

2. Find the equation $f(x) = ax + b$ of the least square line for the points $(1, 0)$, $(-1, 2)$, $(2, 1)$.

$$W_1 = \langle V_1^1 \rangle$$

$$W_2 = V_2 - \frac{\langle W_1, V_2 \rangle}{\langle W_1, W_1 \rangle} W_1$$

$$\begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$$

$$W_1 = \langle V_1^1 \rangle$$

$$W_1 = \sqrt{1^2 + 1^2 + 2^2} = \sqrt{6}$$

$$W_2 = \langle V_2^1 \rangle - \frac{\langle W_1, V_2 \rangle}{\langle W_1, W_1 \rangle} W_1$$

~~Algebra~~

I'm sorry,
I don't know
how to do this

$$A^T \cdot A x = A^T b$$

$$A = \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 \\ -1 & 2 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} 6 & 0 \\ 0 & 5 \end{bmatrix}$$

$$A^T = \begin{bmatrix} 1 & -1 & 2 \\ 0 & 2 & 1 \end{bmatrix}$$

$$\det A^T A = 6 \cdot 5 = 30$$

$$\det A^T = (-1 \cdot 1 - 2 \cdot 2) + (1 \cdot 1 - 2 \cdot 0) + (1 \cdot 2 - 0) = -2$$

$$f(x) = 30x - 2$$

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