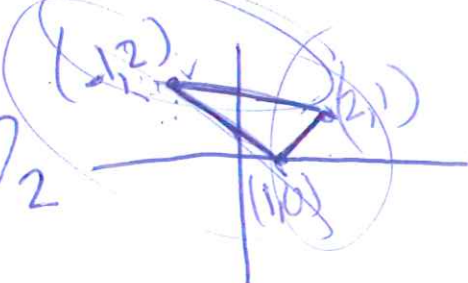


What's b?

$A_1 A_2 A_3$

2. Find the equation $f(x) = ax + b$ of the least square line for the points $(1, 0)$, $(-1, 2)$, $(2, 1)$.

$A = \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$
 $B = \begin{bmatrix} 0 \\ 2 \\ 1 \end{bmatrix}$
 $A^T = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix}$
 $A^T B = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 5 \end{bmatrix}$



Least Square

$$(A^T A)^{-1} (A^T b) = \begin{bmatrix} x \\ y \end{bmatrix}$$

$A = \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$
 $A^T A = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 5 \end{bmatrix}$

$\frac{2}{1-0} = \frac{1}{1}$
 $\frac{1}{1-0} = 1$

$\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \begin{bmatrix} \sqrt{8} \\ \sqrt{10} \\ \sqrt{2} \end{bmatrix} = \begin{bmatrix} \sqrt{8} + \sqrt{10} + 2\sqrt{2} \\ 0 + 2\sqrt{10} + \sqrt{2} \end{bmatrix}$

$\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 5 \end{bmatrix}$

$\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 5 \end{bmatrix}$

$\begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix} \begin{bmatrix} \sqrt{8} + \sqrt{10} + 2\sqrt{2} \\ 2\sqrt{10} + \sqrt{2} \end{bmatrix}$

$f(x) = \frac{\sqrt{8}}{5} - \frac{\sqrt{10}}{5} + \frac{2\sqrt{2}}{5}x + \frac{2\sqrt{10}}{5} + \frac{\sqrt{2}}{5}$