



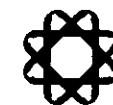
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Q.1) Quantum mechanics is the branch of physics where we studied about to tiny particle which deals with the wave mechanics.

Postulates:

- (i) It must be differential
- (ii) It must be continuous
- (iii) It must be normalized
- (iv) It must have a Singled Value
- (v) It must follow the normalized continuity condition from all space.
- (vi) It must have  $|\psi|^2$
- (vii) the state of System must be defined by  $\psi$
- (viii) The probability of finding the particle is given by  $|\psi|^2$
- (ix) The probability of finding any particle is positive so Wave function is given as  $|\psi|^2$
- (x) It must be Square Integrable.

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$$(b) |\Psi_0\rangle = \frac{1}{\sqrt{2}} |\phi_1\rangle + \frac{i}{2} |\phi_2\rangle + \frac{1}{2} |\phi_3\rangle \quad \dots \text{ (Given)}$$

$$|\Psi\rangle = \frac{1}{\sqrt{3}} |\phi_1\rangle + \frac{i}{\sqrt{3}} |\phi_3\rangle \quad \dots \text{ (Given)}$$

Soln:

$$|\Psi_0\rangle = \frac{1}{\sqrt{2}} |\phi_1\rangle + \frac{i}{2} |\phi_2\rangle + \frac{1}{2} |\phi_3\rangle \quad \dots \text{ (1)}$$

$$\langle \Psi_0 | = \frac{1}{\sqrt{2}} \langle \phi_1 | + -\frac{i}{2} \langle \phi_2 | + \frac{1}{2} \langle \phi_3 | \quad \dots \text{ (1)}$$

$$\text{for normalise } \langle \Psi_0 | \Psi_0 \rangle = 1$$

$$\therefore \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}} - \frac{i}{2} \times \frac{i}{2} + \frac{1}{2} \times \frac{1}{2}$$

$$= \frac{1}{2} + \frac{1}{4} + \frac{1}{4}$$

$$= \frac{1}{2} + \frac{2}{4} \quad \checkmark \quad Q1 \Rightarrow 0$$

$$= \frac{1}{2} + \frac{1}{2}$$

$$= 1$$

Hence  $|\Psi_0\rangle$  is normalised

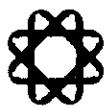
Now,

$$|\Psi_1\rangle = \frac{1}{\sqrt{3}} |\phi_1\rangle + \frac{i}{\sqrt{3}} |\phi_3\rangle \quad \dots \text{ (From Given)} \quad \text{--- (1)}$$

$$\langle \Psi_1 | = \frac{1}{\sqrt{3}} \langle \phi_1 | + -\frac{i}{\sqrt{3}} \langle \phi_3 | \quad \dots \text{ (1)}$$

$\therefore$  Now: for normalised condition

$$\langle \Psi_1 | \Psi_1 \rangle = 1$$



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$$\therefore \frac{1}{\sqrt{3}} \times \frac{1}{\sqrt{3}} - \frac{i}{\sqrt{3}} \times \frac{i}{\sqrt{3}}$$

$$\therefore \frac{1}{3} + \frac{1}{3}$$

$$\therefore \frac{2}{3} \neq 1$$

$\therefore |\Psi_1\rangle$  is not normalised

$$\text{Hence; } \langle \Psi_0 | = \frac{1}{\sqrt{2}} |\Psi_1\rangle + -\frac{i}{2} |\Psi_2\rangle \text{ and ... (from m 1)}$$

$$|\Psi_1\rangle = \frac{1}{\sqrt{3}} (\Psi_1) + \frac{i}{\sqrt{3}} (\Psi_2) \quad \dots \quad (\text{from given})$$

$$\begin{aligned} \therefore \langle \Psi_0 | \Psi_1 \rangle &= \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{3}} - \frac{i}{2} \times \frac{i}{\sqrt{3}} \checkmark \\ &= \frac{1}{\sqrt{6}} - \frac{i}{2} + \frac{i}{2\sqrt{3}} \end{aligned}$$

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$$= \frac{1}{\sqrt{6}} - i \left( \frac{1}{2} - \frac{1}{2\sqrt{3}} \right)$$

$$\boxed{\langle \Psi_0 | \Psi_1 \rangle = \frac{1}{\sqrt{6}} - i \left( \frac{\sqrt{3}-1}{2\sqrt{3}} \right)}$$

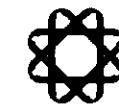
and

$$\langle \Psi_1 | = \frac{1}{\sqrt{3}} |\Psi_1\rangle - \frac{i}{\sqrt{3}} |\Psi_2\rangle \quad |\Psi_0\rangle = \frac{1}{\sqrt{2}} |\Psi_1\rangle + \frac{i}{2} |\Psi_2\rangle + \frac{1}{2} |\Psi_3\rangle$$

$$\therefore \langle \Psi_1 | \Psi_0 \rangle = \frac{1}{\sqrt{6}} + \frac{i}{2} - \frac{i}{2\sqrt{3}}$$

$$= \frac{1}{\sqrt{6}} + i \left( \frac{1}{2} - \frac{1}{2\sqrt{3}} \right)$$

$$\boxed{\langle \Psi_1 | \Psi_0 \rangle = \frac{1}{\sqrt{6}} + i \left( \frac{\sqrt{3}-1}{2\sqrt{3}} \right)}$$



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(3)  $V(x) = \infty \quad x < 0 \quad \text{and} \quad x > a$   
 $= -V_0 \quad 0 < x < \frac{a}{2}$

Solution:-

$$\text{Here } \psi_n(x) = \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right)$$

Now 1st order correction is given as

$$E_n^{(1)} = \langle \psi_n^{(0)} | H' | \psi_n^{(0)} \rangle$$

$$E_n^{(1)} = \int_{-\infty}^{\infty} \psi_n^{(0)*} H' \psi_n^{(0)} dx$$

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$$= \int_0^a \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right) \times (-V_0) \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right) dx$$

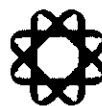
$$= \frac{2}{a} (-V_0) \int_0^a \sin^2\left(\frac{n\pi x}{a}\right) dx$$

$$= \frac{2}{a} (-V_0) \int_0^a 1 - \cos\left(\frac{2n\pi x}{a}\right) dx$$

$$= -\frac{V_0}{a} \int_0^a 1 - \cos\left(\frac{2n\pi x}{a}\right) dx$$

$$= -\frac{V_0}{a} \left[ \int_0^a 1 dx - \int_0^a \cos\left(\frac{2n\pi x}{a}\right) dx \right]$$

$$= -\frac{V_0}{a} \left[ [x]_0^a - \left[ \frac{\sin\left(\frac{2n\pi x}{a}\right) \times a}{2n\pi} \right]_0^a \right]$$



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$$\therefore -\frac{v_0}{a} \left[ 2 \right]_0 - \left[ \sin \left( \frac{2n\pi a}{a} \right) \times \frac{a}{2nm} - \sin(0) \times \frac{a}{2nm} \right]$$

$$\therefore -\frac{v_0}{a} [a - 0] = 0$$

$$= -\frac{v_0}{a} (a)$$

$$= -v_0$$

$$\therefore \boxed{E_n^{(1)} = -v_0}$$



Q4 -&gt; 0

(c)  $E_0 + \epsilon$ 

$$H_0 = \begin{bmatrix} E_0 + \epsilon & 0 \\ 0 & E_0 - \epsilon \end{bmatrix} \quad \text{and} \quad H' = \begin{bmatrix} 0 & A \\ A & 0 \end{bmatrix}$$

Soln:

$$\text{have } |H' - E^{\infty} I| = 0$$

$$\therefore \left| \begin{bmatrix} 0 & A \\ A & 0 \end{bmatrix} - E^{\infty} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \right| = 0$$

$$\therefore \left| \begin{bmatrix} 0 & A \\ A & 0 \end{bmatrix} - \begin{bmatrix} E_n^{(1)} & 0 \\ 0 & E_n^{(1)} \end{bmatrix} \right| = 0$$

for 2nd Order

$$\therefore \left| \begin{bmatrix} -E_n^{(1)} & A \\ A & -E_n^{(1)} \end{bmatrix} \right| = 0$$

$$E_n^{(2)} = \frac{2 \psi_{n+1} (H') |H''|}{E_n^{(1)} - E_m^{(1)}}$$

$$\therefore (E_n^{(1)})^2 - A^2 = 0$$

$$\therefore (E_n^{(1)})^2 = A^2$$

$$\therefore \boxed{E_n^{(1)} = \pm A}$$

$$E_n^{(2)} = \frac{A^2}{2\lambda}$$

1st Order Correction of Energy



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(S)

- (a) It is a mathematical term used as the notation in the Quantum mechanics as the wave function such that

$$\delta(x) = \begin{cases} 0 & x \neq 0 \\ \infty & x = 0 \end{cases}$$

on changing the scale

$$\delta(x - x_0) = \begin{cases} 0 & x \neq x_0 \\ \infty & x = x_0 \end{cases}$$

Here  $\delta(x) \delta(x - x_0) = 1$ Properties

Q5. -&gt; 6

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(1)  $\int_{-\infty}^{\infty} \delta(x) \delta(x - x_0) = 1$

(2)  $\int_a^b \delta(x) \delta(x - x_0) = f(x_0)$

as  $x_0$  lies between  $a$  and  $b$

(3)  $\int_{-\infty}^a f(x) \delta(x - c) = 0$

as  $c$  does not lie in between  $a$  and  $b$

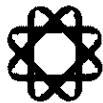
(4)  $\delta(a) = \lim_{x \rightarrow a} \delta(x)$

(5)  $\delta(-x) = \delta(x)$

(6)  $\frac{d}{dx} f(x) = f'(x)$

(7)  $x \delta(x) = 0$

(8)  $\delta(a-x) \delta(x-b) = \delta(a-b)$



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$$(v) \delta(a-b) = \delta(b-a)$$

$$(vi) \int_{-\infty}^{\infty} \delta(x) = 1$$

$$(vii) \int_{-\infty}^{\infty} f(x) \delta(x) = 1$$



Q6 -> 6

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(c) Soln:

$$\hat{x} = \left( \frac{\hbar}{2mw} \right)^{1/2} (a + a^\dagger)$$

$$\text{external perturbation } \hat{x}' = bx$$

Now,

1st order correction to the Energy of the oscillator is given as

$$E_n^{(1)} = \langle \Psi_n^{(0)} | H' | \Psi_n^{(0)} \rangle$$

$$= \langle \Psi_n^{(0)} | b \hat{x}' | \Psi_n^{(0)} \rangle_{a+a^\dagger}$$

$$= \langle \Psi_n^{(0)} | \left( \frac{\hbar}{2mw} \right)^{1/2} b | \Psi_n^{(0)} \rangle$$

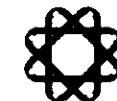
$$= \left( \frac{\hbar}{2mw} \right)^{1/2} b \langle \Psi_n^{(0)} | (a + a^\dagger) | \Psi_n^{(0)} \rangle$$

$$= \left( \frac{\hbar}{2mw} \right)^{1/2} b \langle \Psi_n^{(0)} | (a + a^\dagger) | \Psi_n^{(0)} \rangle$$

$$E_n^{(1)} = 0$$

$$\text{as } (a + a^\dagger) = 0$$

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Q2	6	5	11/29/2025, 10:03:37 AM	jwerry@gmail.com
Q3	6	6	11/29/2025, 10:03:42 AM	jwerry@gmail.com
Q4	0	7	11/29/2025, 10:03:47 AM	jwerry@gmail.com
Q5	6	8	11/29/2025, 10:03:51 AM	jwerry@gmail.com
Q6	6	9	11/29/2025, 10:03:55 AM	jwerry@gmail.com
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