$$A = \begin{bmatrix} a_{11} & \dots & a_{1m} \\ \vdots & & \vdots \\ a_{k1} & \dots & a_{km} \end{bmatrix} \qquad B = \begin{bmatrix} b_{11} & \dots & b_{1n} \\ \vdots & & \vdots \\ b_{m1} & \dots & b_{mn} \end{bmatrix}$$

$$AB = \begin{bmatrix} c_{11} & \dots & c_{1m} \\ \vdots & & \vdots \\ c_{k1} & \dots & c_{km} \end{bmatrix}$$

$$c_{ij} = \begin{bmatrix} a_{i1} & \dots & a_{im} \end{bmatrix} \cdot \begin{bmatrix} b_{1j} \\ b_{1j} \\ \vdots \\ b_{1j} \end{bmatrix} = a_{i1}b_{1j} + a_{i2}b_{2j} + \dots + a_{im}b_{mj}$$
the entry in ith row

Example.

$$A = \begin{bmatrix} 0 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix} \qquad B = \begin{bmatrix} 0 & -1 & 2 & 1 \\ 4 & 5 & 1 & 0 \\ 1 & 2 & 3 & 1 \end{bmatrix}$$

$$2 \times 3$$

$$AB \text{ is defined and it is a } 2 \times 4 \text{ metrix}$$

$$AB = \begin{bmatrix} C_{11} & C_{12} & C_{13} & C_{14} \\ C_{21} & C_{22} & C_{23} & C_{24} \end{bmatrix}$$

$$C_{11} = \begin{bmatrix} 1^{5t} & \text{now of A} \end{bmatrix} \cdot \begin{bmatrix} 1^{5t} & \text{column} \\ 0 & \text{of B} \end{bmatrix} = \begin{bmatrix} 0 & 12 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 4 \\ 1 \end{bmatrix} = 0 \cdot 0 + 1 \cdot 4 + 2 \cdot 1 = 6$$

$$C_{12} = \begin{bmatrix} 1^{nd} & \text{now of A} \end{bmatrix} \cdot \begin{bmatrix} 2^{nd} & \text{column} \\ 0 & \text{of B} \end{bmatrix} = \begin{bmatrix} 0 & 12 \end{bmatrix} \cdot \begin{bmatrix} -1 \\ 5 \\ 2 \end{bmatrix} = 0 \cdot (-1) + 1 \cdot 5 + 2 \cdot 2 = 9$$

$$\vdots$$

$$C_{24} = \begin{bmatrix} 2^{nd} & \text{now of A} \end{bmatrix} \cdot \begin{bmatrix} 4^{th} & \text{column} \\ 0 & \text{of B} \end{bmatrix} = \begin{bmatrix} 3 & 4 & 5 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = 3 \cdot 1 + 4 \cdot 0 + 5 \cdot 1 = 8$$

$$AB = \begin{bmatrix} 6 & 9 & 7 & 2 \\ 21 & 27 & 25 & 8 \end{bmatrix}$$

$$AB = \begin{bmatrix} 6 & 9 & 7 & 2 \\ 21 & 27 & 25 & 8 \end{bmatrix}$$

Example.

- Acme Inc. makes two types of widgets: WG1 and WG2.
- Each widget must go though two processes: assembly and testing.
- The number of hour required to complete each process is as follows:

		assembly	testing
A =	WG1 WG*	3 7	1 3

- Acme Inc. has three plans in New York, Texas, and Minnesota.
- Hourly cost (in dollars) of each process in each plant is as follows:

Problem. What is the cost of producing each type of widgets in each plant?

Cost of WG1 in TX:
$$3.15 + 1.20 = $65$$

$$[3 1] \cdot [15]_{20} = [1st \text{ now A}] \cdot [2^{hd}]_{column}$$

$$[3 1] \cdot [15]_{20} = [1st \text{ now A}] \cdot [2^{hd}]_{column}$$

$$[7 3] \cdot [10]_{15} = [2^{hd}]_{column}$$