Linear programs with Python:

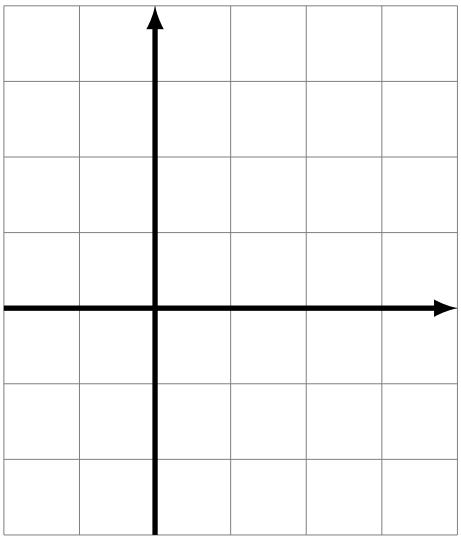
`scipy.optimize.linprog` (looks for the minimum of the objective function).

Cases when a solution of a linear program may not exist:

Infeasibilty: There are no feasible solutions.

Example. Maximize $z = 2x_1 + x_2$ subject to

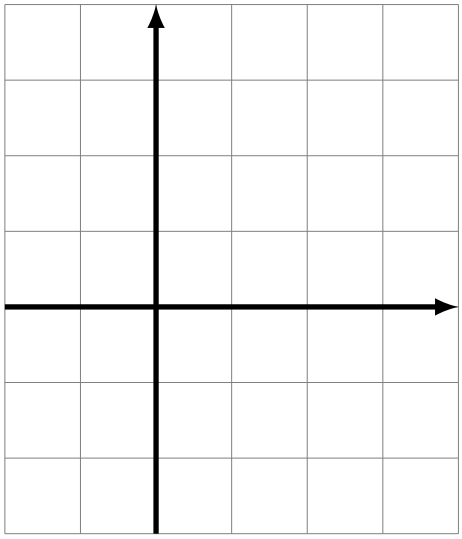
$$\begin{aligned} x_1 + x_2 &\leq 1 \\ -x_1 + x_2 &\leq -3 \\ x_1,\ x_2 &\geq 0 \end{aligned}$$



Unboundedness: The objective function has no minimum (or maximum) in the feasible region.

Example. Maximize $z = x_1$ subject to

$$\begin{aligned} x_1 - \tfrac{2}{3}x_2 &\leq 2 \\ x_1 + x_2 &\geq 1 \\ x_1,\ x_2 &\geq 0 \end{aligned}$$



Note. Even when the feasible region is unbounded the objective function may have a maximum or a minimum in this region.