

LDpred2: BETTER, FASTER, STRONGER

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02 - 07 - 2020

BACKGROUND: LDPRED

Important background



Search



[#DaftPunk](#) [#HarderBetterFaster](#) [#Vevo](#)

Daft Punk - Harder Better Faster (Official Video)

WHAT DOES LDPRED DO?

Published in 2015: ~ 435 citations (less than PRSice from same year)

- matrix of correlation between genetic variants (LD matrix), summary statistics from GWAS (β , p – value), genotype and phenotype files from test and validation sets

Infinitesimal:

- All markers are causal
- Effect sizes drawn from Gaussian
- Computationally efficient
- Not very plausible

Non-infinitesimal

- Assumes p of variants are causal - more plausible
- Analytical solution hard - approximate MCMC Gibbs sampler (not efficient nor robust)

WHAT DOES LDPRED DO?

But *actually* also requires:

- big LD reference panel, correct model specifications - not trivial
- Steps:
 - ▶ Coordinating summary stats, LD reference genotypes, validation or test genotypes
 - ▶ Estimating weights for variants - which requires additional parameters.
 - ▶ Calculating PRS
 - ▶ User needs to calculate partial- R^2 on their own (e.g. in R)

LDpred uses a Bayesian framework to assess effect sizes from provided summary statistics and LD information

$$P(\theta|x) = \frac{P(x|\theta)P(\theta)}{P(x)} \quad (1)$$

LDpred MODEL - OVERVIEW

Unlinked markers and non-infinitesimal architecture
Effects are drawn from a mixture distribution:

$$\beta_j \sim \begin{cases} N(0, \frac{h^2}{M\rho}), & \text{with probability } p. \\ 0, & \text{otherwise.} \end{cases} \quad (2)$$

- LDpred1: h^2 estimated with constrained LD score regression (fixed intercept=1)
- Gibbs sampler algorithm:

GIBBS SAMPLER ALGORITHM: MAIN STEPS

1. residualized effect sizes for each variant j : $\tilde{\beta}_j$
2. probability that variant j is causal: \bar{p}_j
3. β_j is sampled according to:

$$\beta_j | \tilde{\beta}_j \sim \begin{cases} N(\frac{1}{1+\frac{M_p}{nh^2}} \tilde{\beta}_j, \frac{1}{1+\frac{M_p}{nh^2}} \frac{1}{n}), & \text{with probability } p. \\ 0, & \text{otherwise.} \end{cases} \quad (3)$$

4. posterior mean of $\beta_j | \tilde{\beta}_j$: ω_j

GIBBS SAMPLER ALGORITHM: MAIN STEPS

Algorithm 1 LDpred, with hyper-parameters p and h^2 , LD matrix \mathbf{R} and summary statistics $\hat{\gamma}$, $\text{se}(\hat{\gamma})$ and

- 1: $\hat{\beta} \leftarrow \frac{\hat{\gamma}}{\text{se}(\hat{\gamma}) \cdot \sqrt{n}}$ ▷ Initialization of scaled marginal effects (see previous slide)
- 2: $\Omega \leftarrow \mathbf{0}$ ▷ Initialization of posterior means
- 3: **for** $k = 1, \dots, N_{\text{burn-in}} + N_{\text{iter}}$ **do** ▷ Gibbs iteration
- 4: **for** each variant j **do** ▷ All variants
- 5: Compute $\tilde{\beta}_j$ according to (3)
- 6: Compute \tilde{p}_j according to (4)
- 7: Sample β_j according to (5)
- 8: Compute ω_j according to (6)
- 9: **end for**
- 10: **if** $k > N_{\text{burn-in}}$ **then**
- 11: $\Omega \leftarrow \Omega + \omega$
- 12: **end if**
- 13: **end for**
- 14: $\Omega \leftarrow \Omega / N_{\text{iter}}$ ▷ Average of all ω after burn-in
- 15: Return $\Omega \cdot \text{se}(\hat{\gamma}) \cdot \sqrt{n}$ ▷ Return posterior means, scaled back (see previous slide)

LDpred: PROS AND CONS OVERVIEW

PROS:

- elegant modelling of genetic architecture
- assigns weights to variants instead of arbitrary P+T
- also offers P+T in the same framework
- mostly runs PLINK in the background, and Python scripts

CONS:

- Errors messages are cryptic
- **Slow**
- Gibbs sampler **extremely sensitive to model parameters**
- particularly bad for long-range LD regions (e.g HLA)
- MCMC setup might or not improve things and makes it *much slower*
- No manual available.

NEW METHOD: LDPRED2

LDpred2: WHAT'S NEW?

- Runs in bigsnpr package in **R**.
- LDpred-auto: learns parameters from the data. **Stronger**
- **More accurate** PRS: simulation and real data benchmarking
- Compares favorably to LDpred 1 and other methods [sort of]
- parallelization in C++ - **FASTER**
- **has tutorial!!** - **Better** <https://privefl.github.io/bigsnp/articles/LDpred2.html>

SIMULATIONS: METHODS

Binary phenotypes; each set 10X (average AUC is reported)

- UKBB data
- unrelated individuals - 360K
 - ▶ 10,000 for validation, LD reference
 - ▶ 300,000 for GWAS
 - ▶ $\sim 52,000$ as test set
- HapMap3 variants - 1.1 Million
- $h^2 = 0.4$ or $h^2 = 0.3$, prevalence 15%
- $M = \{300, 3000, 30000, 300000\}$
- Variance of genetic liability= h^2
- HLA region
- Implemented in bigsnpr

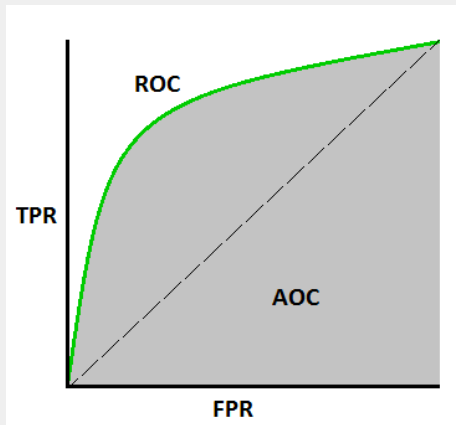
REAL DATA: METHODS

- Unrelated individuals - 360K
- All case-control phenotypes
- 10,000 for validation, LD reference
- $\sim 352,000$ as test set
- Compare LDpred1, LDpred2, C+T, SCT, lassosum, PRS-CS
- summary statistics:

Trait	GWAS citation	GWAS sample size	GWAS #variants
Breast cancer (BRCA)	Michailidou <i>et al.</i> (2017)	137,045 / 119,078	11,792,542
Rheumatoid arthritis (RA)	Okada <i>et al.</i> (2014)	29,880 / 73,758	9,739,303
Type 1 diabetes (T1D)	Censin <i>et al.</i> (2017)	5913 / 8828	8,996,866
Type 2 diabetes (T2D)	Scott <i>et al.</i> (2017)	26,676 / 132,532	12,056,346
Prostate cancer (PRCA)	Schumacher <i>et al.</i> (2018)	79,148 / 61,106	20,370,946
Depression (MDD)	Wray <i>et al.</i> (2018)	59,851 / 113,154	13,554,550
Coronary artery disease (CAD)	Nikpay <i>et al.</i> (2015)	60,801 / 123,504	9,455,778
Asthma	Demenaïs <i>et al.</i> (2018)	19,954 / 107,715	2,001,280

Table 1: Summary of external GWAS summary statistics used. The GWAS sample size is the number of cases / controls in the GWAS.

METHODS: PERFORMANCE COMPARISONS



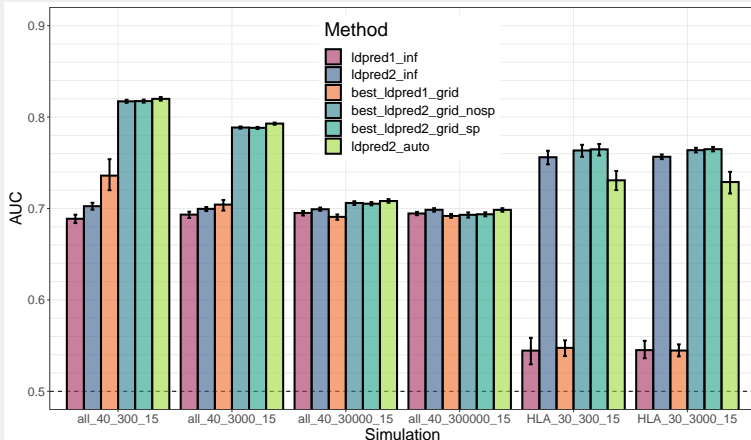
$$TPR = \frac{TP}{TP+FN}$$

$$Specificity = \frac{TN}{TN+FP}$$

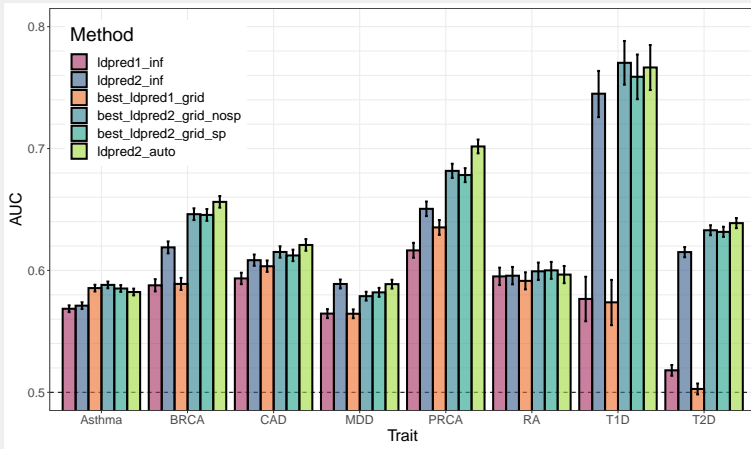
$$FPR = 1 - Specificity$$

Image: <https://towardsdatascience.com/understanding-auc-roc-curve-68b2303cc9c5>

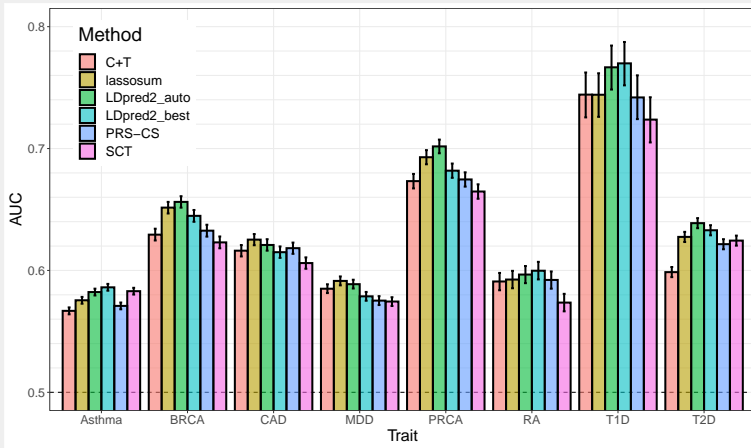
SIMULATIONS: RESULTS



REAL DATA: RESULTS



REAL DATA: RESULTS



CONCLUSIONS

- Strengths: long-range LD and less polygenic traits, does not require validation step
 - solves gibbs sampler inconsistencies
 - higher prediction accuracy then LDpred1
 - Use HapMap3 variants
-
- Not really better than lassosum?
 - Still kinda slow

QC FOR LDPRED2-AUTO

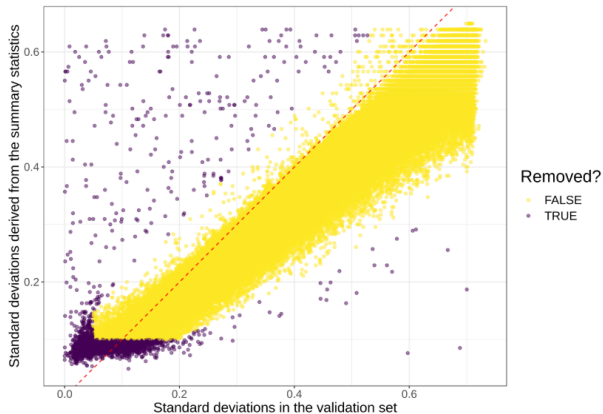


Figure S2: Standard deviations derived from summary statistics of breast cancer based on equation (S1) versus the standard deviations of genotypes of individuals in the validation set. Coloring shows the quality control applied in this paper.