

Next:

How to solve a system of linear equations

system of equations

$$\begin{cases} -x_1 + 2x_2 + 3x_3 = 4 \\ 2x_1 + 6x_3 = 9 \\ 4x_1 - x_2 - 3x_3 = 0 \end{cases}$$

*make  
a matrix*

augmented  
matrix

*Gauss-Jordan  
elimination*

solutions

$$\begin{cases} x_1 = \dots \\ x_2 = \dots \\ x_3 = \dots \end{cases}$$

*read off  
solutions*

matrix in reduced  
row echelon form

## Matrices

matrix = rectangular array of numbers

**Example.**

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 0 \\ 7 & -5 & 1 \\ 8 & 10 & 7 \\ 6 & 4 & 3 \end{bmatrix}$$

### Note

Every system of linear equations can be represented by a matrix.

**Example.**

$$\begin{cases} -x_1 + 2x_2 + 3x_3 = 4 \\ 2x_1 + 6x_3 = 9 \\ 4x_1 - x_2 - 3x_3 = 0 \end{cases}$$

### Elementary row operations:

1) Interchange of two rows.

2) Multiplication of a row by a non-zero number.

3) Addition of a multiple of one row to another row.

## Proposition

Elementary row operations do not change solutions of the system of equations represented by a matrix.

