$$\begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} \rightarrow \begin{bmatrix} 0$$

- 5. For each of the statements given below decide if it is true or false. If it is true explain why. If it is false give a counterexample.
- a) If A is a 2×2 matrix and v is an eigenvector of A corresponding to an eigenvalue λ then 2v is an eigenvector of A corresponding to the eigenvalue 2λ .
- b) If V is a subspace of \mathbb{R}^2 and \mathbf{w} is a vector such that $\operatorname{proj}_V \mathbf{w} = -\mathbf{w}$ then \mathbf{w} must be the zero vector.
- c) If A is a square matrix which is both symmetric and orthogonal then A^2 is the identity matrix.
- d) If A and B are 2×2 matrices which are both orthogonally diagonalizable, then the matrix A + B is also orthogonally diagonalizable.

- b) True, because OAMO for the proj to equal the original vector,
- +3 the vector must, already fall on the projected plan with 0=-0 as the only vector that could & possibly be equal to it's negative proj
- c) fatse, because A= [0 0 0] is a square, symmetric, 4 orthogonal

 H matrix but A= [0 0 0] which is not the Identity matrix
- D) True, because the resulting matrix will still be symmetrical which means that it will also be orthogonally diagonizable