

**Example.** A company needs to hire people for 5 different positions  $P_1, \dots, P_5$ . There are 7 candidates  $C_1, \dots, C_7$  who interviewed for these positions. The table below shows the interview score (higher is better) how each person is qualified for each position. Blank entries indicate the score of 0 (i.e. a candidate is either not suitable or not interested in the corresponding position).

	$C_1$	$C_2$	$C_3$	$C_4$	$C_5$	$C_6$	$C_7$
$P_1$	70	90		75	55		60
$P_2$	40	95	85			80	
$P_3$	50		75		70		65
$P_4$			60	80		35	
$P_5$		75		70		35	20

Which candidate should be offered which position so that the sum of scores of the assignment is the largest possible?

### Definition

A *graph* (or a *network*) is a pair  $G = (V, E)$  where:

- $V$  is the set of *vertices* (or *nodes*);
- $E$  is the set of *edges*;
- each edge connects two vertices.

**Example.**

### Definition

A *bipartite graph* is a graph  $G = (V, E)$  such the set of nodes is a union of two disjoint subsets  $V = V_1 \cup V_2$  and that every edge connects some node in  $V_1$  with some node in  $V_2$ .

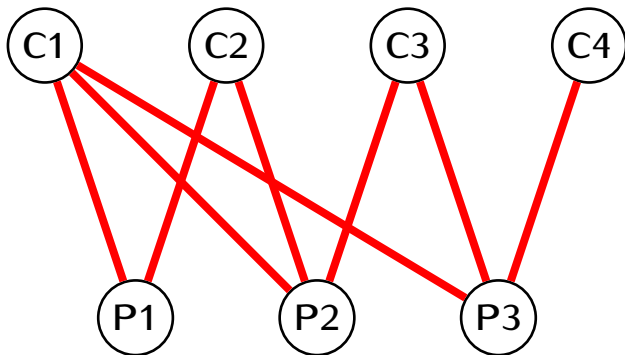
**Example.**

### Definition

The *edge incidence matrix* of a graph  $G = (V, E)$  is a matrix  $A$  such that:

- rows of  $A$  are labeled by vertices of  $G$
- columns of  $A$  are labeled by edges of  $G$
- the entry in the row of a vertex  $v$  and the column of an edge  $e$  is 1 if the edge  $e$  is attached to  $v$ ; otherwise it is 0.

**Example.**



**Goal:** All basic feasible solutions of an assignment problem consist of integers.