Manual Neural Network

This is really cool, and it's something I've wanted to do. I've got this and several other ways to do a similar thing. This one gets done first. It's going to mimic the TensorFlow API. When I get back to TensorFlow, I should have a better understanding.

From Jose

In this notebook we will manually build out a neural network that mimics the TensorFlow API. This will greatly help your understanding when working with the real TensorFlow!

```
In [1]: ## It can be useful to see errors to know how to fix them.
##+ However, it messes with the "compute all cells" type of
##+ stuff. Here, you can decide whether to see the errors or
##+ not. (In some places, I've put the error text in
##+ markdown cells.)

do_show_errors = False
```

Some Info About super() and Object Oriented Programming in General

```
class SimpleClassLecture0():
In [2]:
            def __init__(self):
                print("hello")
            ##endof: __init__(self)
        ##endof: SimpleClassLecture0
In [3]:
        s = "world"
        type(s)
In [4]:
Out[4]: str
In [5]:
        # s.<then press [Tab]>
        # Gives a list of methods
In [6]: x0 = SimpleClassLecture0
In [7]: x0 # what we get without the parentheses - __init__ doesn't get called
Out[7]: __main__.SimpleClassLecture0
In [8]: x0 = SimpleClassLecture0()
        hello
In [9]: x0 # Instance of SimpleClassLecture and where it exists in memory
Out[9]: <__main__.SimpleClassLecture0 at 0x20d42cf24a8>
```

```
class SimpleClassLecture1():
In [10]:
             def __init__(self):
                 print("hello")
             ##endof: __init__(self)
             def yell(self):
                 print("YELLING")
             ##endof: yell(self)
         ##endof: SimpleClassLecture1
In [11]: x1 = SimpleClassLecture1()
         hello
         # I'm going to type 'x1.' then hit [Tab].
In [12]:
         #+ it will autocomplete 'x1.yell', after
         #+ which I'll add the parenthesis
         x1.yell()
         YELLING
In [13]: # Now, I'll just type it all out.
         x1.yell()
         YELLING
In [14]:
         ## adding in this illustration. These first calls will work fine.
         sc = SimpleClassLecture1()
         print("--- some separation ---")
         sc.yell()
         hello
         --- some separation ---
         YELLING
```

```
In [15]: ## continuing with the illustration. This is called
    ##+ as if it were the lecture notes. It will throw
    ##+ an error/exception/whatever-you-want-to-call-it
    if do_show_errors:
        sc_oops = SimpleClassLecture1("Basket Weaving 101")
        print("--- some separation ---") # won't execute b/c error before
        sc_oops.yell() # won't execute b/c error before
    ##endof: if do_show_errors
```

OUTPUT (error) should be

Remember the code:

```
class SimpleClassLecture1():
    def __init__(self):
        print("hello")
    ##endof: __init__(self)
    def yell(self):
        print("YELLING")
    ##endof: yell(self)
##endof: SimpleClassLecture1
In [16]: class ExtendedClassLecture0(SimpleClassLecture1):
             def __init__(self):
                 print("EXTEND!")
             ##endof: __init__(self)
         ##endof: ExtendedClassLecture0(SimpleClassLecture1)
         y0 = ExtendedClassLecture0()
In [17]:
         # Remember, there's no 'super' call for '__init__'
         EXTEND!
In [18]:
         # No 'super' with '__init__', but other things work
         y0.yell()
         YELLING
```

Now, let's use the super keyword.

```
In [19]: class ExtendedClassLecture1(SimpleClassLecture1):
    def __init__(self):
        super().__init__()
        print("EXTEND!")
    ##endof: __init__(self)

##endof: ExtendedClassLecture(SimpleClassLecture)

In [20]: y1 = ExtendedClassLecture1()
    hello
    EXTEND!

In [21]: y1.yell()
    YELLING
```

Here, we're going to add an argument to the SimpleClass __init__ (i.e. its constructor). Since this is the final state in which Jose leaves it, I'm going to use SimpleClassLecture instead of continuing with SimpleClassLecture2 . I'll do similarly with the extended class - using ExtendedClassLecture instead of staying with the pattern and using ExtendedClassLecture2 .

```
x = SimpleClassLecture("Dave")
In [23]:
         hello Dave
In [24]: x.yell()
         YELLING
In [25]:
         class ExtendedClassLecture(SimpleClassLecture):
             def __init__(self):
                 super().__init__("Davidushka!")
                 print("EXTEND!")
             ##endof: __init__(self)
         ##endof: ExtendedClassLecture(SimpleClassLecture)
In [26]: | y = ExtendedClassLecture()
         hello Davidushka!
         EXTEND!
         y.yell()
In [27]:
         YELLING
```

From the class material

```
In [28]: class SimpleClass():

    def __init__(self, str_input):
        # DWB: I'm not fixing his lack of space after "SIMPLE".
        #+ 1701111285_2023-11-27T115445-0700
        print("SIMPLE" + str_input)
        ##endof: __init__(self, str_input)

##endof: SimpleClass
```

I'll do the same two illustrations.

```
In [29]: if do_show_errors:
    sc = SimpleClass() # will throw an error
##endof: if do_show_errors
```

OUTPUT (which is an error) should be:

SIMPLEBasket Weaving 101

Remember the code (defined in the lecture notes)

```
class SimpleClass():
    def __init__(self, str_input):
        # DWB: I'm not fixing his lack of space after "SIMPLE".
                1701111285_2023-11-27T115445-0700
        print("SIMPLE" + str_input)
    ##endof: init (self, str input)
##endof: SimpleClass
In [31]: class ExtendedClassNoSuper(SimpleClass):
             def __init__(self):
                 print('EXTENDED')
             ## endof: __init__(self)
         ##endof: ExtendedClassNoSuper
In [32]: s = ExtendedClassNoSuper()
         EXTENDED
```

With the output, remember that we *overwrote* the __init__(self) method.

What I'll call ExtendedClass is building upon the ExtendedClassNoSuper code. I could have added Super at the end (ExtendedClassSuper), or I could have done as the lecture notes did and call both ExtendedClass, with one replacing the other. Anyway, ExtendedClass will use super.

```
# remember to use 'class' instead of 'def'
In [33]:
         #+ (Oops, DWB 1701111919_2023-11-27T120519-0700)
         class ExtendedClass(SimpleClass):
             def __init__(self):
                 super().__init__(" My String") # Jose puts the space in the string here.
                 print('EXTENDED')
             ##endof: def __init__(self)
         ##endof: ExtendedClass
In [34]: s = ExtendedClass()
         SIMPLE My String
         EXTENDED
```

We've finished learning some OOP stuff - now for the Manual NN

I've put in a bunch of stuff which should give some general idea of what's going on (though there will be a lot of memory addresses rather than useful info). You can turn this on or off in the next cell.

```
In [35]: global_do_show_steps_bool = True
```

Operation

```
In [36]: class Operation():
             def __init__(self, input_nodes=[],
                          do_show_steps=global_do_show_steps_bool):
                 if do_show_steps:
                     dashes = "-"*50
                     print("\n\n" + dashes)
                     print("In __init__")
                     print()
                 ##endof: if do_show_steps
                 self.input_nodes = input_nodes
                 if do_show_steps:
                     print("\n Now, self.input_nodes = ")
                              " + str(self.input_nodes))
                     print()
                 ##endof: if do_show_steps
                 self.output_nodes = []
                 for node in input_nodes:
                     if do_show_steps:
                         print("\n Current node is:")
                                     node = " + str(node))
                         print("
                         print()
```

```
##endof: if do show steps
            node.output_nodes.append(self)
            if do_show_steps:
                print("\n After assignment, node.output_nodes.append(self)")
                           node = " + str(node))
                print("
                print()
               print(dashes)
                print()
           ##endof: if do_show_steps
        ##endof: for node in input nodes
        if do_show_steps:
            print("\n Before appending self to _default_graph,")
                       _default_graph = ")
                                 " + str( default graph))
            print("
            print()
        ##endof: if do_show_steps
        _default_graph.operations.append(self) # Came back to add this
                                               #+ after we had created
                                              #+ the graph class
        if do_show_steps:
            print("\n After appending self to _default_graph,")
                       _default_graph = ")
            print("
                                 " + str( default graph))
            print("
            print()
       ##endof: if do_show_steps
    ##endof: __init__(self, input_nodes=[]):
    def compute(self):
        pass
    ##endof: compute(self)
##endof: Operation
```

```
In [37]:
         class OperationCNV():
             An Operation is a node in a "Graph". TensorFlow will also use this concept of a Graph.
             This Operation class will be inherited by other classes that actually compute the specific
             operation, such as adding or matrix multiplication.
             def __init__(self, input_nodes=[]):
                 Initialize an Operation
                 self.input_nodes = input_nodes # The list of input nodes coming in to the node
                 self.output nodes = []
                                                # List of nodes that will consume the output
                                                #+ of this node
                 # For every node in the input, we append this operation (self) to the list of
                 #+ to the list of the input nodes' consumers (i.e. this operation becomes an
                 #+ output node)
                 for node in input nodes:
                     node.output nodes.append(self)
                 ##endof: for node in input nodes
                 # There will be a global default graph (TensorFlow works this way)
                 #+ We will append this particular operation (to the global default graph)
                 # Append this operation to the list of operations in the currently-active
                 #+ default graph
                 _default_graph.operations.append(self)
             ##endof: __init_(self, input_nodes=[])
             def compute(self):
                 This is a placeholder function. It will be overwritten by the actual specific operation
                 that inherits from this class
                  111
```

pass

##endof: compute(self)

##endof: class OperationCNV()

Example Operations

Addition

```
class Add(Operation):
In [38]:
             def __init__(self, x, y,
                          do_show_steps=global_do_show_steps_bool):
                 self.do_show_steps = do_show_steps
                 if self.do_show_steps:
                     dashes = "-"*35
                     print("\n" + dashes)
                     print("\n Initializing an Add operation")
                     print()
                 ##endof: if do_show_steps
                 super().__init__([x, y])
             ##endof: __init__(self, x, y)
             def compute(self, x_var, y_var):
                 if self.do_show_steps:
                     print("\n Now, computing the Add operation ")
                     print()
                 ##endof: if do_show_steps
                 self.inputs = [x_var, y_var]
                 if self.do_show_steps:
                     print("\n Now, self.inputs = ")
                     print(" " + str(self.inputs))
                     print()
                 ##endof: if do_show_steps
                 result_of_add = x_var + y_var
                 if self.do_show_steps:
                     print("\n We will return")
                     print(" result_of_add = " + str(result_of_add))
                     dashes = "-"*35
                     print(dashes)
                     print()
```

```
##endof: if do_show_steps

return result_of_add

##endof: compute(self, x_var, y_var):

##endof: class Add(Operation)
```

```
In [39]: class addCNV(OperationCNV):
    def __init__(self, x, y):
        super().__init__([x, y])
    ##endof: __init__(self, x, y)

    def compute(self, x_var, y_var):
        self.inputs = [x_var, y_var]
        return x_var + y_var

    ##endof: compute(self, x_var, y_var)

##endof: addCNV(OperationCNV)
```

Multiplication

```
class Multiply(Operation):
In [40]:
             def __init__(self, x, y,
                          do_show_steps=global_do_show_steps_bool):
                 self.do_show_steps = do_show_steps
                 if self.do_show_steps:
                     dashes = "-"*35
                     print("\n" + dashes)
                     print("\n Initializing a Multiply operation")
                     print()
                 ##endof: if do_show_steps
                 super().__init__([x, y])
             ##endof: __init__(self, x, y)
             def compute(self, x_var, y_var):
                 if self.do_show_steps:
                     print("\n Now, computing the Multiply operation ")
                     print()
                 ##endof: if do_show_steps
                 self.inputs = [x_var, y_var]
                 if self.do_show_steps:
                     print("\n Now, self.inputs = ")
                             " + str(self.inputs))
                     print("
                     print()
                 ##endof: if do_show_steps
                 result_of_multiply = x_var * y_var
                 if self.do_show_steps:
                     print("\n We will return")
                               result_of_multiply = " + str(result_of_multiply))
                     print("
                     dashes = "-"*35
                     print(dashes)
                     print()
                 ##endof: if do_show_steps
                 return result_of_multiply
```

```
##endof: compute(self, x_var, y_var):
##endof: class Multiply(Operation)
```

```
In [41]: class multiplyCNV(OperationCNV):
    def __init__(self, a, b):
        super().__init__([a, b])
    ##endof: __init__(self, a, b)
    def compute(self, a_var, b_var):
        self.inputs = [a_var, b_var]
        return a_var * b_var

    ##endof: compute(self, a_var, b_var)
##endof: multiplyCNV(OperationCNV)
```

Matrix Multiplication

```
class MatMul(Operation):
In [42]:
             def __init__(self, x, y,
                          do_show_steps=global_do_show_steps_bool):
                 self.do_show_steps = do_show_steps
                 if self.do_show_steps:
                     dashes = "-"*35
                     print("\n" + dashes)
                     print("\n Initializing a MatMul operation")
                     print()
                 ##endof: if do_show_steps
                 super().__init__([x, y])
             ##endof: __init__(self, x, y)
             def compute(self, x_var, y_var):
                 if self.do_show_steps:
                     print("\n Now, computing the MatMul operation")
                     print()
                 ##endof: if do_show_steps
                 self.inputs = [x_var, y_var]
                 if self.do_show_steps:
                     print("\n Now, self.inputs = ")
                             " + str(self.inputs))
                     print("
                     print()
                 ##endof: if do_show_steps
                 # We're assuming we have numpy arrays (matrices), so we can
                 #+ use the var.dot() operation
                 result_of_matmul = x_var.dot(y_var)
                 if self.do_show_steps:
                     print("\n We will return")
                     print(" result_of_matmul = " + str(result_of_matmul))
                     dashes = "-"*35
                     print(dashes)
                     print()
                 ##endof: if do_show_steps
```

```
return result_of_matmul

##endof: compute(self, x_var, y_var):

##endof: class MatMul(Operation)
```

```
In [43]: class matmulCNV(OperationCNV):
    def __init__(self, a, b):
        super().__init__([a, b])
    ##endof: __init__(self, a, b)
    def compute(self, a_mat, b_mat):
        self.inputs = [a_mat, b_mat]
        return a_mat.dot(b_mat)

    ##endof: compute(self, a_mat, b_mat)

##endof: matmulCNV(OperationCNV)
```

Placeholders

Variables

Lecture Version - with (maybe) Dave's additions

```
In [46]: class Variable():
    def __init__(self, initial_value=None):
        self.value = initial_value
        self.output_nodes = []
        __default_graph.variables.append(self)
        ##endof: __init__(self, initial_value=None)
##endof: class Variable
```

Graph

Lecture Version - with (maybe) Dave's additions

```
In [48]: class Graph():
    def __init__(self):
        self.operations = []
        self.placeholders = []
        self.variables = []

    ##endof: __init__(self)

    def set_as_default(self):
        global __default_graph
        __default_graph = self

    ##endof: set_as_default(self)

##endof: Graph()
```

```
In [49]:
         class GraphCNV():
             No docstring in the course notes
             def __init__(self):
                 self.operations = []
                 self.placeholders = []
                 self.variables = []
             ##endof: def __init__(self)
             def set_as_default(self):
                 Sets this Graph instance as the Global Default Graph
                 global _default_graph
                 _default_graph = self
             ##endof: set_as_default(self)
         ##endof: GraphCNV()
```

A Basic Graph

$$z=Ax+b$$
 With $A=10$ and $b=1$
$$z=10x+1$$

Just need a placeholder for \boldsymbol{x} and then, once \boldsymbol{x} is filled in, we can solve it!

```
In [50]: g = Graph()
In [51]: g.set_as_default()
```

```
In [52]: A = Variable(10)
In [53]: b = Variable(1)
In [54]: # Jose comments, "Will be filled out later"
x = Placeholder()
```

In [55]: y = Multiply(A, x)

```
Initializing a Multiply operation
In __init__
       self.input_nodes =
Now.
    [<__main___.Variable object at 0x0000020D42D0C320>, <__main___.Placeholder object at 0x0000020D42D13080>]
Current node is:
    node = <__main__.Variable object at 0x0000020D42D0C320>
After assignment, node.output_nodes.append(self)
    node = <__main__.Variable object at 0x0000020D42D0C320>
-----
Current node is:
    node = <__main__.Placeholder object at 0x0000020D42D13080>
After assignment, node.output_nodes.append(self)
    node = < main__.Placeholder object at 0x0000020D42D13080>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D42D138D0>
After appending self to _default_graph,
    _default_graph =
```

<__main__.Graph object at 0x0000020D42D138D0>

In [56]: z = Add(y, b)

```
Initializing an Add operation
In __init__
       self.input_nodes =
Now.
    [<__main__.Multiply object at 0x0000020D42D1B048>, <__main__.Variable object at 0x0000020D42D0CCF8>]
Current node is:
    node = <__main__.Multiply object at 0x0000020D42D1B048>
After assignment, node.output_nodes.append(self)
    node = <__main__.Multiply object at 0x0000020D42D1B048>
Current node is:
    node = < main__.Variable object at 0x0000020D42D0CCF8>
After assignment, node.output_nodes.append(self)
    node = <__main__.Variable object at 0x0000020D42D0CCF8>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D42D138D0>
After appending self to _default_graph,
    _default_graph =
```

<__main__.Graph object at 0x0000020D42D138D0>

A Comment or 2

Now, we just need to actually compute the z. We need to add in 1) a traverse-post-order function, which allows a post order traversal of nodes, which is necessary to make sure the computation is done in the correct order; 2) a Session class, which actually executes this graph.

The Basic Graph with the Course Notes Version

```
In [57]: g_CNV = GraphCNV()
In [58]: g_CNV.set_as_default()
In [59]: A_CNV = VariableCNV(10)
In [60]: b_CNV = VariableCNV(1)
In [61]: x_CNV = PlaceholderCNV()
In [62]: y_CNV = multiplyCNV(A_CNV, x_CNV)
In [63]: z_CNV = addCNV(y_CNV, b_CNV)
```

We got here, and everything computes, both for my lecture version and the course notes version. When I go through the next lecture, I'll commment out the Course Notes Version. I might come back and do the Course Notes Version. The problem now isn't the same variable names (though I added '_CNV' to all of them) - it's the Graph.set_as_default function.

DWB

```
1701317785_2023-11-29T211625-0700
```

Actually, I think both would be fine, but I'm not going to spend the extra time doing both.

```
1701394493_2023-11-30T183453-0700
```

Session

```
In [64]: import numpy as np
```

Check on graphs, due to error.

```
In [65]: g
Out[65]: <__main__.Graph at 0x20d42d138d0>
In [66]: g_CNV
Out[66]: <__main__.GraphCNV at 0x20d42d1b0b8>
In [67]: g == g_CNV
Out[67]: False
```

Traversing Operation Nodes

Lecture Version of Classes - with Dave's additions - AND of Running the Session

```
def traverse_postorder(operation,
In [68]:
                                do_show_steps=global_do_show_steps_bool):
             PostOrder Traversal of Nodes. Basically makes sure computations are
             done in the correct order ( A*x first , then A*x + b ). Feel free
             to copy and paste this code. (DWB 1701792896_2023-12-05T091456-0700,
             nope, typing it out). It is not super important for understanding
             the basic fundamentals of deep learning.
             nodes postorder = []
             def recurse(node):
                 if do show steps:
                     dashes = "-"*40
                     print("\n" + dashes)
                     print("\n Inside recurse(node)")
                     print()
                     print("
                                 node = " + str(node))
                     print()
                 ##endof: if do show steps
                 if isinstance(node, Operation):
                     if do_show_steps:
                         print("\n node, " + str(node))
                         print(" is an Operation")
                     ##endof: if do_show_steps
                     for input_node in node.input_nodes:
                         if do show steps:
                             print("\n Current input node = ")
                             print(str(input_node))
                         ##endof: if do_show_steps
                         recurse(input node)
                     ##endof: for input_node in node.input_nodes
                 ##endof: if isinstance(node, Operation)
                 nodes postorder.append(node)
             ##endof: recurse(node)
             if do show steps:
                 dashes = "-"*43
                 print("\n\n" + dashes)
```

```
print("\n Calling recurse(operation)")
        print("\n with operation = ")
        print(str(operation))
        print()
    ##endof: if do_show_steps
    recurse(operation)
    if do_show_steps:
        print("\n\n")
        dashes = "-"*43
        print("\n\n")
        print("Exited the recursion")
        print("\n")
        print(" We now have nodes_postorder = ")
        print(str(nodes_postorder))
        print()
    ##endof: if do_show_steps
    return nodes_postorder
##endof traverse_postorder(operation)
```

```
class Session():
In [69]:
                       ## use operation and feed dict as these are the names used by
                      ##+ TensorFlow. feed dict matches placeholders to input values.
                      ##+ Later on, we'll feed our network batches of data through that
                       ##+ dictionary.
                      def run(self, operation, feed_dict={},
                                    do_show_steps=global_do_show_steps_bool):
                             if do show steps:
                                    print("\n\n !!! Running the Session !!!\n")
                             ##endof: if do show steps
                             nodes postorder = traverse postorder(operation)
                             if do_show_steps:
                                    print("\n After running")
                                                  nodes postorder = traverse postorder(operation)")
                                    print(" we have")
                                    print(" nodes postorder = ")
                                    print(str(nodes postorder))
                                    print()
                             ##endof: if do_show_steps
                             for node in nodes_postorder:
                                    if type(node) == Placeholder:
                                           if do_show_steps:
                                                  print("\n We have a Placeholder and will")
                                                  print(" assign feed_dict[node] to node.output")
                                                  print(" ( which which means the value,")
                                                  print(" feed dict[node] = " + str(feed dict[node])) #"print(" feed dict[node] = " + str(feed dict[node])
                                                 print(" will be assigned.")
                                                  print()
                                           ##endof: if do_show_steps
                                           node.output = feed_dict[node]
                                           if do show steps:
                                                  print("\n Checking, node.output = " + str(node.output)) #"print("\n Checking, node.output = " + str(node.output)) #"
                                                  print()
                                           ##endof: if do_show_steps
                                    ##endof: if type(node) == Placeholder
                                    elif type(node) == Variable:
                                           if do_show_steps:
```

```
print("\n We have a Variable and will")
        print(" assign node.value to node.output")
        print(" ( which which means the value,")
       print(" node.value = " + str(node.value))
        print(" will be assigned.")
        print()
    ##endof: if do show steps
    node.output = node.value
    if do show steps:
        print("\n Checking, node.output = " + str(node.output))
        print()
    ##endof: if do show steps
##endof: elif type(node) == Variable
# # DWB commenting out the else and its assumption
# else:
     # <s>OPERATION</s>
## ## DWB, my first attempt here was off.
## elif type(node) == Operation:
elif isinstance(node, Operation):
    if do_show_steps:
        print("\n We have an Operation and will")
        print(" compute the output of the operation")
        print(" based on each input node's output,")
        print(" for each node's input nodes")
        print(" We will assign the result of the")
        print(" computation to  node.output")
        print()
        print(" Some pertinent parts:")
        print(str(node.input nodes))
        print(" I'm not going to mess around finding")
        print(" the output of each input node here,")
        print(" since it will become the node.inputs")
        print()
   ##endof: if do_show_steps
    node.inputs = \
      [input_node.output for input_node in node.input_nodes]
    # For the next command,
    #+ node.output = node.compute((node inputs))
    #+ asterisk is basically a sort of args asterisk.
    #+ Allows us to combine inputs
   #+ without knowing how many we might have. (Note: each of
    #+ the operations we've made only has two inputs, but it's
```

```
#+ nice to have it generalized, as I'm sure Tensorflow has
       #+ it generalized. -DWB 1701796074 2023-12-05T100754-0700)
       if do_show_steps:
            print("\n We will now assign the value of")
            print(" node.output")
            print(" We will use")
           # next line might need
           #+ for nd_inp in *node_inputs: print(nd_inp)
           #+ instead of str(*node_inputs)
            #+ Nope, seems we're okay
           print(" node.inputs = " + str(node.inputs))
            print()
       ##endof: if do show steps
       node.output = node.compute(*node.inputs)
       if do_show_steps:
            print("\n Inspecting, node.output = " + str(node.output))
            print()
       ##endof: if do show steps
    ##endof: elif isinstance(node, Operation)
    else:
        print()
       print("Session: SOMETHING IS WRONG, AND THINGS WILL PROBABLY BREAK")
       print()
   ##endof: if/elif/else <type(node)>
   # Get things numpy-y
   if type(node.output) == list:
       node.output = np.array(node.output)
   ##endof: if type(node.output) == list
##endof: for node in nodes postorder
if do show steps:
   print("\n\n Looking at a few things, where we are getting")
   print(" errors, as shown in a cell below.")
    print()
   print("operation = " + str(operation))
    print()
    op out = operation.output
   print("operation.output = " + str(op_out))
```

```
print()
            print("\n Looking at nodes postorder = ")
            print(str(nodes postorder))
            print()
            print(" Looking at nodes_postorder[0], which I hope is an Operation")
                        nodes postorder[0] = " + str(nodes postorder[0]))
            print("
            print()
            print("\n If we got an Operation, let's print its output")
            print()
            if type(nodes postorder[0]) == Operation:
                print("\n It is an operation, and")
                print("
                           nodes postorder[0].output = " + \
                      str(nodes postorder[0].output))
                print()
            ##endof: if/else type(nodes postorder[0]) == Operation
       ##endof: if do show steps
        output to return = operation.output
       if do_show_steps:
            print("\n\n We will return the output of the operation,")
            equals str = "="*60
            print(" " + equals str)
            print("output to return = operation.output = " + \
                  str(output to return))
            print(" " + equals str)
            print()
            print("\n\n !!! Finished Running the Session !!!\n")
            print()
       ##endof: if do show steps
       return output to return
   ##endof: run(self, operation, feed_dict={}, do_show_steps=True)
##endof: Session()
```

```
In [70]: sess = Session()
```

```
!!! Running the Session !!!
Calling recurse(operation)
    with operation =
<__main__.Add object at 0x0000020D42D1B1D0>
Inside recurse(node)
     node = <__main__.Add object at 0x0000020D42D1B1D0>
node, <__main__.Add object at 0x0000020D42D1B1D0>
is an Operation
Current input_node =
<_main__.Multiply object at 0x0000020D42D1B048>
Inside recurse(node)
     node = <__main__.Multiply object at 0x0000020D42D1B048>
node, <__main__.Multiply object at 0x0000020D42D1B048>
is an Operation
 Current input_node =
<_main__.Variable object at 0x0000020D42D0C320>
Inside recurse(node)
```

```
node = < main .Variable object at 0x0000020D42D0C320>
 Current input node =
< main .Placeholder object at 0x0000020D42D13080>
Inside recurse(node)
     node = < main .Placeholder object at 0x0000020D42D13080>
 Current input_node =
<_main__.Variable object at 0x0000020D42D0CCF8>
 Inside recurse(node)
     node = <__main__.Variable object at 0x0000020D42D0CCF8>
Exited the recursion
We now have nodes postorder =
[<__main__.Variable object at 0x0000020D42D0C320>, <__main__.Placeholder object at 0x0000020D42D13080>, <__ma</pre>
in .Multiply object at 0x0000020D42D1B048>, < main .Variable object at 0x0000020D42D0CCF8>, < main .Add
object at 0x0000020D42D1B1D0>]
 After running
   nodes postorder = traverse postorder(operation)
 we have
 nodes postorder =
[<__main__.Variable object at 0x0000020D42D0C320>, <__main__.Placeholder object at 0x0000020D42D13080>, <__ma</pre>
in__.Multiply object at 0x0000020D42D1B048>, <__main__.Variable object at 0x0000020D42D0CCF8>, < main .Add
```

object at 0x0000020D42D1B1D0>]

We have a Variable and will assign node.value to node.output (which which means the value, node.value = 10 will be assigned.

Checking, node.output = 10

We have a Placeholder and will assign feed_dict[node] to node.output (which which means the value, feed_dict[node] = 10 will be assigned.

Checking, node.output = 10

We have an Operation and will compute the output of the operation based on each input_node's output, for each node's input_nodes
We will assign the result of the computation to node.output

Some pertinent parts:

[<__main__.Variable object at 0x0000020D42D0C320>, <__main__.Placeholder object at 0x0000020D42D13080>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs

We will now assign the value of node.output
We will use
node.inputs = [10, 10]

```
Now, computing the Multiply operation
```

```
Now, self.inputs = [10, 10]
```

```
We will return
    result_of_multiply = 100
```

Inspecting, node.output = 100

We have a Variable and will assign node.value to node.output (which which means the value, node.value = 1 will be assigned.

Checking, node.output = 1

We have an Operation and will compute the output of the operation based on each input_node's output, for each node's input_nodes
We will assign the result of the computation to node.output

Some pertinent parts:

[<__main__.Multiply object at 0x0000020D42D1B048>, <__main__.Variable object at 0x0000020D42D0CCF8>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs

We will now assign the value of node.output
We will use
node.inputs = [100, 1]

```
Now, computing the Add operation
Now, self.inputs =
    [100, 1]
We will return
    result_of_add = 101
Inspecting, node.output = 101
Looking at a few things, where we are getting
 errors, as shown in a cell below.
operation = <__main__.Add object at 0x0000020D42D1B1D0>
operation.output = 101
Looking at nodes postorder =
[<__main__.Variable object at 0x0000020D42D0C320>, <__main__.Placeholder object at 0x0000020D42D13080>, <__ma</pre>
in__.Multiply object at 0x0000020D42D1B048>, <__main__.Variable object at 0x0000020D42D0CCF8>, <__main__.Add
object at 0x0000020D42D1B1D0>]
 Looking at nodes postorder[0], which I hope is an Operation
    nodes postorder[0] = <__main__.Variable object at 0x0000020D42D0C320>
If we got an Operation, let's print its output
We will return the output of the operation,
 ______
output to return = operation.output = 101
  _____
```

!!! Finished Running the Session !!!

Course Notes Version of Classes AND of Running the Session

```
def traverse_postorder_CNV(operation):
In [72]:
             PostOrder Traversal of Nodes. Basically makes sure computations are done in
             the correct order (Ax first , then Ax + b). Feel free to copy and paste this code.
             It is not super important for understanding the basic fundamentals of deep learning.
             nodes postorder = []
             def recurse(node):
                 if isinstance(node, OperationCNV):
                     for input node in node.input nodes:
                         recurse(input node)
                 nodes postorder.append(node)
             recurse(operation)
             return nodes postorder
         ##endof traverse_postorder_CNV(operation)
         ##+ I just copy/pasted it and added the '_CNV'
         ##+ or "CNV" where necessary
         ##+ DWB 1701800683 2023-12-05T112443-0700
```

```
class SessionCNV():
In [73]:
             def run(self, operation, feed_dict = {}):
                   operation: The operation to compute
                   feed dict: Dictionary mapping placeholders to input values (the data)
                 # Puts nodes in correct order
                 nodes_postorder = traverse_postorder_CNV(operation)
                 for node in nodes_postorder:
                     if type(node) == PlaceholderCNV:
                         node.output = feed_dict[node]
                     elif type(node) == VariableCNV:
                         node.output = node.value
                     else: # Operation
                          node.inputs = [input_node.output for input_node in node.input_nodes]
                         node.output = node.compute(*node.inputs)
                     # Convert lists to numpy arrays
                     if type(node.output) == list:
                         node.output = np.array(node.output)
                 # Return the requested node value
                 return operation.output
         ##endof: class SessionCNV()
         ##+ I just copy/pasted it and added the '_CNV'
         ##+ or "CNV" where necessary
         ##+ DWB 1701800683_2023-12-05T112443-0700
```

That worked. We also fixed the bug in my version. On we go! Time for Q&R as I continue forward.

Now, some matrix multiplication

Lecture Version of matrix multiplication

```
Initializing a MatMul operation
In __init__
       self.input_nodes =
Now.
    [<__main__.Variable object at 0x0000020D43077208>, <__main__.Placeholder object at 0x0000020D43077470>]
Current node is:
     node = <__main__.Variable object at 0x0000020D43077208>
After assignment, node.output_nodes.append(self)
    node = <__main__.Variable object at 0x0000020D43077208>
 Current node is:
    node = <__main__.Placeholder object at 0x0000020D43077470>
After assignment, node.output_nodes.append(self)
    node = <__main__.Placeholder object at 0x0000020D43077470>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D42D96978>
After appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D42D96978>
```

```
Initializing an Add operation
In __init__
Now, self.input_nodes =
    [<__main___.MatMul object at 0x0000020D430775C0>, <__main___.Variable object at 0x0000020D42D96A58>]
Current node is:
    node = <__main__.MatMul object at 0x0000020D430775C0>
After assignment, node.output_nodes.append(self)
    node = <__main__.MatMul object at 0x0000020D430775C0>
Current node is:
    node = <__main__.Variable object at 0x0000020D42D96A58>
After assignment, node.output_nodes.append(self)
    node = < main .Variable object at 0x0000020D42D96A58>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D42D96978>
After appending self to _default_graph,
    _default_graph =
```

<__main__.Graph object at 0x0000020D42D96978>

In [78]: sess_mat = Session()

In [79]: | sess_mat.run(operation=z_mat, feed_dict={x_mat:10})

```
!!! Running the Session !!!
Calling recurse(operation)
    with operation =
<__main__.Add object at 0x0000020D43077240>
Inside recurse(node)
     node = <__main__.Add object at 0x0000020D43077240>
node, <__main__.Add object at 0x0000020D43077240>
 is an Operation
Current input_node =
<__main__.MatMul object at 0x0000020D430775C0>
Inside recurse(node)
     node = <__main__.MatMul object at 0x0000020D430775C0>
node, <__main__.MatMul object at 0x0000020D430775C0>
is an Operation
 Current input_node =
<_main__.Variable object at 0x0000020D43077208>
Inside recurse(node)
```

```
node = <__main__.Variable object at 0x0000020D43077208>
 Current input node =
< main .Placeholder object at 0x0000020D43077470>
Inside recurse(node)
     node = < main .Placeholder object at 0x0000020D43077470>
 Current input_node =
<_main__.Variable object at 0x0000020D42D96A58>
 Inside recurse(node)
     node = <__main__.Variable object at 0x0000020D42D96A58>
Exited the recursion
We now have nodes postorder =
[<__main__.Variable object at 0x0000020D43077208>, <__main__.Placeholder object at 0x0000020D43077470>, <__ma</pre>
in__.MatMul object at 0x0000020D430775C0>, <__main__.Variable object at 0x0000020D42D96A58>, <__main__.Add ob
ject at 0x0000020D43077240>]
 After running
   nodes_postorder = traverse_postorder(operation)
 we have
 nodes postorder =
[<__main__.Variable object at 0x0000020D43077208>, <__main__.Placeholder object at 0x0000020D43077470>, <__ma</pre>
in__.MatMul object at 0x0000020D430775C0>, <__main__.Variable object at 0x0000020D42D96A58>, <__main__.Add ob
```

```
ject at 0x0000020D43077240>]
```

We have a Variable and will assign node.value to node.output (which which means the value, node.value = [[10, 20], [30, 40]] will be assigned.

Checking, node.output = [[10, 20], [30, 40]]

We have a Placeholder and will assign feed_dict[node] to node.output (which which means the value, feed_dict[node] = 10 will be assigned.

Checking, node.output = 10

We have an Operation and will compute the output of the operation based on each input_node's output, for each node's input_nodes
We will assign the result of the computation to node.output

Some pertinent parts:

[<__main__.Variable object at 0x0000020D43077208>, <__main__.Placeholder object at 0x0000020D43077470>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs

```
Now, computing the MatMul operation
```

```
Now, self.inputs =
    [array([[10, 20],
      [30, 40]]), 10]
We will return
    result of matmul = [[100 200]
[300 400]]
Inspecting, node.output = [[100 200]
[300 400]]
We have a Variable and will
assign node.value to node.output
( which which means the value,
node.value = [1, 2]
will be assigned.
Checking, node.output = [1, 2]
We have an Operation and will
compute the output of the operation
based on each input_node's output,
for each node's input_nodes
We will assign the result of the
computation to node.output
Some pertinent parts:
[<__main__.MatMul object at 0x0000020D430775C0>, <__main__.Variable object at 0x0000020D42D96A58>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs
```

```
We will now assign the value of
 node.output
 We will use
 node.inputs = [array([[100, 200],
       [300, 400]]), array([1, 2])]
Now, computing the Add operation
 Now, self.inputs =
     [array([[100, 200],
       [300, 400]]), array([1, 2])]
 We will return
     result_of_add = [[101 202]
 [301 402]]
 Inspecting, node.output = [[101 202]
 [301 402]]
 Looking at a few things, where we are getting
 errors, as shown in a cell below.
operation = <__main__.Add object at 0x0000020D43077240>
operation.output = [[101 202]
 [301 402]]
Looking at nodes_postorder =
[<__main__.Variable object at 0x0000020D43077208>, <__main__.Placeholder object at 0x0000020D43077470>, <__ma</pre>
in__.MatMul object at 0x0000020D430775C0>, <__main__.Variable object at 0x0000020D42D96A58>, <__main__.Add ob
ject at 0x0000020D43077240>1
 Looking at nodes_postorder[0], which I hope is an Operation
     nodes_postorder[0] = <__main__.Variable object at 0x0000020D43077208>
```

```
If we got an Operation, let's print its output
```

!!! Finished Running the Session !!!

```
Out[79]: array([[101, 202], [301, 402]])
```

Course Notes Version of matrix multiplication

```
In [80]: g_mat_CNV = GraphCNV()
    g_mat_CNV.set_as_default()

A_mat_CNV = VariableCNV([[10, 20],[30, 40]])
    b_mat_CNV = VariableCNV([1, 1])

x_mat_CNV = PlaceholderCNV()

y_mat_CNV = matmulCNV(A_mat_CNV, x_mat_CNV)

z_mat_CNV = addCNV(y_mat_CNV, b_mat_CNV)

In [81]: sess_mat_CNV = SessionCNV()

In [82]: result_mat_CNV = sess_mat_CNV.run(operation=z_mat_CNV, feed_dict={x_mat_CNV:10})
```

Classification

Activation Function

```
In [84]: import matplotlib.pyplot as plt
%matplotlib inline
```

Sigmoid as an Operation

Lecture Version - with Dave's additions

```
In [85]: def Sigmoid(z):
    return 1 / (1 + np.exp(-z))
##endof: Sigmoid(z)

In [86]: sample_z = np.linspace(-10, 10, 100)
    sample_a = Sigmoid(sample_z)
```

```
In [87]: plt.plot(sample_z, sample_a)
Out[87]: [<matplotlib.lines.Line2D at 0x20d42d96ac8>]

10
08
06
04
02
-10.0 -7.5 -5.0 -2.5 0.0 2.5 5.0 7.5 10.0
```

```
In [88]: class Sigmoid(Operation):

    def __init__(self, z):
        super().__init__([z]) # need z inside square brackets
##endof: __init__(self, z)

    def compute(self, z_val):
        return 1 / (1 + np.exp(-z_val))
        ##endof: compute(self, z)

##endof: Sigmoid(Operation)
```

Course Notes Version

```
In [89]: class sigmoidCNV(OperationCNV):
    def __init__(self, z):
        super().__init__([z])
    ##endof: __init__(self, z)
    def compute(self, z_val):
        return 1 / (1 + np.exp(-z_val))
    ##endof: compute(self, z_val)
##endof: sigmoidCNV(Operation)
```

Classification Example

```
In [90]: from sklearn.datasets import make_blobs
```

Lecture Version

In [92]: data # first array is features, second array is labels

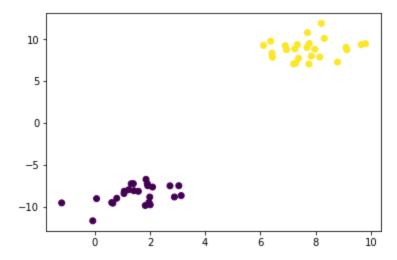
```
Out[92]: (array([[ 7.3402781 ,
                                  9.36149154],
                    9.13332743,
                                  8.74906102],
                    1.99243535,
                                 -8.85885722],
                    7.38443759,
                                  7.72520389],
                    7.97613887,
                                  8.80878209],
                    7.76974352,
                                  9.50899462],
                    8.3186688 ,
                                 10.1026025 ],
                    8.79588546,
                                 7.28046702],
                    9.81270381,
                                  9.46968531],
                    1.57961049,
                                 -8.17089971],
                    0.06441546,
                                 -9.04982817],
                    7.2075117 ,
                                  7.04533624],
                    9.10704928,
                                  9.0272212 ],
                    1.82921897,
                                 -9.86956281],
                   7.85036314,
                                 7.986659 ],
                    3.04605603,
                                 -7.50486114],
                    1.85582689, -6.74473432],
                    2.88603902,
                                 -8.85261704],
                 [ -1.20046211,
                                 -9.55928542],
                    2.00890845,
                                 -9.78471782],
                    7.68945113,
                                  9.01706723],
                                  8.33356412],
                    6.42356167,
                    8.15467319,
                                  7.87489634],
                    1.92000795,
                                 -7.50953708],
                    1.90073973,
                                 -7.24386675],
                    7.7605855 ,
                                  7.05124418],
                    6.90561582,
                                  9.23493842],
                    0.65582768,
                                 -9.5920878 ],
                    1.41804346,
                                 -8.10517372],
                    9.65371965,
                                  9.35409538],
                    1.23053506,
                                 -7.98873571],
                    1.96322881,
                                 -9.50169117],
                    6.11644251,
                                  9.26709393],
                    7.70630321,
                                 10.78862346],
                    0.79580385, -9.00301023],
                    3.13114921,
                                 -8.6849493 ],
                    1.3970852 ,
                                 -7.25918415],
                    7.27808709,
                                 7.15201886],
                    1.06965742,
                                 -8.1648251 ],
                                  9.77705761],
                    6.37298915,
                    7.24898455,
                                  8.85834104],
                    2.09335725,
                                 -7.66278316],
                    1.05865542,
                                 -8.43841416],
```

```
[ 6.43807502, 7.85483418],
  [ 6.94948313, 8.75248232],
  [ -0.07326715, -11.69999644],
  [ 0.61463602, -9.51908883],
  [ 1.31977821, -7.2710667 ],
  [ 2.72532584, -7.51956557],
  [ 8.20949206, 11.90419283]]),
array([1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1, 1))
```

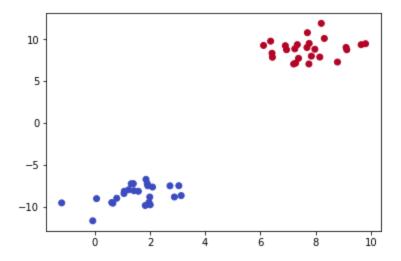
```
In [93]: features = data[0]
labels = data[1]
```

```
In [94]: plt.scatter(features[:, 0], features[:, 1], c=labels)
```

Out[94]: <matplotlib.collections.PathCollection at 0x20d45e6c860>



Out[95]: <matplotlib.collections.PathCollection at 0x20d45ef1c18>



Course Notes Verison

```
In [96]: # Maybe later
#
# ### Quick later, only need date once. I'm on Windows
# #!powershell -c (Get-Date -UFormat "%s_%Y%m%dT%H%M%S%Z00") -replace '[.][0-9]*_', '_'
```

Result was: 1704284456_20240103T122056-0700

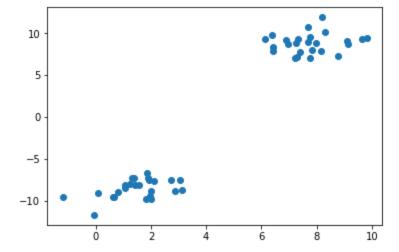
```
In [97]: data_CNV = make_blobs(n_samples=50, n_features=2, centers=2, random_state=75)
```

In [98]: data_CNV

```
Out[98]: (array([[ 7.3402781 ,
                                  9.36149154],
                    9.13332743,
                                  8.74906102],
                    1.99243535,
                                 -8.85885722],
                    7.38443759,
                                  7.72520389],
                    7.97613887,
                                  8.80878209],
                    7.76974352,
                                  9.50899462],
                    8.3186688 ,
                                 10.1026025 ],
                    8.79588546,
                                 7.28046702],
                    9.81270381,
                                  9.46968531],
                    1.57961049,
                                 -8.17089971],
                    0.06441546,
                                 -9.04982817],
                    7.2075117 ,
                                  7.04533624],
                    9.10704928,
                                  9.0272212 ],
                    1.82921897,
                                 -9.86956281],
                   7.85036314,
                                 7.986659 ],
                    3.04605603,
                                 -7.50486114],
                    1.85582689, -6.74473432],
                    2.88603902,
                                 -8.85261704],
                 [ -1.20046211,
                                 -9.55928542],
                    2.00890845,
                                 -9.78471782],
                    7.68945113,
                                  9.01706723],
                                  8.33356412],
                    6.42356167,
                    8.15467319,
                                  7.87489634],
                    1.92000795,
                                 -7.50953708],
                    1.90073973,
                                 -7.24386675],
                    7.7605855 ,
                                  7.05124418],
                    6.90561582,
                                  9.23493842],
                    0.65582768,
                                 -9.5920878 ],
                    1.41804346,
                                 -8.10517372],
                    9.65371965,
                                  9.35409538],
                    1.23053506,
                                 -7.98873571],
                    1.96322881,
                                 -9.50169117],
                    6.11644251,
                                  9.26709393],
                    7.70630321,
                                 10.78862346],
                    0.79580385, -9.00301023],
                    3.13114921,
                                 -8.6849493 ],
                    1.3970852 ,
                                 -7.25918415],
                    7.27808709,
                                 7.15201886],
                    1.06965742,
                                 -8.1648251 ],
                                  9.77705761],
                    6.37298915,
                    7.24898455,
                                  8.85834104],
                    2.09335725,
                                 -7.66278316],
                    1.05865542,
                                 -8.43841416],
```

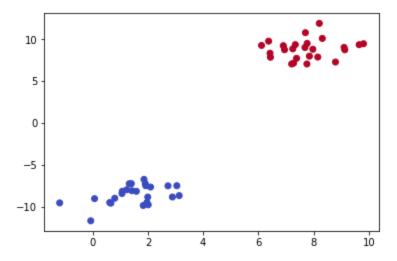
```
[ 6.43807502, 7.85483418],
    [ 6.94948313, 8.75248232],
    [ -0.07326715, -11.69999644],
    [ 0.61463602, -9.51908883],
    [ 1.31977821, -7.2710667 ],
    [ 2.72532584, -7.51956557],
    [ 8.20949206, 11.90419283]]),
array([1, 1, 0, 1, 1, 1, 1, 1, 1, 0, 0, 1, 1, 0, 0, 0, 0, 0, 0, 1, 1,
    1, 0, 0, 1, 1, 0, 0, 1, 1, 0, 0, 0, 1, 0, 1, 1, 0, 0, 0, 1,
    1, 0, 0, 0, 0, 1]))
```

Out[99]: <matplotlib.collections.PathCollection at 0x20d45f5a240>



```
In [100]: labels_CNV = data_CNV[1]
plt.scatter(features_CNV[:, 0], features_CNV[:, 1], c=labels_CNV, cmap='coolwarm')
```

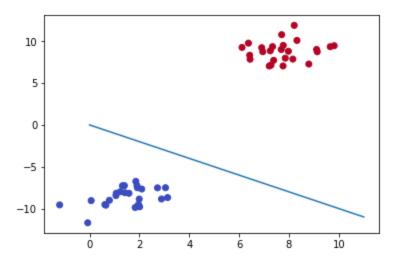
Out[100]: <matplotlib.collections.PathCollection at 0x20d45fc6d68>



Try to get a line separating the two blobs

Lecture Version

Out[101]: [<matplotlib.lines.Line2D at 0x20d45f95438>]



NameError: name 'x_line' is not defined

Anything above that line belongs to the red class. Anything below the line belongs to the blue class.

Formalized as y = mx + b

Could be restated as $f_2=mf_1+b$ with m=-1 and b=5

We want a placeholder ready, into which we can put the features.

Now, we're going to do a matrix representation to create a perceptron model and do our classification.

https://stackoverflow.com/a/59594891/6505499 (https://stackoverflow.com/a/59594891/6505499)

https://web.archive.org/web/20231231183005/https://stackoverflow.com/questions/59098171/how-to-insert-python-variable-into-latex-matrix-in-jupyter-notebook-markdown-cel (https://web.archive.org/web/20231231183005/https://stackoverflow.com/questions/59098171/how-to-insert-python-variable-into-latex-matrix-in-jupyter-notebook-markdown-cel)

https://www.physicsread.com/latex-column-vector-and-column-matrix/ (https://www.physicsread.com/latex-column-vector-and-column-matrix/) https://web.archive.org/web/20231231183214/https://www.physicsread.com/latex-column-vector-and-column-matrix/ (https://web.archive.org/web/20231231183214/https://www.physicsread.com/latex-column-vector-and-column-matrix/)

https://tex.stackexchange.com/a/367971/188930 (https://tex.stackexchange.com/a/367971/188930)
https://web.archive.org/web/20231231183433/https://tex.stackexchange.com/questions/367960/creating-a-matrix-with-column-or-row-vectors-as-arguments (https://web.archive.org/web/20231231183433/https://tex.stackexchange.com/questions/367960/creating-a-matrix-with-column-or-row-vectors-as-arguments)

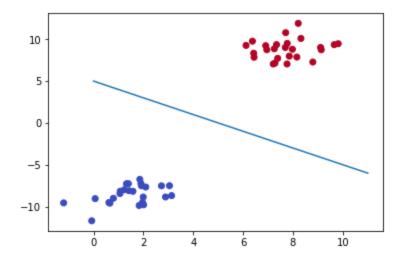
Course Notes Version

```
In [103]: # Not now - Q&R
# # Okay, maybe now. Only need date once => comment out
# !powershell -c (Get-Date -UFormat "%s_%Y%m%dT%H%M%S%Z00") -replace '[.][0-9]*_', '_'
```

Output: 1704285338 20240103T123538-0700

```
In [104]: # > DRAW A LINE THAT SEPARATES CLASSES
    x_line_CNV = np.linspace(0, 11, 10)
    y_line_CNV = -x_line_CNV + 5
    plt.scatter(features_CNV[:, 0], features_CNV[:, 1], c=labels_CNV, cmap='coolwarm')
    plt.plot(x_line_CNV, y_line_CNV)
```

Out[104]: [<matplotlib.lines.Line2D at 0x20d45f758d0>]



Defining the Perceptron

$$y=mx+b \ y=-x+5 \ f_2=m\,f_1+b\ ,\ m=1 \ f_2=-f_1+5 \ f_1+f_2-5=0$$

Jose uses $f_{whatever}$ for a feauture

Convert to a Matrix Representation of Features

Dave/Lecture Version

TL/DR

 $\$ \begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \overleftarrow{\overrightarrow{ f }} - 5 = 0 \$\$

$$\begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \overset{\longrightarrow}{f} - 5 = 0$$

Verbosity Turned Up

For our matrix, continuing the *Defining the Perceptron* cell, we're basically looking at

FeatMatrix[1, 1] - 5 = 0

or, more nicely than Jose's

(1,1) * f - 5 = 0

we can use

\$\$ \begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \textbf{f} - 5 = 0 \$\$

which gives us

$$[1 \ 1] \cdot \mathbf{f} - 5 = 0$$

or, even better,

 $\$ \begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \overset{\rightharpoonup} {\overset{\leftharpoondown f} - 5 = 0 \$\$

$$egin{bmatrix} egin{bmatrix} 1 & 1 \end{bmatrix} \cdot \stackrel{
ightharpoondown}{\overleftarrow{f}} - 5 = 0 \end{bmatrix}$$

where

Matrix Notes

The matrix, $\$ \overset{\rightharpoonup} {\overset{\leftharpoondown} f} $\$ is defined as

 $\$ \overline{\overline{ f }} \; \cdot\overline{ Delta} = \; \; \begin{bmatrix} f_1 \\ f_2 \end{bmatrix} \$\$

$$egin{array}{c} \overline{\widetilde{f}} & \stackrel{\Delta}{=} & \left[egin{array}{c} f_1 \ f_2 \end{array}
ight] \end{array}$$

My favorite matrix notation is

 $\ \$ \overset{\rightharpoonup} {\overset{\leftharpoondown} f} \$\$ \$\$ f

though I think a nice second is the one I just thought to try:

\$\$ \overset{=} f **\$\$**

 \bar{f}

and third place going to the standard textbook form,

\$\$ \textbf{f} \$\$

 \mathbf{f}

Course Notes Version

(after Defining the Perceptron)

Convert to a Matrix Representation of features

$$w^T x + b = 0$$

As Jose had it

$$\beta$$
 \Big(1, 1\Big) f - 5 = 0 \$\$

$$\Big(1,1\Big)f-5=0$$

My preference is

 $\$ \begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \overset{\rightharpoonup} {\overset{\leftharpoondown} f} - 5 = 0 \$\$ $\stackrel{\sim}{=}$

$$\begin{bmatrix} 1 & 1 \end{bmatrix} \cdot \overline{\overset{
ightharpoonup}{f}} - 5 = 0$$

Then if the result is > 0 its[sic] it's label [=] 1, if it is less than 0, it is label=0

Example Point

Lecture version

Picking one that will quite obviously be in the red-dot side. We should get a positive number, since it's over the line. Jose went with (8,10)

```
In [105]: np.array([1, 1]).dot(np.array([[8], [10]])) - 5
Out[105]: array([13])
```

It's very positive, so it's in the red class.

Now for one in the blue points, which will give us a negative number. Jose went with (2, -10).

```
In [106]: np.array([1, 1]).dot(np.array([[2],[-10]]))
Out[106]: array([-8])
```

That's negative, so it's in the blue class (the class under the line).

Course Notes Version, with Dave making things look nicer

Let's say we have the point, f1=2, f2=2 ($Ithink Joseme ant toput f_1 = 8$, $f_2 = 10$), otherwise states as (8, 10) \$. Then we have

<Jose has>

```
$$
\begin{pmatrix}
1 , 1
\end{pmatrix}
\begin{pmatrix}
8 \\
10
\end{pmatrix} + 5 = $$
```

$$(1,1)\left(rac{8}{10}
ight)+5=$$

Let's give him a parentheses matrix (pmatrix) instead of our previously used (square) bracket matrix (bmatrix), and see if we can make things look nicer (as well as completing the RHS of the equation).

$$\$$
 \begin{pmatrix} 1 & 1 \end{pmatrix} \begin{pmatrix} 8 \\ 10 \end{pmatrix} + 5 = 0 \$\$
$$(1 - 1) \left(\frac{8}{10} \right) + 5 = 0$$

It's in the 0 class, below the line, but the algorithm isn't as sure.

Using an Example Session Graph

Lecture Version

```
In [110]: g_perc = Graph() # I use "perc" for "perceptron"
In [111]: g_perc.set_as_default()
In [112]: x_perc = Placeholder()
```

```
In [113]: w_perc = Variable([1, 1]) # Weights
In [114]: b_perc = Variable(-5)
```

```
In [115]: # Due to these problems, I was going to put in the course notes version,
## but it's working.

## Seems my version has a problem with combining the operations
##+ Nope, it was a non-list in the Sigmoid.
##+ I got the same decimal value as Jose with this one
z_perc = Add(MatMul(w_perc, x_perc), b_perc) # Combining two operations!

### This one worked, but gave me 1.0 rather than a -.999and-so-on
# y_perc = MatMul(x_perc, x_perc)
# z_perc = Add(y_perc, b_perc)
```

```
Initializing a MatMul operation
In __init__
       self.input_nodes =
Now.
    [<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>]
Current node is:
     node = <__main__.Variable object at 0x0000020D46124710>
After assignment, node.output_nodes.append(self)
    node = <__main__.Variable object at 0x0000020D46124710>
 Current node is:
    node = <__main__.Placeholder object at 0x0000020D46162860>
After assignment, node.output_nodes.append(self)
    node = <__main__.Placeholder object at 0x0000020D46162860>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D46162048>
After appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D46162048>
```

```
Initializing an Add operation
In __init__
Now, self.input_nodes =
    [<__main___.MatMul object at 0x0000020D46118F28>, <__main___.Variable object at 0x0000020D46118A90>]
Current node is:
    node = <__main__.MatMul object at 0x0000020D46118F28>
After assignment, node.output_nodes.append(self)
    node = <__main__.MatMul object at 0x0000020D46118F28>
Current node is:
    node = <__main__.Variable object at 0x0000020D46118A90>
After assignment, node.output_nodes.append(self)
    node = <__main__.Variable object at 0x0000020D46118A90>
Before appending self to _default_graph,
    _default_graph =
              <__main__.Graph object at 0x0000020D46162048>
After appending self to _default_graph,
    _default_graph =
```

<__main__.Graph object at 0x0000020D46162048>

```
In [116]: | a_perc = Sigmoid(z_perc)
          In __init__
           Now, self.input_nodes =
               [<__main__.Add object at 0x0000020D46118BA8>]
           Current node is:
               node = <__main__.Add object at 0x0000020D46118BA8>
           After assignment, node.output_nodes.append(self)
               node = <__main__.Add object at 0x0000020D46118BA8>
           Before appending self to _default_graph,
               _default_graph =
                         <__main__.Graph object at 0x0000020D46162048>
           After appending self to _default_graph,
               _default_graph =
                         <__main__.Graph object at 0x0000020D46162048>
```

First session, with the obvious red (above the line, positive).

```
In [117]: sess_perc = Session()
```

In [118]: sess_perc.run(operation=a_perc, feed_dict={x_perc:[8, 10]})

```
!!! Running the Session !!!
Calling recurse(operation)
    with operation =
<__main__.Sigmoid object at 0x0000020D46118438>
Inside recurse(node)
     node = <__main__.Sigmoid object at 0x0000020D46118438>
node, <__main__.Sigmoid object at 0x0000020D46118438>
is an Operation
Current input_node =
<__main__.Add object at 0x0000020D46118BA8>
Inside recurse(node)
     node = <__main__.Add object at 0x0000020D46118BA8>
node, <__main__.Add object at 0x0000020D46118BA8>
is an Operation
 Current input_node =
<__main__.MatMul object at 0x0000020D46118F28>
Inside recurse(node)
```

```
node, <__main__.MatMul object at 0x0000020D46118F28>
is an Operation
Current input_node =
<__main__.Variable object at 0x0000020D46124710>
Inside recurse(node)
    node = <__main__.Variable object at 0x0000020D46124710>
Current input_node =
<_main_.Placeholder object at 0x0000020D46162860>
_____
Inside recurse(node)
    node = <__main__.Placeholder object at 0x0000020D46162860>
Current input_node =
<_main__.Variable object at 0x0000020D46118A90>
Inside recurse(node)
```

node = <__main__.Variable object at 0x0000020D46118A90>

node = <__main__.MatMul object at 0x0000020D46118F28>

Exited the recursion

```
We now have nodes postorder =
[< main .Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
 After running
   nodes postorder = traverse postorder(operation)
 we have
 nodes postorder =
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
 We have a Variable and will
 assign node.value to node.output
 ( which which means the value,
 node.value = [1, 1]
 will be assigned.
 Checking, node.output = [1, 1]
 We have a Placeholder and will
 assign feed_dict[node] to node.output
 ( which which means the value,
 feed dict[node] = [8, 10]
 will be assigned.
 Checking, node.output = [8, 10]
 We have an Operation and will
 compute the output of the operation
 based on each input node's output,
 for each node's input nodes
 We will assign the result of the
 computation to node.output
```

```
Some pertinent parts:
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs
We will now assign the value of
node.output
We will use
node.inputs = [array([1, 1]), array([ 8, 10])]
Now, computing the MatMul operation
Now, self.inputs =
    [array([1, 1]), array([ 8, 10])]
We will return
    result_of_matmul = 18
Inspecting, node.output = 18
We have a Variable and will
assign node.value to node.output
( which which means the value,
node.value = -5
will be assigned.
Checking, node.output = -5
We have an Operation and will
compute the output of the operation
based on each input_node's output,
for each node's input_nodes
We will assign the result of the
```

computation to node.output Some pertinent parts: [< main .MatMul object at 0x0000020D46118F28>, < main .Variable object at 0x0000020D46118A90>] I'm not going to mess around finding the output of each input_node here, since it will become the node.inputs We will now assign the value of node.output

Now, computing the Add operation

Now, self.inputs = [18, -5]

node.inputs = [18, -5]

We will use

We will return result_of_add = 13

Inspecting, node.output = 13

We have an Operation and will compute the output of the operation based on each input_node's output, for each node's input_nodes We will assign the result of the computation to node.output

Some pertinent parts: [< main .Add object at 0x0000020D46118BA8>] I'm not going to mess around finding the output of each input_node here,

since it will become the node.inputs

```
We will now assign the value of
 node.output
We will use
 node.inputs = [13]
Inspecting, node.output = 0.999997739675702
 Looking at a few things, where we are getting
 errors, as shown in a cell below.
operation = < main .Sigmoid object at 0x0000020D46118438>
operation.output = 0.999997739675702
Looking at nodes_postorder =
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
Looking at nodes_postorder[0], which I hope is an Operation
    nodes postorder[0] = < main .Variable object at 0x0000020D46124710>
If we got an Operation, let's print its output
We will return the output of the operation,
  _____
output to return = operation.output = 0.999997739675702
  _____
  !!! Finished Running the Session !!!
```

Out[118]: 0.999997739675702

Second session, with the obvious blue (below the line, negative).

In [120]: sess_perc_2.run(operation=a_perc, feed_dict={x_perc:[2, -10]})

```
!!! Running the Session !!!
Calling recurse(operation)
    with operation =
<__main__.Sigmoid object at 0x0000020D46118438>
Inside recurse(node)
     node = <__main__.Sigmoid object at 0x0000020D46118438>
node, <__main__.Sigmoid object at 0x0000020D46118438>
is an Operation
Current input_node =
<__main__.Add object at 0x0000020D46118BA8>
Inside recurse(node)
     node = <__main__.Add object at 0x0000020D46118BA8>
node, <__main__.Add object at 0x0000020D46118BA8>
is an Operation
 Current input_node =
<__main__.MatMul object at 0x0000020D46118F28>
Inside recurse(node)
```

```
node = <__main__.MatMul object at 0x0000020D46118F28>
node, <__main__.MatMul object at 0x0000020D46118F28>
is an Operation
Current input_node =
<__main__.Variable object at 0x0000020D46124710>
Inside recurse(node)
    node = <__main__.Variable object at 0x0000020D46124710>
Current input_node =
<_main_.Placeholder object at 0x0000020D46162860>
_____
Inside recurse(node)
    node = <__main__.Placeholder object at 0x0000020D46162860>
Current input_node =
<_main__.Variable object at 0x0000020D46118A90>
Inside recurse(node)
```

node = <__main__.Variable object at 0x0000020D46118A90>

Exited the recursion

```
We now have nodes postorder =
[< main .Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
 After running
   nodes postorder = traverse postorder(operation)
 we have
 nodes postorder =
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
 We have a Variable and will
 assign node.value to node.output
 ( which which means the value,
 node.value = [1, 1]
 will be assigned.
 Checking, node.output = [1, 1]
 We have a Placeholder and will
 assign feed_dict[node] to node.output
 ( which which means the value,
 feed dict[node] = [2, -10]
 will be assigned.
 Checking, node.output = [2, -10]
 We have an Operation and will
 compute the output of the operation
 based on each input node's output,
 for each node's input nodes
 We will assign the result of the
 computation to node.output
```

```
Some pertinent parts:
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs
We will now assign the value of
node.output
We will use
node.inputs = [array([1, 1]), array([ 2, -10])]
Now, computing the MatMul operation
Now, self.inputs =
    [array([1, 1]), array([ 2, -10])]
We will return
    result_of_matmul = -8
Inspecting, node.output = -8
We have a Variable and will
assign node.value to node.output
( which which means the value,
node.value = -5
will be assigned.
Checking, node.output = -5
We have an Operation and will
compute the output of the operation
based on each input_node's output,
for each node's input_nodes
We will assign the result of the
```

computation to node.output

Some pertinent parts:

[<__main__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs

We will now assign the value of node.output
We will use
node.inputs = [-8, -5]

Now, computing the Add operation

Now, self.inputs = [-8, -5]

We will return result_of_add = -13

Inspecting, node.output = -13

We have an Operation and will compute the output of the operation based on each input_node's output, for each node's input_nodes
We will assign the result of the computation to node.output

Some pertinent parts:

[<__main__.Add object at 0x0000020D46118BA8>]
I'm not going to mess around finding
the output of each input_node here,
since it will become the node.inputs

```
We will now assign the value of
 node.output
We will use
 node.inputs = [-13]
Inspecting, node.output = 2.2603242979035746e-06
 Looking at a few things, where we are getting
 errors, as shown in a cell below.
operation = < main .Sigmoid object at 0x0000020D46118438>
operation.output = 2.2603242979035746e-06
Looking at nodes_postorder =
[<__main__.Variable object at 0x0000020D46124710>, <__main__.Placeholder object at 0x0000020D46162860>, <__ma</pre>
in__.MatMul object at 0x0000020D46118F28>, <__main__.Variable object at 0x0000020D46118A90>, <__main__.Add ob
ject at 0x0000020D46118BA8>, < main .Sigmoid object at 0x0000020D46118438>]
Looking at nodes_postorder[0], which I hope is an Operation
    nodes postorder[0] = < main .Variable object at 0x0000020D46124710>
If we got an Operation, let's print its output
We will return the output of the operation,
  _____
output to return = operation.output = 2.2603242979035746e-06
  _____
   !!! Finished Running the Session !!!
```

Out[120]: 2.2603242979035746e-06

Course Notes Verison

```
In [121]:
          # Maybe Later
          # Doing it like the other ones
In [122]:
          g_perc_CNV = GraphCNV()
In [123]:
          g_perc_CNV.set_as_default()
In [124]:
          x_perc_CNV = PlaceholderCNV()
In [125]:
          w_perc_CNV = VariableCNV([1, 1])
          b_perc_CNV = VariableCNV(-5)
In [126]:
In [127]:
          z_perc_CNV = addCNV(matmulCNV(w_perc_CNV, x_perc_CNV), b_perc_CNV)
          a_perc_CNV = sigmoidCNV(z_perc_CNV)
In [128]:
In [129]: sess_perc_CNV = SessionCNV()
In [130]: sess_perc_CNV.run(operation=a_perc_CNV, feed_dict={x_perc_CNV:[8, 10]})
Out[130]: 0.999997739675702
          sess_perc_CNV.run(operation=a_perc_CNV, feed_dict={x_perc_CNV:[0, -10]})
In [131]:
Out[131]: 3.059022269256247e-07
```

That's all for now, folks!