

- 5. For each of the statements given below decide if it is true or false. If it is true explain why. If it is false give a counterexample.
- a) If A is a 2 \times 2 matrix and v is an eigenvector of A corresponding to an eigenvalue λ then 2v is an eigenvector of A corresponding to the eigenvalue 2λ .
- b) If V is a subspace of \mathbb{R}^2 and \mathbf{w} is a vector such that $\operatorname{proj}_V \mathbf{w} = -\mathbf{w}$ then \mathbf{w} must be the zero vector.
- c) If A is a square matrix which is both symmetric and orthogonal then A^2 is the identity matrix.

d) If A and B are 2 × 2 matrices which are both orthogonally diagonalizable, then the matrix A+B is also orthogonally diagonalizable.

Et A=[0 2] then [0 2-1] ques A=1, 2 for A=1 Expensector=[0]

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The boundary for Projum (v. v) or proportion (w. v)

True bocause the metrix is symmetric A=A, and offragonal

A+A=I. A² will be equivalent to A-A+ as A=A+ there

Por equating to the identity matrix.

True

Tru

Therefore w can be a non-zero vector