

# **MPCs, MPEs and Multipliers: A Trilemma for New Keynesian Models**

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Adrien Auclert   Bence Bardóczy   Matthew Rognlie

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## What do micro data tell us about macro models?

- New Keynesian (NK) models can match macro moments very well.
  - comovement of time series, impulse responses to identified shocks...
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  - comovement of time series, impulse responses to identified shocks...
- We need **more data** to choose from competing models and to make further progress!
- **This paper:** use a mix of **micro** and **macro** moments to
  1. reject canonical NK with sticky prices and flexible wages
  2. argue for NK with **sticky wages** & **household heterogeneity**

# Three Facts to judge business cycle models

► Where do our Facts come from?

- **Micro**: How do individuals respond to a one-time increase in income?
  - consume more: marginal propensity to consume, **MPC**
  - work less: marginal propensity to earn, **MPE**
  - save more:  $1 - \text{MPC} - \text{MPE}$
- **Macro**: How does GDP respond to an increase in government spending?
  - **cumulative fiscal multiplier**:  $\text{PDV}(dY)/\text{PDV}(dG)$

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## Facts

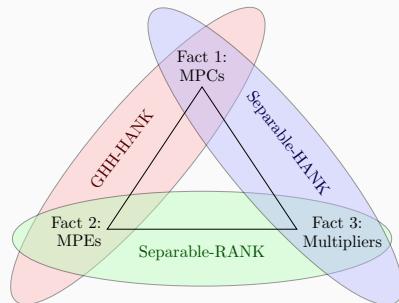
**Fact 1:** Average MPCs are high, around 0.25 quarterly or 0.5 annually.

**Fact 2:** Average MPEs are low, between 0 and 0.04 annually.

**Fact 3:** Fiscal multipliers are moderate, between 0.6 and 2 when monetary policy is accommodative.

# The trilemma and its solution

- New Keynesian models with **frictionless labor market fail** to match at least one of the Facts.
  - separable-RANK: Galí (2015)
  - separable-HANK: Kaplan, Moll and Violante (2018)
  - GHH-HANK: Bayer, Lütticke, Pham-Dao and Tjaden (2019)

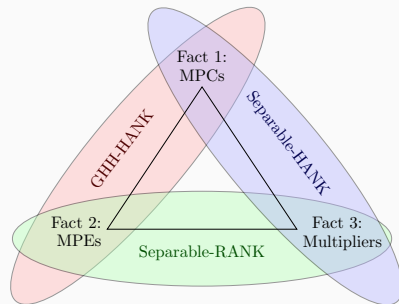


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HANK: heterogeneous agent

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- **One solution:** HANK models with
  - sticky wages and demand-determined labor
  - weak consumption-labor complementarity
  - calibrated to match high MPCs



RANK: representative agent  
HANK: heterogeneous agent

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2. **RANK analytics:** high CI dramatically increases multipliers.
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## The MPC-MPE relationship

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# Standard household model with frictionless labor supply

- Households are indexed by their skill  $e$  and assets  $a$ .
- Skills evolve according to Markov chain  $\Pi(e'|e)$ .

$$V_t(e, a) = \max_{c, n, a'} U(c, n) + \beta \mathbb{E}_t[V_{t+1}(e', a')]$$

$$\text{s.t. } c + a' = (1 + r_t)a + w_t(e)n + T_t$$

$$a' \geq \underline{a}$$

- Nests rep agent model for  $e \equiv 1$  and  $\underline{a} = -\infty$ .

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- Formally, Fact 1 and Fact 2 are about the **population averages** of

$$\text{MPC} = \frac{\partial c_t(e, a; T_t)}{\partial T_t} \qquad \text{MPE} = -w \frac{\partial n_t(e, a; T_t)}{\partial T_t}$$

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- Nests rep agent model for  $e \equiv 1$  and  $\underline{a} = -\infty$ .
- $U(c, n)$ : strictly concave, twice cont differentiable, satisfies Inada conditions.
- All agents are on their **FOC for labor supply** (even the borrowing constrained):

$$-U_n(c, n) = w \cdot U_c(c, n) \tag{1}$$

**Proposition 1 (MPC-MPE relationship)**

Let's define **consumption-labor complementarity index** as

$$CI \equiv \frac{\partial c(\lambda, w)}{\partial w} \bigg/ w \frac{\partial n(\lambda, w)}{\partial w}.$$

Optimality of labor supply implies that for every individual and every period,

$$\boxed{\frac{MPE}{MPC} = \frac{wn}{c} \cdot \frac{\text{Frisch}}{\text{EIS}} \cdot (1 - CI) .}$$

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- **Takeaway:** matching Fact 1 & Fact 2 requires **high CI**.



1. **Consumer theory:** high MPC + low MPE requires high consumption-labor complementarity (CI).
2. **RANK analytics:** high CI dramatically increases multipliers.
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# **Complementarity and multipliers**

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## Embed rep-agent household in a New Keynesian model

- Household (Euler eq + labor supply):

$$U_c(C_t, N_t) = \beta(1 + r_t^e)U_c(C_{t+1}, N_{t+1}), \quad (1 - \tau^w)w_t = -\frac{U_n(C_t, N_t)}{U_c(C_t, N_t)}$$

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- Firms (production fun + Phillips curve):

$$Y_t = f(N_t), \quad \log(1 + \pi_t) = \kappa \left( \frac{w_t}{f'(N_t)} - \frac{\epsilon - 1}{\epsilon} \right) + \frac{1}{1 + r_t^e} \frac{Y_{t+1}}{Y_t} \log(1 + \pi_{t+1})$$

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- Monetary policy sets  $r_t$ , fiscal policy adjusts  $T_t$  to balance budget.

## Micro meets macro: Fact 1, 2 vs Fact 3

### Proposition 2 (Fiscal multipliers in RANK)

Let  $\tau$  denote the **steady-state labor wedge**:

$$\tau \equiv 1 + \frac{U_n(C_t, N_t)}{U_c(C_t, N_t)} \frac{1}{f'(N_t)} = 1 - (1 - \tau^w) \frac{\epsilon - 1}{\epsilon}$$

The marginal effect of a government spending shock on output in a canonical RANK model with constant real interest rate is

$$\frac{dY_t}{dG_s} = \frac{1}{1 - (1 - \tau) CI} \cdot \mathbf{1}_{s=t}$$

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- **Takeaway:** matching Fact 3 requires **low CI**.

## Proof sketch for intuition

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- **Round 2:** aggregate demand increases by  $dY = CI(1 - \tau)dG$ .
- Multiplier process converges to

$$dY = [1 + CI(1 - \tau) + CI^2(1 - \tau)^2 + \dots] dG = \frac{dG}{1 - (1 - \tau) CI}$$

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# Trilemma in HANK models

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## The goal of this section

- HANK models are famed for delivering Fact 1 (high MPC).
- Assess trade-off between Fact 2 (low MPE  $\sim$  high CI) and Fact 3 (moderate multiplier  $\sim$  low CI) conditional on matching Fact 1.
- **Preview:** no  $CI \in [0, 1]$  can solve the trilemma.

## Embed heterogeneous households in the same New Keynesian model

- Households trade in one-period real gov't bonds and firm equity.
- Certainty equivalence wrt aggregate shocks  $\implies$  as if single asset.
- Progressive labor income tax achieves realistically high labor wedge ( $\tau = 0.43$ ).
- Gov't adjusts labor income tax to pay for its spending.

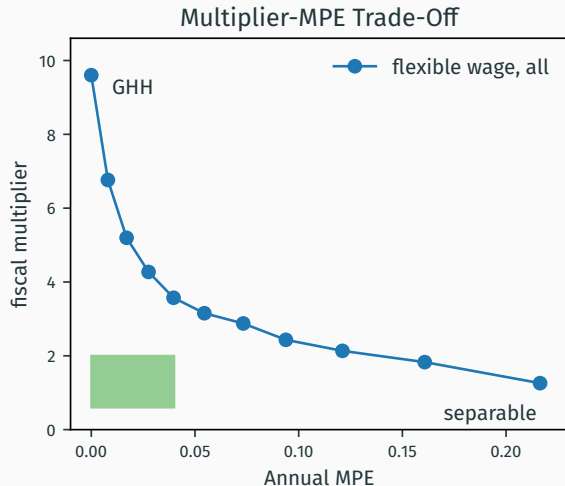
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- Gov't adjusts labor income tax to pay for its spending.
- **GHH-plus preferences** allow for any  $CI \in [0, 1]$  as a function of  $\alpha \in [0, 1]$  :

$$U(c, n) = \frac{1}{1-\sigma} \left( c - \varphi \alpha \frac{n^{1+\nu}}{1+\nu} \right)^{1-\sigma} - \varphi (1-\alpha) \frac{n^{1+\nu}}{1+\nu}$$

$\alpha = 0$  = CI is separable preferences;

$\alpha = 1$  = CI is GHH preferences.



■ is the target for Fact 2 and Fact 3.

● are equilibria for full range  $CI \in [0, 1]$ .  
Calibration holds “everything else” constant.

**Trilemma:** It takes high CI to match Fact 2 and low CI to match Fact 3.

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## **Sticky-wage HANK**

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- Frictionless hours choice at the household level  $\implies$  tight connection between income effects on consumption and labor supply.
- Data call for high income effect on consumption and low on labor supply.
- Optimal response only if consumption-labor complementarity is high.
- High complementarity leads to large demand multiplier in NK.

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- **Break MPC-MPE formula  $\implies$  freedom to choose low CI.**

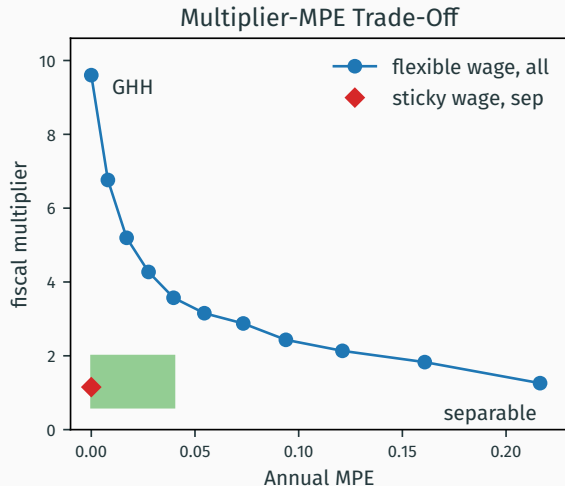


- Households supply differentiated labor services  $n_{ikt}$  to unions  $k \in [0, 1]$ .
- Union  $k$  sets wage  $w_{kt}$  to maximize household welfare subject to
  - quadratic nominal wage adjustment cost
  - labor demand from with elasticity  $\epsilon$

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- Union  $k$  sets wage  $w_{kt}$  to maximize household welfare subject to
  - quadratic nominal wage adjustment cost
  - labor demand from with elasticity  $\epsilon$
- Yields wage Phillips curve in the spirit of Erceg, Henderson and Levin (2000):

$$\log(1 + \pi_t^w) = \kappa N_t \left[ \underbrace{\int U_n(c_{it}, N_t) di}_{\text{avg disutil of labor}} - \left( \frac{\epsilon - 1}{\epsilon} \right) \underbrace{\int w_t(e_i) U_c(c_{it}, N_t) di}_{\text{avg util from higher wage}} \right] + \beta \log(1 + \pi_{t+1}^w)$$

# Eliminates trade-off between MPEs and multipliers



Unions represent all households.

Idiosyncratic shocks to household income affect neither wages nor hours.

MPE is 0 by construction.

Aggregate demand-labor feedback loop still a concern  $\Rightarrow$  use low CI (e.g separable prefs).

**Sticky-wage model solves the trilemma.**

# Conclusion

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  1. high MPCs
  2. low MPEs
  3. moderate fiscal multipliers (even when monetary policy is accommodative)
- Our novel **analytical & numerical results** show that this is because consumption-labor complementarity has to be high for Fact 2 and low for Fact 3.
- **One solution** is to use New Keynesian models with
  - well-calibrated household heterogeneity  $\implies$  Fact 1 ✓
  - sticky wages and demand-determined labor  $\implies$  Fact 2 ✓
  - weak consumption-labor complementarity  $\implies$  Fact 3 ✓

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  - well-calibrated household heterogeneity  $\implies$  Fact 1 ✓
  - **sticky wages and demand-determined labor**  $\implies$  Fact 2 ✓ **alternative: search frictions**
  - weak consumption-labor complementarity  $\implies$  Fact 3 ✓

# Takeaways for macro modelers

1. Don't just assume that **micro heterogeneity** does not matter for macro. 😊
  - solving HANK is easier than you think → <https://github.com/shade-econ/sequence-jacobian>
2. **Separable preferences** are a good choice in RANK & HANK.
  - key is low CI, GHH can get problematic very easily
  - if want higher CI: high labor wedge, aggressive monetary policy can mask trilemma
3. **Demand-determined labor** (w sticky wages) is a useful device.
  - no labor supply response to idiosyncratic shocks
  - can specify labor income risk directly

**Thank you!**



- **MPC:** 0.25 quarterly, 0.5 annually
  - Kaplan and Violante (2014): review of large literature
- **MPE:** between 0 and 0.04 annually
  - Cesarini, Lindqvist, Notowidigdo and Östling (2017): Swedish lottery (one-time, small winnings, large sample)
  - Imbens, Rubin, and Sacerdote (2001): MA lottery (20-year annuity that we adjust, small sample)
- **Fiscal multiplier:** between 0.6 and 2 with accommodative monetary policy
  - Ramey (2019): review of large literature

- $\lambda$ : marginal utility of consumption,  $w$ : effective wage
- Frisch elasticity of labor supply:

$$\text{Frisch} = \frac{\partial \log n(\lambda, w)}{\partial \log w}$$

- Elasticity of intertemporal substitution:

$$\text{EIS} = -\frac{\partial \log c(\lambda, w)}{\partial \log \lambda}$$

parameter	name	value/target
A. Fixed parameters		
$1/\nu$	Frisch elasticity	0.5
$\rho_e$	persistence of income process	0.966
$\tau^g$	income tax level	0.191
$\gamma$	income tax progressivity	0.177
$\epsilon$	elast of substitution for varieties	7
$B$	government bonds	$0.55 \cdot 4Y$
$\rho_B$	persistence of public debt	0.9
$\underline{a}$	borrowing constraint	0
B. Internally calibrated parameters		
$\beta_1$	upper discount factor	$r = 0.02/4$
$\beta_2$	lower discount factor	MPC = 0.25
$1/\sigma$	$U_c$ curvature	average EIS = 0.5
$\varphi$	disutility of labor	$N = 1$
$Z$	aggregate labor productivity	$Y = 1$
$\sigma_e$	std of income shocks	$\text{Var} [\log(n_i e_i)] = 0.92^2$
$F$	fixed cost	$p = 0.85 \cdot 4Y$

- Union  $k$  sets nominal wage  $W_{kt}$  to maximize household utility




$$J_{kt}(W_{kt-1}) = \max_{W_{kt}} \int U(c_{it}, n_{it}) di - \underbrace{\frac{\epsilon}{2\kappa} \log \left( \frac{W_{kt}}{W_{kt-1}} \right)^2}_{\text{wage adjustment cost}} + \beta \mathbb{E}_t [J_{kt+1}(w_{kt})]$$

- Subject to labor demand

$$n_{kt} = \left( \frac{W_{kt}}{W_t} \right)^{-\epsilon} N_t$$

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