

Recall:How to solve a system of linear equations

system of equations

$$\begin{cases} -x_1 + 2x_2 + 3x_3 = 4 \\ 2x_1 + 6x_3 = 9 \\ 4x_1 - x_2 - 3x_3 = 0 \end{cases}$$

*make
a matrix*augmented
matrix*Gauss-Jordan
elimination*

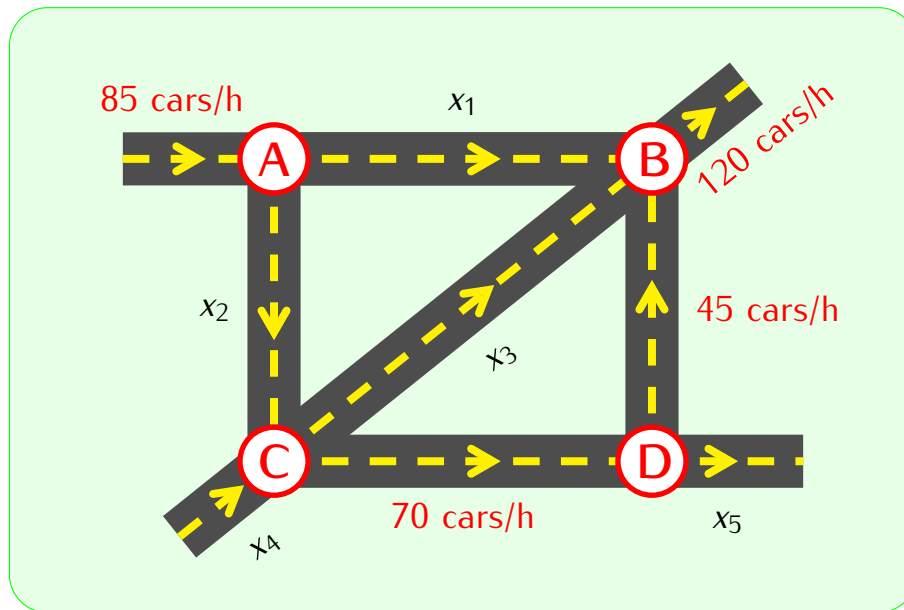
solutions

$$\begin{cases} x_1 = \dots \\ x_2 = \dots \\ x_3 = \dots \end{cases}$$

*read off
solutions*matrix in reduced
row echelon formNext: Some applications of systems of linear equations:

- Computations of traffic flow.
- Balancing chemical equations.
- Google PageRank.

Computations of traffic flow



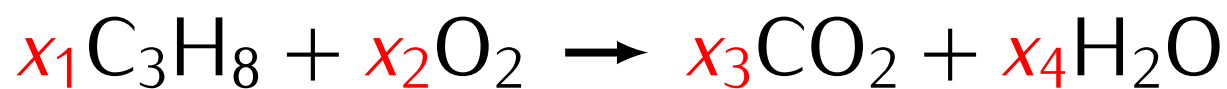
Problem. Find the flow rate of cars on each segment of streets.

Note:

- flow into an intersection = flow out of that intersection
- total flow in = total flow out

Balancing chemical equations

Burning propane:

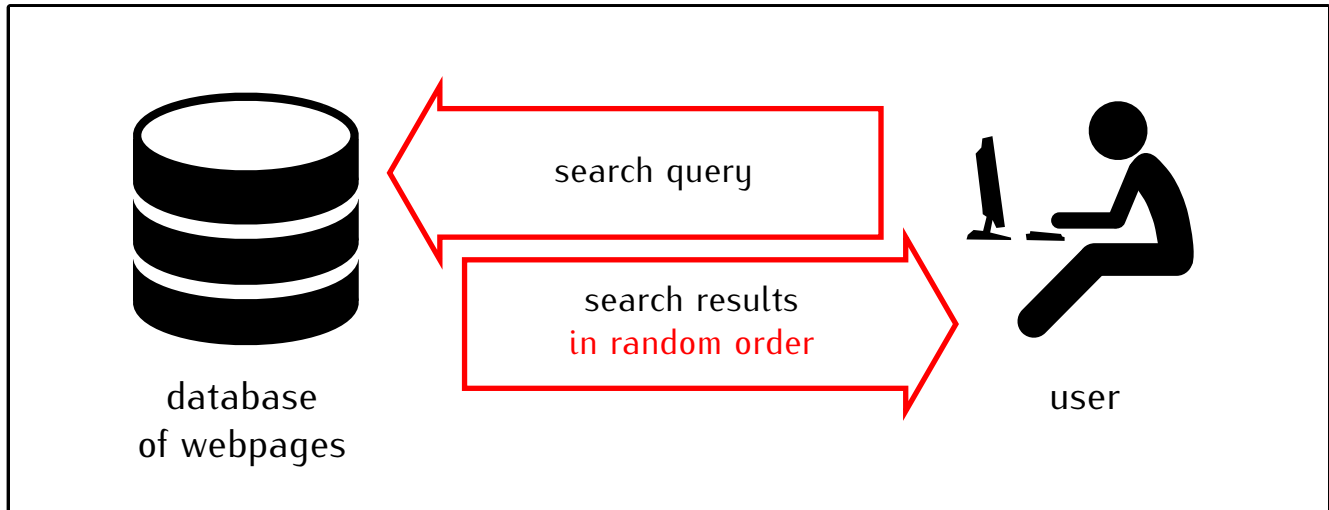


Note:

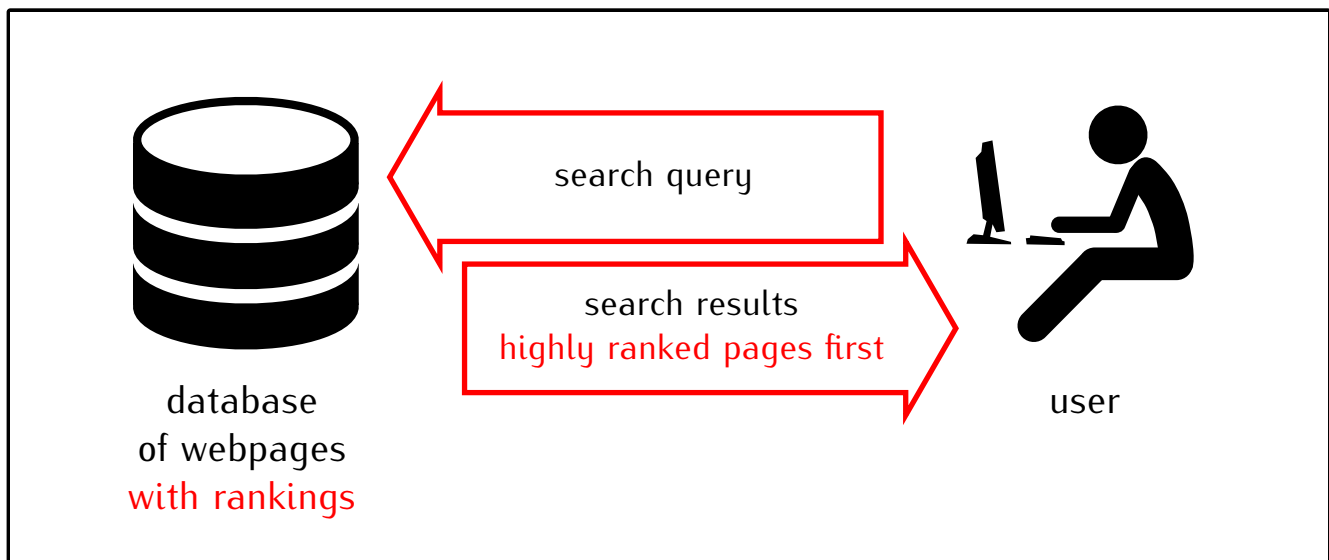
- The numbers x_1, x_2, x_3, x_4 are integers.
- The number of atoms of each element on the left side is the same as the number of atoms of that element on the right side.

Google PageRank

Early search engines:



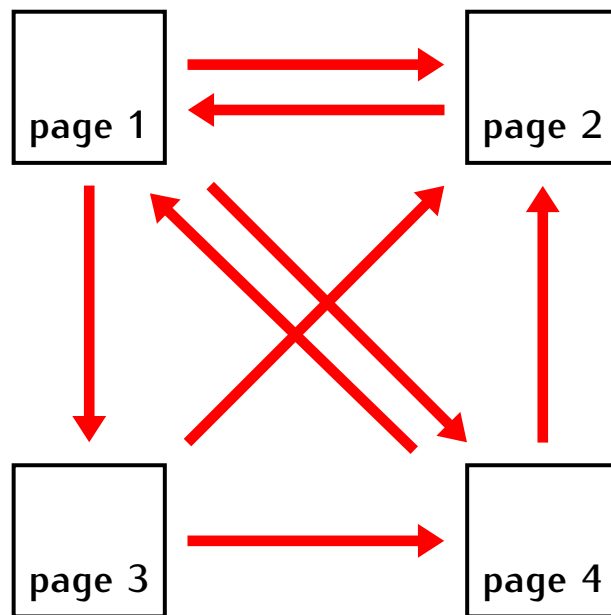
Google search engine:



How to rank webpages?

Very simple ranking:

$$\text{ranking of a page} = \left(\begin{array}{c} \text{number of links} \\ \text{pointing to that page} \end{array} \right)$$



Network of web pages.

Problem. This is very easy to manipulate.

How to rank webpages?

Google PageRank: Links from highly ranked pages are worth more than links from lower ranked pages.

If:

- the rank of a page is x
- the page has n links to other pages

then each link from that page is worth x/n .

