$$X \times \{0\} \cup A \times [0,1] \xrightarrow{\bar{h}} X \times [0,1] \xrightarrow{\bar{h}} A$$