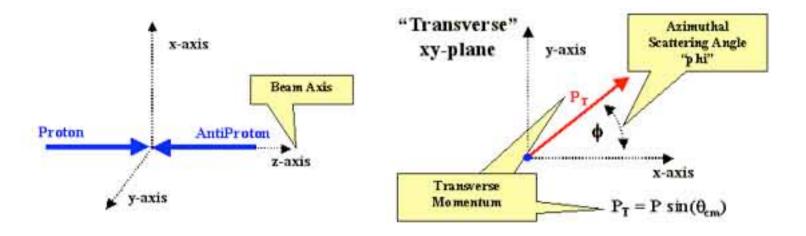


#### Lecture outlook

- Introduction to particle accelerators and detectors
  - Basic principles of particle accelerators
  - Fixed target and collider experiments
  - Luminosity
  - Basic building blocks of a particle physics experiments
- Data analysis tools:
  - Variables in the laboratory frame
  - Momentum conservation:
    - Transverse momentum and missing mass
    - Examples: two jets events, three jet events, W discovery
  - Method of invariant mass

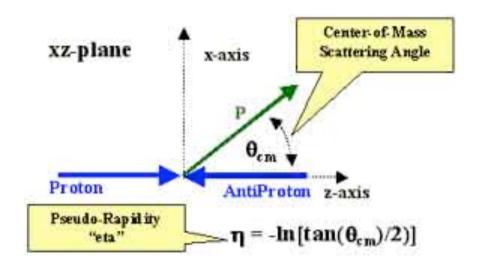
# Laboratory frame

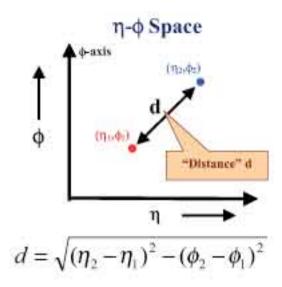
- The momentum of each particle produced in a collision can be decomposed in:
  - Component parallel to the beams (longitudinal, parallel to z)
  - Component perpendicular to the beams (transverse, in x-y plane)
  - The transverse component is:  $P_T = P \sin(\theta_{CM})$
- Example:
  - Longitudinal and transverse momentum in proton-antiproton scattering



### Pseudorapidity

To measure the longitudinal angle of the emerging particle jet one usually uses a variable called **pseudo-rapidity** 



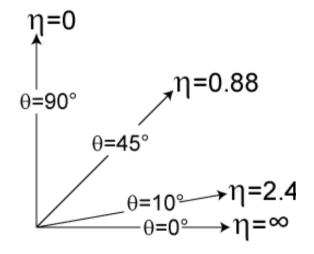


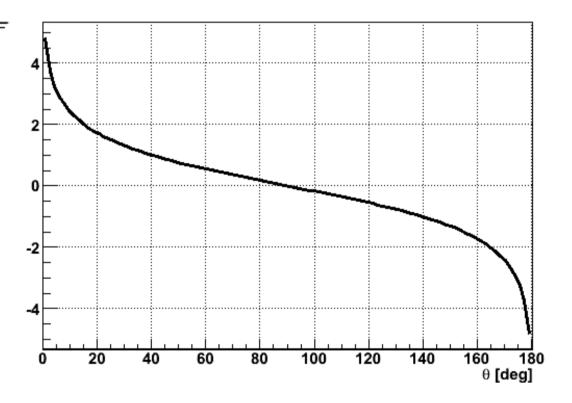
- The pseudorapidity  $(\eta)$  is **Lorentz invariant under longitudinal boosts**
- Momenta in the transverse plane are also invariant under longitudinal relativistic transformations
- Distance between particles or jets is usually measured in the (η,φ) plane

# Pseudorapidity

- Particles produced at  $\theta$ =90° have zero pseudorapidity
- High |η| values are equivalent to very shallow scattering angles
- Typical coverage of central detectors extends to  $|\eta|$ ~3.
  - Coverage of high rapidities ( $\theta$ <5°) achieved with detectors at large z positions

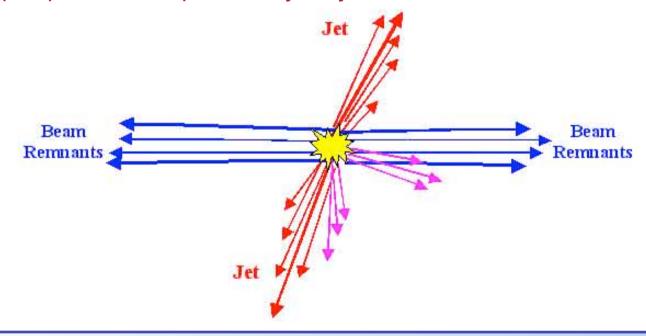
$$\eta = -\ln\left[\tan\left(\frac{\theta}{2}\right)\right],$$



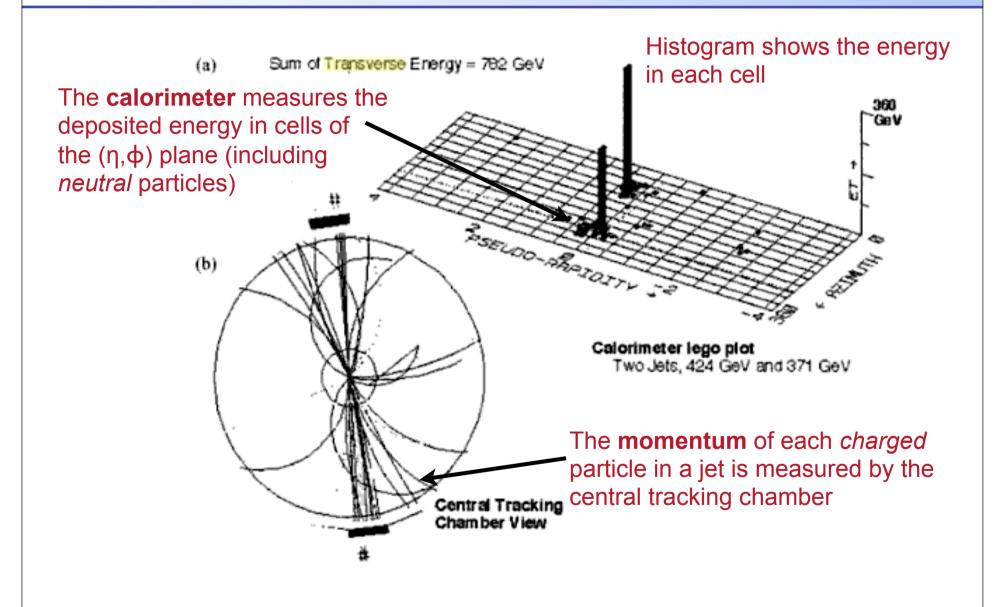


#### Collider physics

- Experiments in hadron colliders usually deal with particles at high transverse momentum
- Reasons:
  - Incoming particles collide head-on (no transverse momentum)
  - Final state particles must have zero total transverse momentum
  - Hard processes (large momentum transfer) produce particles in the center of the detector
- Example: proton + antiproton → jet + jet



### Two jets events in eta, phi plane



# Two jets events

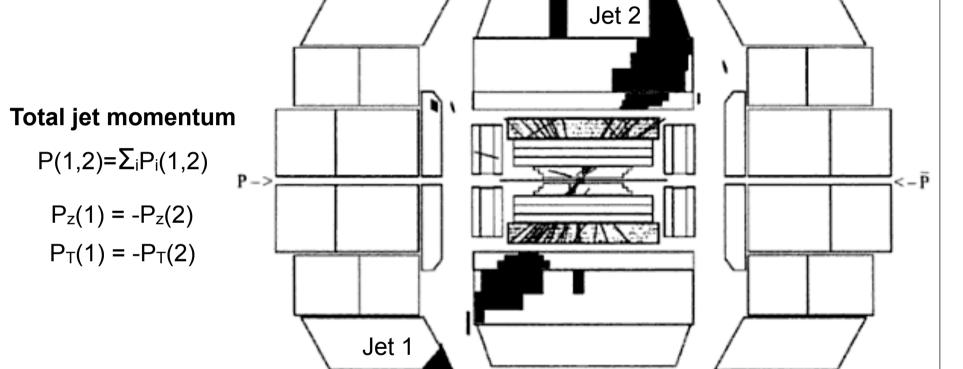
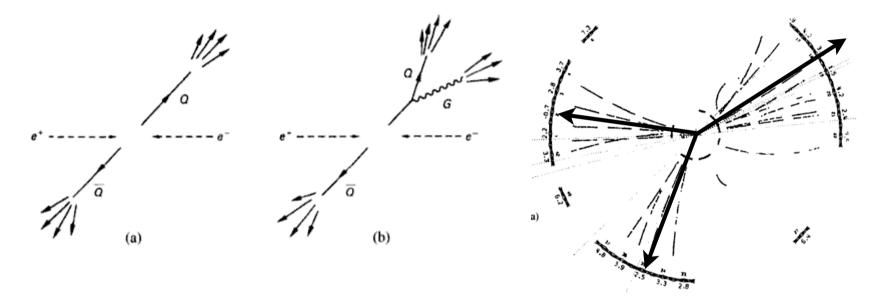


Figure 2.19 Schematic representation of a two jet event at D0. The shading represents the scale of energy deposited in the calorimeters. The first compartment is the electromagnetic calorimeter followed by two hadronic compartments. This is a projection in polar angle ([8] – D0 – with permission).

#### Three jets in e+e- annihilation

- Electron-proton pairs can annihilate producing quark pairs (e.g. at LEP)
- In some cases, a gluon can be radiated from the out-coming quark



- In the latter case one observes three particle jets in the final state:
  - Two quark jets and one gluon jet
- If no particle escapes the detector the three jets must have total transverse energy equal to zero

### Missing mass

- A collision is characterized by an initial total energy and momentum (E<sub>in</sub>, **p**<sub>in</sub>)
- In the final state we have n particles:
  - $E = \sum_{i} E_{i}$ ,  $p = \sum_{i} p_{i}$
  - Sometime we measure E<E<sub>in</sub> and p≠p<sub>in</sub>
- In this case one of more particles have not been detected
  - Typically: **neutral particles**
  - Most often neutrinos, but also neutrons,  $\pi^0$ ,  $K^0$ <sub>L</sub> (the latter for long decay time)
- We define the concept of **missing mass**:

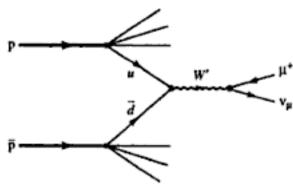
Missing mass = 
$$[(E_{in}-E)^2-(p_{in}-p)^2]^{1/2}$$

If the spectrum of the missing mass has a well-defined peak one particle has escaped our detector

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### W boson decays

The W boson is produced in proton collisions mainly via the following process:



- A u-quark collides with a anti-d quark producing a W+ boson
- The W+ decays into lepton (muon) and neutrino pairs
- The muon is detected and its momentum can be measured
- The neutrino escapes the detector undetected:
- The total sum of the transverse momenta is not zero!
  - In other words, the experimental signature of the neutrino in the experiment is the missing transverse momentum

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### Example: W boson discovery

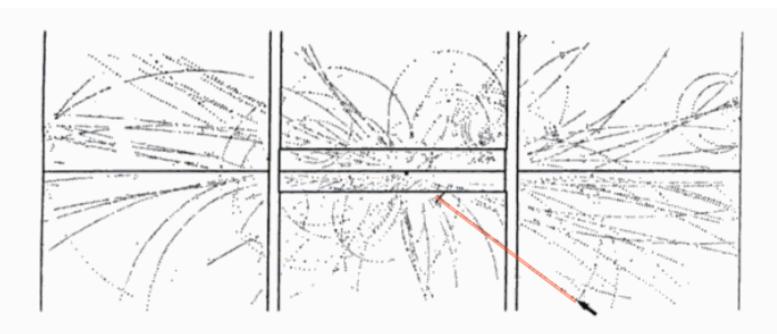


Fig. 2.8. One of the first events attributed to production and decay of a W boson,  $W^+ \rightarrow e^+ + \nu_e$ . The picture shows a reconstruction of the drift chamber signals in a large detector, UA1, surrounding the beam pipe of the CERN proton-antiproton collider. These signals originated in the collision of a 270 GeV proton (from the right) with a 270 GeV antiproton (from the left). Among the 66 tracks observed, one, shown by the arrow, is a very energetic (42 GeV) positron identified in a surrounding electromagnetic calorimeter. The transverse momentum of the positron is 26 GeV/c, while the missing transverse momentum in the whole event is 24 GeV/c, consistent with that of the neutrino (from Arnison et al. 1983).

#### **Invariant mass**

- The **invariant mass** is a characteristic of the total energy and momentum of an object or a system of objects that is the same in all frames of reference.
- When the system as a whole is at rest, the invariant mass is equal to the total energy of the system divided by c². If the system is one particle, the invariant mass may also be called the **rest mass**.

$$(mc^2)^2 = E^2 - \|\mathbf{p}c\|^2$$
 natural units (c=1):  $m^2 = E^2 - \|\mathbf{p}\|^2$ .

For a system of N particles:

$$(Wc^2)^2 = \left(\sum E\right)^2 - \left\|\sum \mathbf{p}c\right\|^2$$

- where W is the invariant mass of the decaying particle
- In a two body decay  $M\rightarrow 1+2$ :

$$M^2 = (E_1 + E_2)^2 - \|\mathbf{p}_1 + \mathbf{p}_2\|^2 = m_1^2 + m_2^2 + 2(E_1 E_2 - \mathbf{p}_1 \cdot \mathbf{p}_2).$$

# Invariant mass: applications

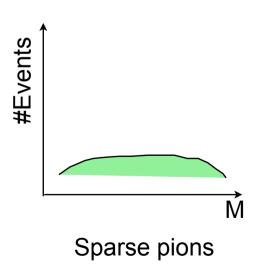
- Particles like  $\rho$ ,  $\omega$ ,  $\varphi$  have average lifetime of 10-22-10-23 s
  - How do we know of their existence if they live so shortly?
- Example: reaction pp→ppπ<sup>+</sup>π<sup>-</sup>
  - We identify all four particles in the final state and measure their momentum
  - Let's focus on the pion pair, the total energy & momentum are:

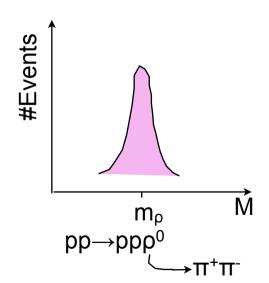
$$E=E_++E_ p=p_++p_-$$

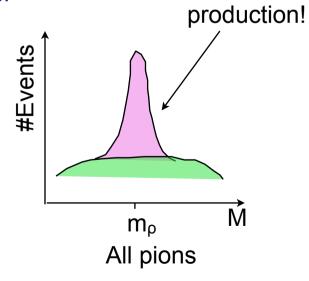
The invariant mass is:

$$M = (E^2 - \mathbf{p}^2)^{1/2}$$

The event distribution for the variable M will look like:



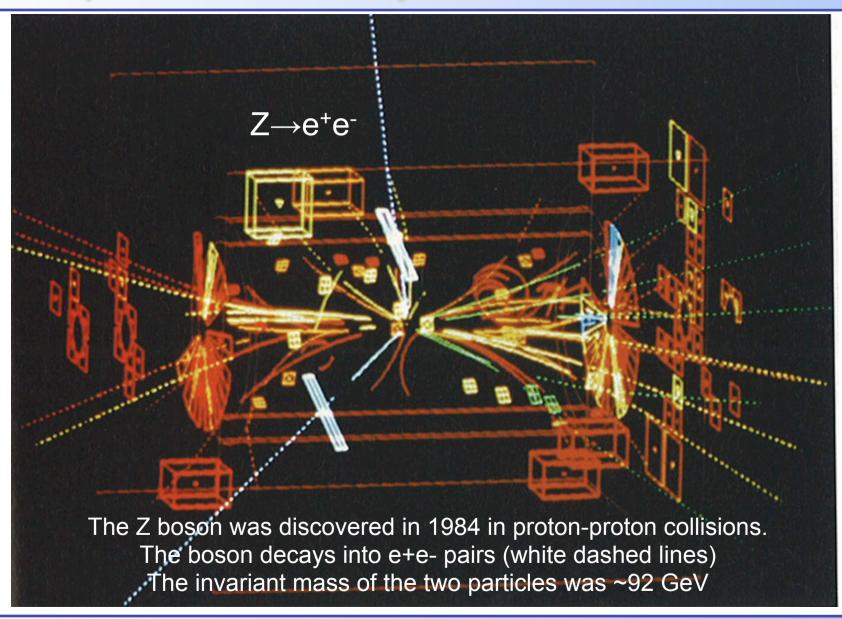




**Fvidence** 

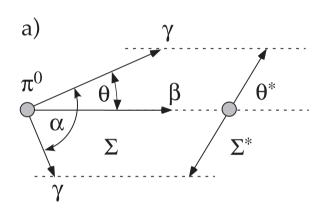
for p

# Example: Z discovery

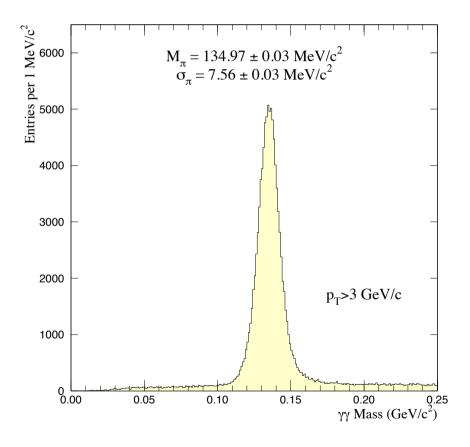


# Example: π<sup>0</sup> reconstruction

- Neutral pions decay in photon pairs
  - Measuring the angle and energy of the emitted photons one can reconstruct the mass of the decaying pion



Exercise: calculate invariant mass formula for massless decay products (e.g. photons)



# Invariant mass: 3 body decay

In case of a 3-body decay:

$$R \Rightarrow 1 + 2 + 3$$
.

We can construct three invariant masses:

$$m_{12}^2 \equiv (\mathcal{P}_1 + \mathcal{P}_2)^2,$$
  
 $m_{13}^2 \equiv (\mathcal{P}_1 + \mathcal{P}_3)^2,$   
 $m_{23}^2 \equiv (\mathcal{P}_2 + \mathcal{P}_3)^2$ 

For the three body case one finds:

$$m_{12}^2 + m_{13}^2 + m_{23}^2 = m_1^2 + m_2^2 + m_3^2 + (\mathcal{P}_1 + \mathcal{P}_2 + \mathcal{P}_3)^2$$
  
=  $m_1^2 + m_2^2 + m_3^2 + M^2$ .

Only two independent invariant masses

#### Example: Dalitz plot

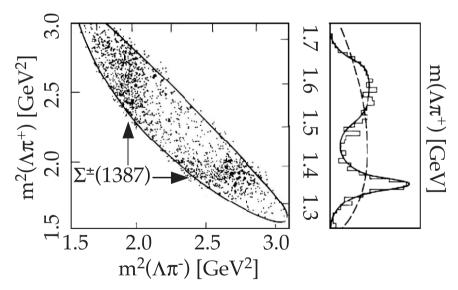
As an example, let's study the reaction:

$$K^-p \to \Lambda \pi^+\pi^- (\Lambda \to \pi^-p),$$

We can measure two invariant masses

Let 
$$m_{12} \equiv m(\Lambda \pi^-)$$
 be  $m_{13} \equiv m(\Lambda \pi^+)$ 

The so-called "Dalitz plot" shows the relation between  $(m_{13})^2$  and  $(m_{12})^2$ 



The Σ<sup>±</sup> resonance appears as two bands in the Dalitz plot around 1.4 GeV

$$\Sigma^{\pm}(1387) \to \Lambda \pi^{\pm}$$
.