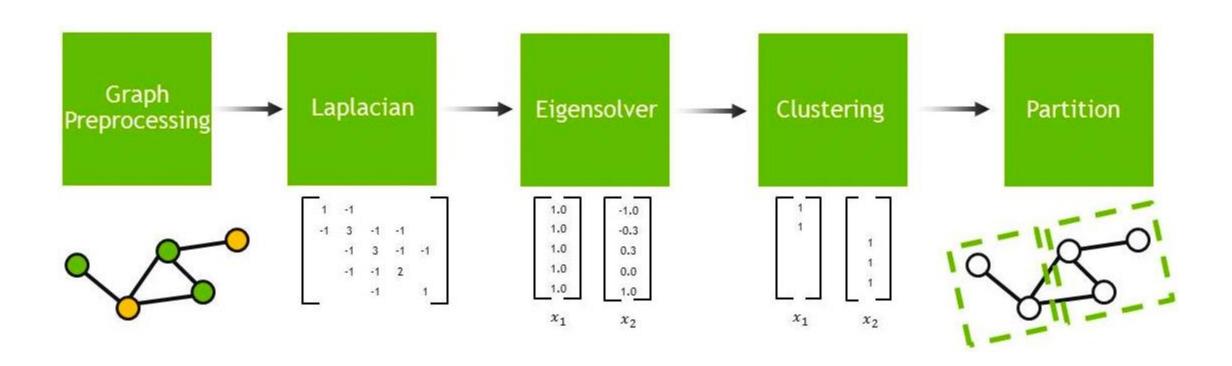
Limitations

- >O(|V|d) parameters are needed
- ➤It is impossible to generate embeddings for the nodes that have not been seen during training

Conclusion

- ➤ As an online algorithm, DeepWalk is scalable
- ➤It is possible to create meaningful representations for graphs too large to run spectral methods on
- This approach is parallelizable, allowing workers to update different parts of the model concurrently

Spectral Clustering

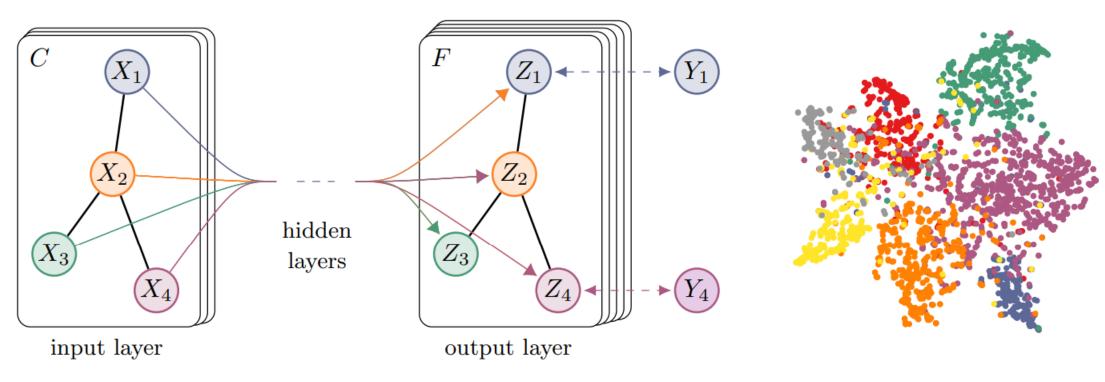


GCN step

$$H^{(l+1)} = \sigma \left(\tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}} H^{(l)} W^{(l)} \right).$$

Here, $\tilde{A}=A+I_N$ is the adjacency matrix of the undirected graph $\mathcal G$ with added self-connections. I_N is the identity matrix, $\tilde{D}_{ii}=\sum_j \tilde{A}_{ij}$ and $W^{(l)}$ is a layer-specific trainable weight matrix. $\sigma(\cdot)$ denotes an activation function, such as the $\operatorname{ReLU}(\cdot)=\max(0,\cdot)$. $H^{(l)}\in\mathbb{R}^{N\times D}$ is the matrix of activations in the l^{th} layer; $H^{(0)}=X$.

Example



(a) Graph Convolutional Network

(b) Hidden layer activations

Experiments

Dataset	Type	Nodes	Edges	Classes	Features	Label rate
Citeseer	Citation network	3,327	4,732	6	3,703	0.036
Cora	Citation network	2,708	5,429	7	1,433	0.052
Pubmed	Citation network	19,717	44,338	3	500	0.003
NELL	Knowledge graph	65,755	266,144	210	5,414	0.001

- ➤ Citation networks: three citation network datasets are used. They contain sparse bag-of-words feature vectors for each document and a list of citation links between documents. Each document has a class label.
- ➤ NELL is a dataset extracted from the knowledge graph

Results

Method	Citeseer	Cora	Pubmed	NELL
ManiReg [3]	60.1	59.5	70.7	21.8
SemiEmb [28]	59.6	59.0	71.1	26.7
LP [32]	45.3	68.0	63.0	26.5
DeepWalk [22]	43.2	67.2	65.3	58.1
ICA [18]	69.1	75.1	73.9	23.1
Planetoid* [29]	64.7 (26s)	75.7 (13s)	77.2 (25s)	61.9 (185s)
GCN (this paper)	70.3 (7s)	81.5 (4s)	79.0 (38s)	66.0 (48s)

Limitations

➤ Memory requirement

➤ Directed edges and edge features

Conclusion

- ➤ One step realization
- ➤ Model outperforms several recently proposed methods by a significant margin
- ➤ Model is still being computationally efficient