- 5. For each of the statements given below decide if it is true or false. If it is true explain why. If it is false give a counterexample.
- a) If A is a 2×2 matrix and v is an eigenvector of A corresponding to an eigenvalue λ then 2v is an eigenvector of A corresponding to the eigenvalue 2λ .
- b) If V is a subspace of \mathbb{R}^2 and w is a vector such that $\operatorname{proj}_V w = -w$ then w must be the zero vector.
 - c) If A is a square matrix which is both symmetric and orthogonal then A^2 is the identity matrix.
 - d) If A and B are 2×2 matrices which are both orthogonally diagonalizable, then the matrix A+B is also orthogonally diagonalizable.

a) False, just because there is an eigenvalue
$$\lambda$$
 does not mean there is an eigenvalue 2λ . There is no guarantee $2\lambda = val$ is another solution to $|A - I(val)| = 0$ Ex) $A = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} 2_2 = -1$

b)
$$V_{11} = \frac{W_{1} V_{11} + W_{2} V_{21}}{V_{11} + V_{21}} = \frac{W_{1} V_{12} + W_{2} V_{22}}{V_{12} + V_{22}} = \frac{V_{11}}{V_{11}} = \frac{V_{11} + V_{21}}{V_{11} + V_{21}} = \frac{V_{11} + V$$

True, the projection of a vector on some space can be visualized as the shoold carry shadow" of that vector on that space, in any projection of w, we somewhere else should carry shadow" of that vector on that space, in any projection of w, we somewhere else should carry shadow" of that vector on that space, in any projection of w, we somewhere else should carry shadow" of that vector on that space, in any projection of w, we somewhere else should carry shadow" of that vector on that space, in any projection of w, we somewhere else should carry shadow.

1) Eatse
$$A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
 $B = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$ $A+B = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$

does not have Z linearly independent exervectors