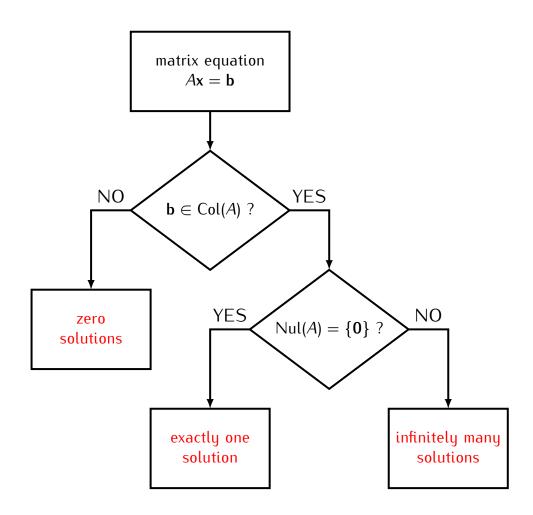
Recall:

- 1) We can multiply vectors by matrices.
- 2) Matrix equation: Ax = b



Col(A) = (span of column vectors of A)

Nul(A) = (set of solutions of Ax = 0)

Recall: Nul(A) can be always described as a span of some vectors.

Example. Find the null space of the matrix

$$A = \left[\begin{array}{rrrr} 1 & 1 & 0 & 2 \\ -2 & -2 & 1 & -5 \\ 1 & 1 & -1 & 3 \end{array} \right]$$

Example. Solve the matrix equation $A\mathbf{x} = \mathbf{b}$ where

$$A = \begin{bmatrix} 1 & 1 & 0 & 2 \\ -2 & -2 & 1 & -5 \\ 1 & 1 & -1 & 3 \end{bmatrix} \qquad \mathbf{b} = \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$$

Proposition

Let \mathbf{v}_0 be some chosen solution of a matrix equation $A\mathbf{x}=\mathbf{b}$. Then any other solution \mathbf{v} of this equation is of the form

$$\mathbf{v}=\mathbf{v}_0+\mathbf{n}$$

where $n \in Nul(A)$.

