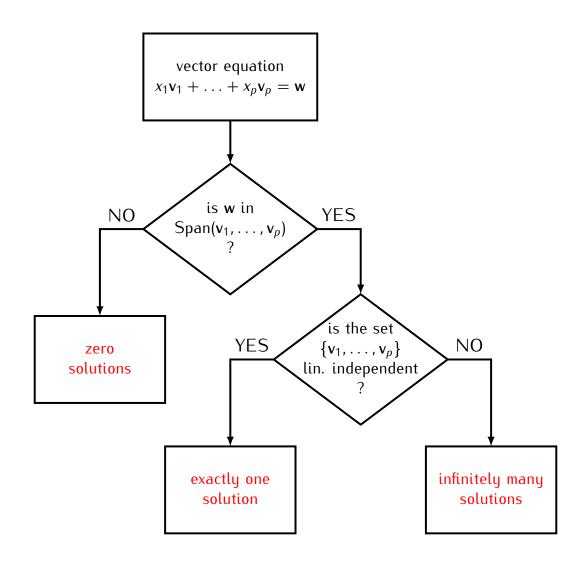
Recall:

1) Span(
$$v_1, ..., v_p$$
) =
$$\begin{cases} \text{the set of all} \\ \text{linear combinations} \\ c_1 v_1 + ... + c_p v_p \end{cases}$$

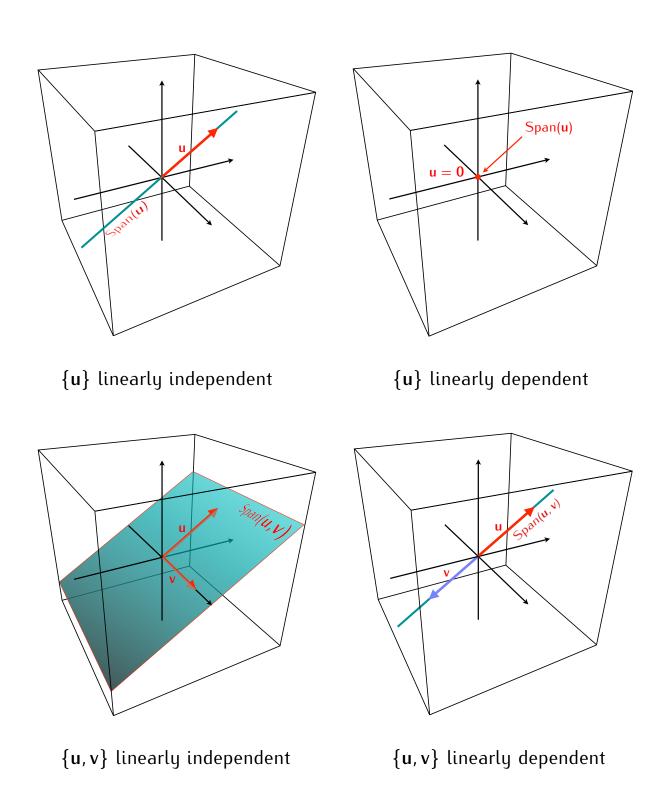
2) A set of vectors $\{v_1,\ldots,v_p\}$ is linearly independent if the equation

$$x_1\mathbf{v}_1 + \ldots + x_p\mathbf{v}_p = \mathbf{0}$$

has only one, trivial solution $x_1 = 0, \ldots, x_p = 0$.



Linear independence vs. Span



Theorem

If $\{v_1, \ldots, v_p\}$ is a linearly dependent set of vectors, then for some \mathbf{v}_i we have

$$Span(\mathbf{v}_1,\ldots,\mathbf{v}_p)=Span(\mathbf{v}_1,\ldots,\mathbf{v}_{i-1},\mathbf{v}_{i+1},\ldots,\mathbf{v}_p)$$

Example.

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad \mathbf{v}_2 = \begin{bmatrix} 2 \\ 0 \end{bmatrix} \quad \mathbf{v}_3 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$