

where $\begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$ is eigenvector corresponding to λ

3. Consider the following matrix A:

$$\begin{matrix} + & - & + \\ - & + & - \\ + & - & + \end{matrix}$$

$$A = \begin{bmatrix} 0 & 1 & 2 \\ 1 & 1 & 0 \\ 4 & 2 & 2 \end{bmatrix}$$

$$v_2 + v_3 = \lambda v_1$$

$$v_1 + v_2 = \lambda v_2$$

$$4v_1 + 2v_2 + 2v_3 = \lambda v_3$$

For each value of λ given below determine if it is an eigenvalue of A.

- a) $\lambda = 0$ No b) $\lambda = -1$ No c) $\lambda = -2$ Yes

$$-\lambda I = \det \left(\begin{bmatrix} -\lambda & 1 & 2 \\ 1 & 1-\lambda & 0 \\ 4 & 2 & 2-\lambda \end{bmatrix} \right) = 0 = -1 \left[2-\lambda-4 \right] + (1-\lambda) \left[-2\lambda+\lambda^2-8 \right] = 0$$

$$2+\lambda + (-2\lambda+\lambda^2-8+2\lambda^2-\lambda^3+8\lambda) = 0$$

$$-\lambda^3+3\lambda^2+7\lambda-6=0$$

$$\lambda^3-3\lambda^2-7\lambda+6=0 \quad \checkmark$$

a) $0^3-3(0)^2-7(0)+6=0 \quad 6 \neq 0 \rightarrow \text{Not an eigenvalue}$

b) $(-1)^3-3(-1)^2-7(-1)+6=0 \quad \checkmark$

$-1-3+7+6=0$
 $9 \neq 0 \rightarrow \text{Not an eigenvalue} \quad \checkmark$

c) $(-2)^3-3(-2)^2-7(-2)+6=0 \quad \checkmark$

$-8-12+14+6=0$
 $0=0 \quad \checkmark \rightarrow \text{IS an eigenvalue}$

20/20