

# Causal Inference

## Introduction: Causality and the Fundamental Problem of Causal Inference

Ken Stiller

25th April 2022

# Causal Inference

*“Felix, qui potuit rerum cognoscere causas”*

- *Virgil, 29BC.*

## Why Causal Inference?

- ▶ Our world is full of causal claims!
- ▶ This is inevitable!
- ▶ Can you think of anything that relates to knowledge that does not rely on a chain of cause and effect
- ▶ Can we answer questions about the (social) world, without making assumptions about whether X and Y are causally related?
- ▶ It will make you a better voter, informed citizen, allow you to make better decisions, and differentiate fake news.

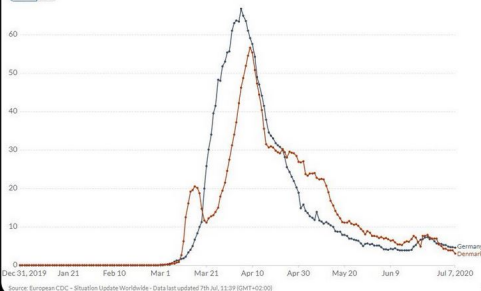
# Do Masks Protect You Against Covid?

Because masks do not have any effect on the shape of the curve: **Denmark** without masks vs. **Germany** with mask - can you tell me where you see the effects of masks in **Germany** ??

Daily new confirmed COVID-19 cases per million people

Shown is the rolling 7-day average. The number of confirmed cases is lower than the number of actual cases; the main reason for that is limited testing.

LINEAR LOG



One (among too many!) weird, weird thoughts on Twitter.

# Do Masks Protect You Against Covid? II



Backed up by a real doctor - seems legit.

# Do Masks Protect You Against Covid? III



So they do help? Probably, but how can we know?

# Do Masks Protect You Against Covid? IV

RESEARCH ARTICLE | APPLIED PHYSICAL SCIENCES | OPEN ACCESS



## An upper bound on one-to-one exposure to infectious human respiratory particles

Gholamhossein Bagheri  , Birte Thiede , Bardia Hejazi , , and Eberhard Bodenschatz   [Authors Info & Affiliations](#)

December 2, 2021 | 118 (49) e2110117118 | <https://doi.org/10.1073/pnas.2110117118>

 27.778  7



We're confident at this point - but it is pretty hard to actually know something!

# Let's Look at a Hard Case

Why did Russia decide to invade Ukraine (now)?



## Ukraine - Territorial Gains?

# Opinion: What we can expect after Putin's conquest of Ukraine



By Robert Kagan

Contributing columnist

February 21, 2022 at 5:39 p.m. EST



**Listen to article** 6 min

# Ukraine - Domestic Reasons?

Opinion **Russian politics**

## Putin's threats disguise a weakening position

A regional sphere of influence made up of corrupt autocracies is vulnerable to uprisings and instability

GIDEON RACHMAN [+ Add to myFT](#)



# Ukraine - Identity?



President of Russia

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## Article by Vladimir Putin "On the Historical Unity of Russians and Ukrainians"

July 12, 2021 17:00

## Ukraine -Security Concerns?

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# Why the Ukraine Crisis Is the West's Fault

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The Liberal Delusions That Provoked Putin

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*John J. Mearsheimer*

## Ukraine - Ukraine's Agency?

# NATO recognises Ukraine as Enhanced Opportunities Partner

12 Jun. 2020 - | Last updated: 12 Jun. 2020 15:47



English | [French](#) | [Russian](#) | [Ukrainian](#)



On Friday (12 June 2020), the North Atlantic Council recognised Ukraine as an Enhanced Opportunities Partner. This status is part of NATO's Partnership Interoperability Initiative, which aims to maintain and deepen cooperation between Allies and partners that have made significant contributions to NATO-led operations and missions.

# Why did Russia decide to invade Ukraine (now)?

For all these reasons?

- ▶ Possibly to some extent
- ▶ But this is not a really satisfactory or helpful answer
- ▶ *We seek to make accurate, precise and 'helpful' claims*

# Why Do We Do Science?

- ▶ To *explain* things?
  - ▶ Why did something happen?
  - ▶  $? \rightarrow Y$
- ▶ To *predict* things?
  - ▶ What will happen?
  - ▶  $X \rightarrow ?$
- ▶ Are these two mutually exclusive?
  - ▶ It's always about the relationship between two events (i.e. causation).
  - ▶  $X \rightarrow Y$
- ▶ Is it much better to know something about everything than everything about something?
  - ▶ This - again - is a false dichotomy!
  - ▶ Looking at causality (might) help overcome it

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## Why Causal Inference

- ▶ The focus of Causal Inference is applied econometrics, developing tools to answer questions of the form “what is the effect of  $X$  on  $Y$  ”
  - ▶ What is the effect of reading the Daily Mail on voting intentions in the UK?
  - ▶ What is the effect of parents’ education on children’s income?
  - ▶ What is the effect of the minimum wage on unemployment?
  - ▶ What happens to a country if it withdraws from a trade agreement?
  - ▶ What is the effect of getting a high grade in Causal Inference on your likelihood of getting into a PhD?
- ▶ Answering such questions is difficult. Our world is full of data and observations, but often careless interpretations.
- ▶ Being reasonably confident about a causal effect is usually not that easy

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# Welcome to Causal Inference

Setup of the course:

- ▶ 2 hours Lecture (Monday)
- ▶ 2 hours Lab (Thursday)
- ▶ 1 hour Drop-In Session (tba)
- ▶ Assigned readings for both labs and lectures from next week

The lectures:

- ▶ Motivation
- ▶ Theory
- ▶ Examples

The lab sessions:

- ▶ Apply what you learn You'll be able to apply all methods by the end of term
- ▶ Using R, R Markdown



## Ken Stiller

I just joined the University of Bayreuth. I'm also affiliated with Nuffield College and the Department of Politics and International Relations at the University of Oxford. I'm about to receive a PhD in International Relations from the Department of Politics of International Relations at the University of Oxford, and I hold an MPhil in IR from Oxford.



## Syllabus: Causal Inference

1. Introduction, Causality, FPCI
2. Potential Outcomes Framework and Selection Bias
3. Randomised Control Experiments
4. Selection on Observables, Multiple Regression and Matching
5. Panel Data and Fixed Effects Models
6. Differences-In-Differences
7. Instrumental Variables and 2SLS Estimation
8. Regression Discontinuity Designs
9. Revisiting Instrumental Variables and Fuzzy Regression Discontinuity Design
10. *Advances in Diff-in-Diff? Synthetic Controls? Any suggestions?*

## Lab Sessions

- ▶ Download R, R Studio and try to familiarize yourself with the interface.
- ▶ I strongly encourage you to become familiar with the lab assignment before coming to class.
- ▶ Week 1: R Basics & R Markdown
- ▶ There's no reading for this week's lab

**Auditors and attendance:** Auditing students are only allowed to attend lectures, and **not labs**. Under exceptional circumstances, you may request to attend labs by emailing me - But you have to commit to attending all the eight labs in this case.

## Assessments

- ▶ **Assignment 1: Distributed Week 2, Deadline Friday of Week 5 (20%)**
- ▶ Assignment 2: Distributed Week 5, Deadline Friday of Week 8 (20%)
- ▶ Assignment 3: Distributed Week 8, Deadline Friday of Week 11 (20%)
- ▶ Take Home Exam: Distributed Week 11, Deadline 1 August 2022 (40%)

## Assessments, II

- ▶ Assessments are intended to motivate you to keep up with the course material, and require work throughout but will ease your final exam preparation.
- ▶ Collaboration on problem sets is not allowed. Each student is required to produce his or her own final code and write-up, and to indicate on the write-up which classmates he or she collaborated with. Students will be penalized for violating this rule.
- ▶ All assignments should be submitted to me via email in PDF format - the final submission must include *all* lines of code. In labs we will teach you to produce PDF reports using R markdown, which allows you to produce clearly formatted documents with math notations (using Latex), R code, and R output. Please make sure to keep within the word limit of each assignment.

## Where to find our course materials

- ▶ You'll find all resources (slides, lab code, assignments) on our course page:  
<https://bayreuth-politics.github.io/CI22/>

## Extra Assignment

- ▶ The world is full of incorrect causal claims (unfortunately).
- ▶ Look out for them!
- ▶ If you find a really bad one, send them to me by email.
- ▶ Best one (i.e. most ridiculous incorrect claim) gets an honorary mention at the end of the last lecture for this term!

# Table of Contents

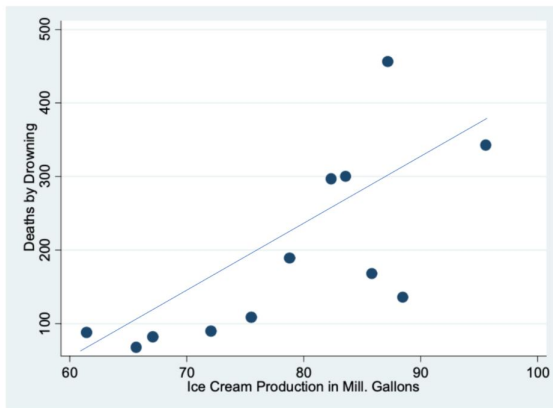
Introduction

Course Specifics

**Causality**

Fundamental Problem of Causal Inference

# What is the Effect of Ice Cream Production on Drowning?



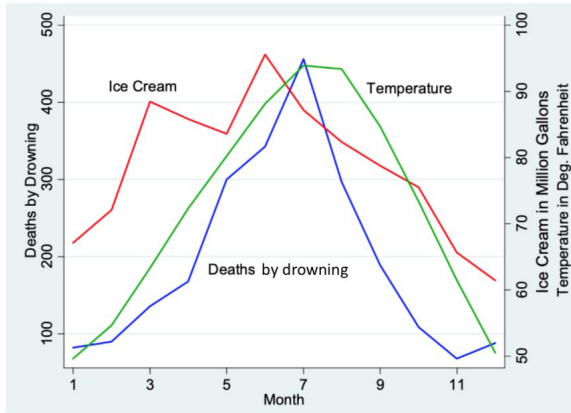
Monthly data for the USA in 2004 – a strong relationship between ice cream sales and drownings



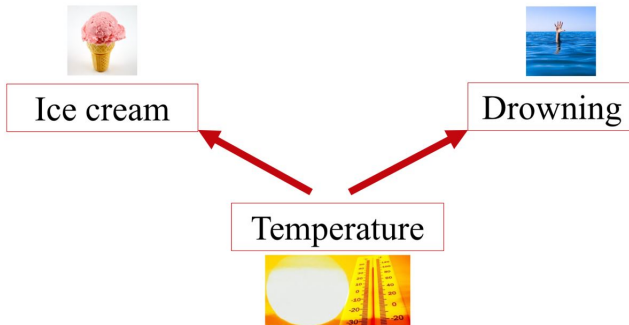
# What Causes Drownings?

1. Ice cream
2. Lots of swimming in High temperatures
3. Irresponsible parents
4. Something else
5. I don't know

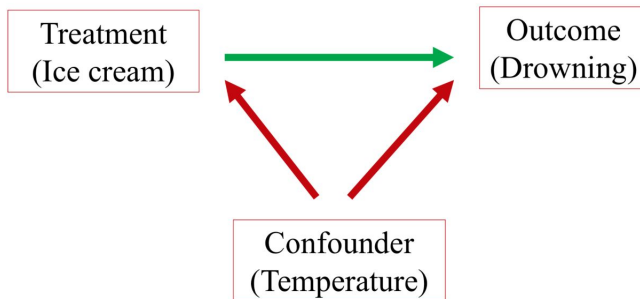
# Drowning, Ice Cream, and the Heat



# Correlation is Not Causation: A Third Variable can Cause Both



# Correlation is Not Causation: A Third Variable can Cause Both



# Definitions

## Causality

Refers to the relationship between events where one set of events (the effects) is a direct consequence of another set of events (the causes). (Hidalgo & Sekhon 2012)

## Causal Inference

The process by which one can use data to make claims about causal relationships. (Hidalgo & Sekhon 2012)

Inferring causal relationships is a central task of science.

## Examples

- ▶ What is the effect of peace-keeping missions on peace?
- ▶ What is the effect of church attendance on social capital?
- ▶ What is the effect of minimum wage on employment?

# A Counterfactual Logic

## Counterfactual Logic

**If X had/had not been the case, Y would/would not have happened**

**Example:** *Does college education increase earnings?*

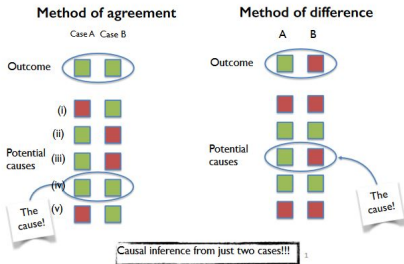
- ▶ If high school grads had instead obtained a college degree, how much would their income change?
- ▶ If college grads had only obtained a high school diploma, how much would their income change?

## John Stuart Mill: A System of Logic (1843)

A series of “canons” for inductive inference. Two well-known methods of comparison:

- ▶ Method of Difference: Units similar in all respects but one manipulable treatment. Units differ in their outcomes.
- ▶ (Method of Indifference: Units dissimilar in all respects but one. Outcome same in both units.)

Suppose all of the potential causes can be enumerated and accurately measured. Then these two methods will under certain conditions tell us the cause of an outcome:



# Mill & the Counterfactual Logic of Causality

## Causal Inference as a counterfactual Problem

Rather than defining causality purely in reference to observable events, counterfactual models define causation in terms of a comparison of observable and unobservable events.

- We need to construct counterfactuals of the observed world as comparison units (Method of Difference).



## A hypothetical example

Imagine two students who are interested in getting a very high score on their thesis. They are considering the courses they should take and they are undecided between *Causal Inference* or sticking with *Intro to Statistics*.

$Y_i$  : Thesis score is the outcome variable of interest for unit  $i$ .

$$D_i = \begin{cases} 1 & \text{if unit } i \text{ received the treatment (taking Causal inference)} \\ 0 & \text{otherwise.} \end{cases}$$

$$Y_{di} = \begin{cases} Y_{1i} & \text{Potential thesis score for student } i \text{ with Causal Inference} \\ Y_{0i} & \text{Potential thesis score for student } i \text{ without Causal Inference} \end{cases}$$

Q: What is the effect of taking Causal Inference on your thesis score?

# Defining the Potential Outcomes

## Definition: Treatment

$D_i$  : Indicator of treatment status for unit  $i$

$$D_i = \begin{cases} 1 & \text{if unit } i \text{ received the treatment} \\ 0 & \text{otherwise.} \end{cases}$$

## Definition: Observed Outcome

$Y_i$  : Observed outcome variable of interest for unit  $i$ . (Realized after the treatment has been assigned)

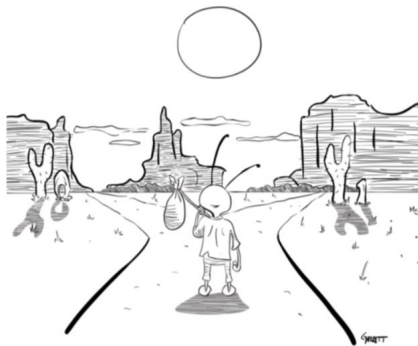
# Defining the Potential Outcomes

## Definition: Potential Outcomes

$Y_{0i}$  and  $Y_{1i}$ : Potential Outcomes for unit  $i$

$$Y_{di} = \begin{cases} Y_{1i} & \text{Potential outcome for unit } i \text{ with treatment} \\ Y_{0i} & \text{Potential outcome for unit } i \text{ without treatment} \end{cases}$$

# The Road Not Taken (by Robert Frost)



It shows (1) the actual road that you chose, and (2) the counterfactual road that you could have chosen but did not. **How can we know it made the difference? We don't know what would have happened on the other path.**

## Causality with Potential Outcomes

Let  $D_i$  denote a binary treatment for unit  $i$ , where  $D_i \in \{0, 1\}$ . Let  $Y_i$  represent the observed outcome for unit  $i$ . The potential outcomes are thus,  $Y_{1i}, Y_{0i}$

**The causal effect of  $D$  on  $Y$  for  $i$  is  $\tau_i = Y_{1i} - Y_{0i}$**

### Definition: Causal Effect

Causal Effect of the treatment on the outcome for unit  $i$  is the difference between its two potential outcomes:

$$\tau_i = Y_{1i} - Y_{0i}$$

# The Fundamental Problem of Causal Inference

## The Fundamental Problem of Causal Inference

It is impossible to observe for the same unit  $i$  the values  $D_i = 1$  and  $D_i = 0$  as well as the values  $Y_{1i}$  and  $Y_{0i}$  and, therefore, it is impossible to observe the effect of  $D$  on  $Y$  for unit  $i$ .

This is why we call this a **missing data problem**. We cannot observe both potential outcomes, hence we cannot estimate:

$$\tau_i = Y_{1i} - Y_{0i}$$

		$Y_{i1}$	$Y_{i0}$
Person 1	Treatment Group ( $D = 1$ )	Observable as $Y$	<b>Counterfactual</b>
Person 2	Control Group ( $D = 0$ )	<b>Counterfactual</b>	Observable as $Y$

## But: We Aim to Make Causal Inference!

In the coming weeks, we will learn ways to address the FPCI.

- ▶ Even though it cannot be fully resolved, we can achieve confidence about our findings
- ▶ If college grads had only obtained a high school diploma, how much would their income change?
- ▶ It is absolutely crucial to always be aware what we can claim - as well as about the limitations of our methods
- ▶ Next week: The limits of linear regressions in the context of the FPCI and why experiments help Any questions?