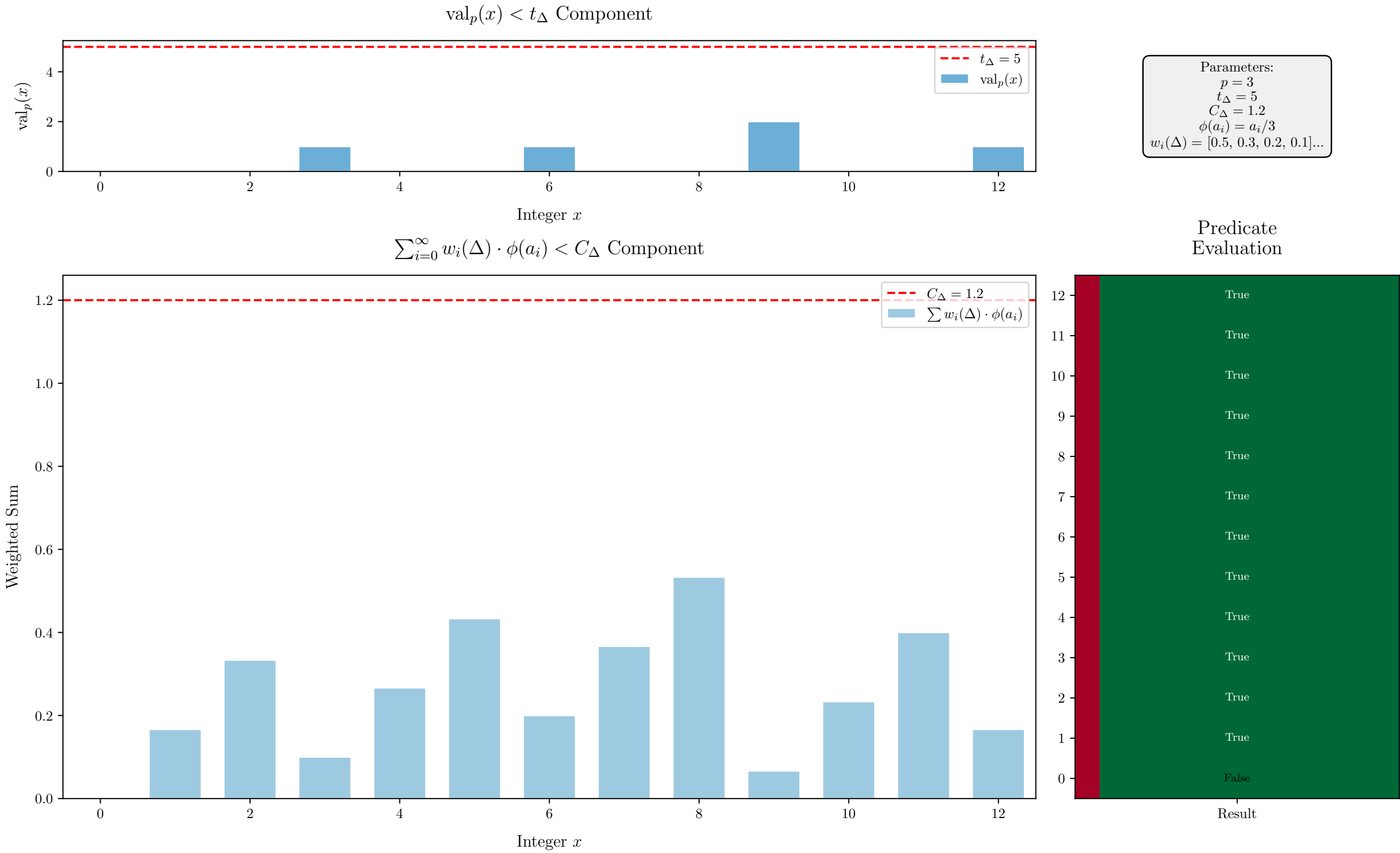


$$\mathcal{P}_\Delta(\text{bin}_p(x)) = (\text{val}_p(x) < t_\Delta) \wedge (\sum_{i=0}^\infty w_i(\Delta) \cdot \phi(a_i) < C_\Delta)$$



Parameters:

$p = 3$
 $t_\Delta = 5$
 $C_\Delta = 1.2$
 $\phi(a_i) = a_i/3$
 $w_i(\Delta) = [0.5, 0.3, 0.2, 0.1] \dots$

Figure: Visualization of the predicate evaluation for test ideal membership. The top panel shows the p -adic valuation compared to $t_\Delta = 5$. The bottom left panel shows the weighted sum of the transformed digits compared to $C_\Delta = 1.2$. The right panel shows the final evaluation result.