

Сверточные нейронные сети

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Факультет компьютерных наук

18 октября 2018 г.

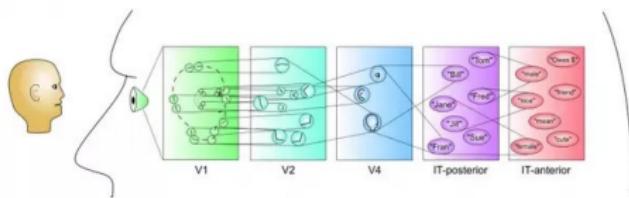
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Введение

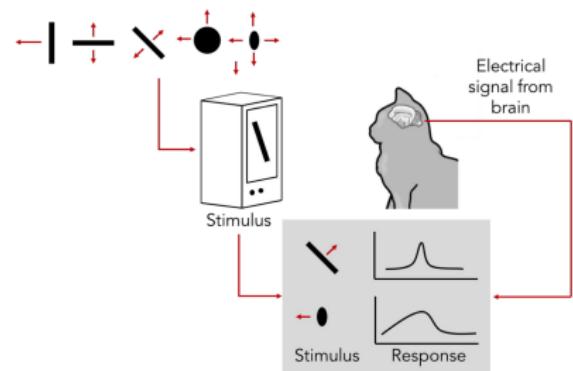
Введение

Human visual cortex



Source: <https://towardsdatascience.com/understanding-convolutional-neural-networks-221930904a8e>

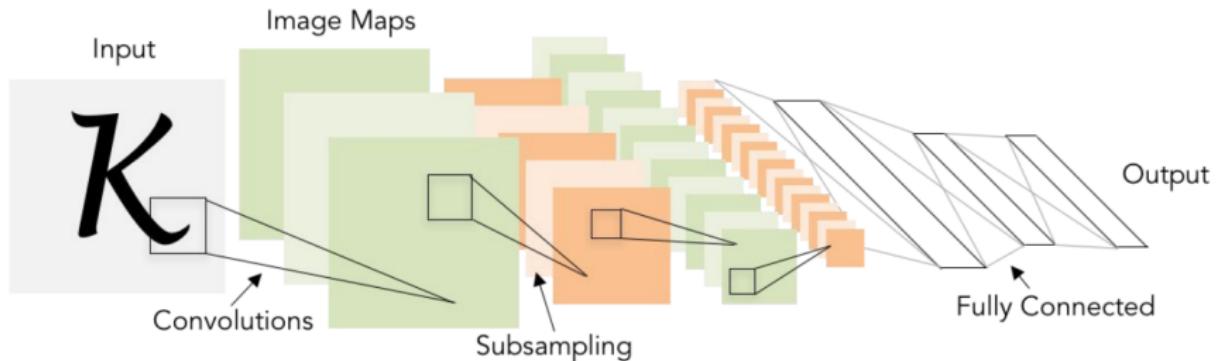
Hubel & Wiesel experiments



Source: Stanford CS class CS231n slides

Введение

The first Convolutional Neural Network – LeNet-5 LeCun, Bottou, Bengio, Haffner 1998



Source: Stanford CS class CS231n slides

Введение

Почему не стоит использовать полносвязную архитектуру для изображений?

- CIFAR-10 - картинки размера 32x32x3

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- CIFAR-10 - картинки размера 32x32x3
- Уже один нейрон на первом слое полносвязной нейронной сети будет иметь $32 \cdot 32 \cdot 3 + 1 = 3073$ параметров

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- Что-то более приличное по размеру - 200x200x3

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- Что-то более приличное по размеру - 200x200x3
- $200 \cdot 200 \cdot 3 + 1 = 120\ 001$ параметров
- 256 нейронов в слое - 30 720 256 параметров

Архитектура

Сверточный слой: фильтры

Основной компонент - фильтр свертки:

1	1	1	0	0
0	1	1	1	0
0	0	1	1	1
0	0	1	1	0
0	1	1	0	0

Input

1	0	1
0	1	0
1	0	1

Filter / Kernel

Receptive field or filter size **F** -
3x3

Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

Сверточный слой: фильтры

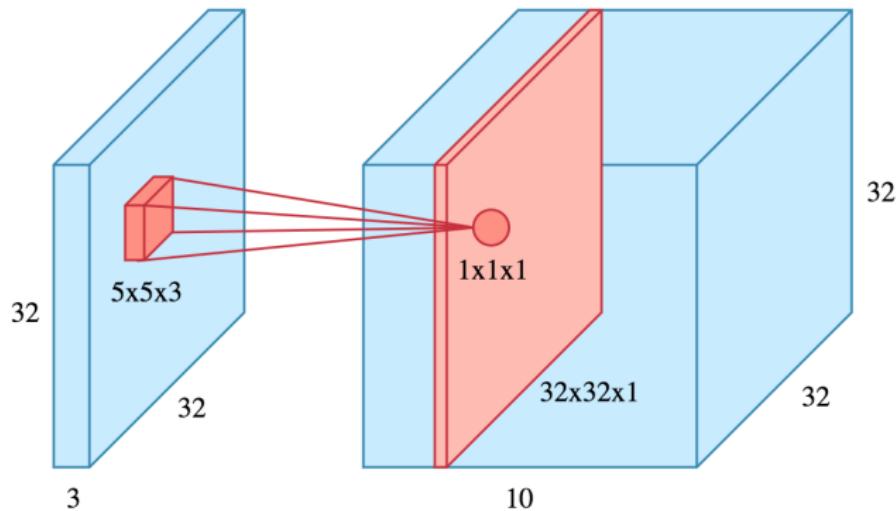
Как работает фильтр свертки?

2D - пример:

Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134cie2>

Сверточный слой: фильтры

Связь нейронов с входным слоем локальная (*local connectivity*):



Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134cie2>

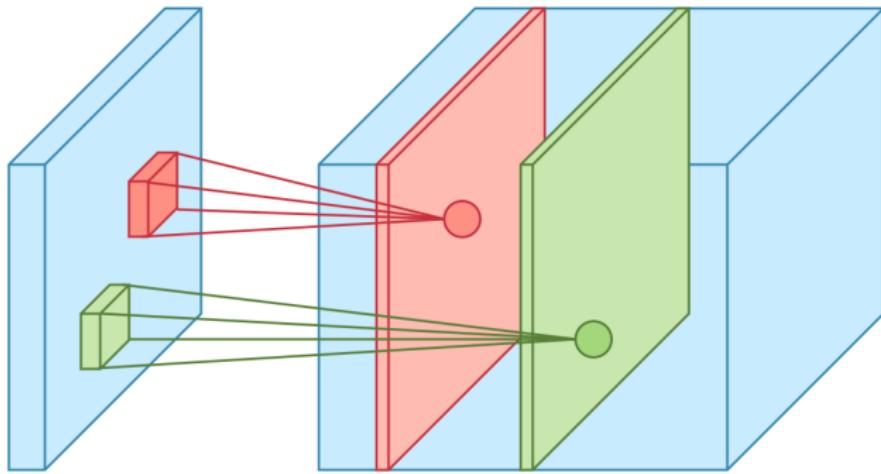
Сверточный слой: фильтры

Операция свертки в действии:

Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

Сверточный слой: фильтры

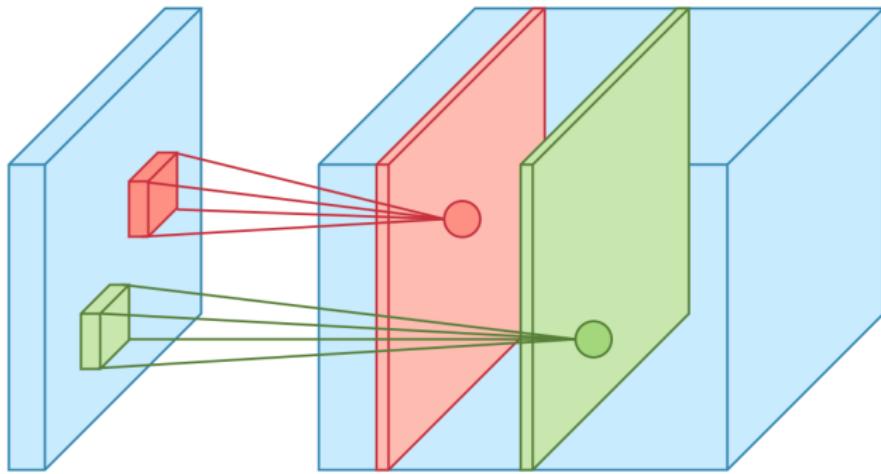
- Выход сверточного слоя - карты признаков:



Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

Сверточный слой: фильтры

- Выход сверточного слоя - карты признаков:

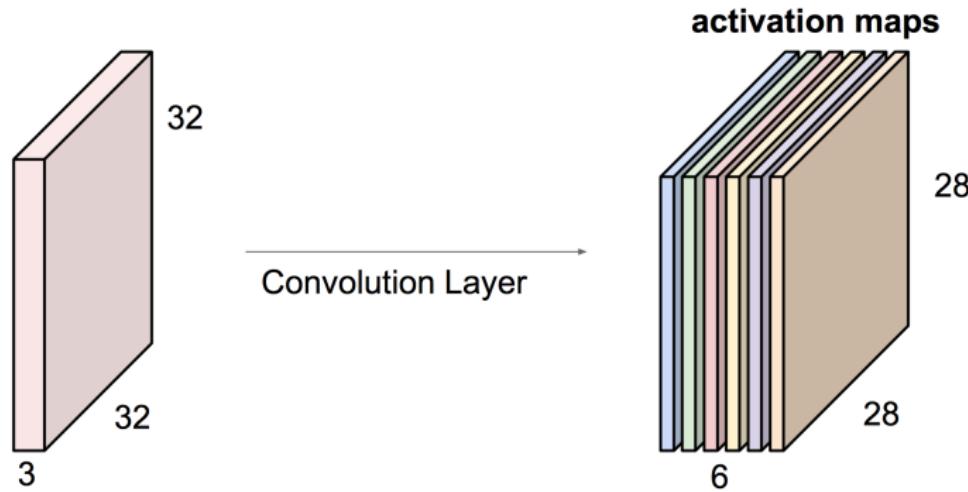


Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

- Какие размеры у выхода?

Сверточный слой: глубина выхода

Количество фильтров $K \in \mathbb{N}$



Source: Stanford CS class CS231n slides

Сверточный слой: отступы

Stride $\mathbf{S} \in \{1, 2, 3, \dots\}$

Source:

<https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

Сверточный слой: заполнение нулями

Padding $\mathbf{P} \in \{0, 1, 2, \dots\}$

Source: <https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

Сверточный слой: размер выхода

Пусть $\mathbf{W}_1 \times \mathbf{H}_1 \times \mathbf{D}_1$ - размер входного слоя

- \mathbf{F} - размер фильтра
- \mathbf{K} - количество фильтров
- \mathbf{P} - padding
- \mathbf{S} - stride

Тогда размер выходного слоя - $\mathbf{W}_2 \times \mathbf{H}_2 \times \mathbf{D}_2$

- $\mathbf{W}_2 = \frac{\mathbf{W}_1 - \mathbf{F} + 2\mathbf{P}}{\mathbf{S}} + 1$
- $\mathbf{H}_2 = \frac{\mathbf{H}_1 - \mathbf{F} + 2\mathbf{P}}{\mathbf{S}} + 1$
- $\mathbf{D}_2 = \mathbf{K}$

Сверточный слой: количество параметров

Наивная схема:

- Вход - [227x227x3]
- $F = 11, S = 4, P = 0, K = 96$
- Выход - [55x55x96]
- Всего $55 \cdot 55 \cdot 96 = 290,400$ нейронов, каждый соединен с областью размера [11x11x3]
- Каждый нейрон имеет $11 \cdot 11 \cdot 3 + 1 = 364$ параметра
- Всего $290400 \cdot 364 = 105,705,600$ параметров

Сверточный слой: количество параметров

Parameter sharing:

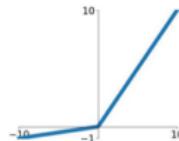
- Вход - [227x227x3]
- $F = 11, S = 4, P = 0, K = 96$
- Выход - [55x55x96]
- Все нейроны на одном *depth slice* используют одни и те же веса
- Всего 96 различных наборов весов
- Итого $96 \cdot 11 \cdot 11 \cdot 3 + 96 = 34,944$ параметра

Сверточный слой: нелинейность

Activation Functions

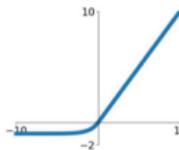
Leaky ReLU

$$\max(0.1x, x)$$



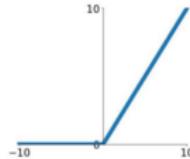
ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



ReLU

$$\max(0, x)$$

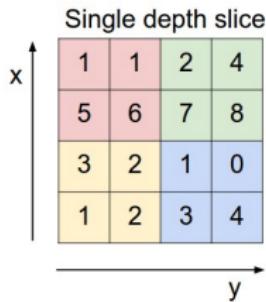


Source: Stanford CS class CS231n slides

Downsampling

Обычно используют:

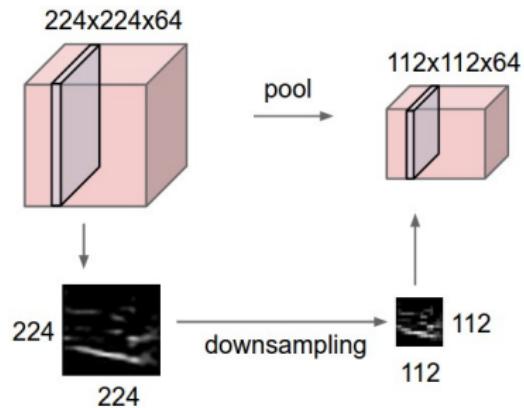
- Max pooling
- Average pooling



max pool with 2x2 filters
and stride 2



6	8
3	4



Source: Stanford CS class CS231n slides

Downsampling

Как это работает?

Пусть $\mathbf{W}_1 \times \mathbf{H}_1 \times \mathbf{D}_1$ - размер входного слоя

- \mathbf{F} - размер окна
- \mathbf{S} - stride

Тогда размер выходного слоя - $\mathbf{W}_2 \times \mathbf{H}_2 \times \mathbf{D}_2$

- $\mathbf{W}_2 = \frac{\mathbf{W}_1 - \mathbf{F}}{\mathbf{S}} + 1$
- $\mathbf{H}_2 = \frac{\mathbf{H}_1 - \mathbf{F}}{\mathbf{S}} + 1$
- $\mathbf{D}_2 = \mathbf{D}_1$

Downsampling

Зачем?

- Наличие признака важнее чем его точная позиция
- Понижаем размерность выходного слоя
- Уменьшаем количество обучаемых параметров сети
- Тем самым уменьшаем время обучения
- Контролируем переобучение

Downsampling

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- Наличие признака важнее чем его точная позиция
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Впрочем, есть подходы к проектированию сети без слоя pooling:

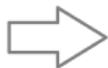
Striving for Simplicity: The All Convolutional Net

[Springenberg, Dosovitskiy, Brox, Martin, 2015]

Полносвязные слои

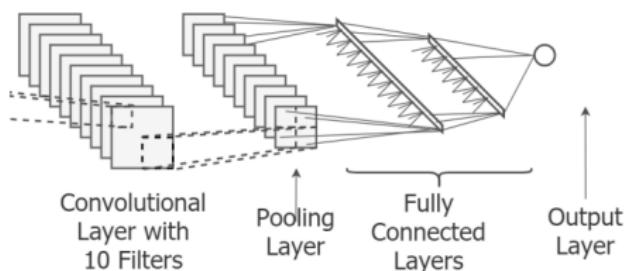
Flatten

1	1	0
4	2	1
0	2	1



1
1
0
4
2
1
0
2
1

Последние слои CNN



Source: <https://towardsdatascience.com/light-on-math-machine-learning-intuitive-guide-to-convolutional-neural-networks-e3f054dd5daa>

Source: <https://rubikscode.net/2018/02/26/introduction-to-convolutional-neural-networks>

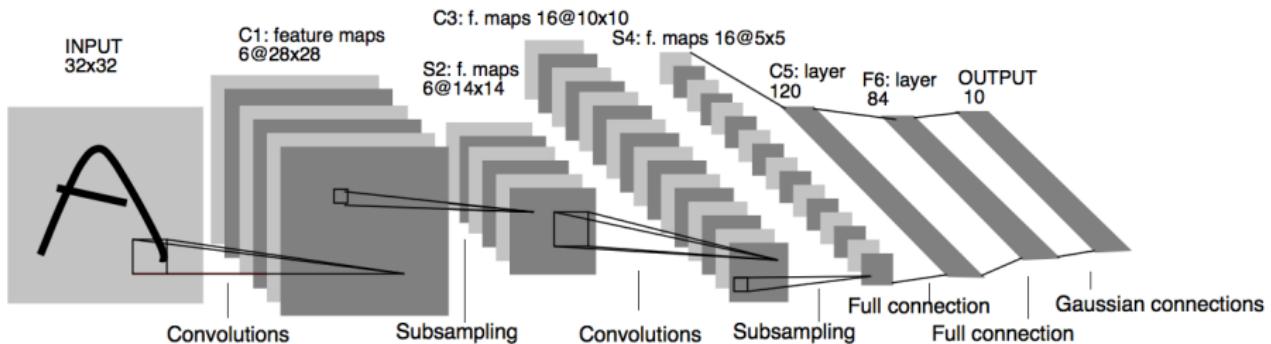
Стандартная архитектура целиком

$\text{INPUT} \rightarrow [\text{[CONV} \rightarrow \text{RELU}]^* N \rightarrow \text{POOL?}]^* M \rightarrow [\text{[FC} \rightarrow \text{RELU}]^* K \rightarrow \text{FC}]$

Стандартная архитектура целиком

INPUT → [[**CONV** → **RELU**] * N → **POOL?**] * M → [**FC** → **RELU**] * K → **FC**

LeNet-5 architecture:



Source: Gradient-based learning applied to document recognition [Y. Lecun et al., 1998]

Обучение

Backpropagation: градиент по фильтру

$$\begin{array}{|c|c|} \hline O_{11} & O_{12} \\ \hline O_{21} & O_{22} \\ \hline \end{array} = \text{Convolution} \left(\begin{array}{|c|c|c|} \hline X_{11} & X_{12} & X_{13} \\ \hline X_{21} & X_{22} & X_{23} \\ \hline X_{31} & X_{32} & X_{33} \\ \hline \end{array}, \begin{array}{|c|c|} \hline F_{11} & F_{12} \\ \hline F_{21} & F_{22} \\ \hline \end{array} \right)$$

$$O_{11} = F_{11}X_{11} + F_{12}X_{12} + F_{21}X_{21} + F_{22}X_{22}$$

$$O_{12} = F_{11}X_{12} + F_{12}X_{13} + F_{21}X_{22} + F_{22}X_{23}$$

$$O_{21} = F_{11}X_{21} + F_{12}X_{22} + F_{21}X_{31} + F_{22}X_{32}$$

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$$\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{11}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{11}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{11}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{11}}$$

$$\frac{\partial E}{\partial F_{12}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{12}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{12}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{12}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{12}}$$

$$\frac{\partial E}{\partial F_{21}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{21}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{21}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{21}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{21}}$$

$$\frac{\partial E}{\partial F_{22}} = \frac{\partial E}{\partial O_{11}} \frac{\partial O_{11}}{\partial F_{22}} + \frac{\partial E}{\partial O_{12}} \frac{\partial O_{12}}{\partial F_{22}} + \frac{\partial E}{\partial O_{21}} \frac{\partial O_{21}}{\partial F_{22}} + \frac{\partial E}{\partial O_{22}} \frac{\partial O_{22}}{\partial F_{22}}$$

Source: <https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

Backpropagation: градиент по фильтру

$$\begin{array}{|c|c|} \hline O_{11} & O_{12} \\ \hline O_{21} & O_{22} \\ \hline \end{array} = \text{Convolution} \left(\begin{array}{|c|c|c|} \hline X_{11} & X_{12} & X_{13} \\ \hline X_{21} & X_{22} & X_{23} \\ \hline X_{31} & X_{32} & X_{33} \\ \hline \end{array}, \begin{array}{|c|c|} \hline F_{11} & F_{12} \\ \hline F_{21} & F_{22} \\ \hline \end{array} \right)$$

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$$\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}}X_{11} + \frac{\partial E}{\partial O_{12}}X_{12} + \frac{\partial E}{\partial O_{21}}X_{21} + \frac{\partial E}{\partial O_{22}}X_{22}$$

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Source: <https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

Backpropagation: градиент по фильтру

$$\begin{bmatrix} \partial E / \partial F_{11} & \partial E / \partial F_{12} \\ \partial E / \partial F_{21} & \partial E / \partial F_{22} \end{bmatrix} = \text{Convolution} \left(\begin{array}{|c|c|c|} \hline X_{11} & X_{12} & X_{13} \\ \hline X_{21} & X_{22} & X_{23} \\ \hline X_{31} & X_{32} & X_{33} \\ \hline \end{array} \right) \cdot \begin{bmatrix} \partial E / \partial O_{11} & \partial E / \partial O_{12} \\ \partial E / \partial O_{21} & \partial E / \partial O_{22} \end{bmatrix}$$

$$\frac{\partial E}{\partial F_{11}} = \frac{\partial E}{\partial O_{11}} X_{11} + \frac{\partial E}{\partial O_{12}} X_{12} + \frac{\partial E}{\partial O_{21}} X_{21} + \frac{\partial E}{\partial O_{22}} X_{22}$$

$$\frac{\partial E}{\partial F_{12}} = \frac{\partial E}{\partial O_{11}} X_{12} + \frac{\partial E}{\partial O_{12}} X_{13} + \frac{\partial E}{\partial O_{21}} X_{22} + \frac{\partial E}{\partial O_{22}} X_{23}$$

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Source: <https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

Backpropagation: градиент по входу

$$\begin{array}{|c|c|} \hline O_{11} & O_{12} \\ \hline O_{21} & O_{22} \\ \hline \end{array} = \text{Convolution} \left(\begin{array}{|c|c|c|} \hline X_{11} & X_{12} & X_{13} \\ \hline X_{21} & X_{22} & X_{23} \\ \hline X_{31} & X_{32} & X_{33} \\ \hline \end{array}, \begin{array}{|c|c|} \hline F_{11} & F_{12} \\ \hline F_{21} & F_{22} \\ \hline \end{array} \right)$$

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$$\frac{\partial E}{\partial X_{11}} = \frac{\partial E}{\partial O_{11}}F_{11} + \frac{\partial E}{\partial O_{12}}0 + \frac{\partial E}{\partial O_{21}}0 + \frac{\partial E}{\partial O_{22}}0$$

$$\frac{\partial E}{\partial X_{12}} = \frac{\partial E}{\partial O_{11}}F_{12} + \frac{\partial E}{\partial O_{12}}F_{11} + \frac{\partial E}{\partial O_{21}}0 + \frac{\partial E}{\partial O_{22}}0$$

$$\frac{\partial E}{\partial X_{13}} = \frac{\partial E}{\partial O_{11}}0 + \frac{\partial E}{\partial O_{12}}F_{12} + \frac{\partial E}{\partial O_{21}}0 + \frac{\partial E}{\partial O_{22}}0$$

$$\frac{\partial E}{\partial X_{21}} = \frac{\partial E}{\partial O_{11}}F_{21} + \frac{\partial E}{\partial O_{12}}0 + \frac{\partial E}{\partial O_{21}}F_{11} + \frac{\partial E}{\partial O_{22}}0$$

$$\frac{\partial E}{\partial X_{22}} = \frac{\partial E}{\partial O_{11}}F_{22} + \frac{\partial E}{\partial O_{12}}F_{21} + \frac{\partial E}{\partial O_{21}}f_{12} + \frac{\partial E}{\partial O_{22}}F_{11}$$

$$\frac{\partial E}{\partial X_{23}} = \frac{\partial E}{\partial O_{11}}0 + \frac{\partial E}{\partial O_{12}}F_{22} + \frac{\partial E}{\partial O_{21}}0 + \frac{\partial E}{\partial O_{22}}F_{11}$$

$$\frac{\partial E}{\partial X_{31}} = \frac{\partial E}{\partial O_{11}}0 + \frac{\partial E}{\partial O_{12}}0 + \frac{\partial E}{\partial O_{21}}F_{21} + \frac{\partial E}{\partial O_{22}}0$$

$$\frac{\partial E}{\partial X_{32}} = \frac{\partial E}{\partial O_{11}}0 + \frac{\partial E}{\partial O_{12}}0 + \frac{\partial E}{\partial O_{21}}F_{22} + \frac{\partial E}{\partial O_{22}}F_{21}$$

$$\frac{\partial E}{\partial X_{33}} = \frac{\partial E}{\partial O_{11}}0 + \frac{\partial E}{\partial O_{12}}0 + \frac{\partial E}{\partial O_{21}}0 + \frac{\partial E}{\partial O_{22}}F_{22}$$

Source:

<https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

Backpropagation: градиент по входу

$\partial E / \partial X_{11}$	$\partial E / \partial X_{12}$	$\partial E / \partial X_{13}$
$\partial E / \partial X_{21}$	$\partial E / \partial X_{22}$	$\partial E / \partial X_{23}$
$\partial E / \partial X_{31}$	$\partial E / \partial X_{32}$	$\partial E / \partial X_{33}$

= Full_Convolution

$\partial E / \partial O_{11}$	$\partial E / \partial O_{12}$
$\partial E / \partial O_{21}$	$\partial E / \partial O_{22}$

,

F_{22}	F_{21}
F_{12}	F_{11}

$$\begin{aligned}\frac{\partial E}{\partial X_{11}} &= \frac{\partial E}{\partial O_{11}} F_{11} + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{12}} &= \frac{\partial E}{\partial O_{11}} F_{12} + \frac{\partial E}{\partial O_{12}} F_{11} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{13}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} F_{12} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{21}} &= \frac{\partial E}{\partial O_{11}} F_{21} + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{11} + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{22}} &= \frac{\partial E}{\partial O_{11}} F_{22} + \frac{\partial E}{\partial O_{12}} F_{21} + \frac{\partial E}{\partial O_{21}} F_{12} + \frac{\partial E}{\partial O_{22}} F_{11} \\ \frac{\partial E}{\partial X_{23}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} F_{22} + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} F_{11} \\ \frac{\partial E}{\partial X_{31}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{21} + \frac{\partial E}{\partial O_{22}} 0 \\ \frac{\partial E}{\partial X_{32}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} F_{22} + \frac{\partial E}{\partial O_{22}} F_{21} \\ \frac{\partial E}{\partial X_{33}} &= \frac{\partial E}{\partial O_{11}} 0 + \frac{\partial E}{\partial O_{12}} 0 + \frac{\partial E}{\partial O_{21}} 0 + \frac{\partial E}{\partial O_{22}} F_{22}\end{aligned}$$

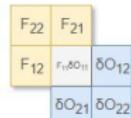
Source:

<https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

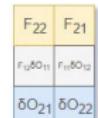
Backpropagation: градиент по входу

$\partial E / \partial X_{11}$	$\partial E / \partial X_{12}$	$\partial E / \partial X_{13}$
$\partial E / \partial X_{21}$	$\partial E / \partial X_{22}$	$\partial E / \partial X_{23}$
$\partial E / \partial X_{31}$	$\partial E / \partial X_{32}$	$\partial E / \partial X_{33}$

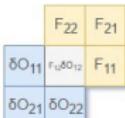
= Full_Convolution



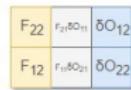
$$\delta X_1 = F_{11}\delta O_{11}$$



$$\delta X_2 = F_{12}\delta O_{11} + F_{21}\delta O_{12}$$



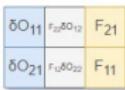
$$\delta X_3 = F_{12}\delta O_{11} + F_{21}\delta O_{12}$$



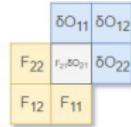
$$\delta X_2 = F_{21}\delta O_{11} + F_{11}\delta O_{21}$$



$$\delta X_2 = F_{22}\delta O_{11} + F_{21}\delta O_{12} + F_{12}\delta O_{21} + F_{11}\delta O_{22}$$



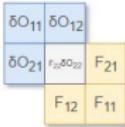
$$\delta X_3 = F_{22}\delta O_{11} + F_{21}\delta O_{12}$$



$$\delta X_1 = F_{21}\delta O_{21}$$



$$\delta X_2 = F_{22}\delta O_{21} + F_{21}\delta O_{22}$$



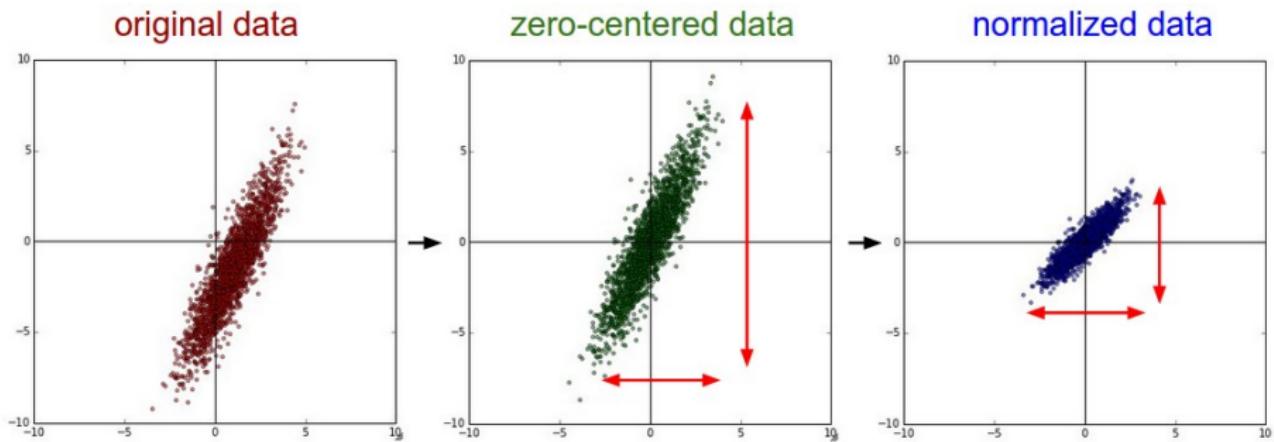
$$\delta X_3 = F_{22}\delta O_{21} + F_{21}\delta O_{22}$$

Source:

<https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>

Предобработка данных

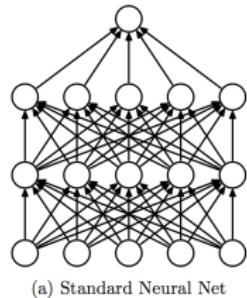
- Mean subtraction
- Normalization
- PCA / Whitening - не используются в CNN



Source: Stanford CS class CS231n slides

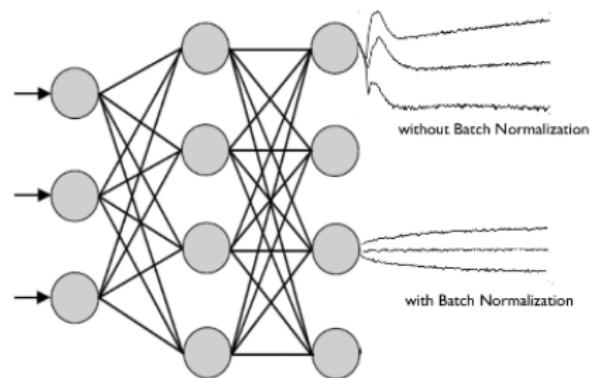
Регуляризация

Dropout



Source: Dropout: A Simple Way to Prevent Neural Networks from Overfitting [N. Srivastava et al., 2014]

Batch Normalization



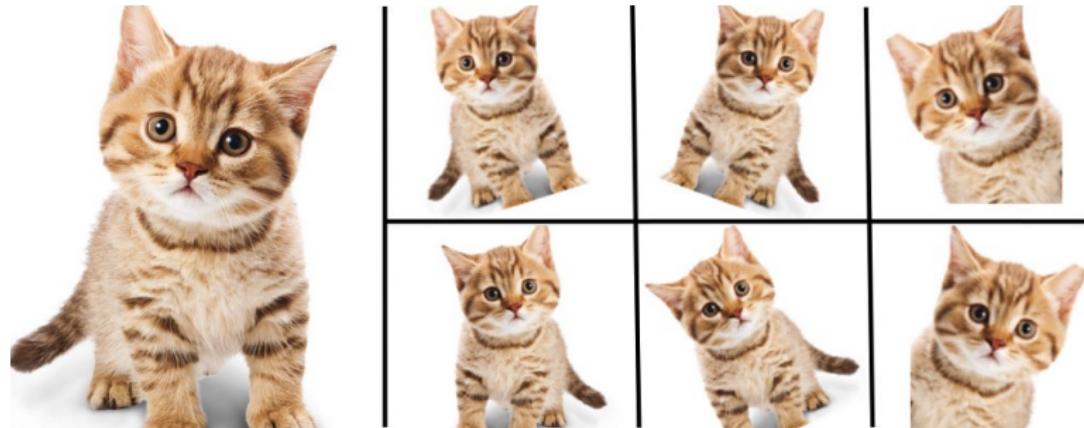
Source: <https://calculatedcontent.com/2017/06/16/normalization-in-deep-learning/>

Data augmentation

- Придумали "state-of-the-art" архитектуру под задачу?
- Но очень мало данных?
- Выход есть!

Data augmentation

- Придумали "state-of-the-art" архитектуру под задачу?
- Но очень мало данных?
- Выход есть!



Enlarge your Dataset

Source: <https://medium.com/nanoneets/how-to-use-deep-learning-when-you-have-limited-data-part-2-data-augmentation-c26971dc8ced>

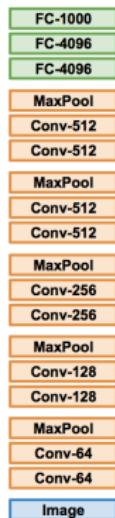
Data augmentation

Популярные техники:

- Flip
- Rotation
- Scale
- Crop
- Translation
- Color jitter (Randomize contrast and brightness)
- Gaussian Noise
- and so on...

Transfer learning

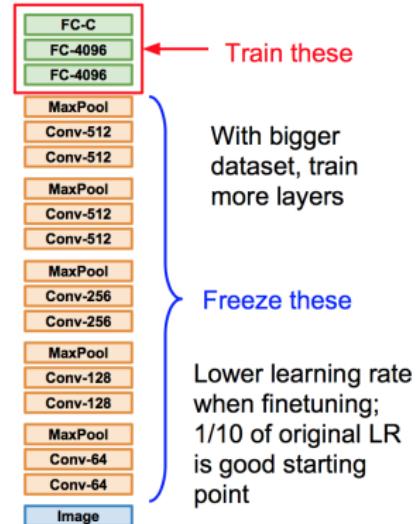
1. Train on Imagenet



2. Small Dataset (C classes)



3. Bigger dataset



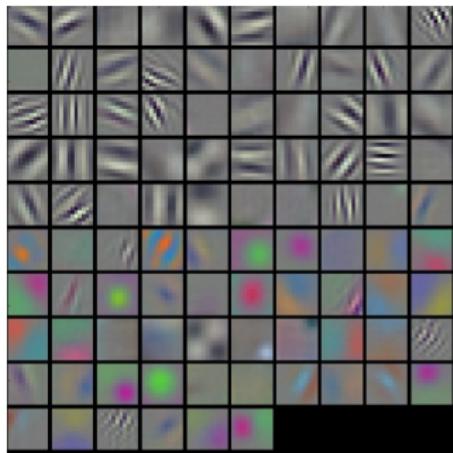
Source: Stanford CS class CS231n slides

Визуализация

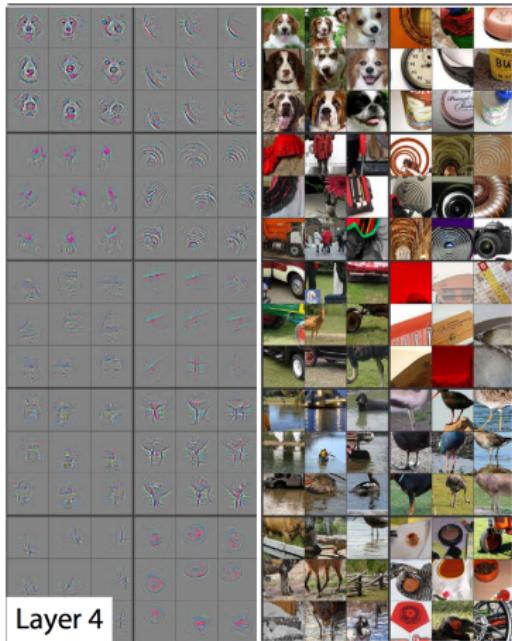
Визуализация

Reconstructed patterns that cause high activations

Фильтры первого слоя



Source: Stanford CS class CS231n slides

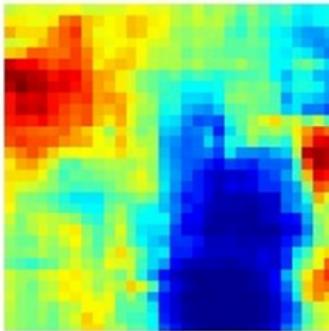
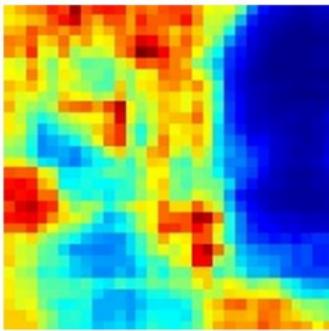
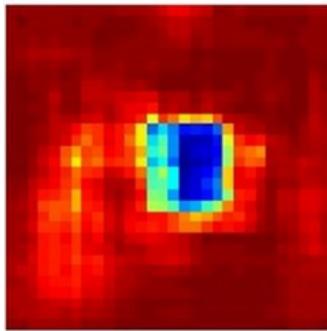
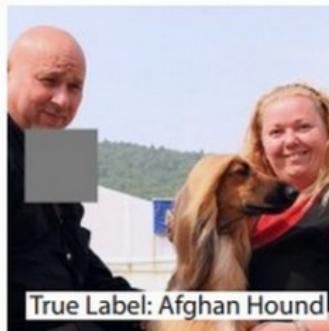


Layer 4

Source: Visualizing and Understanding
Convolutional Networks [Matthew D. Zeiler,
Rob Fergus, 2013]

Визуализация

Probability of the correct class as a heatmap



Source: Visualizing and Understanding Convolutional Networks [Matthew D. Zeiler, Rob Fergus, 2013]

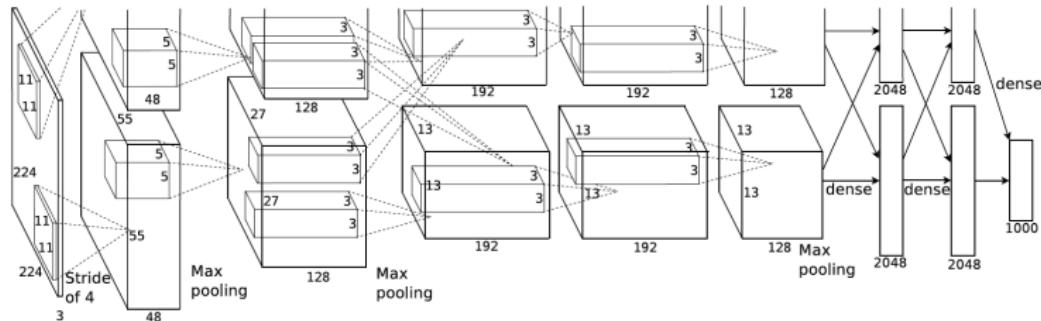
Современные архитектуры

Современные архитектуры

- ImageNet – 14,197,122 images, 21841 synsets indexed
- ILSVRC – ImageNet Large Scale Visual Recognition Challenge (1000 classes)

AlexNet

- 60M parameters
- ReLU activations
- Dropout
- Data augmentation
- 2 GPUs / 1 week
- ILSVRC-2012 winner - top-5 error of 15.3%



Source: ImageNet Classification with Deep Convolutional Neural Networks [Alex Krizhevsky et al., 2012]

VGGNet

- Simple - 3x3 filters only
- Deep - 16/19 layers
- Data augmentation
- 4 GPUs / 2-3 weeks
- ILSVRC-2014 2nd place
- top-5 7.3% error

ConvNet Configuration									
A	A-LRN	B	C	D	E				
11 weight layers	11 weight layers	13 weight layers	16 weight layers	16 weight layers	19 weight layers				
input (224 × 224 RGB image)									
conv3-64	conv3-64 LRN	conv3-64 conv3-64	conv3-64 conv3-64	conv3-64 conv3-64	conv3-64 conv3-64				
		maxpool							
conv3-128	conv3-128	conv3-128 conv3-128	conv3-128 conv3-128	conv3-128 conv3-128	conv3-128 conv3-128				
		maxpool							
conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256	conv3-256 conv3-256 conv1-256	conv3-256 conv3-256 conv3-256	conv3-256 conv3-256 conv3-256				
		maxpool							
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 conv1-512	conv3-512 conv3-512 conv3-512	conv3-512 conv3-512 conv3-512				
		maxpool							
conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512	conv3-512 conv3-512 conv1-512	conv3-512 conv3-512 conv3-512	conv3-512 conv3-512 conv3-512				
		maxpool							
FC-4096									
FC-4096									
FC-1000									
soft-max									

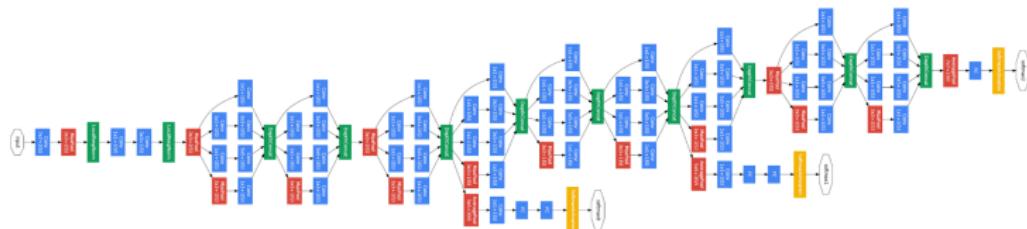
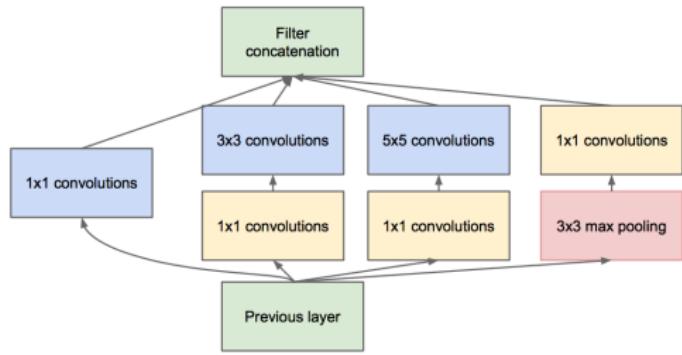
Table 2: Number of parameters (in millions).

Network	A,A-LRN	B	C	D	E
Number of parameters	133	133	134	138	144

Source: Very Deep Convolutional Networks for Large-Scale Image Recognition [Simonyan & Zisserman, 2014]

GoogleNet

- 9 inception modules
- Very deep ≈ 100 layers in total
- $\approx 5M$ parameters
- "Few high-end GPUs" / 1 week
- ILSVRC-2014 winner - top-5 6.7% error



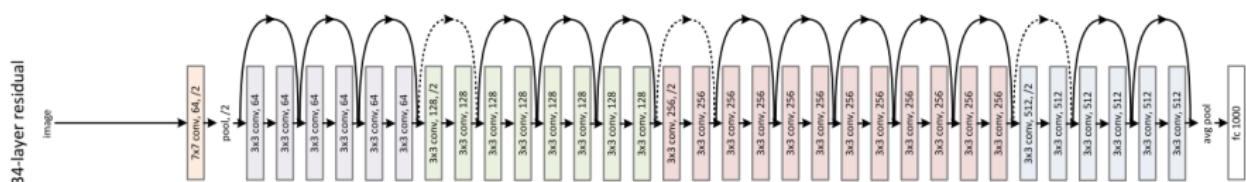
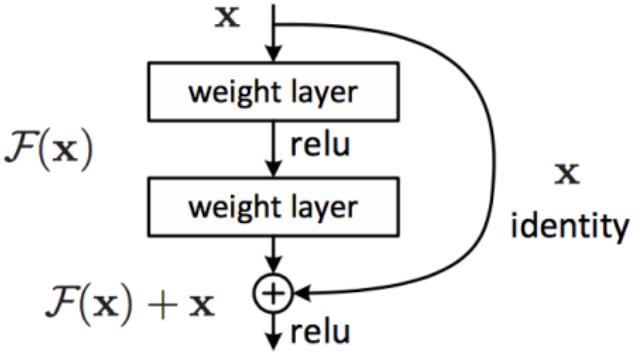
Source: Going Deeper with Convolutions [C. Szegedy1, W. Liu et al., 2015]



"Well said, Leo, well said"

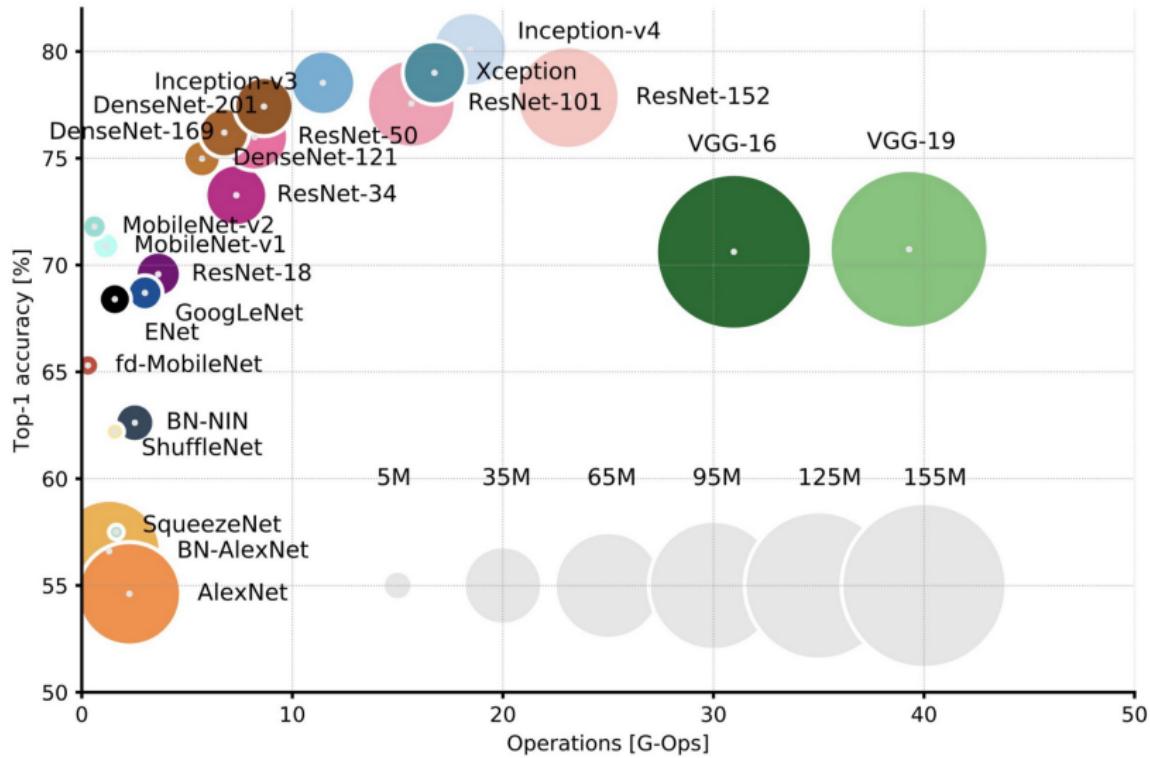
Microsoft ResNet

- 152 layers (tried 1202 layers)
- Residual block
- 8 GPUs / 2-3 weeks
- ILSVRC-2015 winner - top-5 3.57% error



Source: Deep Residual Learning for Image Recognition [Kaiming He, Xiangyu Zhang et al., 2015]

Сравнение



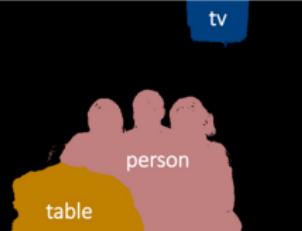
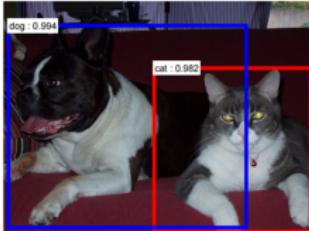
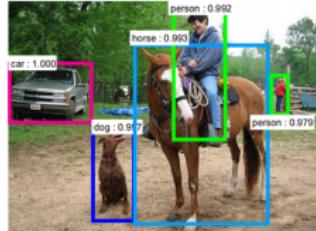
Source: <https://towardsdatascience.com/neural-network-architectures-156e5bad51ba>

Области применения

Области применения

- Image Classification
- Object Detection
- Video Classification
- Object Tracking
- Edge Detection
- Semantic Segmentation
- Human Pose Estimation
- Image Captioning
- Question Answering (based on image)
- Image Generation

Области применения



What kind of store is this?	bakery baker pastry	art supplies grocery grocery
Is the display case as full as it could be?	no no no	no yes yes



How many bikes are there?	2 2 2	3 4 12
What number is the bus?	48 48 48	4 46 number 6



man in black shirt is playing guitar.



construction worker in orange safety vest is working on road.



two young girls are playing with lego toy.



boy is doing backflip on wakeboard.

Source: <https://skymind.ai/wiki/convolutional-network>

Итоги

- Основные компоненты CNN - сверточный слой, pooling слои, полносвязные слои
- В одном сверточном слое используют набор фильтров
- Градиент по матрице весов или входного слоя можно вычислить, применив свертку
- Batch Normalization и Data augmentation для регуляризации
- Transfer learning – способ добиться хорошего качества на малом объеме данных
- Современные архитектуры очень глубокие, применяются нестандартные подходы к проектированию

Источники

 Stanford CS class CS231n lecture notes

 Applied Deep Learning - Part 4: Convolutional Neural Networks,
<https://towardsdatascience.com/applied-deep-learning-part-4-convolutional-neural-networks-584bc134c1e2>

 The 9 Deep Learning Papers You Need To Know About,
<https://adeshpande3.github.io/The-9-Deep-Learning-Papers-You-Need-To-Know-About.html>

 Forward And Backpropagation in Convolutional Neural Network,
<https://medium.com/@2017csm1006/forward-and-backpropagation-in-convolutional-neural-network-4dfa96d7b37e>