5. For each of the statements given below decide if it is true or false. If it is true explain why. If it is false give a counterexample.

a) If A is a 2 \times 2 matrix and v is an eigenvector of A corresponding to an eigenvalue λ then 2v is an eigenvector of A corresponding to the eigenvalue 2λ .

b) If V is a subspace of \mathbb{R}^2 and w is a vector such that proj, w = -w then w must be the zero vector. True, it is impossible for the projection to return sw

c) If A is a square matrix which is both symmetric and orthogonal then A2 is the identity matrix. True, properties of ofthonormal vectors vior; = { | if i = i } ?

d) If A and B are 2×2 matrices which are both orthogonally diagonalizable, then the matrix A+B is also orthogonally diagonalizable.

d) True, If A and B are orthography diagonalizable then they have to be symmetric Matrices

A+B will still be symmetric as adding B top of diagonal will cancel out with B5 bottom of diagonal.

Since (A+B) is symmetric it is orthogonally diagognilbable

det [[3-1/2]]

 $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \qquad \frac{1/q + 4/q + 4/q = 1}{4/q + 4/q = 1} \qquad \frac{2/q + \frac{2}{q} - \frac{4}{q + \frac{2}{q}}}{\frac{2/q - 4/q = 0}{4/q - \frac{2}{q}}} \qquad \frac{2/q + \frac{4}{q} - \frac{4}{q + \frac{2}{q}}}{\frac{4/q - 4/q = 0}{4/q - \frac{2}{q}}} \qquad \frac{2/q - \frac{4}{q + \frac{2}{q}}}{\frac{4/q - \frac{2}{q}}{\frac{2}{q}}} = 0 \qquad \frac{4/q - \frac{2}{q} - \frac{2}{q}}{\frac{2}{q}} = 0$