$$\operatorname{colim}(c_1 \stackrel{f_1}{\longleftarrow} c_0 \stackrel{f_2}{\longrightarrow} c_2) \stackrel{\cong}{\longrightarrow} \operatorname{colim}(c_1' \stackrel{f_1'}{\longleftarrow} c_0' \stackrel{f_2'}{\longrightarrow} c_2')$$