# **ACIDS, BASES AND SOLUTION EQUILIBRIA**

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### **HILARY TERM** Lecture 3

#### 5. Redox reactions and equilibria

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### 5. Redox reactions and equilibria

Redox reactions involve a change in the *oxidation numbers* of the species involved.

*Electron transfer* reactions are the simplest of redox processes:

$$X^m + Y^n \rightarrow X^{m-1} + Y^{n+1}$$

X = oxidant, Y = reductant, and M = oxidation are formal oxidation numbers before the reaction. The term oxidation number is a formal assignment. An element is often said to be in a certain oxidation state and have a certain oxidation number. In practice, the terms oxidation number and oxidation state are used interchangeably.

Atom transfer reactions are also redox reactions:

$$XO + Y \rightarrow X + YO$$
  
 $X + YH_2 \rightarrow XH_2 Y$ 

In terms of thermodynamics, electron-transfer and atom transfer reactions can be treated alike. They are related through acid-base chemistry.

Redox reactions can occur entirely in solution, e.g.

$$\label{eq:Fe} \text{Fe}^{2+}_{(aq)} \ + \ \text{Cr}^{2+}_{(aq)} \ \to \ \text{Fe}^{2+}_{(aq)} \ + \ \text{Cr}^{3+}_{(aq)}$$
 
$$3\text{CH}_3\text{CH}_2\text{OH} \ + \ 2\text{Cr}\text{O}_4^{2-} \ + \ 10\text{H}^+ \ \to \ 3\text{CH}_3\text{CHO} \ + \ 2\text{Cr}^{3+}_{(aq)}$$

or at the interface, e.g. on an electrode

$$Cu^{2+} \ + \ 2e^{-} \ \rightarrow \ Cu_{(s)}$$

### 5.1. Thermodynamics of electron transfer: The Nernst equation

Consider oxidant and reductant in equilibrium with  $H^+$  (unit activity) and  $H_2$  (1atm pressure).

$$A_{ox} + H_2 \leftrightarrow A_{red} + 2H^+_{(aq)}$$

At equilibrium:

$$K = \frac{[A_{red}][H^+]^2}{[A_{ox}][H_2]} = 10^{\left(\frac{-\Delta G^o_{rxn}}{2.3RT}\right)}$$

If we consider the reaction in terms of electron transfer, we can write the equilibrium as two half-reactions (c.f. proton transfer):

$$A_{ox} + 2e^{-} \leftrightarrow A_{red}$$
  
 $2H^{+}_{(aq)} + 2e^{-} \leftrightarrow H_{2}$   
 $\Delta G^{o}_{rxn} = \Delta G^{o}_{A} - \Delta G^{o}_{H}$ 

however, by definition  $\Delta G^{o}_{H} = 0$ , so  $\Delta G^{o}_{rxn} = \Delta G^{o}_{A}$ 

$$\Delta G^{\circ} = -nE^{\circ}F$$

where  $E^{\circ}$  is the standard reduction potential (vs the Standard Hydrogen Electrode – SHE) of  $A_{ox}$ . Another way of putting that is that  $E^{\circ}$  is the difference in standard reduction potentials for the couples  $A_{ox}/A_{red}$  and  $2H^{+}/H_{2}$ .

$$E^{\circ} = (2.3RT/nF)\log K$$

For any system:  $\Delta G = \Delta G^{\circ} + 2.3RT \log Q$ 

Where Q is the reaction quotient  $\frac{[A_{red}][H^+]^2}{[A_{ox}][H_2]}$ , which is equal to  $\frac{[A_{red}]}{[A_{ox}]}$  when referenced against SHE.

#### The Nernst equation

$$E = E^{o} - \frac{2.3RT}{nF} log \left( \frac{[A_{red}]}{[A_{ox}]} \right)$$

$$E = E^{o} + \frac{2.3RT}{nF} log \left( \frac{[A_{ox}]}{[A_{red}]} \right)$$

at 298K: 
$$E = E^o + 0.059 log \left( \frac{[A_{ox}]}{[A_{red}]} \right)$$

The thermodynamics of any redox reaction can be computed by comparing their E° values. As a result:

$$A_{ox} + B_{red} \leftrightarrow A_{red} + B_{ox}$$
  $K_{AB}$ 

Comprises of the two half-reactions:

$$A_{ox} + ne^- \leftrightarrow A_{red}$$
  $E^{\circ}_{A}$   
 $B_{ox} + ne^- \leftrightarrow B_{red}$   $E^{\circ}_{B}$ 

Subsequently: 
$$log K_{AB} = (nF/2.3RT)(E_A^o - E_B^o)$$

The quantity  $\underline{\mathsf{nE}^\circ}$  is the volt-equivalent. It is very important to realise that  $\underline{\mathsf{E}^\circ}$  values cannot be manipulated without the inclusion of n.

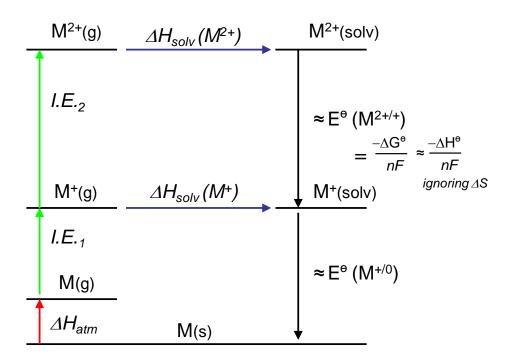
### 5.2. Reduction potentials, ionisation potentials and solvation effects

Reduction potentials refer to a half-reaction written in the following form:

$$A_{ox} + ne^- \leftrightarrow A_{red}$$

in which the other half reaction is the reference (SHE), with  $E^{\circ} = 0$ .

Ignoring entropy terms, standard reduction potentials E° can be related to ionisation potentials and enthalpies of solvation and atomisation using the following thermodynamic cycle:



The higher (more positive) E°, the stronger the oxidant. High oxidation states are favoured (E° lowered) by a strong interaction with solvent. High enthalpies of atomisation decrease the reducing power of metals (raise E°).

#### Sequential electron transfers

Consider the disproportionation reaction:

$$2M^{n+} \hspace{0.1in} \leftrightarrow \hspace{0.1in} M^{(n+1)+} \hspace{0.1in} + \hspace{0.1in} M^{(n-1)+}$$

which comprises of the following two half-reactions:

$$M^{n+} + e^{-} \leftrightarrow M^{(n-1)+} E^{o}_{1}$$
 $M^{(n+1)+} + e^{-} \leftrightarrow M^{n+} E^{o}_{2}$ 
 $\log K_{disp} = (nF/2.3RT)(E^{o}_{1}-E^{o}_{2}) = 16.9n (E^{o}_{1}-E^{o}_{2})$ 

Then

If  $E_1^0 > E_2^0$ , then  $M^+$  is unstable with regard to disproportionation.

Example: Stability of Cu<sup>+</sup>(aq)

## 6. Latimer and Frost diagrams

### Latimer digrams

A Latimer diagram is a simple way of representing a series of step-wise half-reactions.

$$Cu^{2+}_{aq} \xrightarrow{0.15V} Cu^{+}_{aq} \xrightarrow{0.52V} Cu_{(s)}$$

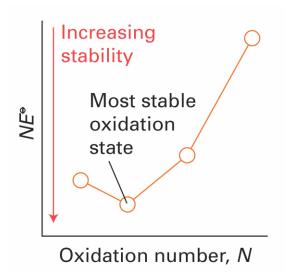
$$0.37V$$

$$MnO_{4~aq}^{-} \xrightarrow{\hspace*{1cm}} MnO_{4~aq}^{2-} \xrightarrow{\hspace*{1cm}} MnO_{2(s)} \xrightarrow{\hspace*{1cm}} MnO_{3+} \xrightarrow{\hspace*{1cm}} Mn^{3+}_{aq} \xrightarrow{\hspace*{1cm}} Mn^{2+}_{aq} \xrightarrow{\hspace*{1cm}} Mn^{(s)}$$

Reduction potentials for transformations between any species in the series are easily calculated. An important point is that E° values alone cannot be used since they are not additive. Instead, it is essential to use *volt-equivalents* (nE°).

#### Frost digrams

A Frost diagram is another way of depicting multiple step-wise electron transfers. It is a plot of volt equivalents against oxidation state. The slope of a line joining any two data points is the reduction potential for that process. It is easy to assess whether a species in a redox series will be stable or unstable with regard to disproportionation.

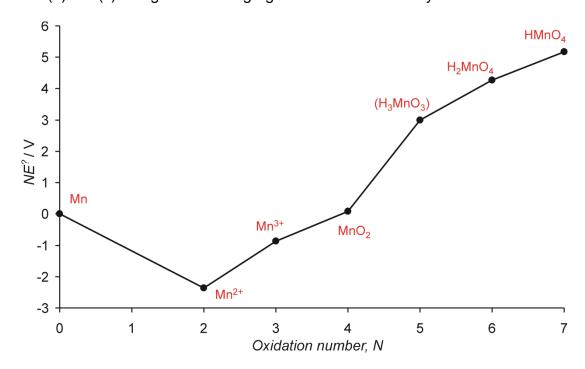


A *Frost diagram* portrays inherent stability and is also a convenient way to see how good (thermodynamically) a species is an oxidising or a reducing agent.

The species lying in the 'well' is *inherently* more stable.

#### 6.1 Inherent stabilities of oxidation states

A Frost diagram for **Manganese** aqua species at pH = 0 is pictured. The 'thermodynamic sink' is Mn(II). Mn(s) is a good reducing agent.  $Mn^{3+}$  is inherently unstable.



The Frost diagram for **Nitrogen** aqua species at pH = 0 and pH = 14. The nitrogen molecule ( $N_2$ ) is inherently very stable. Although note that  $N_2$  should be reducible to  $NH_4^+$  at pH = 0. Hydroxylamine ( $NH_2OH$ ) is inherently very unstable under both acidic and alkaline conditions. <u>A Frost diagram does not offer us any information on kinetics</u>. Formation if  $NH_4^+$  from  $N_2$  is extremely slow without a catalyst.

