$\pi_1(S^1 \vee S^1, x_0) \cong \operatorname{colim}(\mathbb{Z} \longleftarrow \{1\} \longrightarrow \mathbb{Z}) \cong \mathbb{Z} * \mathbb{Z}$