1. Consider the following vectors in  $\mathbb{R}^4$ :

$$v_1 = \begin{bmatrix} 1 \\ 0 \\ -1 \\ 1 \end{bmatrix}, \quad v_2 = \begin{bmatrix} 2 \\ 1 \\ -1 \\ 0 \end{bmatrix}, \quad v_3 = \begin{bmatrix} 2 \\ -2 \\ -1 \\ 3 \end{bmatrix}, \quad u = \begin{bmatrix} 3 \\ 3 \\ 3 \\ 3 \end{bmatrix}$$

The set  $\mathcal{B} = \{v_1, v_2, v_3\}$  is a basis of some subspace V of  $\mathbb{R}^4$ .

- a) Find an orthogonal basis  $\mathcal{D} = \{w_1, w_2, w_3\}$  of the subspace V.
- b) Compute the vector  $proj_V \mathbf{u}$ , the orthogonal projection of  $\mathbf{u}$  on V.

