

### One-loop Scalar Integral $I_S$ (series in $\epsilon$ )

$$-\frac{M_2^2}{16\pi^2\epsilon} + \frac{\gamma M_2^2}{32\pi^2} - \frac{M_2^2}{32\pi^2} - \frac{M_2^2 \log\left(\frac{4\pi\mu_2}{M_2}\right)}{32\pi^2} + O(\epsilon^2)$$

### One-loop Effective Potential $\Delta V$ (series in $\epsilon$ )

$$-\frac{M_2^2}{32\pi^2\epsilon} + \frac{\gamma M_2^2}{64\pi^2} - \frac{M_2^2}{64\pi^2} - \frac{M_2^2 \log\left(\frac{4\pi\mu_2}{M_2}\right)}{64\pi^2} + O(\epsilon^2)$$

### Double-Bubble Diagram (two-loop, series in $\epsilon$ )

$$\frac{M_2^4}{256\pi^4\epsilon^2} + \frac{M_2^4 \left(4 \log\left(\frac{4\pi\mu_2}{M_2}\right) - 4\gamma + 4\right)}{1024\pi^4\epsilon} + \frac{M_2^4 \left(\frac{\log\left(\frac{4\pi\mu_2}{M_2}\right)}{2} - \frac{\gamma}{2} + \frac{1}{2}\right)^2}{256\pi^4} + O(\epsilon^2)$$

### Sunset Diagram (two-loop, series in $\epsilon$ )

$$\epsilon \left( -\frac{M_2 \log(M_2)^2}{1024\pi^4} - \frac{\gamma M_2 \log(M_2)}{512\pi^4} + \frac{M_2 \log(M_2)}{512\pi^4} + \frac{M_2 \log(\pi) \log(M_2)}{512\pi^4} + \frac{M_2 \log(2) \log(M_2)}{256\pi^4} - \frac{M_2 \log(4)}{256\pi^4} \right)$$

### Basketball Diagram (three-loop, series in $\epsilon$ )

$$\epsilon \left( \frac{M_2^2 \log(M_2)^2}{131072\pi^6} - \frac{3M_2^2 \log(M_2)}{131072\pi^6} - \frac{M_2^2 \log(2) \log(M_2)}{32768\pi^6} - \frac{M_2^2 \log(\pi) \log(M_2)}{65536\pi^6} + \frac{\gamma M_2^2 \log(M_2)}{65536\pi^6} - \frac{3\gamma M_2^2}{131072\pi^6} \right)$$

### Beta Function Structure Summary

$$\beta(\lambda) = \cdots - c_1 \lambda^2 + c_2 \lambda^3 - c_3 \lambda^4$$