



MIDDLE EAST TECHNICAL UNIVERSITY

EE564

DESIGN OF ELECTRICAL MACHINES

Project-1 Inductance and Transformer Modeling

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1 INDUCTOR DESIGN

In this study, inductor wrapped around a toroidal core will be analyzed. Designed inductor is aimed to be used in an application where inductor current is composed of a large DC component and a small AC component at 40 kHz. For this application, inductor is expected to have an inductance value more than 500 μ H when carrying the maximum current of 40A. In order to evaluate the low cost powder core materials in such an application, Kool M μ MAX has been selected as the core material. And after investigating available products and using stored energy (LI^2 Product) **0079337A7** from Magnetics has been selected as the inductor core for this study.

PROPERTIES OF THE SELECTED CORE

Physical properties of the selected core has been given in Figure 1.1 and material properties are given in [1] and [2] in detail.

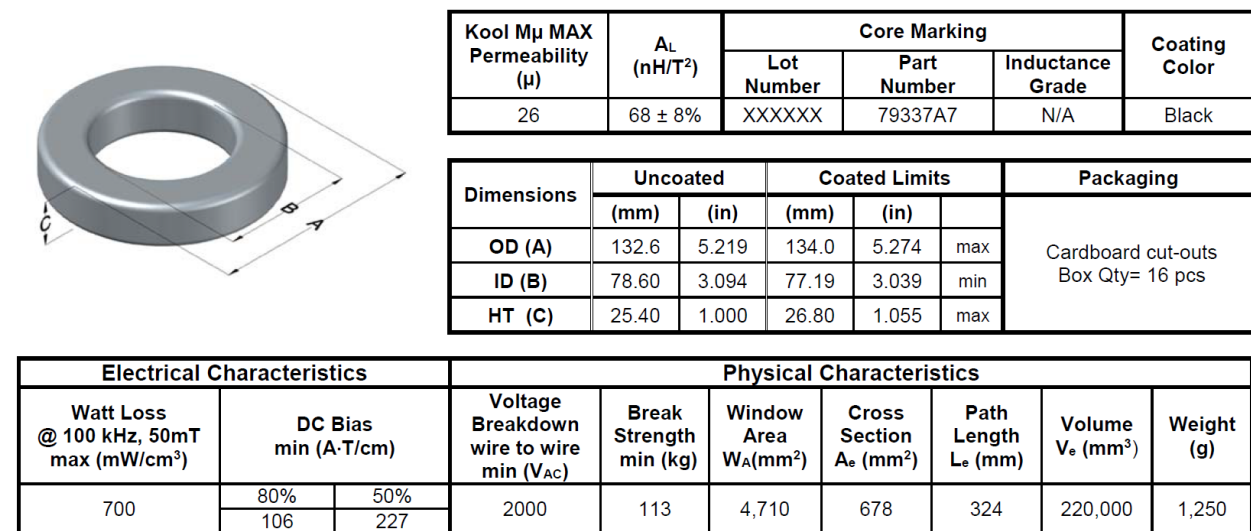


Figure 1.1 Properties of 0079337A7

B-H characteristics of the selected core material is given in Figure 1.2 and a linearized version is given in Figure 1.3. Since powder core materials show "soft saturation" characteristics it is not an easy process to select a saturation region. Because of that an operating point ($H= 300A.T/cm$)

where B-H curve slope considerably reduced and winding factor stays below 0.5 has been selected for the specified inductor current rating. Resulting turn count is then found to be 240.

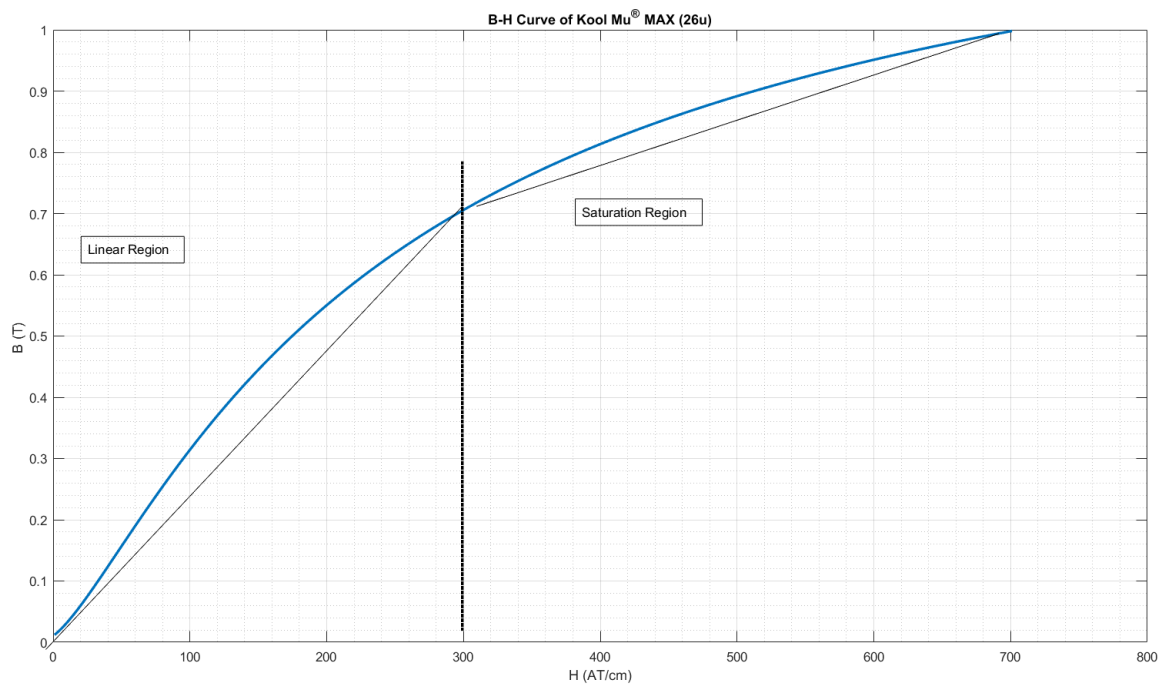


Figure 1.2 B-H Curve of the selected toroid core (Kool mu MAX 26u)

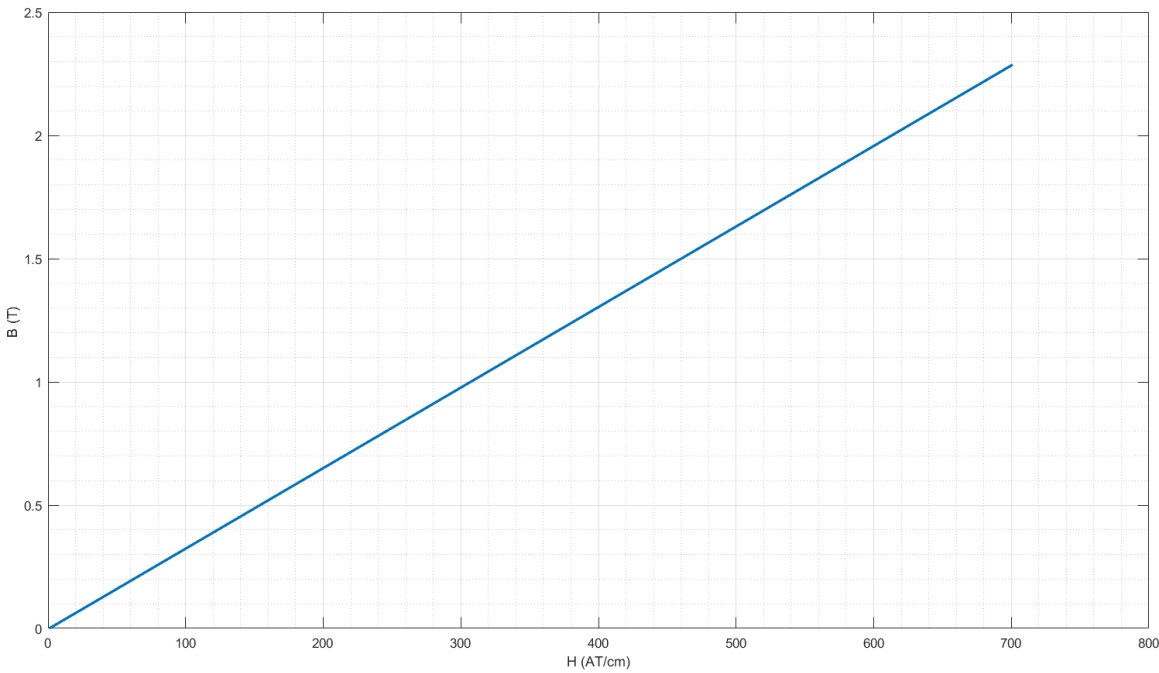


Figure 1.3 Linearized B-H Curve for the selected core material (Kool mu MAX 26u)

Part A Analytical Calculations

- **Inductance calculation with homogeneous flux distribution and linear B-H characteristics**

$$L = \frac{\Lambda}{I} = \frac{N\Phi}{I} \quad , \quad \Phi = BA_e \quad \text{and} \quad B = \frac{NIu_r u_0}{l_e}$$

then:

$$L = \frac{N^2 A_e u_r u_0}{l_e}$$

Where A_e (Figure 1.1) is equal to core area, $N=240$ is the number of turns, u_r is the relative permeability of the core which is taken as 26 for this calculation, I is the DC current which is equal to 40A and l_e is the mean flux path length.

Then inductance L is found to be 3.9 mH

- **Inductance calculation with non-homogeneous flux distribution and linear B-H characteristics**

$$\Phi = H_{core} \int_{r_{in}}^{r_{out}} B(r) dr \quad \text{where} \quad B(r) = \frac{NIu_r u_0}{2\pi r}$$

Where H_{core} is the height of the core and u_r is again 26

$L = \frac{N\Phi}{I}$ is then found to be 4 mH using Matlab

- **Inductance Calculation with homogeneous flux distribution, non-linear B-H characteristics and DC current is increased by 50%**

From Figure 1.4, $B=0.85$ T and $L=2.3$ mH

- Inductance calculation with non-homogeneous flux distribution, non-linear BH characteristics and DC current is increased by 50%

$$\Phi = H_{core} \int_{r_{in}}^{r_{out}} B(r) dr \quad \text{where} \quad B(r) = \frac{NIu(r)u_0}{2\pi r}$$

Using B-H relation fitting formula given in [2], L found to be 2.9 mH

- Inductance calculation of gapped toroid with homogeneous flux distribution, linear BH characteristics

$$\Phi = BA_e$$

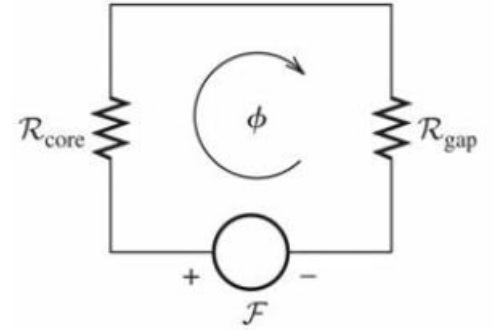
$$\Phi = A_e \frac{NI}{(R_{gap} + R_{core})}$$

Where

$$R_{core} = \frac{l_e}{(A_e u_r u_0 + R_{core})} \quad \text{and} \quad u_r = 26$$

$$R_{gap} = \frac{l_{gap}}{(A_{gap} u_0)} \quad A_{gap} = A_e$$

$$L=3.4 \text{ mH}$$



- Inductance calculation of gapped toroid with homogeneous flux distribution, linear BH characteristics and considering fringing flux

This time air gap area will be taken larger fringing area would be proportional to the gap length therefore gap dimensions can be enlarged by the gap length, i.e.

$$A_{gap} = (width_of_the_core + l_{gap}) * (depth_of_the_core + l_{gap})$$

$$L=3.5\text{mH}$$

Part B Finite Element Analysis (FEA) of Toroid Inductor

Constructed model of the designed inductor is given in Figure 1.5. In this model, the copper coil is represented by 24 homogeneously distributed copper regions and each of them represents 10 series wounded windings. An air region is placed inside and outside of the toroid.

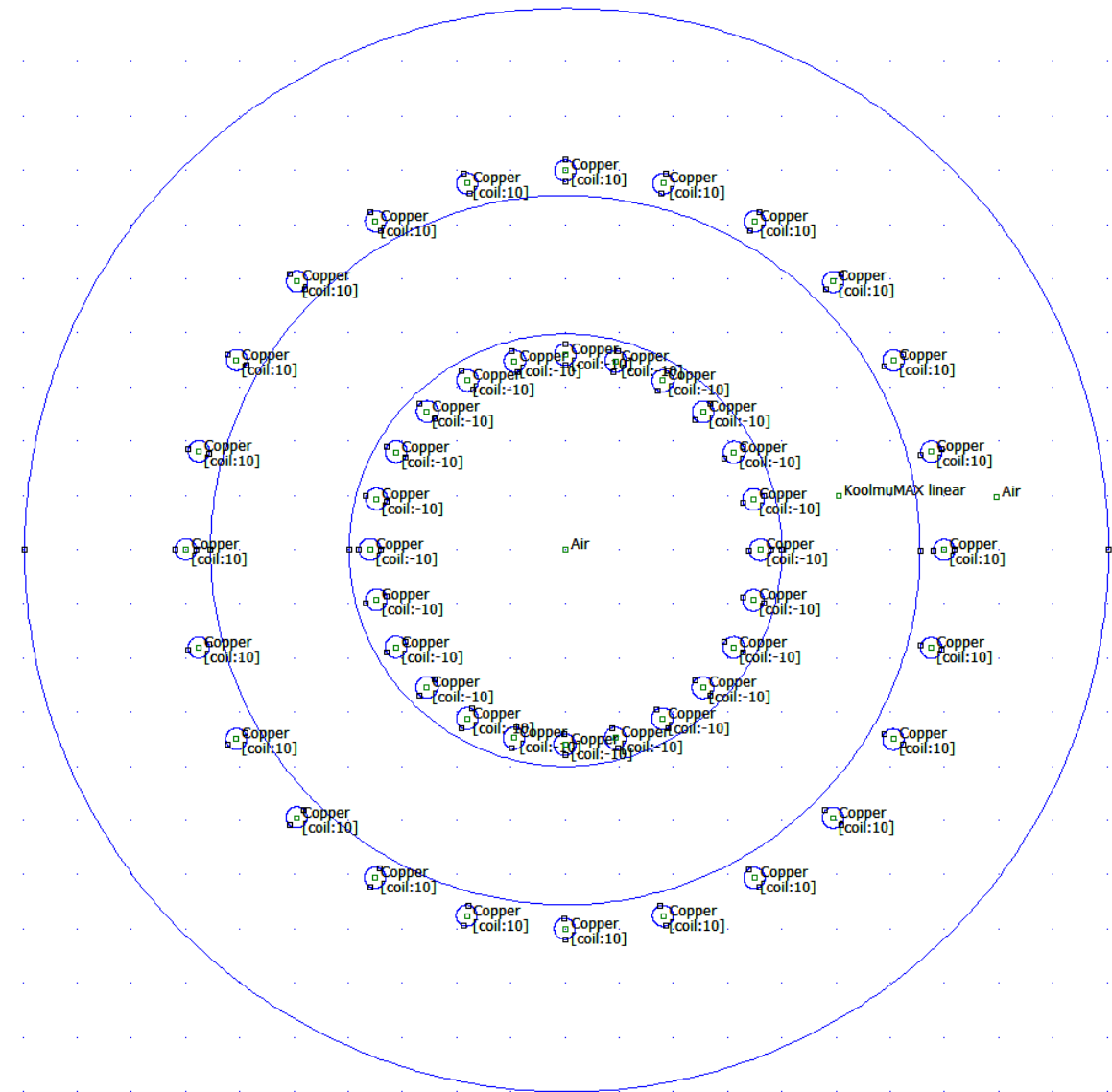


Figure 1.5 FEA model of the designed inductor in FEMM

Flux distribution with linear core characteristics

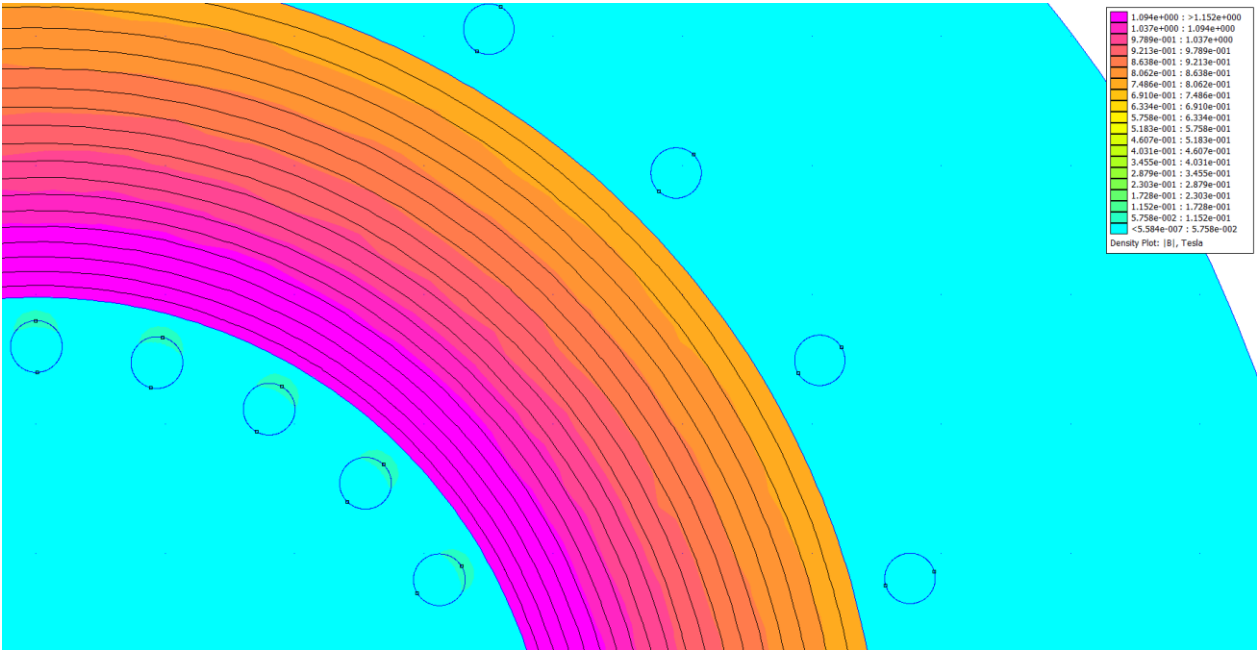


Figure 1.6 Flux distribution with linear core characteristics

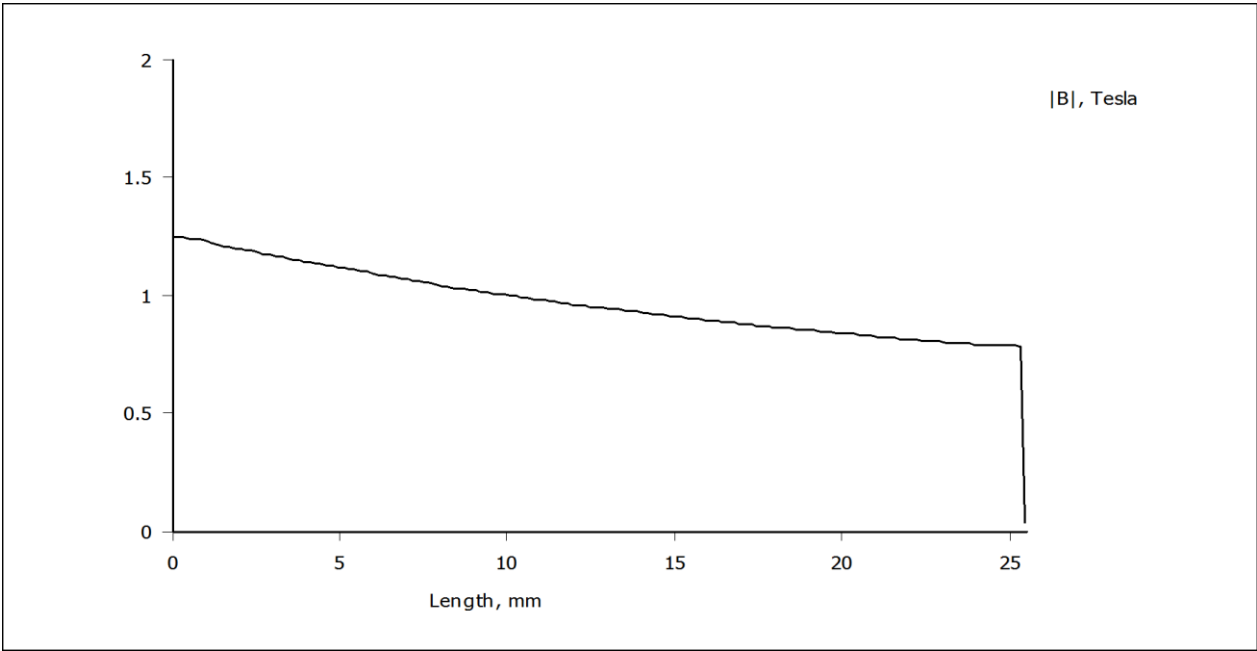
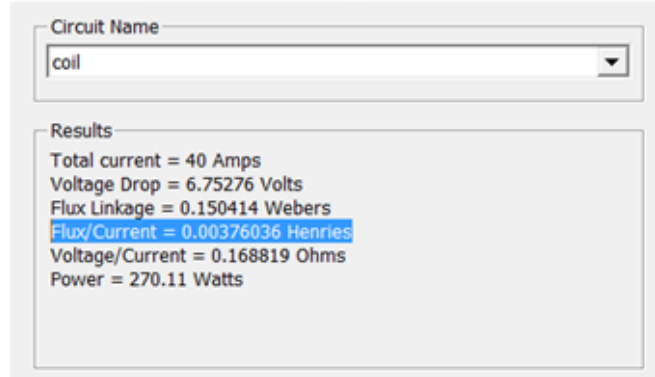


Figure 1.7 Variation of flux density from inner wall to outer wall

Inductance Calculation Method 1

Flux linkage and total inductance of the coil is calculated automatically by the software and reported as shown in the figure at the right side



The screenshot shows a software window with a 'Circuit Name' dropdown menu set to 'coil'. Below it, a 'Results' section displays the following values: Total current = 40 Amps, Voltage Drop = 6.75276 Volts, Flux Linkage = 0.150414 Webers, Flux/Current = 0.00376036 Henries (highlighted in blue), Voltage/Current = 0.168819 Ohms, and Power = 270.11 Watts.

Parameter	Value
Total current	40 Amps
Voltage Drop	6.75276 Volts
Flux Linkage	0.150414 Webers
Flux/Current	0.00376036 Henries
Voltage/Current	0.168819 Ohms
Power	270.11 Watts

Inductance Calculation Method 2

Alternatively, total inductance can be calculated using the stored energies in the air and core regions as follows:

Magnetic energy stored in the air: $W_{air} = 0.03789 \text{ Joules}$

then:

$$L_{lk} = \frac{2 * W_{air}}{I^2} = 47 \text{ uH}$$

Magnetic energy stored in the core: $W_{core} = 2.9631 \text{ Joules}$

then:

$$L_{core} = \frac{2 * W_{core}}{I^2} = 3.703 \text{ mH}$$

$$L_{total} = L_{core} + L_{lk} = 3.75 \text{ mH}$$

For linear core properties, it has seen that both method gives similar results.

Flux distribution with nonlinear core characteristics

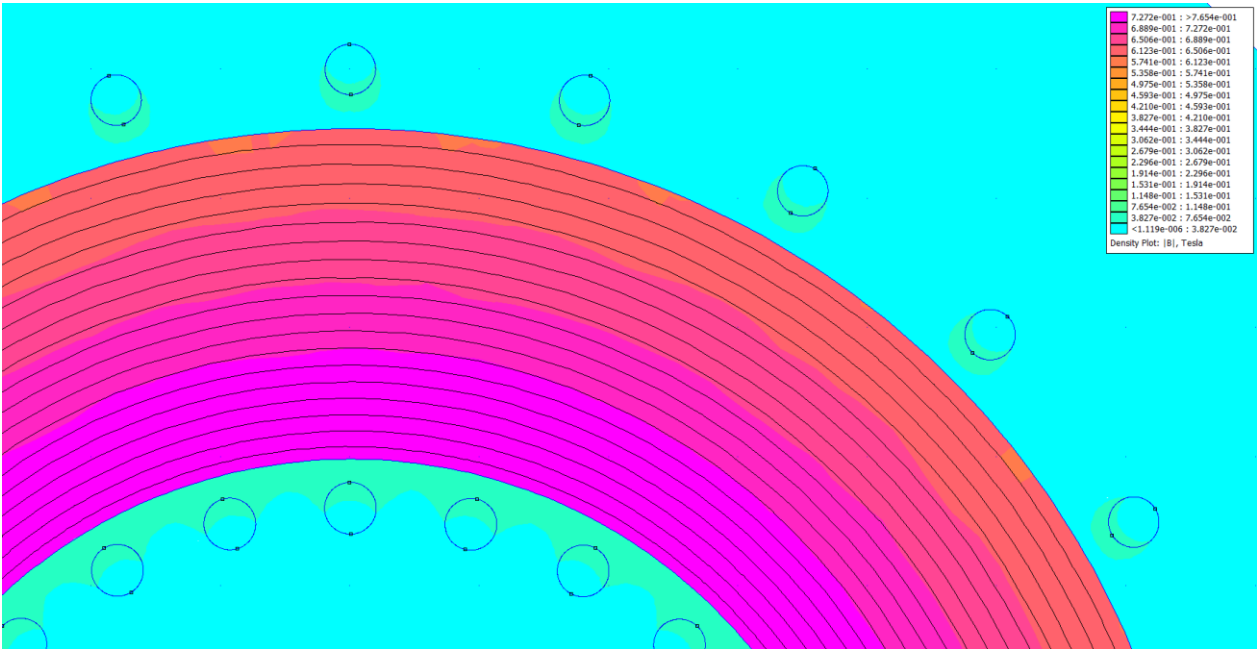


Figure 1.8 Flux distribution with linear core characteristics

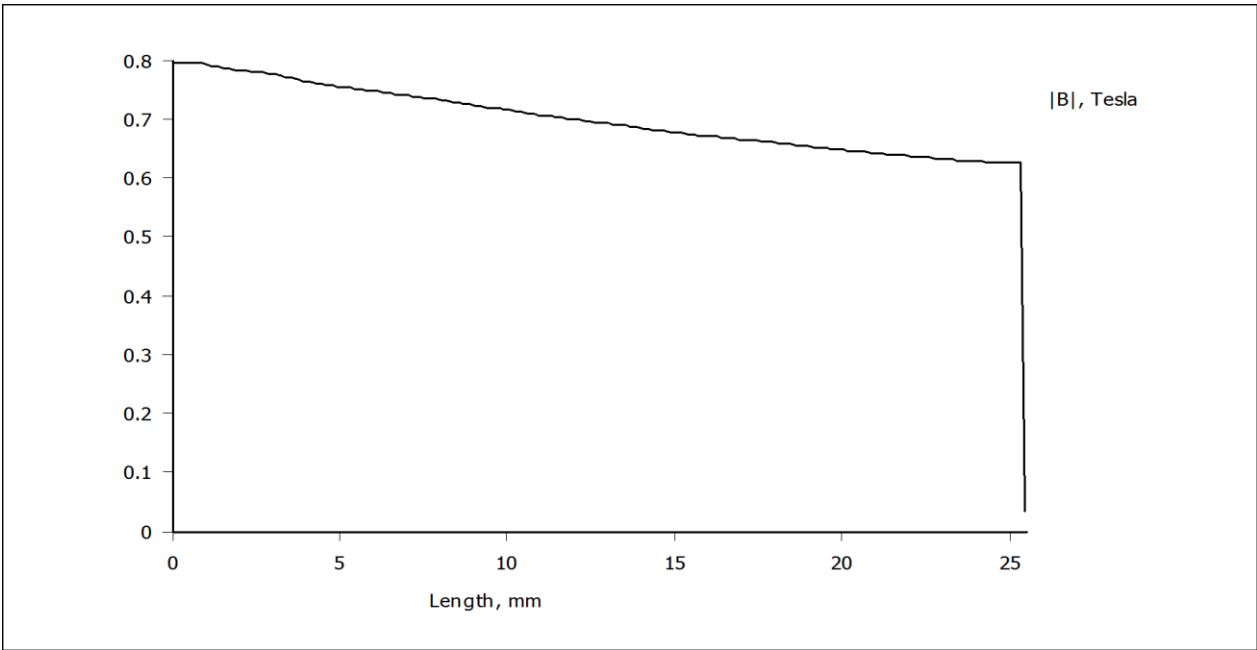
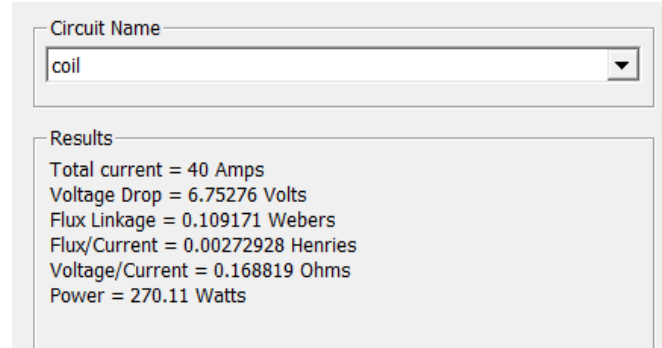


Figure 1.9 Variation of flux density from inner wall to outer wall

Inductance Calculation Method 1

Flux linkage and total inductance of the coil is calculated automatically by the software and reported as shown in the figure at the right side



The screenshot shows a software window with a 'Circuit Name' dropdown menu set to 'coil'. Below it, a 'Results' section displays the following values:

Parameter	Value
Total current	40 Amps
Voltage Drop	6.75276 Volts
Flux Linkage	0.109171 Webers
Flux/Current	0.00272928 Henries
Voltage/Current	0.168819 Ohms
Power	270.11 Watts

Inductance Calculation Method 2

Alternatively, inductance can be calculated using the stored energies in the air and core regions as follows:

Magnetic energy stored in the air: $W_{air} = 0.03784 \text{ Joules}$

then:

$$L_{lk} = \frac{2 * W_{air}}{I^2} = 47 \text{ uH}$$

Magnetic energy stored in the core: $W_{core} = 1.7838 \text{ Joules}$

then:

$$L_{core} = \frac{2 * W_{core}}{I^2} = 2.229 \text{ mH}$$

$$L_{total} = L_{core} + L_{lk} = 2.276 \text{ mH}$$

However, in this case there is a significant difference between obtained inductance values with these two methods. In [3], it has been reported that it is usually better to use method1 since FEMM calculates the flux linkage using a method that accounts for this additional energy (energy is stored outside the modeled problem domain i.e boundaries), whereas integrating $B \times H$ over all elements does not.

Flux distribution of the gapped toroid

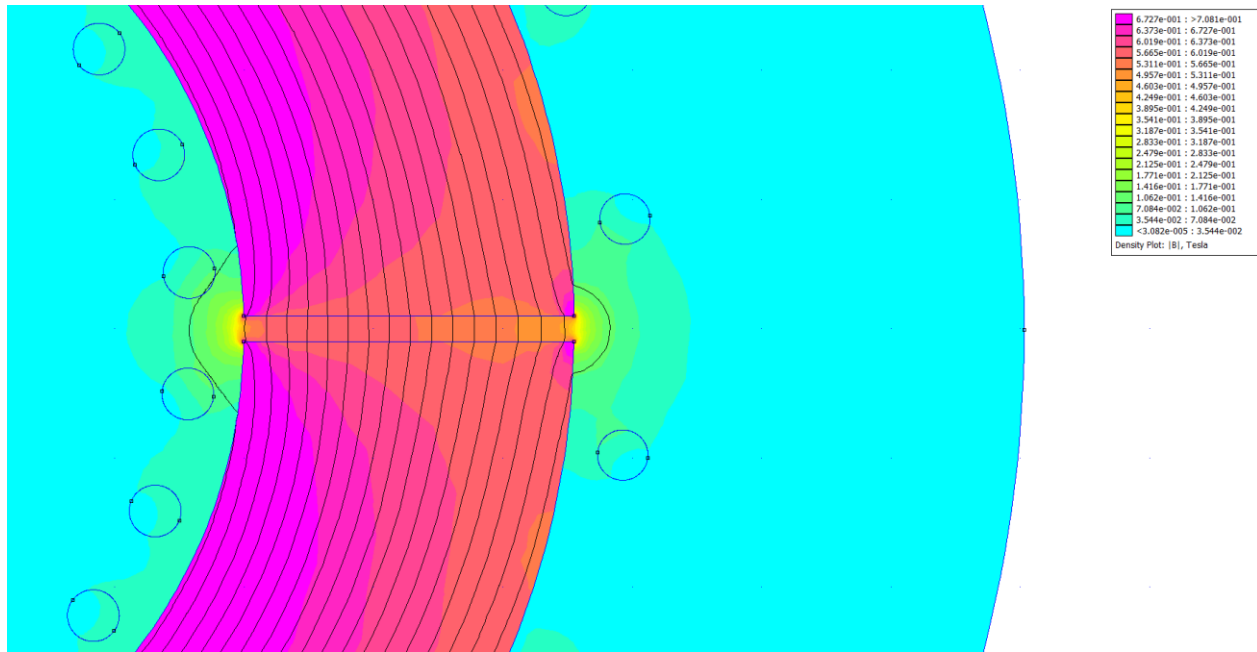


Figure 1.10 Flux distribution of the gapped toroid inductor

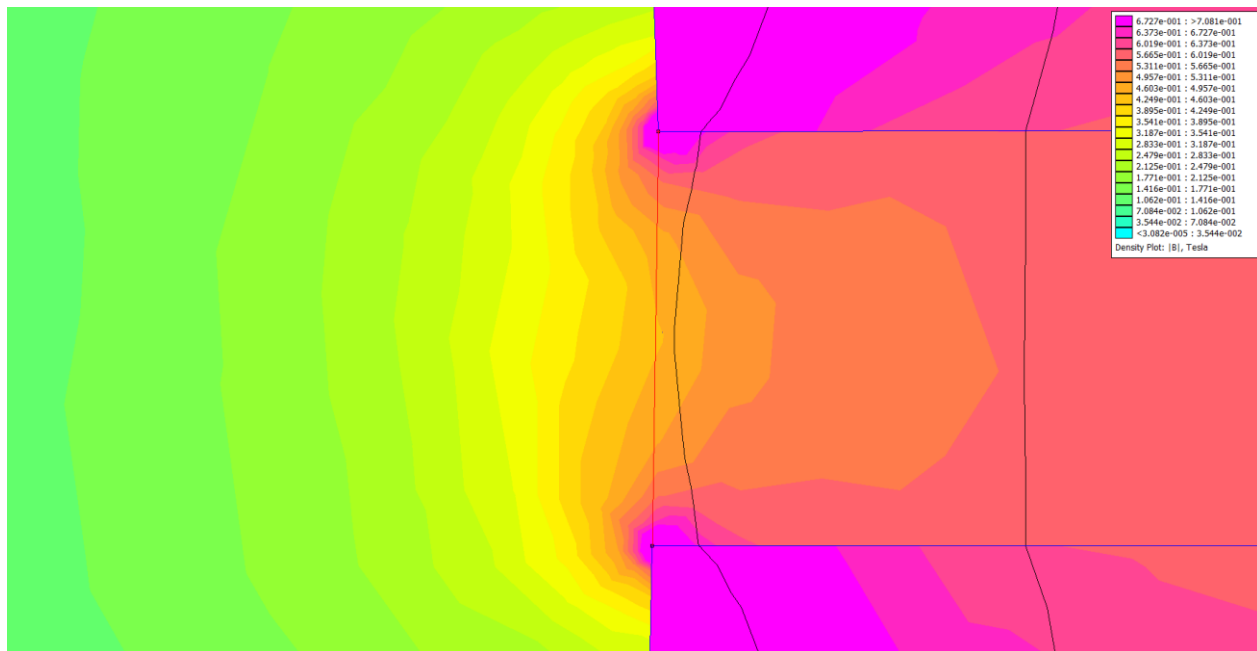


Figure 1.11 Flux distribution of the gapped toroid inductor (zoomed)

As it has shown in Figure 1.10 and in Figure 1.11, flux distribution not only at the outside of the core but also at the inside of the core is seriously affected with the placement of the air gap. It has seen that, at the vicinity of the air gap, magnetic flux inside the core loose its uniformity and it is concentrated at the edges of the gap. Air gap flux has also a non-uniform distribution and flows outside of the gap area and it has seen that effective air gap area enlarged by the length of air gap at both sides. However, flux density in this enlarged section is almost half of that in the inside of the gap.

Another important point which should be noted is the high concentration of the magnetic flux which is normal to the core surface at the edges of gap. As Figure 1.12 illustrates, a high magnetic flux density, perpendicular to the core, is observed at the edges of the core. This is an aspect of the gapped inductor design and it should be considered when placing conductors in order to prevent high Eddy current losses.

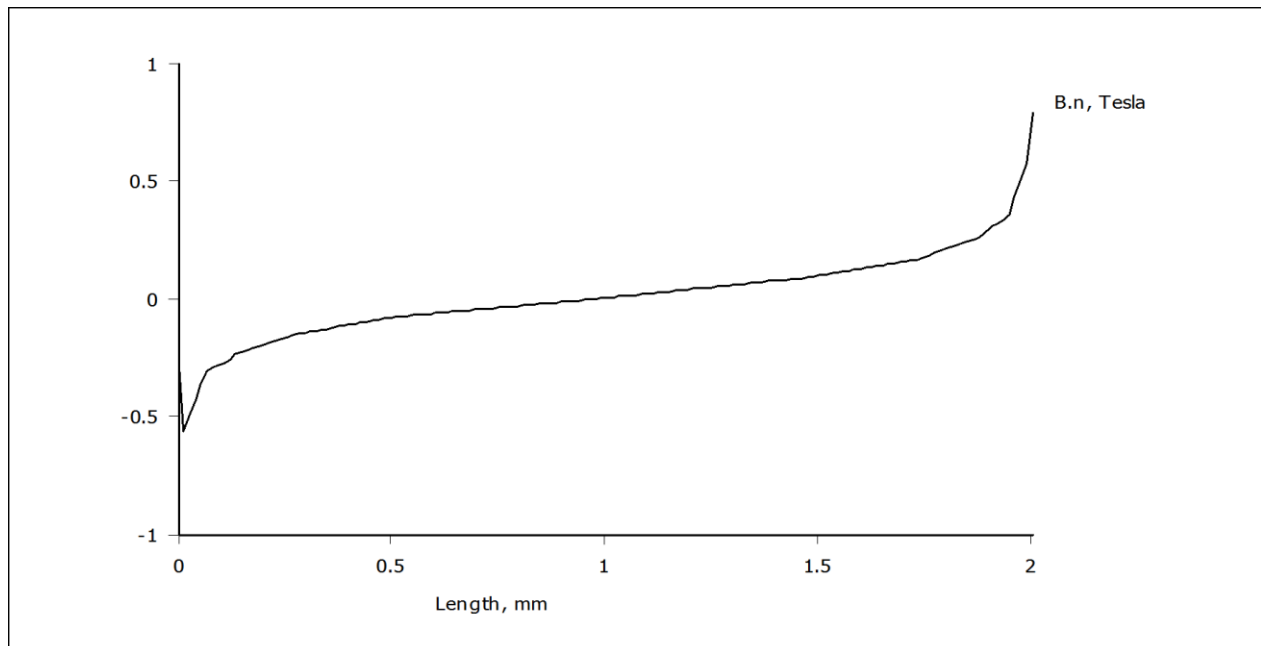
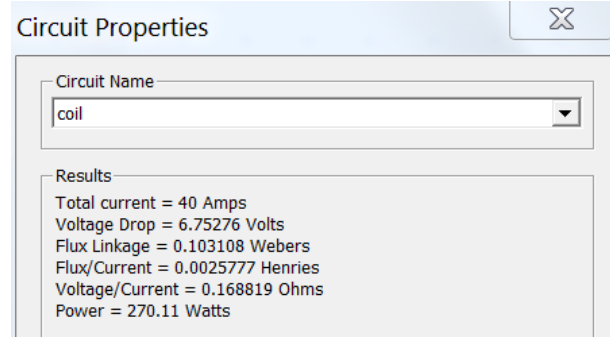


Figure 1.12 Flux distribution which is perpendicular to core through the air gap

Inductance Calculation

Method 1

Flux linkage and total inductance of the coil is calculated automatically by the software and reported as shown in the figure at the right side



Method 2

Alternatively, inductance can be calculated using the stored energies in the air and core regions as follows:

Magnetic energy stored in the air: $W_{air} = 0.2215 \text{ J}$

then:

$$L_{lk} = \frac{2 * W_{air}}{I^2} = 277 \text{ uH}$$

Magnetic energy stored in the core: $W_{core} = 1.5616 \text{ J}$

then:

$$L_{core} = \frac{2 * W_{core}}{I^2} = 1.952 \text{ mH}$$

$$L_{total} = L_{core} + L_{air} = 2.229 \text{ mH}$$

However, in this case there is a significant difference between obtained inductance values with these two methods. In [3], it has been reported that it is usually better to use method1 since FEMM calculates the flux linkage using a method that accounts for this additional energy (energy is stored outside the modeled problem domain i.e boundaries), whereas integrating $B \times H$ over all elements does not.

Part C- Discussion

	L (Analytic Calculation)	L (Simulation)
Linear Core Model	4 mH	3.75 mH
Non-linear Core Model	2.9 mH	2.72 mH
Gapped Linear	3.5 mH	
Gapped non-linear		2.229 mH

Although, FEA tool calculates the leakage flux in addition to the core flux, it has seen that analytic calculations result in slightly higher inductance values. Which is an unexpected situation and probably caused by a modeling mistake.

In 2D analysis the we can only analyze core flux distribution and leakage flux distribution in two dimension and assume same for all depths. This may not cause a large discrepancy for the core flux calculation. However, leakage flux would be concentrated in a toroid space rather than a cylindrical. Additionally, calculation of the fringing flux will also give better results with 3D simulation.

2 TRANSFORMER DESIGN

Specifications

- 500 kVA, Single Phase
- 34.5kV/25 kV
- 50 Hz
- Ambient Temp: -30C-50C
- Core Material Grain oriented Steel.

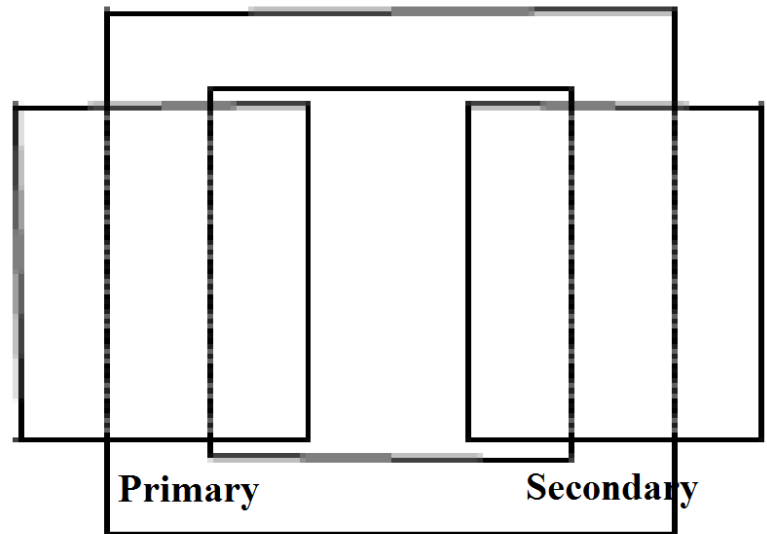


Figure 2.2.1 Core type single phase transformer

Optimum operating point of a transformer can be calculated analytically as shown in Figure 2.3. However, in this study an optimum operating point will be obtained by numerical iterations in the accompanying excel file.

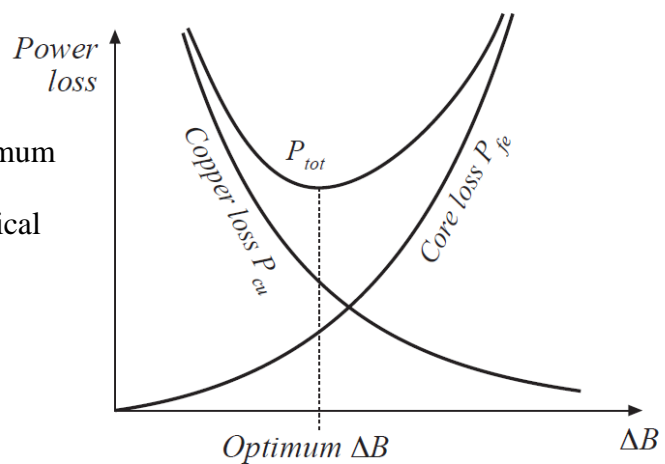


Figure 2.2 Optimum operating point of a transformer

3 REFERENCES

[1] [0079337A7](#) datasheet.

[2] [2017-Magnetics-Powder-Core-Catalog](#).

[3] Finite Element MethodMagneticsInductanceExample, online:
<http://www.femm.info/wiki/inductanceexample>

[4] M4 Grain Oriented Steel price, online: https://www.alibaba.com/product-detail/Silicon-Steel-Prices-M4-M5-for_60295733102.html?spm=a2700.7724857.main07.24.7dfd177bcoSDFd&s=p.

[5] JFE Grain Oriented Steel Cathalog , online:
<http://www.jfesteel.co.jp/en/products/electrical/catalog/f1e-001.pdf>