3. Consider the following matrix A:

$$A = \left[\begin{array}{ccc} 0 & 1 & 2 \\ 1 & 1 & 0 \\ 4 & 2 & 2 \end{array} \right]$$

For each value of λ given below determine if it is an eigenvalue of A.

a)
$$\lambda = 0$$
 b) $\lambda = -1$ c) $\lambda = -2$

$$\lambda = 0$$

$$\lambda$$

O is not an eigen value of A

$$\begin{array}{c} (a) \lambda = -1 \\ (b) \lambda = -1 \\ (c) \lambda = -1$$

$$\begin{array}{c} C) \lambda = -\lambda & A+\lambda I \\ \rightarrow \begin{bmatrix} \lambda & 0 & \lambda \\ 1 & 3 & 0 \\ 4 & \lambda & 4 \end{bmatrix} \stackrel{\downarrow}{\downarrow} \stackrel{\downarrow}{R_3} \begin{bmatrix} 1 & 0 & 1 \\ 1 & 3 & 0 \\ 2 & 1 & \lambda \end{bmatrix} \stackrel{R_1 \cdot R_1}{R_2 \cdot R_1} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 3 & -1 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_2 \cdot R_1}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \begin{bmatrix} 1 & 0 & 1 \\ 0 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \stackrel{R_3 \cdot R_4}{R_3 \cdot R_4} \stackrel{R_4 \cdot R_4}{R_4 \cdot R_4}$$

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