

5 questions to be done today

1. Count of set bits
 2. Find good days
 3. Every element appear thrice except one
- 4a Subarrays = 1
- 4b Subarrays = 0
5. Maximum AND Pair

Q.

int $\rightarrow \frac{32}{\cdot}$

$N = \underline{12}$

set = 1

1100 $\rightarrow 2$

$N = 21$

10101 $\rightarrow 3$

$N = 57$

111001 $\rightarrow 4$

Approach 1 -

int N $\rightarrow \frac{32 \text{ bits}}{\downarrow}$

4 bytes

$N = 12$

31 0	8 7 6 5 4 3 2 1 0 0 0 0 0 0 0 1 1 0 0
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A1

count = 0

for (i=0 ; i < 32 ; i++) {

if ($N \& (1 << i) > 0$)

count ++

}

return count

TC \downarrow
 $O(32)$
 $O(1)$

K & R Ritchie solution
Kerningham

$N = 57$
 $\& 56$

$$\begin{array}{r}
 \cancel{1} \ 1 \ 1 \ 0 \ 0 \ 1 \\
 \cancel{1} \ 1 \ 1 \ 0 \ 0 \ 0 \\
 \hline
 1 \ 1 \ 1 \ 0 \ 0 \ 0
 \end{array}$$

4 4

111001
111000
110000
100000
000000

$N = N \& N-1$

$N = 56$

$\& N-1 = 55$

$N = N \& N-1$

$$\begin{array}{r}
 1 \ 1 \ 1 \ 0 \ 0 \ 0 \\
 \cancel{1} \ 1 \ 0 \ 1 \ 1 \ 1 \\
 \hline
 1 \ 1 \ 0 \ 0 \ 0 \ 0 \leftarrow 48
 \end{array}$$

$N = 48$

110000

$$\& N-1 = 47$$

$$\& \begin{array}{r} 101111 \\ 100000 \\ \hline \end{array} = 32$$

$$N = 32$$

$$\& N-1 = 31$$

0

$$32 = 100000$$

$$\& 31 = 011111$$

$$000000$$

$N = 0 \leftarrow \text{STOP}$

A2

count = 0
while ($N > 0$) {

$N = N \& N - 1$

count ++;

}

return count.

TC =
 $O(\text{count of set bits})$

$$57 =$$

$$\begin{array}{r} 111001 \\ \hline \end{array}$$

(4)

A3

count = 0

div and mod

while ($N > 0$) {

if ($N \% 2 \neq 0$)

count ++

$$\underline{N = N / 2}$$

}

TC =

$$N \rightarrow \frac{N}{2} \rightarrow \frac{N}{4} \rightarrow \frac{N}{8} \dots \dots 1$$

$O(\log N)$

2	57	1
2	28	0
2	14	0
2	7	1
2	3	1
2	1	1
	0	0

Q2

Find Good days

$$13 = \underline{\underline{1\ 1\ 0}} \\ 2^3\ 2^2\ 2^1\ 2^0$$

Cat

$$127 = \underline{\underline{1\ 1\ 1\ 1\ 1\ 1\ 1}} \\ 2^6\ 2^5\ 2^4\ 2^3\ 2^2\ 2^1\ 2^0$$

Sum of fishes cat

1	$\xrightarrow{x2}$	2	$\xrightarrow{x2}$	4	$\xrightarrow{x2}$	8	$\xrightarrow{x2}$	16	$\xrightarrow{x2}$	32	\dots	64	$=$
unit fishes		—		—		—		—		—			
Day 1	2	3	4	5	6	7							

5 fishes \longrightarrow 2 days

16 fishes \longrightarrow 1 day

21 fishes \longrightarrow 3 days

$$\underline{\underline{2\ 1}} = \underline{\underline{2^5\ 2^4\ 2^3\ 2^2\ 2^1\ 2^0}}$$

ans = count set bits of N

Doubts :

int $N = \underline{57}$
↓
32 bits

111001

0000...0111001



bitwise operators

&
|
^

20

a 1 2 4 8 16 32 ...
 -
 1 2 3 4 5

4 → 2 → 1

$$20 = \underline{16} + \underline{4} = 2 \\ = \text{sum of power of } 2$$

$$23 = 16 + 4 + 2 + 1 = 4$$

Q3 →

Problem Statement

Given an integer array, all the elements will occur thrice but one. Find the unique element.

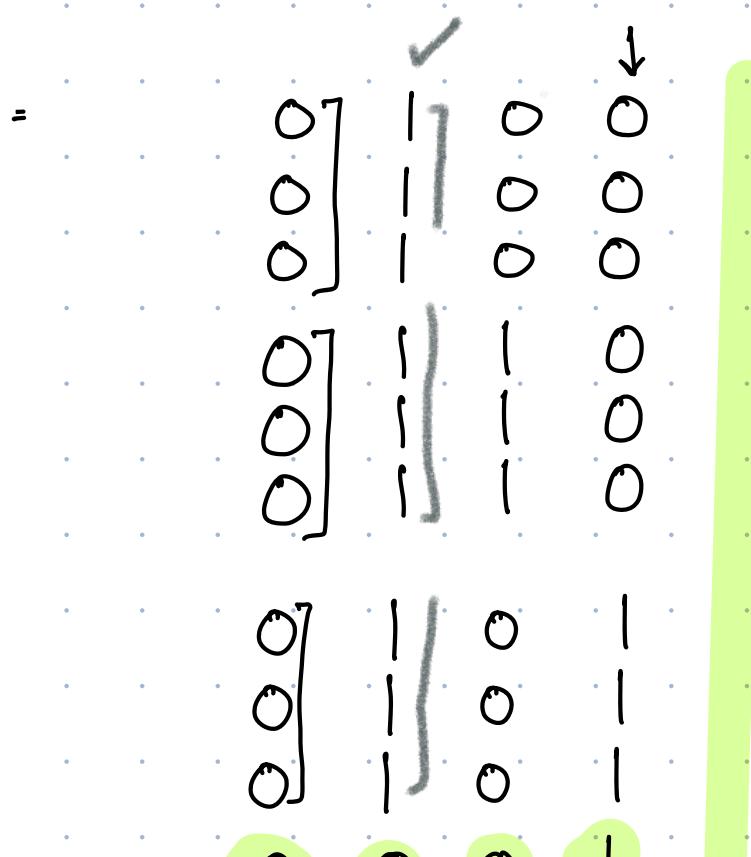
Example

Input: [4, 5, 5, 4, 1, 6, 6, 4, 5, 6]

Output: 1

Only 1 occurs a single time

4 4
5 4
5 4
4 6
1 6
6 6
6 5
4 5
5 5
6 1



$$\begin{array}{r} 0 \quad 9 \quad 3 \\ 0 \quad 0 \quad 0 \quad 1 \\ \hline 0 \quad 9 \quad 3 \quad 4 \\ 0 \quad 0 \quad 0 \quad 1 \\ \hline 0 \quad 9 \quad 3 \quad 3 \end{array}$$

0%3 9%3 3%3

$3n+1$

or

$3n$

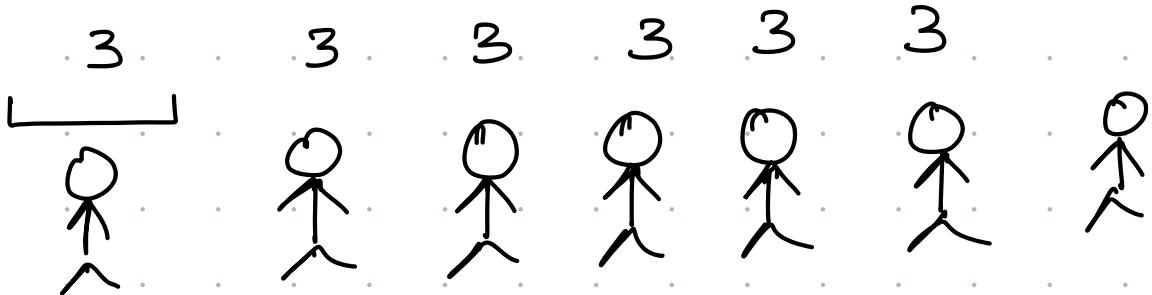
5 + 6 + 7 + 2 = 20

Choco Choco Choco Choco

$20 / 3 = 6$

- -

2 rem



3

1 1 1
3

1

4

rem
1

0 0 0

0 0 0

1

```

total = 0
for ( i=0            i < 32            i++) {
    // at pos i , for every no.
    sum = 0
    for (j=0            j < N            j++) {
        if (arr[j] & (1<<i) > 0)
            sum = sum + 1
}

```

$$\frac{3n+1}{3^n} = 1 \quad \text{rep} = \sum \% 3$$

$$3^n = 0 \quad \text{total} = \text{total} + \text{rep} * \underline{2^i}$$

}

return total

0	0	1	1	0	1	
i=3	..	i=4	i=3	i=2	i=1	i=0

total = 0
 for (i=0 i < 32 i++) {

// at pos i, for every no.

sum = 0
 for (j=0 j < N j++) {

if (arr[j] & (1 << i) > 0)
 sum = sum + 1

}

$$\frac{3n+1}{3n} = 1 \quad \text{rep} = \text{sum} \% 3$$

$$\text{total} = \text{total} + \text{rep} * \frac{2^i}{\downarrow} \rightarrow 1 << i$$

$\text{Math.pow}(2, i)$

}

return total

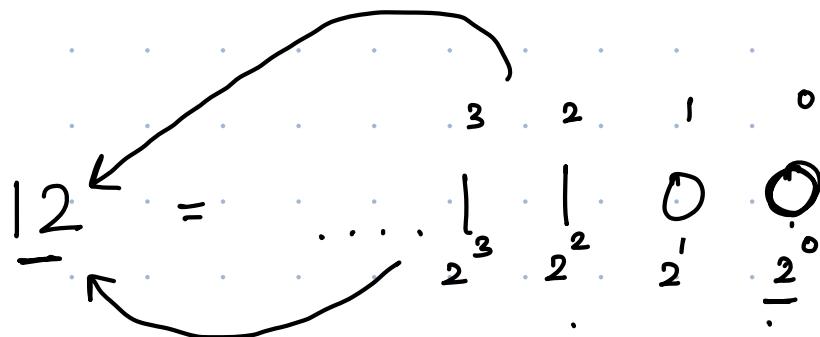
$$\frac{3x}{3} \rightarrow 0$$

$$3x + 1 \rightarrow 1$$

0 9 3 4

sum
0 0 0 1

3x



$$= 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$$

$$= 8 + 4 + 0 + 0 = 12$$

int = 4B
32 bits
31 . . . 3 2 1 0

Q4

Binary array $\hookrightarrow_N \rightarrow []$

$\text{arr}[i] = 1 \text{ or } 0$

a. Number of subarrays, whose OR = 0

b. Number of subarrays, whose OR = ≥ 1

$\left[\begin{array}{c} 1 \\ \vdots \\ 1 \end{array}, \begin{array}{c} 0 \\ \vdots \\ 0 \end{array}, \begin{array}{c} 1 \\ \vdots \\ 1 \end{array} \right]$

$\stackrel{\text{OR}}{\longrightarrow}$

$1 \quad \dots \rightarrow 1 \quad N = 3$

$1 \ 0 \quad \dots \rightarrow 1 \quad \frac{N * (N+1)}{2} = 6$

$1 \ \vdots \ 1 \quad \rightarrow 1 \quad \text{OR} = 1 \rightarrow 5$

$0 \quad \rightarrow 0 \quad \text{OR} = 0 \rightarrow 1$

$0 \ 1 \quad \rightarrow 1$

$1 \quad \rightarrow 1$

// Number of Subarrays, whose OR = 0 χ

Number of Subarrays, whose OR = 1

$$= \text{Total} - \frac{N*(N+1)}{2}$$

Obs = 2

$[1, \underline{\underline{0, 0}}, 1]$



continuous 0's



OR = 0

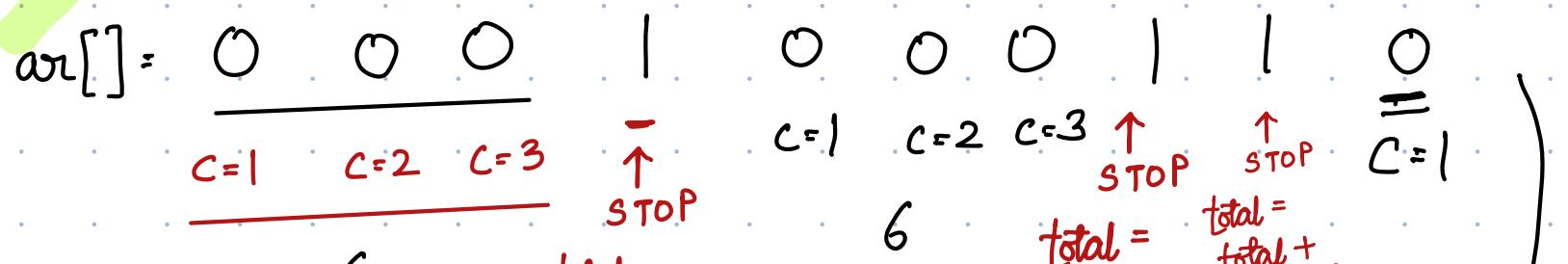
0 0 1
↓

a single 1]

→ OR → 1

$$\text{Total} = 0 + 6 + 6 + 0 + 1$$

0 1 2 3 4 5 6 7 8 9



6

$$\begin{aligned} \text{total} &= \\ \text{total} &+ \\ \frac{c*(c+1)}{2} & \\ c=0 & \end{aligned}$$

6

$$\begin{aligned} \text{total} &= \\ \text{total} &+ \\ \frac{c*(c+1)}{2} & \\ c=0 & \end{aligned}$$

$\uparrow \quad c=1$

if ($\text{ar}[i] == 0$)

$c++$

else if ($\text{ar}[i] \uparrow == 1$) {

$$\begin{aligned} \text{total} &= \\ \text{total} &+ \\ \frac{c*(c+1)}{2} & \\ c=0 & \end{aligned}$$

3

}

$\uparrow \quad \text{STOP}$

\Rightarrow

$$\begin{aligned} \text{total} &= \\ \text{total} &+ \\ \frac{c*(c+1)}{2} & \\ c=0 & \end{aligned}$$

$\text{return } \underline{c=0} \quad \text{total}$

$$\begin{aligned} \text{total} &= \\ \text{total} &+ \\ \frac{c*(c+1)}{2} & \\ c=0 & \end{aligned}$$

$\frac{1 * 2}{2}$

1

No of subarrays
with OR = 0

4b

No of subarrays
with OR = 1

Total - No of
subarrays
with
OR = 0

Q5

maximum AND pair

array of N integers

arr[i]

$$\text{arr[]} = \{5, 4, 6, 8, 5\}$$

$$5 \& 4 = \frac{101}{110} = \underline{\underline{4}}$$

$$5 \& 6 = \frac{101}{110} = \underline{\underline{4}}$$

$$5 \& 8 = \frac{101}{1000} = \underline{\underline{0}}$$

$$6 \& 8 = \frac{110}{1000} = \underline{\underline{0}}$$

$$6 \& 5 = \underline{\underline{4}}$$

$$8 \& 5 = \underline{\underline{0}}$$

$$5 \& 5 = \begin{array}{r} 101 \\ 101 \end{array} = \textcircled{5}$$

$$4 \& 6 = \begin{array}{r} 100 \\ 110 \end{array} = \textcircled{4}$$

$$4 \& 8 = \begin{array}{r} 100 \\ 1000 \end{array} = \textcircled{0}$$

$$4 \& 5 = \textcircled{4}$$

ans = 5 ans

$\Rightarrow N^2 \rightarrow 2 \text{ loops}$

$\Rightarrow O(N)$

or = [21, 18, 24, 17, 16]

$$21 = \begin{array}{r} 10101 \checkmark \end{array}$$

$$18 = \begin{array}{r} 10010 \end{array}$$

$$24 = \begin{array}{r} 11000 \end{array}$$

$$17 = \begin{array}{r} 10001 \checkmark \end{array}$$

$$16 = \begin{array}{r} 10000 \end{array}$$

$$4 \ 3 \ 2 \ 1 \ 0 =$$

10001

max. $\left[\begin{matrix} a \\ b \\ f \end{matrix} \right] \Rightarrow \begin{array}{r} \begin{array}{r} 1 & 0 & 0 & 0 & 1 \\ \underline{-} & \underline{-} & \underline{-} & \underline{-} & \underline{-} \\ 1 & 0 & 0 & 0 & 1 \end{array} \\ \begin{array}{c} 4 \\ 3 \\ 2 \\ 1 \\ = \end{array} \\ \begin{array}{c} \downarrow \\ \text{No} \end{array} \quad \begin{array}{c} \downarrow \\ \text{No} \end{array} \quad \begin{array}{c} \downarrow \\ \text{No} \end{array} \quad \begin{array}{c} \downarrow \\ \text{No} \end{array} \end{array} \quad \text{where more 1's are aligned}$

at that pos \rightarrow Count of 1's ≥ 2

max
and
parv

Solution

max no of 1's aligneds
app.

Left \longrightarrow Right

$$\begin{array}{r}
 \begin{array}{r}
 4 \\
 2 \\
 1 \\
 \hline
 4
 \end{array}
 \begin{array}{r}
 0 \\
 0 \\
 \hline
 3
 \end{array}
 \begin{array}{r}
 + \\
 0 \\
 \hline
 2
 \end{array}
 \begin{array}{r}
 0 \\
 0 \\
 \hline
 1
 \end{array}
 \begin{array}{r}
 1 \\
 0 \\
 \hline
 0
 \end{array}
 \end{array}
 \quad 2^{\circ} = 17$$

count of 1's ≥ 2 Align 1
N O

$$\begin{array}{c}
 \left[\begin{array}{c} 21 \\ 18 \\ 24 \\ \text{or}[i] \ 90 \\ 0 \ 16 \end{array} \right] = \begin{array}{c} L \\ 1 \\ 0. \ 1 \ 0 \end{array} \\
 \left[\begin{array}{c} 21 \ 18 \\ 21 \ 24 \\ 21 \ 16 \\ 18 \ 24 \\ 18 \ 16 \\ 24 \ 16 \end{array} \right] 4 \Rightarrow \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} \\
 \hline
 \begin{array}{r}
 21 & 18 \\
 21 & 24 \\
 21 & 16 \\
 18 & 24 \\
 18 & 16 \\
 24 & 16
 \end{array}
 \end{array}$$

$$\begin{array}{c}
 29. \quad = \quad 1 \ 1 \ 0 \ 1 \\
 18 \ 0 \quad = \quad 0 \ 0 \ 0 \ 0 \\
 24 \quad = \quad 1 \ 0 \ 0 \ 0 \\
 \hline
 \begin{array}{r}
 29 \ 18 \\
 29 \ 24 \\
 29 \ 16 \\
 18 \ 24
 \end{array}
 \end{array}$$

$$= \underline{24}$$

~~18276~~
~~24216~~
if you
don't
replace

29

1. 1 1 0 1

18

1. 0 0 1 0

24

1. 1 0 0 0

9.
16

0 1 0 0 1.
1 0 0 0 0
4✓ 3 2 1 0

1 1 0 0 1

→ 25

5.

[1 0 1
1 0 0]

30

0 0 0

20

0 0 0

X0

0 0 0
— 1 0
2 — 0

1 0 0 → 4

Pseudocode :

for ($i = 31$ _____ 0) {
 → $c = 0$
 for ($j = 0$ $j < N$ $j++$) {
 if ($\text{arr}[j] \& (1 \ll i) > 0$) $c++$
 }
}

}
if ($c \geq 2$) {
 make 0 → 0
 ans → i → 1 }
—

return ans

32 {
 N

if ($c >= 2$)
 N

}

$$\begin{aligned} TC &= 32(N + N) = 64N \\ &= O(N) \end{aligned}$$