## Order consistent logic

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https://github.com/bayship-org/mathematics

In the article above, in its first two pages, all prerequisite definitions for this

## 1 Prerequisite definitions and notations

 $GitHub: Minor\_of\_memBer.pdf$ 

article are given. Especially, the second page of the above article defines that	2
two memBers $(x, y)$ are said $(x \text{ is a } \mathbf{minor} \text{ of } y)$ .	3
Definition 1.1.	4
"And" is also written as " $_{and}\wedge$ ".	5
"Or" is also written as " $_{or}\vee$ ".	6
2 Introduction	7
This article defines new words, "a logical expression is order consistent",	8
and gives a conjecture for the new words and the notion of minors of memBers.	9
In the rest of this introduction, the main conjecture is roughly introduced in a	10
style of an example.	11
	12
Let $(X, T^2)$ be the Euclidean space of 2-dimension.	13
Let $x1$ be some closed line segment in terms of some coordinate system.	14
Let $C := \{x \mid ((T^2, x), (T^2, x_1)) \text{ are isomorphic } \}.$	15
Let $f$ be a function on $C$ as $f(x) = \text{length}(x)$ .	16
Take $y :\in \text{image}(f)$ ,	17

Let $k := \{x \mid f(x) = y\}.$	18
Then the conjecture claim that	19
if the definition of $k$ is order consistent	20
then $k$ is a minor of $(X, T^2)$ .	<b>2</b> 1
3 Definitions	22
Definition 3.1 (Order consistent).	23
Take $\forall L$ as a logical expression such that *1 holds.	24
Then $L$ is said order consistent.	25
<b>1.</b> Take $\forall (f, p, q, r, d1, d2)$	26
such that (*2 $_{and} \land \dots  _{and} \land $ *9) holds	27
then (*10 $_{and} \wedge$ *11) holds.	28
<b>2.</b> $L$ defines $f$ .	29
<b>3.</b> $f$ is a function.	30
4. $\{p,q,r\} \subset \operatorname{domain}(f)$ .	31
<b>5.</b> $(d1, d2)$ are total orders on $\{p, q, r\}$ .	32
<b>6.</b> Take $\forall d :\in \{d1, d2\}.$	33
7. Take $\forall (s,t) :\in d$ .	34
<b>8.</b> There exists $\exists x : \in \text{domain}(f)$ .	35
<b>9.</b> Evaluation of $f(x)$ refers to $(s,t)$ .	36
<b>10.</b> $d1 = d2$ .	37
<b>11.</b> If $p < q < r$	38
then $f(p) \le f(q) \le f(r) \lor f(r) \le f(q) \le f(p)$ .	39
4 Main conjecture	40
Conjecture 4.1 (Main conjecture).	41
Let $(n, X, T^n)$ be the Euclidean space of <i>n</i> -dimension.	42
Take $\forall (L, f, k)$ such that (*1 $and \land and \land *3$ ).	43
Then $k$ is a minor of $(X, T^n)$	11

1. L is an order consistent logical expression.	45
<b>2.</b> L takes $(n, X, T^n)$ as the antecedent.	46
<b>3.</b> L as a consequent specifies a function f relatively to the antecedent, $(n, X, T^n)$ .	47
<b>4</b> There exists $\exists y :\in \text{image}(f)$ . Then $k = \{x \in \text{domain}(f) \mid f(x) = y\}$ .	48
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5 Examples	50
This section just gives examples of substituting actual values into variables of the antecedent of the main conjecture.	51 52 53
<b>Definition 5.1</b> (Unknot). For the main conjecture, this example substitutes values into $L$ as (*1 $_{and} \land \dots  _{and} \land *10$ ).	54 55 56
<b>1.</b> $n := 3$ .	57
<b>2.</b> $(n, X, T^n)$ is the Euclidean space $(X, T^n)$ of <i>n</i> -dimension.	58
3. Let $x1$ be an unknot.	<b>5</b> 9
<b>4.</b> Let $C := \{x \mid ((T^n, x), (T^n, x1)) \text{ are isomorphic } \}.$	60
5. Take $\forall x :\in C$ .	61
<b>6.</b> $f1(x) := \{d \mid d \text{ is a proper knot diagram of } x\}.$	62
7. $f2(x) := \{r \mid \exists d :\in f1(x) \text{ and } \land f \text{ is the number of crossings on } d \}.$	63 64 65 66
<b>8.</b> $f(x)$ returns the maximum number of $f(x)$ .	67
<b>19.</b> Take $\forall y :\in \text{image}(f)$ .	68
<b>10.</b> 1 Let $k := \{x \in \text{domain}(f) \mid f(x) = y\}$	69
	70

<sup>&</sup>lt;sup>1</sup>For example, you can specify y as y := 10.

Proposition 1 (Non order consistent).	71
Refer to $f$ of the previous definition.	72
Let $g(x) := (f(x) - 2)^2$ .	<b>7</b> 3
Then the definition of $g$ is not order consistent.	74
Proof.	<b>7</b> 5
• Refer to the previous definition for $f2$ .	<b>7</b> 6
• The definition of $g$ is dependent on $f2$ and the standard order on image $(f2)$ .	77
• By the way, let $(p, q, r) := (1, 2, 3)$ .	78
• Then $p < q < r \land g(q) < g(p) = g(r)$ .	79
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## 6 Appendix-Specification

In mathematics, to specify an entity is always relative to the context. For	82
example, let the antecedent take $\forall (n, X, T, M)$ as a Euclidean space $(X, Y, M)$	83
of $n$ dimension then as the consequent you can not specify any single point of	84
the space. Contrary, if the antecedent has taken a coordinate system $C$ , the	85
consequent can specify any point of the space relatively to the antecedent.	86
Although the Euclidean space $(X, T, M)$ is not specified the specific dimension,	87
(X,T,M) is said specified for the consequent. But $(X,T,M)$ is not said specified	88
for the antecedent.	89
<b>Definition 6.1.</b> For all variable $x$ of the consequent, if exactly one entity of the antecedent can be substituted into $x$ then $x$ is said having been specified relatively to the antecedent.	90 91 92

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