

Agenda

- Longest Substring Without Repeat
- First Non Repeating Element
- Check if there exists a subarray with sum = 0
- Check if there exists a subarray with sum = K

Q.

a b c a b c b b

abc
bca
cab
abc

}

3

b b b b b = 1

p w w k e w = 3

Brute force:

generate all substrings $O(N^2)$

$O(N^3)$

$O(N)$

Check if all characters are unique
Keep track of length of longest

substring

5 mins

4

s.....
a b c d b b c
s

expand till
repeat
happens

b ↴

a
b
c
d

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16
a b c d e a f g h i b j k l m n
_____ ↑
s

e ↑

i
f
j
c
d
e
a
g
h
b

biggest possible length - e → repeating char

e - s

$$16 - 2 = 14$$

~~start = 0~~
~~end = 0~~
~~maxLength = 0~~

str

hashset = empty set

while (end < N) {
 while (end < N && hashset. search
 (str.charAt(end)) ==
 (str.charAt(end))) {
 hashset.add(str.charAt(end));
 end++;
 }
 }
}

[mylen = end - start]

[if (mylen > maxLength) {maxLength = mylen}]

[if (end == N) break;]

remove
from start

[while (start != end &&
 hashset.search(str.charAt(end)) == true) {
 hashset.remove(str.charAt(start));
 start++;
 }]

0 1 2 3 4 5 6 7
 n a V d e e p
 ↑ s ↑ e

$$\text{mylen} = e - s = 5 \quad e - s = 2$$

$$\underline{\text{maxL}} = 5$$

e
p

0 1 2 3 4 5 6 7 8 9 10
 p i n a l j a R h a r
 ↑ s ↑ e

$$\text{mylen} = 6 - 0 = 6$$

$$\underline{\text{maxL}} = 6$$

l
j

$$\begin{array}{c} \text{I} \\ S == e \end{array}$$

$$s != e$$

II

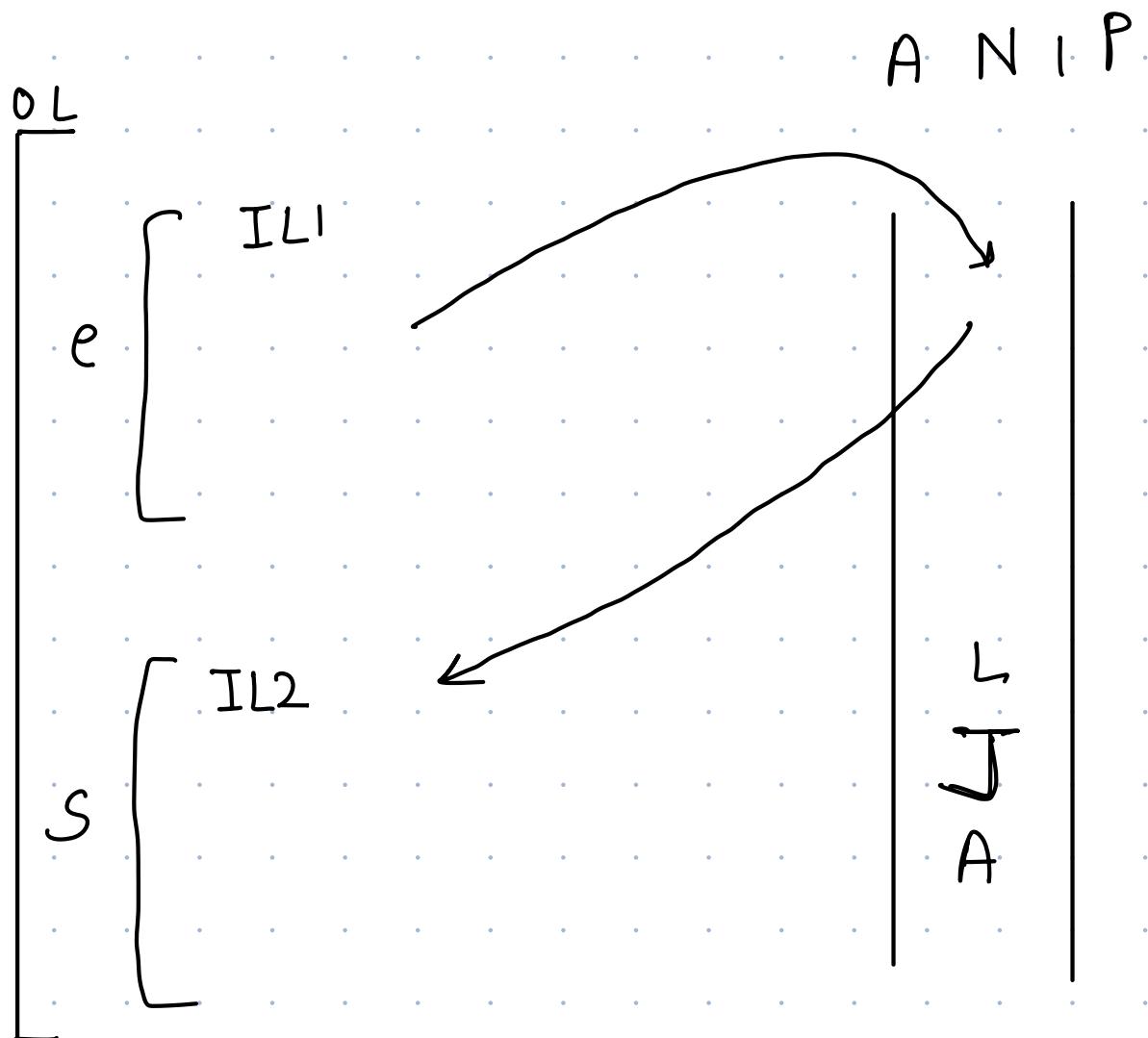
`hashset.search(a) == false`

&

`hs.search(a) == true`

[expanding
 shrinking]

 window ✓

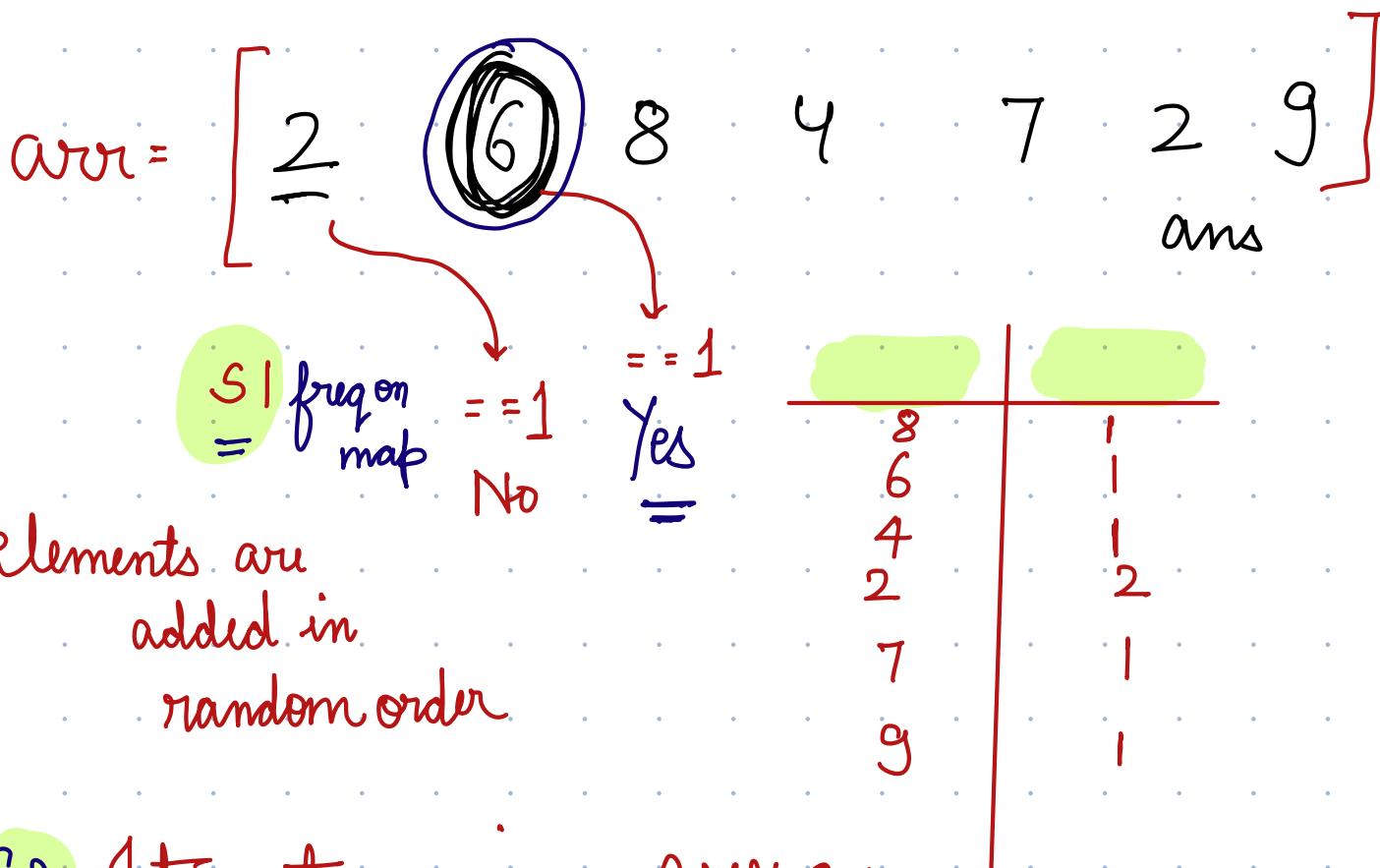


$$\text{arr}[i] = 2N = \underline{\mathcal{O}(N)}$$

Q2

$$\begin{array}{r}
 1 \\
 - \\
 2 \\
 - \\
 3
 \end{array}
 \quad
 \begin{array}{r}
 1 \\
 - \\
 2 \\
 - \\
 5
 \end{array}
 \quad
 \text{ans} = 3$$

$$\begin{array}{r}
 4 \\
 - \\
 3 \\
 - \\
 3 \\
 - \\
 2
 \end{array}
 \quad
 \begin{array}{r}
 5 \\
 - \\
 6 \\
 - \\
 4 \\
 - \\
 5
 \end{array}
 \quad
 \text{ans} = 2$$



S2: Iterate using array

on hm

\Rightarrow

$= = 1$
Yes

Problem Statement

Given an array of N elements, check if there exists a subarray with a sum equal to 0.

Example

if Subarray with sum = 0?

Input:

N = 10

2 2 1 -3 4 3 1 -2 -3 2 true

Output:

if we add elements from index 1 to 3, we get 0; therefore, the answer is **true**.

1) $\Rightarrow N = 6$

2, 2, 1, -3, 4, 3 Yes

2) $N = 6$
4 5 -6 -3 8 9 Yes

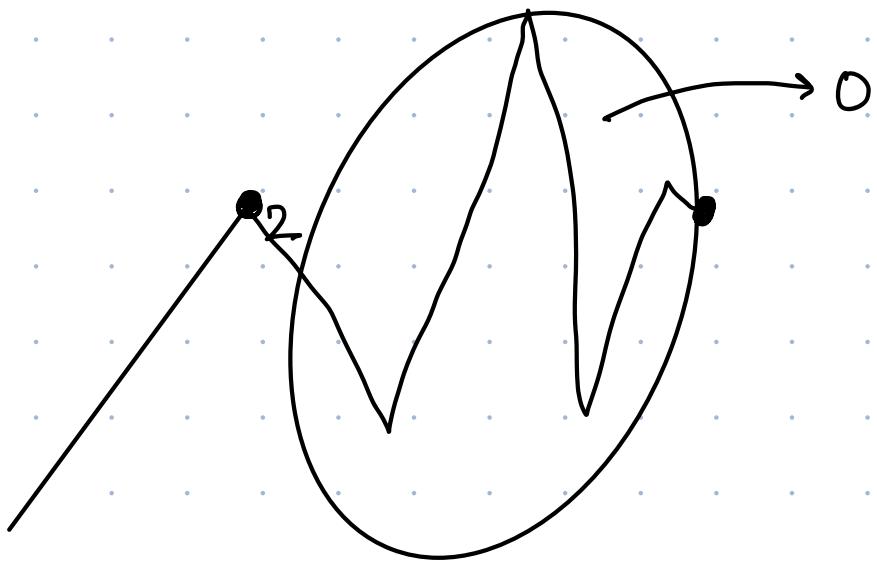
$N = 6$

2, 2, 1, -3, 4, 3
↓
2 4 5 2 6 9

$$\text{ar}[0] + \text{ar}[1] + \text{ar}[2] + \text{ar}[3] \\ = 2 + 4 + 5 + 2 = 13$$

2
0 i

$$\text{ar}[0] = 2 = \text{psum}[0]$$



$$j > i$$

$$0 - i = 0 - j$$

$$\underbrace{0 + 1 + 2 \dots i}_{= 0 + 1 + 2 \dots + \dots i + \dots j} = \underbrace{0 + 1 + 2 \dots + \dots i + \dots j}_{\text{Sum } i+1 \text{ to } j}$$

\Rightarrow if psum value repeats, yes → subarray sum = 0

$psum[0]$	$psum[1]$	$psum[2]$	$psum[3]$	$psum[4]$
0-0	0-1	0-2	0-3	0-4

$$\begin{aligned}
 psum[1] &= psum[4] \\
 \text{sum}(0+1) &\quad \text{sum}(0+1+2+3+4) \\
 &\quad \text{0}
 \end{aligned}$$

S1: find psum array

S2: keep on adding psum values
 in hashset $\xrightarrow{\text{if repetition comes}}$
 return true.

$$\Rightarrow [-1, 1]$$

$psum = -1, 0$ repetition of psum X
 directly $psum = 0$

S1: find psum array

S1.1 = check if $psum[i] = 0$ ✓
return true

S2: keep on adding psum values
in hashset → if repetition comes
✓ return true

return false .

Problem Statement

Given an array $\text{arr}[n]$ check if there exists a subarray with sum = K

Example:

We have the following array

Index 0 1 2 3 4 5 6 7 8

$\text{arr}[7] \boxed{2} \boxed{3} \boxed{9} \boxed{-4} \boxed{1} \boxed{5} \boxed{6} 2 5$

Check if
it exists

Possible subarrays for the following values of K are,

- $k = 11$: $\{2, 3, 9, -4, 1\}, \{5, 6\}$ Yes
- $k = 10$: $\{2, 3, 9, -4\}$ Yes
- $k = 15$: $\{-4, 1, 5, 6, 2, 5\} = 15$ Yes
- $k = 22$ $\boxed{2} \boxed{3} \boxed{9} \boxed{-4} \boxed{1} \boxed{5} \boxed{6}$ Yes

$$0 = \text{psum}[R]$$
$$0 = \text{psum}[R] - \text{psum}[L-1]$$

$$K = \text{psum}[R]$$
$$K = \text{psum}[R] - \text{psum}[L-1]$$

$$K = 11$$

2

3

9 -4 1 5

6

2

5

2

5

14

10

(11)

16

(22)

24

29

$$\text{pair} = 2 - K \\ = -9$$

$$5 - 11 \\ -6$$

$$14 - 11 \\ 3$$

$$10 - 11 \\ -1$$

$$11 - 11 \\ 0$$

$$16 - 11 \\ 5$$

(22)

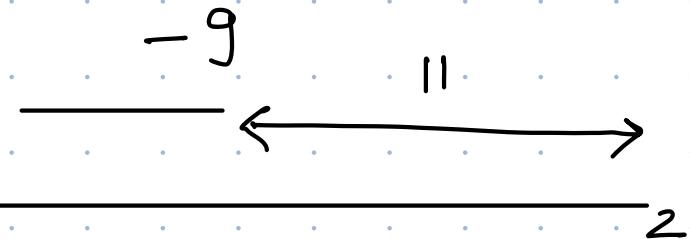
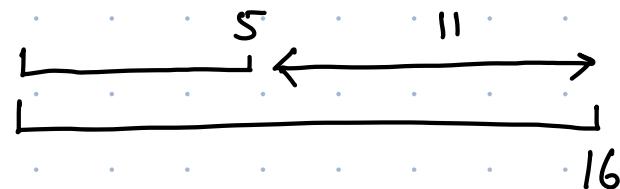
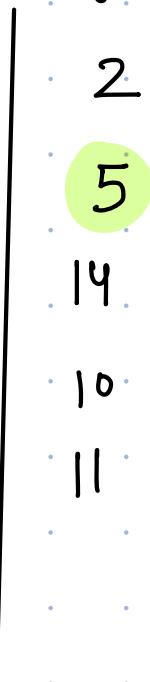
24

29

$$5_K = \text{psum}[R] - \text{psum}[L-1]$$

$$\text{psum}[R] = K + \text{psum}[L-1]$$

$$\text{or } \text{psum}[L-1] = \text{psum}[R] - K$$

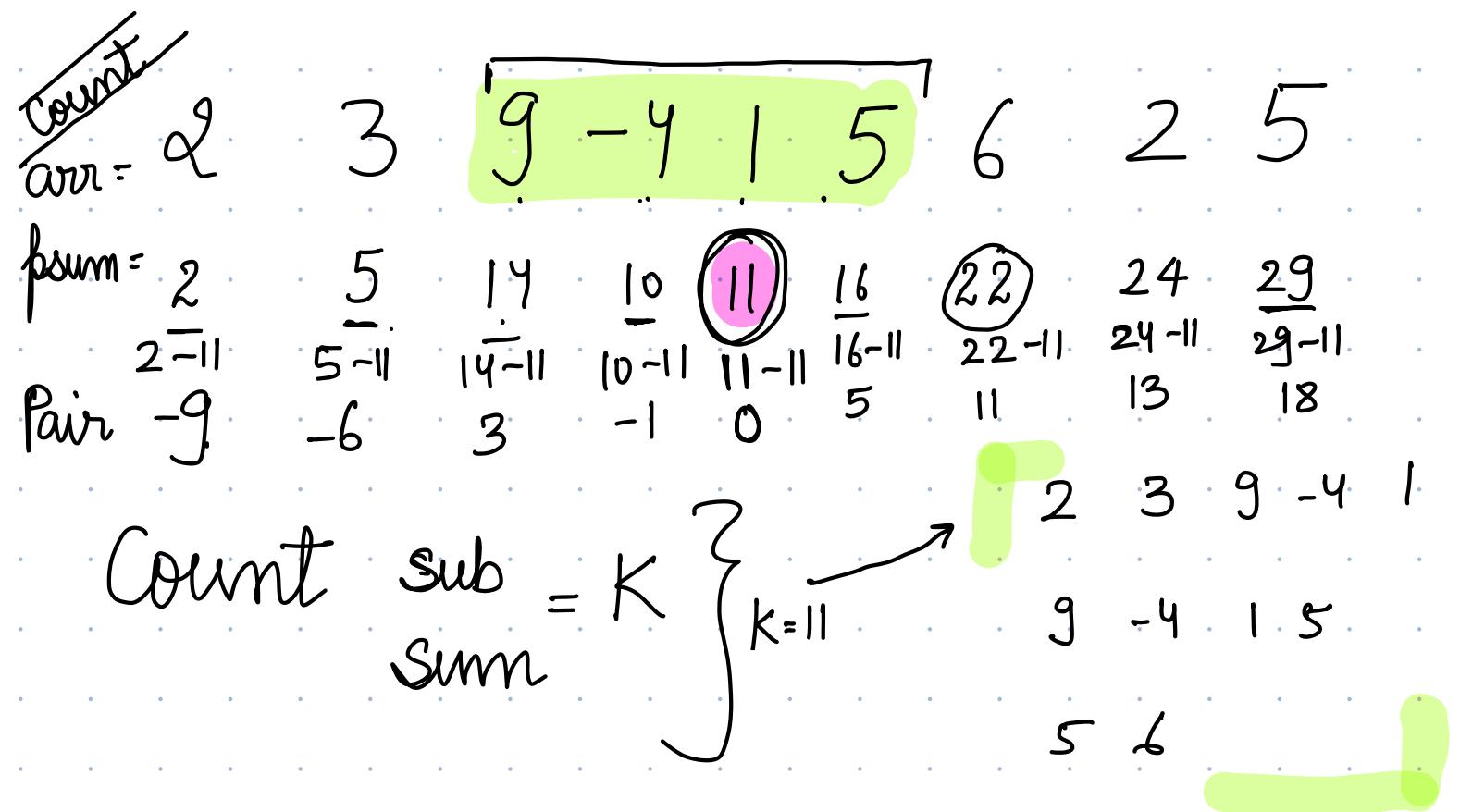


Element traversal - one by one

psum[i]

pair

(psum[i] - K)



$$\begin{aligned}
 \text{count} &= 0 + \underbrace{\frac{1}{=}}_{3} + \underbrace{\frac{1}{=}}_{=} + \underbrace{\frac{1}{=}}_{=} + \dots
 \end{aligned}$$

29	1
24	1
0	1
2	1
11	1
5	1
22	1
14	1
16	1
10	1

0 1 2 3 2 3 -5 -4 4 5 9 11

$$\begin{array}{r} 0 \\ | \\ \text{pair} \end{array} \quad \begin{array}{r} 2 \\ = \\ -9 \end{array} \quad \begin{array}{r} 5 \\ = \\ -6 \end{array} \quad \begin{array}{r} 0 \\ - \\ -11 \end{array} \quad \begin{array}{r} -4 \\ - \\ -15 \end{array} \quad \begin{array}{r} 5 \\ - \\ -6 \end{array} \quad \begin{array}{r} 16 \\ \hline 16 - 11 \\ 5 \end{array}$$

$\leq = 11$

A hand-drawn diagram on dot-grid paper showing a coordinate plane with a horizontal and vertical axis. The vertical axis has tick marks at -4, 0, 5, and 2. The horizontal axis has tick marks at 1, 2, 2, 9, and 1. A green semi-circle is drawn above the x-axis. To the right of the axes, there is a subtraction problem: $16 - 5 = 11$. Below this, it says "2 pairs". Further down, it says $11 [5-5]$. At the bottom, it says $-5 -4 9 11 [2-5]$.

count = count + freq [pair]

psum ✓

hm. add (0, 1)

for every sum value →

$$\text{pair} = \text{sum} - K$$

count = count + freq [pair]

hm. add (psum, $\frac{+1}{1}$)

return count