Neural Networks - Image Recognition

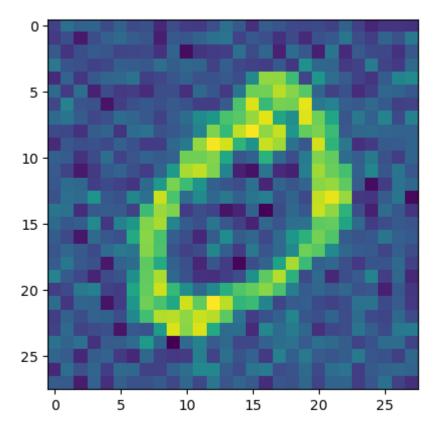
```
In [1]: import keras
         from keras.datasets import mnist
         from keras.models import Sequential
         from keras.optimizers import RMSprop
         from keras.layers import Dense, Dropout, Flatten
         from keras.layers import Conv2D, MaxPooling2D
         from keras import backend
        import matplotlib.pyplot as plt
In [2]:
         %matplotlib inline
In [3]: # the data, shuffled and split between train and test sets
         (x_train, y_train), (x_test, y_test) = mnist.load_data()
         x train = x train.reshape(60000, 784)
         x_{\text{test}} = x_{\text{test.reshape}}(10000, 784)
         x_train = x_train.astype('float32')
         x_test = x_test.astype('float32')
         x train /= 255
         x test /= 255
         print(x_train.shape[0], 'train samples')
         print(x_test.shape[0], 'test samples')
        60000 train samples
        10000 test samples
```

1. Add random noise (see below on size parameter on np.random.normal) to the images in training and testing. Make sure each image gets a different noise feature added to it. Inspect by printing out several images. Note - the size parameter should match the data.

```
In [4]: # Noise is added here
        # Generate random noise with the same shape as the image
        import numpy as np
        mean = .5
        stddev = .16
        noise = np.random.normal(mean, stddev, x train[1].shape)
        # Add the noise to the image
        image noise added = x train[1] + noise
        image_noise_added
        # The max value of the noise should not grossly surpass 1.0
        max(noise)
        0.9814309422337107
Out[4]:
        # Max of noise is less than .1002; very slightly over 1
```

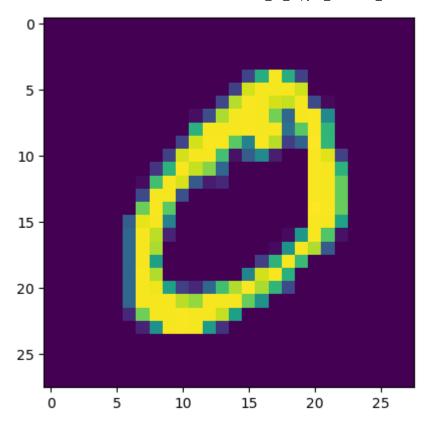
```
In [6]:
        # New Image vs Old
        # New Image
        plt.imshow(image_noise_added.reshape(28, 28))
```

<matplotlib.image.AxesImage at 0x27146484400> Out[6]:



```
In [7]:
        # Old Image
        plt.imshow(x_train[1].reshape(28, 28))
```

<matplotlib.image.AxesImage at 0x271484f4760> Out[7]:



```
In [8]:
        ### Add noise to whole set of images
        # Noise is added here
        # Generate random noise with the same shape as the image
        import numpy as np
        mean = .5
        stddev = .16
        noise = np.random.normal(mean, stddev, x_train.shape)
        # Generate random noise with the same shape as the image
        test_noise = np.random.normal(mean, stddev, x_test.shape)
        y_train_noise = np.random.normal(mean, stddev, y_train.shape)
        y_test_noise = np.random.normal(mean, stddev, y_test.shape)
        # Add noise
        x_train_noise = x_train + noise
        x_test_noise = x_test + test_noise
        y_train_noise = y_train + y_train_noise
        y_test_noise = y_test + y_test_noise
        # Add noise
        x_test_noise[1]
```

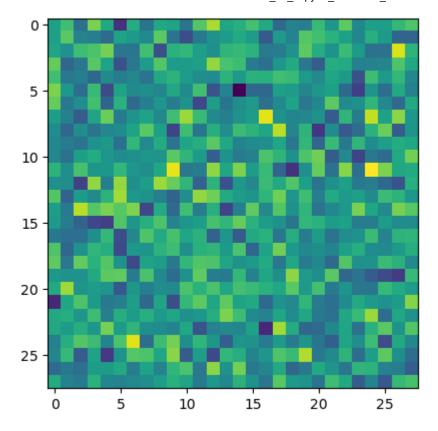
array([0.57687232, 0.40826787, 0.48698683, 0.50217036, 0.645252 Out[8]: 0.41440629, 0.61910315, 0.51303236, 0.63962366, 0.64682592, 0.37467939, 0.52838516, 0.60116104, 0.42979264 0.57147313, 0.47278035, 0.17707505, 0.6037902 , 0.38793955, 0.4623349 , 0.19363086, 0.37676522, 0.67193465, 0.58154555, 0.46630765, 0.34852071, 0.34968219, 0.42603748, 0.60274664, 0.57033017, 0.32556246, 0.34093753, 0.46699395, 0.40841534, 0.31135967, 0.55859174, 0.638774 , 0.40805849, 0.30170078, 0.73114616, 0.37730497, 0.5813878 , 0.63878796, 0.44348356, 0.60068954, 0.28910888, 0.62700597, 0.36169634, 0.46364495, 0.46958263, 0.50642522, 0.4631466 , 0.48307732, 0.63050008, 0.54317324, 0.46467005, 0.76507951, 0.41156469, 0.67368421, 0.45407504, 0.26744614, 0.41759021, 0.52759676, 0.53368195, 0.48003363, 0.38042947, 0.51910648, 0.79028283, 0.72157947, 0.47613033, 0.35599436, 0.71802766, 0.50874887, 0.33294799, 0.33277805 0.29037356, 0.51121625, 0.54504028, 0.80172431, 0.65532005 0.66518034, 0.47198225, 0.36786903, 0.6233744 , 0.42654806, 0.626913 0.39782186, 0.42302727, 0.50334411, 0.4370632 , 0.4251654 , 0.30500427, 0.55564946, 0.38227468, 0.96422872, 0.91836584, 1.24052622, 1.46307529, 1.56094511, 1.25740408, 0.6005917 , 0.69438408, 0.53072081, 0.45989333, 0.31914228, 0.47099433, 0.22500937, 0.5613782 , 0.75790809, 0.70932527, 0.45917871, 0.39644749, 0.33798038, 0.32350235, 0.61883753, 0.39654337, 0.70952601, 0.60944194, 0.50570285, 0.56547912, 0.7316817 , 1.48010999, 1.20563341, 1.5354358 , 1.30711049, 1.5711794 , 1.43229737, 1.29984594, 1.38860626, 0.44369197, 0.34746496, 0.54786675, 0.46418887, 0.72041538, 0.71813562, 0.45970136, 0.47099867, 0.34223791, 1.14808828, 0.27251569, 0.55721335, 0.38836619, 0.29644195, 0.41930418, 0.59695966, 0.53640419, 0.64318424, 0.35857606, 1.12010692, 1.56477894, 1.58059331, 1.60154089, 1.27910914, 1.04854077, 1.45419382, 1.61817443, 0.91370378, 0.5173893 , 1.60501054, 0.58896817, 0.39474733, 0.58212097, 0.46727581, 0.79173531, 0.60242163, 0.45962592, 0.54456266, 0.37801249, 0.56099927, 0.56874342, 0.6159749, 0.50175787, 0.55086682, 0.6257764 , 0.75945265, 1.07127152, 1.36776284, 1.35008523, 1.36692701, 0.77233484, 0.30944101, 1.65998397, 0.57868446, 0.71401451, 1.20846498, 1.29847969, 0.66515439, 0.36115685, 0.22984019, 0.63827504, 0.77902976, 0.51871401, 0.41042776, 0.57781973, 0.4880221 , 0.57619222, 0.3714438 , 0.47110892, 0.67478363, 0.29292569, 0.65160108, 0.67104572, 0.91870886, 1.25853786 0.39016473, 1.43544991, 0.73563021, 0.78235505, 0.38323818, 0.58749505, 0.78000725, 1.69187491, 1.49744226, 0.88697527, 0.79193357, 0.56011929, 0.63032284, 0.69932626, 0.37608275, 0.61027271, 0.52195608, 0.48601603, 0.74008066, 0.40982626, 0.61027295, 0.47972026, 0.3698776 , 0.40591306, 0.55671247, 0.61515198, 0.5449375 , 0.44684098, 0.51541301, 0.4153461 , 0.46303803, 0.57844954, 0.50765033, 0.42400258, 1.22140617, 1.61883959, 1.42202093, 0.58517293, 0.23959164, 0.52297909, 0.64580432, 0.48682419, 0.30327991, 0.34583476, 1.04286853, 0.31668652, 0.59552655, 0.43303125, 0.60815892, 0.21081781, 0.64153105, 0.64774413, 0.71064805, 0.42262043, 0.40247365, 0.44596662, 0.40861889, 0.49788938, 0.52451359, 0.62464182, 0.39184073, 1.34829301, 1.70225717, 1.51560417, 0.48299895 1.53762747, 0.33936687, 0.69238985, 0.32186298, 0.2586233 , 0.28474299 0.52029234, 0.46978064, 0.66648489, 0.32801189, 0.55044112, 0.41059155, 0.58940078, 0.67963343, 0.52471417, 0.61162958, 0.458238 , 0.80035667, 0.66476024, 0.75578721, 0.56674768, 0.3457525 , 0.72454083, 0.93367028, 1.49255573, 1.35476919, 1.14075649, 0.38107664, 1.32076445, 0.40289053, 0.444363

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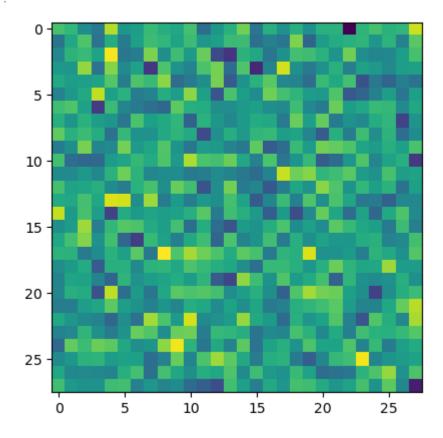
```
# Compare Noises to Ensure they are Different
In [9]:
         # Noise on Image 122
        plt.imshow(noise[122].reshape(28, 28))
```

<matplotlib.image.AxesImage at 0x27148566200> Out[9]:



Noise on Image 124 In [10]: plt.imshow(noise[124].reshape(28, 28))

<matplotlib.image.AxesImage at 0x271485de350> Out[10]:



```
In [11]: # As the two visual representations (images) of the noise show different patterns, the
          # for each image
```

1. Compare the accuracy of train and val after N epochs for MLNN with and without noise.

```
%%capture
In [12]:
         ## Code From Base for Creating Neural Network Without Noise
         batch_size = 128
         num classes = 10
         epochs = 20
         # convert class vectors to binary class matrices
         y_train = keras.utils.to_categorical(y_train, num_classes)
         y test = keras.utils.to categorical(y test, num classes)
         model = Sequential()
         model.add(Dense(512, activation='relu', input_shape=(784,)))
         model.add(Dropout(0.2))
         model.add(Dense(512, activation='relu'))
         model.add(Dropout(0.2))
         model.add(Dense(10, activation='softmax'))
         model.summary()
         model.compile(loss='categorical crossentropy',
                        optimizer="adam",
                        metrics=['accuracy'])
         history = model.fit(x_train, y_train,
                              batch_size=batch_size,
                              epochs=epochs,
                              verbose=1,
                              validation data=(x test, y test))
          score = model.evaluate(x_test, y_test, verbose=0)
          print('Test loss:', score[0])
          print('Test accuracy:', score[1])
In [13]: import pandas as pd
         np.max(x_train_noise),
         np.min(x_train_noise),
         np.max(x_train),
          np.min(x_train)
         (2.317632454193437, -0.4185654653815156, 1.0, 0.0)
Out[13]:
In [14]: # Normalization
         mean = np.mean(x_train_noise)
         std = np.std(x_train_noise)
         x train noise norm = (x train noise - mean) / std
         mean = np.mean(x_test_noise)
          std = np.std(x_test_noise)
          x_test_noise_norm = (x_test_noise - mean) / std
         mean = np.mean(y_train_noise)
```

```
std = np.std(y train noise)
y train noise norm = (y train noise - mean) / std
mean = np.mean(y_test_noise)
std = np.std(y test noise)
y_test_noise_norm = (y_test_noise - mean) / std
```

```
In [15]:
         %%capture
         ## Updated Code for Creating Neural Network With Noise
         batch_size = 128
          num classes = 10
          # epochs = 20 ## Commenting out; this ensures the same number of epochs is used for bo
         # convert class vectors to binary class matrices - using noise added images
         y train bcm = keras.utils.to categorical(y train noise norm, num classes)
         y_test_bcm = keras.utils.to_categorical(y_test_noise_norm, num_classes)
          noisy_model = Sequential()
          noisy_model.add(Dense(512, activation='relu', input_shape=(784,)))
          noisy model.add(Dropout(0.2))
         noisy_model.add(Dense(512, activation='relu'))
          noisy model.add(Dropout(0.2))
          noisy_model.add(Dense(10, activation='softmax'))
          noisy model.summary()
          noisy_model.compile(loss='categorical_crossentropy',
                        optimizer="adam",
                        metrics=['accuracy'])
         history = noisy_model.fit(x_train_noise_norm, y_train_bcm,
                              batch_size=batch_size,
                              epochs=epochs,
                              verbose=1,
                              validation_data=(x_test_noise_norm, y_test_bcm))
          noisy_score = noisy_model.evaluate(x_test_noise_norm, y_test_bcm, verbose=0)
          print('Test loss:', noisy_score[0])
          print('Test accuracy:', noisy_score[1])
```

```
In [16]: | print('Test loss:', score[0]) # Test loss & accuracy statistics for the model trained
         print('Test accuracy:', score[1])
         print('Test loss:', noisy_score[0]) # The same statistics for the model trained with
         print('Test accuracy:', noisy_score[1])
```

Test loss: 0.0920642837882042 Test accuracy: 0.9800999760627747 Test loss: 0.1428346335887909 Test accuracy: 0.9804999828338623

In [17]: # Comparing the without-noise and with-noise models, we find that the noise reduces at # a training series lasting n=20 epochs. Additionally, the test loss statistic is noic

> 1. Vary the amount of noise by changing the scale parameter in np.random.normal by a factor. Use .1, .5, 1.0, 2.0, 4.0 for the scale and keep track of the accuracy for training and validation and plot these results.

```
In [18]: %capture
         ## Combining Noise Code with Model-Running code for a single, repeatable block:
         # Listing Scale (i.e. Standard Deviation) Values over which to train models
          stddev_values = [0.1, 0.5, 1.0, 2.0, 4.0] # Values given
          # Initializing Lists
         loss_values = []
         accuracy values = []
          # Loon:
          for stddev in stddev values:
             # Generate random noise with the same shape as the image
             mean = .5
             stddev = .16
             # Generate random noise with the same shape as the image
             x_train_noise = np.random.normal(mean, stddev, x_train.shape)
             x test noise = np.random.normal(mean, stddev, x test.shape)
             y train noise = np.random.normal(mean, stddev, y train.shape)
             y_test_noise = np.random.normal(mean, stddev, y_test.shape)
             # Add noise
             x_train_noise = x_train + x_train_noise
             x_test_noise = x_test + x_test_noise
             y_train_noise = y_train + y_train_noise
             y test noise = y test + y test noise
             ## Updated Code for Creating Neural Network With Noise
             batch size = 128
             num_classes = 10
             epochs = 20 # Always using same number of epochs
             # convert class vectors to binary class matrices
             y_train_bcm = keras.utils.to_categorical(y_train_noise_norm, num_classes)
             y test bcm = keras.utils.to categorical(y test noise norm, num classes)
             noisy model = Sequential()
             noisy model.add(Dense(512, activation='relu', input shape=(784,)))
             noisy model.add(Dropout(0.2))
             noisy model.add(Dense(512, activation='relu'))
             noisy model.add(Dropout(0.2))
             noisy model.add(Dense(10, activation='softmax'))
             noisy model.summary()
              noisy model.compile(loss='categorical crossentropy',
                            optimizer="adam",
                            metrics=['accuracy'])
             history = noisy model.fit(x train noise norm, y train bcm,
                                  batch size=batch size,
                                  epochs=epochs,
                                  verbose=1,
                                  validation data=(x test noise norm, y test bcm))
              noisy_score = noisy_model.evaluate(x_test_noise_norm, y_test_bcm, verbose=0)
              print('Test loss:', noisy_score[0])
              print('Test accuracy:', noisy_score[1])
              # Append Loss & Accuracy To List
             test_loss = noisy_score[0]
```

```
test accuracy = noisy score[1]
loss values.append(test loss)
accuracy_values.append(test_accuracy)
```

In [19]: # Compile Loss and Accuracy statistics for the models into a single data frame accuracy loss results dataframe = pd.DataFrame({'stddev values': stddev values, 'loss accuracy loss results dataframe

```
Out[19]:
              stddev_values loss_values accuracy_values
           0
                                0.161019
                         0.1
                                                    0.9780
           1
                         0.5
                                0.135908
                                                    0.9786
           2
                         1.0
                                0.144020
                                                    0.9772
           3
                         2.0
                                0.136160
                                                    0.9782
           4
                                0.150436
                                                    0.9775
                         4.0
```

```
In [20]: # Plotting Results
         fig, ax1 = plt.subplots()
         loss line = ax1.plot(stddev values, loss values, color = 'green', label = 'Test Loss 5
          # Loss line Plot
          ax1.set xlabel('Scale (Standard Deviation)')
          ax1.set ylabel('Loss Values')
          ax1.set title('Combined Loss and Accuracy vs Scale Plot')
         # Accuracy line Plot
          ax2 = ax1.twinx()
          accuracy_line = ax2.plot(stddev_values, accuracy_values, color='orange', label='Test /
          ax2.set_ylabel('Accuracy Values')
         # Combine Both Lines Into One Plot
         lines = loss line + accuracy line
          labels = [l.get_label() for l in lines]
          ax1.legend(lines, labels, loc='lower right')
```

<matplotlib.legend.Legend at 0x2719c61b880> Out[20]:

