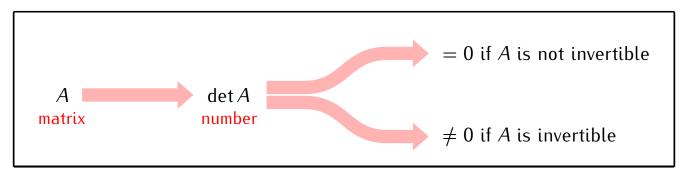
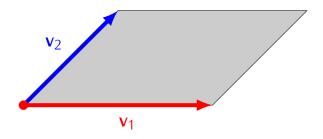
## Recall:



**Note.** Any two vectors in  $\mathbb{R}^2$  define a parallelogram:



Notation 
$$\text{area}(v_1,v_2) = \begin{pmatrix} \text{area of the parallelogram} \\ \text{defined by } v_1 \text{ and } v_2 \end{pmatrix}$$

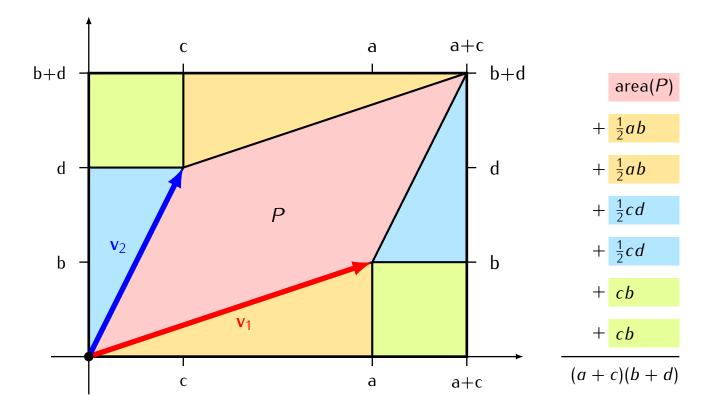
## Theorem

If 
$$\mathbf{v}_1, \mathbf{v}_2 \in \mathbb{R}^2$$
 then

$$area(\textbf{v}_1,\textbf{v}_2) = \begin{vmatrix} det \left[ \begin{array}{cc} \textbf{v}_1 & \textbf{v}_2 \end{array} \right] \end{vmatrix}$$

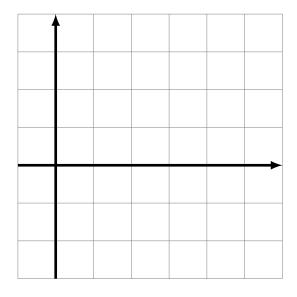
Idea of the proof.

$$\mathbf{v}_1 = \left[ \begin{array}{c} a \\ b \end{array} \right], \quad \mathbf{v}_2 = \left[ \begin{array}{c} c \\ d \end{array} \right]$$

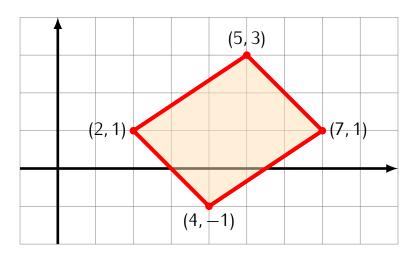


Example.

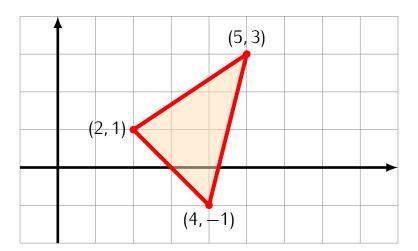
$$\mathbf{v}_1 = \begin{bmatrix} 2 \\ 3 \end{bmatrix}, \quad \mathbf{v}_2 = \begin{bmatrix} 2 \\ -2 \end{bmatrix}$$



**Example.** Calculate the area of the parallelogram with vertices at the points (2,1), (5,3), (7,1), (4,-1).



**Example.** Calculate the area of the triangle with vertices at the points (2, 1), (5, 3), (4, -1).



**Note.** In order to compute areas of other polygons, subdivide them into triangles.

