4. Consider the matrix

$$A = \begin{bmatrix} 1 & 8 & 4 \\ -2 & 11 & 4 \\ 2 & -8 & -1 \end{bmatrix}$$

Knowing that eigenvalues of A are $\lambda_1=3$ and $\lambda_2=5$ diagonalize this matrix; that is, find a diagonal matrix D and an invertible matrix P such that

 $A = PDP^{-1}$ $A = \frac{1}{2} \begin{bmatrix} -2 & 8 & 4 & 5 \\ -2 & 8 & 4 & 5 \\ 2 & -8 & -4 & 5 \end{bmatrix}$ $D = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 3 \end{bmatrix}$ $0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 2 & -8 & -4 & 1 & 2 & 0 \end{bmatrix}$ Note: you do not need to compute P^{-1} . $A-\lambda_{2} = \begin{bmatrix} -4 & 4 & 4 & 7 & 0 \\ -2 & 6 & 4 & 8 & 5 \\ 2 & -8 & -6 & 8 & 5 \end{bmatrix}$ 2-8-60-6 0 1 1 0 2.4 P= [-142] D= [500]
D= [030]