

- 5. For each of the statements given below decide if it is true or false. If it is true explain why. If it is false give a counterexample.
- a) If A is a 2×2 matrix and v is an eigenvector of A corresponding to an eigenvalue λ then 2v is an eigenvector of A corresponding to the eigenvalue 2λ .
- b) If V is a subspace of \mathbb{R}^2 and w is a vector such that $\operatorname{proj}_V w = -w$ then w must be the zero vector.
- c) If A is a square matrix which is both symmetric and orthogonal then A^2 is the identity matrix.

d) If A and B are 2×2 matrices which are both orthogonally diagonalizable, then the matrix A + B is also orthogonally diagonalizable.

-B is also orthogonally diagonalizable.

False, consider [2 3] $\lambda = 2$.

True, because projon es o if w is orthogonal to V.

and projection commot reverse a direction.)?

The only case when projow = -w would be if w=0

because - w=0

True, AT=AT (outhogonal) A=AT (symmetric) A.A. I (outhogonal)

(A). A = I since symmetric A=I

& True, Since both A&B are nxn matrices, which are bothogonally déagonézable, which means they have to be symmetric of $A = \begin{cases} x & m \\ m & y \end{cases} b = \begin{bmatrix} p & x \\ r & q \end{bmatrix}$

then AfB = [x+p m+y]

6 [m+y y+q]

A+B is Symmetric & nxn

So outrogonally diagonizable.