

## Addressing Confounding and Exposure Measurement Error Using Conditional Score Functions

Bryan S. Blette<sup>1</sup>, Peter B. Gilbert<sup>2</sup>, and Michael G. Hudgens<sup>1,\*</sup>

<sup>1</sup>Department of Biostatistics, University of North Carolina at Chapel Hill

Chapel Hill, NC, U.S.A.

<sup>2</sup>Department of Biostatistics, University of Washington and Fred Hutchinson Cancer Research Center

Seattle, Washington, U.S.A.

\**email*: mhudgens@email.unc.edu

**SUMMARY:** Confounding and measurement error are common barriers to drawing causal inference. While there are broad methodologies for addressing each phenomenon individually, confounding and measurement biases frequently co-occur and there is a paucity of methods that address them simultaneously. The few existing methods that do so rely on supplemental data or strong distributional and extrapolation assumptions to correct for measurement error. In this paper, methods are derived which instead leverage the likelihood structure under classical additive measurement error to draw inference using only measured variables. Three estimators are proposed based on g-computation, inverse probability weighting, and doubly-robust estimation techniques. The estimators are shown to be consistent and asymptotically normal and the doubly-robust estimator is shown to exhibit its namesake property. The methods perform well in finite samples under both confounding and measurement error as demonstrated by simulation studies. The proposed doubly-robust estimator is applied to study the effects of two biomarkers on HIV-1 infection using data from the HVTN 505 vaccine trial.

**KEY WORDS:** Causal inference; Confounding; G-formula; HIV/AIDS; Marginal structural models; Measurement error.

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## 1. Introduction

Confounding bias and measurement error are common barriers to identification, estimation, and inference of causal effects. These phenomena often occur together, but are rarely both addressed in an analysis, with researchers typically focusing on whichever is more egregious in their study or ignoring both entirely. The last few decades witnessed a proliferation of interest in and development of methods for causal inference and a parallel trend for methods accounting for measurement error, but comparatively few methods exist at the important intersection of these fields.

The measurement error literature is commonly split into (i) functional methods, which make no or limited assumptions on the distribution of mismeasured variables, and (ii) structural methods, which make explicit distributional assumptions (Carroll et al., 2006). Several causal methods based on structural approaches have been developed (Kuroki and Pearl, 2014; Edwards et al., 2015; Braun et al., 2017; Hong, Rudolph, and Stuart, 2017). Likewise, three of the four most popular functional methods (regression calibration, SIMEX, and methods based on instrumental variables) have been adapted to a variety of causal problems (Vansteelandt, Babanezhad, and Goetghebeur, 2009; Cole et al., 2010; Kendall, 2015; Lockwood and McCaffrey, 2015; Kyle et al., 2016; Wu et al., 2019). These methods all rely on either supplemental data, such as replication, validation, or instrumental data, or on strong distributional and extrapolation assumptions to draw inference.

In contrast, the fourth main functional approach, that of score functions, leverages the likelihood structure under classical additive measurement error to draw inference without supplemental data or such strong assumptions. Despite this advantage, this method has only been adapted to perform causal inference in very limited capacity, perhaps due to its increased complexity over other functional approaches and lack of available software. In particular, McCaffrey, Lockwood, and Setodji (2013) suggested using weighted conditional

score equations to correct for measurement error in confounders and the approach was eventually implemented in Shu and Yi (2019). In this paper, we expand this methodology in multiple directions, considering exposure/treatment measurement error and defining g-formula, IPW, and doubly-robust estimators.

The proposed methods are motivated by the HVTN 505 vaccine trial. This trial evaluated a candidate HIV vaccine and stopped administering immunizations in 2013 after reaching predetermined cutoffs for futility (Hammer et al., 2013). However, follow-up analyses of trial data described several correlates of risk among trial participants (Decamp et al., 2017; Janes et al., 2017; Fong et al., 2018; Neidich et al., 2019). Some of these biomarkers correspond to possible target immune responses for future vaccine trials, but their causal effects on HIV-1 infection have not been described. The methods derived in this paper are motivated by this problem, where the biomarkers are measured with error and their effects are likely subject to confounding, but there is no supplemental data available.

This paper proceeds as follows. In Section 2 notation and the estimand are defined. In Section 3 assumptions are stated and three estimators that adjust for concurrent confounding and exposure measurement error using a conditional score approach are proposed. In Section 4 the proposed estimators are evaluated in a simulation study, and in Section 5 one of the estimators is applied to study two biomarkers collected in the HVTN 505 vaccine trial. Section 6 concludes with a discussion of the advantages and limitations of the proposed methods.

## 2. Notation and Estimand

Suppose there are  $m$  exposures/treatments of interest which may or may not be measured correctly. Let  $\mathbf{A}_i = (A_{i1}, A_{i2}, \dots, A_{im})$  be a row vector denoting the true exposures for individual  $i$  and  $\mathbf{A}_i^* = (A_{i1}^*, A_{i2}^*, \dots, A_{im}^*)$  be the corresponding set of measured exposures. Suppose only the first  $j$  exposures are measured with error, such that  $A_{ik} = A_{ik}^*$  for  $k > j$ .

For example, in the HVTN 505 trial, a biomarker of interest  $A$  is antibody-dependent cellular phagocytosis activity. This biomarker was not observed exactly, but an imperfect phagocytic score  $A^*$  was measured using flow cytometry analysis. Exposures subject to measurement error are assumed to be continuous random variables, while exposures known to be correctly measured may be continuous or discrete. Let  $Y_i$  be the outcome of interest. Define  $Y_i(\mathbf{a})$  to be the potential outcome under treatments  $\mathbf{A} = \mathbf{a} = (a_1, a_2, \dots, a_m)$ . Since there is at least one continuous exposure, each individual has infinite potential outcomes. Let  $\mathbf{L}_i = (L_{i1}, L_{i2}, \dots, L_{ip})$  represent a vector of baseline covariates measured prior to the exposures. Assume that  $n$  i.i.d. copies of the random variables  $(\mathbf{L}, \mathbf{A}^*, Y)$  are observed.

Consider the marginal structural model (MSM)

$$g(E[Y(\mathbf{a})]) = \gamma(1, \mathbf{a})^T \quad (1)$$

where  $g$  is a link function for an exponential family density, e.g.,  $g(\cdot) = \text{logit}(\cdot)$ . The MSM parameter  $\gamma = (\gamma_0, \dots, \gamma_m)$  is a row vector of length  $m + 1$  which quantifies the effects of the exposures on the outcome. The parameter  $\gamma_0$  describes the mean outcome when all exposures are set to 0, which may or may not be of interest depending on the exposures being studied. The linear structure of the MSM is key to employing the conditional score framework described in the next section; more complicated specifications are considered in Web Appendix D.

[Figure 1 about here.]

A compressed version of the directed acyclic graph (DAG) for this setup is presented in Figure 1(a). Note that the DAG implies non-differential measurement error with respect to the outcome, i.e., the exposure error and the outcome are independent because  $\mathbf{A}^*$  is a collider on all paths between them. In Figure 1(b), the DAG is expanded to show the four types of exposures which may belong to  $\mathbf{A}$ : unconfounded and correctly measured, unconfounded and mismeasured, confounded and correctly measured, and confounded and mismeasured. Many

existing methods focus on only mismeasured exposures or on a set of correctly measured exposures with one additional mismeasured exposure; the methods developed in this paper provide a more broadly usable modeling framework where all four types of exposures can be studied simultaneously.

### 3. Methods

#### 3.1 Review of Conditional Score Approach

The proposed methods combine existing methods for (i) correcting exposure measurement error using conditional score equations (CSME) and (ii) adjusting for confounding using g-formula, inverse probability weighting (IPW), and doubly-robust techniques. To begin, CSME methodology is briefly reviewed.

Suppose the conditional density of the outcome on exposures and covariates is in the exponential family (McCullagh and Nelder, 1989), i.e.,  $f(y|\mathbf{a}, \mathbf{l}, \Theta) = \exp[\{y\eta - \mathcal{D}(\eta)\}/\phi + c(y, \phi)]$  where  $\eta = \beta_0 + \mathbf{a}\beta_a + \mathbf{l}\beta_l$ ,  $\mathcal{D}$  and  $c$  are functions,  $\mathbf{a}$  and  $\mathbf{l}$  are realizations of the random variables  $\mathbf{A}$  and  $\mathbf{L}$ , and  $\Theta = (\beta_0, \beta_a^T, \beta_l^T, \phi)$  represents the parameters to be estimated. Assume a classical additive measurement error model  $\mathbf{A}^* = \mathbf{A} + \epsilon_{me}$ , where  $\epsilon_{me}$  is multivariate normal with mean zero and covariance matrix  $\Sigma_{me}$ . To account for  $A_{j+1}, \dots, A_m$  being correctly measured, assume  $\Sigma_{me}$  has the block diagonal form

$$\Sigma_{me} = \begin{bmatrix} \Sigma_e & 0_{j, m-j} \\ 0_{m-j, j} & 0_{m-j, m-j} \end{bmatrix}$$

where  $\Sigma_e$  is the measurement error covariance matrix for exposures  $A_1, \dots, A_j$  and  $0_{a,b}$  denotes an  $a \times b$  matrix of zeros.

The CSME approach leverages the fact that  $\Delta_i = \mathbf{A}_i^* + Y_i(\Sigma_{me}\beta_a)^T/\phi$  is a sufficient statistic for  $\mathbf{A}_i$ . Furthermore, the conditional density of the outcome on covariates and the sufficient statistic is in the exponential family with parameters  $\eta_* = \beta_0 + \boldsymbol{\delta}\beta_a + \mathbf{l}\beta_l$ ,

$\mathcal{D}_*(\eta_*, \phi, \beta_a^T \Sigma_{me} \beta_a) = \phi \log \left[ \int \exp\{y\eta_*/\phi + c_*(y, \phi, \beta_a^T \Sigma_{me} \beta_a)\} dy \right]$ , and  $c_*(y, \phi, \beta_a^T \Sigma_{me} \beta_a) = c(y, \phi) - \frac{1}{2}(y/\phi)^2 \beta_a^T \Sigma_{me} \beta_a$ , where  $\delta$  is a realization of  $\Delta$ . This implies that the score equations from the likelihood conditional on  $\Delta_i$  yield consistent estimators for  $\beta_a$  that only depend on the observed data. The form of the score equations depends on the model specification; the general form is given by

$$\psi(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Theta) = \begin{bmatrix} \{Y_i - E(Y_i | \mathbf{L}_i, \Delta_i)\}(1, \mathbf{L}_i, \Delta_i)^T \\ \phi - \{Y_i - E(Y_i | \mathbf{L}_i, \Delta_i)\}^2 / \{\text{Var}(Y_i | \mathbf{L}_i, \Delta_i) / \phi\} \end{bmatrix} \quad (2)$$

where  $E(Y_i | \mathbf{L}_i, \Delta_i) = \partial \mathcal{D}_* / \partial \eta_*$ ,  $\text{Var}(Y_i | \mathbf{L}_i, \Delta_i) = \phi \partial^2 \mathcal{D}_* / \partial \eta_*^2$ . This procedure can be extended to handle interaction terms (Dagalp, 2001) where now  $\eta = \beta_0 + \mathbf{a}\beta_a + \mathbf{l}\beta_l + \mathbf{a}\beta_{al}\mathbf{l}^T$ ,  $\beta_{al}$  is an  $m \times p$  matrix of interaction parameters,  $\Delta_i = \mathbf{A}_i^* + Y_i \{\Sigma_{me}(\beta_a + \beta_{al}\mathbf{L}_i^T)\}^T / \phi$ , and appropriate elements of  $\beta_{al}$  can be constrained to zero such that only relevant interactions are included in the model. Then the same procedure as above can be applied to derive estimating equations of the form

$$\psi(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Theta) = \begin{bmatrix} \{Y_i - E(Y_i | \mathbf{L}_i, \Delta_i)\}(1, \mathbf{L}_i, \Delta_i, \mathbf{L}_i \otimes \Delta_i)^T \\ \phi - \{Y_i - E(Y_i | \mathbf{L}_i, \Delta_i)\}^2 / \{\text{Var}(Y_i | \mathbf{L}_i, \Delta_i) / \phi\} \end{bmatrix}$$

Here  $\Theta = (\beta_0, \beta_a^T, \beta_l^T, \text{vec}(\beta_{al}), \phi)$ , where  $\text{vec}$  maps the elements of the interaction parameter matrix reading left to right then top to bottom to a row vector, excluding those constrained to zero. Define  $\mathbf{L}_i \otimes \Delta_i$  as a vector of length  $\dim(\text{vec}(\beta_{al}))$  containing the product of the  $k^{th}$  element of  $L_i$  and the  $r^{th}$  element of  $\Delta_i$  if and only if the  $(r, k)$  element of  $\beta_{al}$  is not constrained to be zero.

Next, three methods will be proposed which combine the CSME approach with common causal inference techniques in order to adjust for confounding and measurement error simultaneously. The proposed methods rely on the CSME modeling assumptions stated above as well as a standard set of assumptions used in causal inference: (i) causal consistency,  $Y = Y(\mathbf{a})$  when  $\mathbf{A} = \mathbf{a}$ ; (ii) conditional exchangeability,  $Y(\mathbf{a}) \perp\!\!\!\perp \mathbf{A} | \mathbf{L}$ ; and (iii) positivity,  $f(\mathbf{a} | \mathbf{l}) > 0$  for all  $\mathbf{l}$  such that  $dF_{\mathbf{L}}(\mathbf{l}) > 0$ , where  $F_{\mathbf{L}}$  is the cumulative distribution function

of  $\mathbf{L}$ . As represented in the DAG in Figure 1(a), the exposure measurement error is assumed non-differential with respect to the outcome. Finally, assume that the outcome and covariates are not measured with error and that there is no model mis-specification unless otherwise stated.

### 3.2 G-formula CSME Estimator

The first proposed method combines the g-formula with the CSME method. Let  $\mathbf{A}_{(-j)} = (A_1, \dots, A_{j-1}, A_{j+1}, \dots, A_m)$  be the vector of treatments excluding  $A_j$  and let  $Y(a_j, \mathbf{a}_{(-j)})$  be the potential outcome under  $A_j = a_j$  and  $\mathbf{A}_{(-j)} = \mathbf{a}_{(-j)}$ . Then the g-formula CSME estimator of  $\gamma_j$  for  $j = 1, \dots, m$  is

$$\begin{aligned} \hat{\gamma}_j &= \hat{\mathbb{E}}\{Y(a_j, \mathbf{a}_{(-j)})\} - \hat{\mathbb{E}}\{Y(a_j - 1, \mathbf{a}_{(-j)})\} \\ &= \int_{\mathbf{l} \in \mathbf{L}} \hat{\mathbb{E}}(Y|A_j = a_j, \mathbf{A}_{(-j)} = \mathbf{a}_{(-j)}, \mathbf{L}) d\hat{F}_{\mathbf{L}}(\mathbf{l}) \\ &\quad - \int_{\mathbf{l} \in \mathbf{L}} \hat{\mathbb{E}}(Y|A_j = a_j - 1, \mathbf{A}_{(-j)} = \mathbf{a}_{(-j)}, \mathbf{L}) d\hat{F}_{\mathbf{L}}(\mathbf{l}) \end{aligned}$$

where the predicted mean outcomes are from a fit CSME model with relevant interaction terms and  $a_j$  and  $\mathbf{a}_{(-j)}$  are constants. Equivalently, this estimator is a solution to the estimating equation  $\sum_{i=1}^n \psi_{GF-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Sigma_{me}, \Theta) = 0$ , where  $\Theta = (\beta_0, \beta_a^T, \beta_l^T, \text{vec}(\beta_{al}), \phi, \gamma_1, \dots, \gamma_m)$  and

$$\psi_{GF-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Sigma_{me}, \Theta) = \begin{bmatrix} \{Y_i - \mathbb{E}(Y_i|\mathbf{L}_i, \mathbf{\Delta}_i)\}(1, \mathbf{L}_i, \mathbf{\Delta}_i, \mathbf{L}_i \otimes \mathbf{\Delta}_i)^T \\ \phi - \{Y_i - \mathbb{E}(Y_i|\mathbf{L}_i, \mathbf{\Delta}_i)\}^2 / \{\text{Var}(Y_i|\mathbf{L}_i, \mathbf{\Delta}_i) / \phi\} \\ \beta_{a_1} \mathbf{l}_i^T + \beta_{a_1} - \gamma_1 \\ \vdots \\ \beta_{a_m} \mathbf{l}_i^T + \beta_{a_m} - \gamma_m \end{bmatrix} \quad (3)$$

where  $\beta_a = (\beta_{a_1}, \dots, \beta_{a_m})^T$ ,  $\beta_{al} = (\beta_{a_1l}, \dots, \beta_{a_ml})^T$ , and  $\beta_{a_jl}$  is the  $1 \times p$  vector of parameters corresponding to interactions between  $a_j$  and covariates in  $\mathbf{L}$  for  $j = 1, \dots, m$  (with zeroes for interactions not included in the outcome model).

### 3.3 IPW CSME Estimator

Since the CSME estimator is obtained by solving a set of estimating equations, it's relatively straightforward to define an IPW extension. In particular, consider an estimator of the parameters of interest that solves  $\sum_{i=1}^n \psi_{IPW-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Sigma_{me}, \Theta) = 0$  where:

$$\psi_{IPW-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Sigma_{me}, \Theta) = \begin{bmatrix} SW_i \{Y_i - E(Y_i | \Delta_i)\} (1, \Delta_i)^T \\ SW_i [\phi - \{Y_i - E(Y_i | \Delta_i)\}^2 / \{Var(Y_i | \Delta_i) / \phi\}] \end{bmatrix} \quad (4)$$

$$SW_i = \frac{f(A_{i1}, A_{i2}, \dots, A_{in})}{f(A_{i1}, A_{i2}, \dots, A_{in} | \mathbf{L}_i)} = \frac{f(A_{i1}) f(A_{i2} | A_{i1}), \dots, f(A_{in} | A_{i1}, \dots, A_{i,n-1})}{f(A_{i1} | \mathbf{L}_i) f(A_{i2} | A_{i1}, \mathbf{L}_i), \dots, f(A_{in} | A_{i1}, \dots, A_{i,n-1}, \mathbf{L}_i)} \quad (5)$$

and the new forms of the conditional expectation and variance follow from setting  $\eta_* = \gamma_0 + \delta \gamma_a$  in the equations in Section 3.1 such that  $\hat{\gamma}$  is the solution to (4), along with an additional dispersion parameter estimate. Since weighting eliminates confounding, the estimating equations of (4) are actually simpler than (2) because covariates  $\mathbf{L}$  do not need to be included in the outcome model.

Rather than the factorization used in (6), most MSM with multiple treatments use weights of the form  $SW_i = \prod_{j=1}^m f(A_{ij}) / f(A_{ij} | \mathbf{L}_i)$  as originally described by Hernán et al. (2001), which assumes that the treatments are independent conditional on  $\mathbf{L}$ . For the simulations and application of this paper, this assumption will be made, but note that such a simplification may be dubious in various applications and will not hold if there are direct arrows between treatments in the DAG. For examples of estimating the joint propensity of various dependent exposures using mixed models, see Tchetgen and VanderWeele (2012), Perez-Heydrich et al. (2014), or Liu, Hudgens, and Becker-Dreps (2016). In the remainder of this paper, weights for continuous treatments will be estimated using a ratio of normal densities, but other methods (Hirano and Imbens, 2004) and more flexible choices for weight models (Naimi et al., 2014) can also be used in general.

Estimating the weights provides an additional challenge in that the exposure measurement error has another opportunity to introduce bias. Fortunately, the exposures are now the



propensity model(s) outcomes, and measurement error is usually much less serious for a model outcome than for model covariates (Carroll et al., 2006). In Web Appendix A, the proposed IPW CSME estimator is shown to be consistent even when the propensity models are fit using the mismeasured exposures without correction, under certain assumptions.

### 3.4 Doubly-Robust CSME Estimator

In the absence of measurement error, both the g-formula and IPW methods rely on model specifications that may not be correct in practice. The g-formula provides consistent estimation of potential outcome means only when the outcome model with exposures and confounders is correctly specified. Likewise, the IPW estimator is consistent only when the propensity score model is correctly specified. In contrast, doubly-robust (DR) estimators entail specifying both propensity and outcome models, but remain consistent if one is misspecified and the other is not (Robins, Rotnitzky, and Zhao, 1994; Lunceford and Davidian, 2004; Bang and Robins, 2005).

A DR estimator for the additive measurement error setting can be written similarly to those described in Robins (2000) and Neugebauer and van der Laan (2005) as the solution to the set of estimating equations  $\sum_{i=1}^n \psi_{DR-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Theta) = 0$  where:

$$\psi_{DR-CSME}(Y_i, \mathbf{L}_i, \mathbf{A}_i^*, \Theta) = \begin{bmatrix} SW_i\{Y_i - E(Y_i|\Delta_i) - Q(\mathbf{A}_i, \mathbf{L}_i)\} + \int_{\mathbf{a}} h(\mathbf{a})Q(\mathbf{a}, \mathbf{L}_i)d\mu(\mathbf{a}) \\ SW_i\{Y_i - E(Y_i|\Delta_i) - Q(\mathbf{A}_i, \mathbf{L}_i)\}\Delta_i + \int_{\mathbf{a}} h(\mathbf{a})Q(\mathbf{a}, \mathbf{L}_i)d\mu(\mathbf{a}) \end{bmatrix},$$

$h(\mathbf{a})$  is the numerator of the stabilized weights,  $d\mu(\mathbf{a})$  is a Lebesgue measure, and  $Q(\mathbf{A}, \mathbf{L})$  is a function of  $\mathbf{A}$  and  $\mathbf{L}$ . This estimator is doubly-robust in the sense that it is consistent if either the weights  $SW$  are derived from correctly specified propensity models or if the outcome regression is a correctly specified CSME model, given by  $Q(\mathbf{A}, \mathbf{L}) = \beta_0 + \beta_a\mathbf{A} + \beta_l\mathbf{L} + \beta_{al}(\mathbf{A} \otimes \mathbf{L}^T) - \psi^T(1, \mathbf{A}^T)^T$ . See Web Appendix A for more details.

### 3.5 Handling Unknown Measurement Error Variance

Although the proposed methods require no supplemental data and no distributional assumption on the true exposures  $\mathbf{A}$ , they do require a priori knowledge of the measurement error covariance matrix. Sometimes, this will be known from properties of the measurement tools (e.g., some bioassays, certain widely studied survey instruments) or will be available from a prior study. Here, some guidelines are provided for analyses where this matrix is unknown.

Firstly, there are many types of studies for which the covariance matrix should be diagonal (i.e., the measurement errors should be uncorrelated). For example, biological assays taken on different samples and analyzed by separate machines/researchers should have uncorrelated measurement errors, and different assays taken on the same sample may often have uncorrelated or very weakly correlated measurement errors. For other types of data such as survey responses, analysts should be more cautious, noting that response bias, recall bias, and other forms of measurement error in survey instruments may be correlated within individuals.

Many studies do have a small amount of supplemental data, namely replicates of the potentially mismeasured variables. These replicates can be used to estimate  $\Sigma_{me}$  as described in Carroll et al. (2006). Suppose there are  $k_i$  replicates of the mismeasured exposures,  $\mathbf{A}_{i1}^*, \dots, \mathbf{A}_{ik_i}^*$  with mean for individual  $i$  notated as  $\mathbf{A}_i^*$ . Then an estimator for the measurement error covariance is given by:

$$\hat{\Sigma}_{me} = \frac{\sum_{i=1}^n \sum_{j=1}^{k_i} (\mathbf{A}_i^* - \mathbf{A}_{i.}^*)(\mathbf{A}_i^* - \mathbf{A}_{i.}^*)^T}{\sum_{i=1}^n (k_i - 1)}$$

noting that when replicates are available, some of the existing methods described in the introduction are applicable and should give similar results to the proposed methods.

When no replicates are available and there is no prior knowledge of  $\Sigma_{me}$ , the proposed methods can still be used in the context of a sensitivity analysis. Often an upper bound for measurement error variance of individual variables can be ascertained - it is atypical for

measurement error variance to be higher than the variance of a variable itself, for example. Once upper bounds are identified or chosen, repeating the proposed methods under a few reasonable  $\Sigma_{me}$  specifications yields a sensitivity analysis showing how robust the effect sizes and confidence intervals are to increasing additive measurement error; this procedure is more straightforward when the matrix is small and diagonal and becomes difficult to interpret as the number of parameters grows.

### 3.6 Large-Sample Properties and Variance Estimation

In Web Appendix A, each of the three proposed estimators are shown to be consistent and asymptotically normal by showing they are M-estimators and that their corresponding estimating functions have expectation 0 (Stefanski and Boos, 2002). In addition, the DR estimator is shown to be consistent when only one of the propensity and outcome models is correctly specified. Finally, the proposed estimators are shown to be generalizations of existing popular estimators used in the no measurement error setting.

Since each proposed estimator is an M-estimator, consistent estimators of their asymptotic variances are given by the empirical sandwich variance technique. Estimating equations corresponding to the estimation of weights (and  $\hat{\Sigma}_{me}$  if estimated) should be added to the estimating equation stacks for each method to achieve nominal coverage rates. The `geex` R package (Saul and Hudgens, 2020) streamlines variance estimation for M-estimators and is used in the simulation and application sections. Wald  $100(1 - \alpha)\%$  confidence intervals for the parameters of interest are then given by  $\hat{\psi}_i \pm z_{1-\alpha/2} SE(\hat{\psi}_i)$  where  $z_q$  is the  $q$ -quantile of the standard normal distribution and  $SE(\hat{\psi}_i)$  is the square root of the  $i^{th}$  element of the diagonal of the sandwich covariance matrix. Wald hypothesis testing procedures can be defined similarly.

#### 4. Simulation Study

The performance of the proposed methods was evaluated in two simulation studies. The first simulation compared the proposed g-formula CSME and IPW CSME approaches to standard methods within a scenario where confounding and additive exposure measurement error were present. A total of 2000 data sets of  $n = 800$  individuals were simulated, each with the following variables and distributions: a confounder  $L_1 \sim \text{Bern}(0.5)$ , a second confounder  $L_2 \sim \text{Bern}(0.35)$ , first true exposure  $A_1 \sim \mathcal{N}(4 + L_1, 1)$ , second true exposure  $A_2 \sim \mathcal{N}(1.25 + 0.5L_2, 0.5)$ , third true exposure  $A_3 \sim \mathcal{N}(2.5, 0.7)$  and an outcome  $Y \sim \mathcal{N}(-0.1 + 0.3A_1 + 0.2L_1 - 0.4A_2 - 0.3L_2 - 0.05A_3 - 0.15A_1L_1 - 0.2A_2L_2, 0.5)$  such that  $E\{Y(a_1, a_2, a_3)\} = \psi_0 + \psi_1a_1 + \psi_2a_2 + \psi_3a_3 = -0.105 + 0.225a_1 - 0.47a_2 - 0.05a_3$ . The second exposure  $A_2$  was allowed to be correctly measured, while  $A_1$  and  $A_3$  were subject to additive measurement error simulated as  $A_1^* \sim \mathcal{N}(A_1, 0.3)$  and  $A_3^* \sim \mathcal{N}(A_3, 0.5)$  (such that the measurement error covariance matrix was diagonal).

Six methods were compared in performance estimating  $\psi_1$ ,  $\psi_2$ , and  $\psi_3$  using the observed data  $\{Y, A_1^*, A_2, A_3^*, L_1, L_2\}$ . These methods were: (i) linear regression specifying  $Y$  as a function of  $A_1^*, A_2, A_3^*, L_1, L_2$  and the interactions between  $A_1^*$  and  $L_1$  as well as  $A_2$  and  $L_2$ ; (ii) the CSME method with the same outcome specification as the linear regression and correctly specified measurement error variances; (iii) the g-formula with a correctly specified outcome model using the mismeasured exposures; (iv) an IPW estimator where a correctly specified propensity model was fit for each confounded measured exposure and the product of the resulting inverse probability weights were used to weight a linear regression of  $Y$  on the three exposures; (v) the proposed g-formula CSME estimator with a correctly specified outcome regression; and (vi) the proposed IPW CSME estimator using weights from a correctly specified propensity model.

[Table 1 about here.]

The average bias, average estimated standard error, empirical standard error, and percentage of estimated confidence intervals covering the true values were estimated across the 2000 simulation runs and are presented in Table 1. For  $\psi_3$ , the parameter corresponding to the mismeasured but unconfounded exposure, methods (ii), (iii), and (vi) achieved near-zero average bias and approximately nominal coverage, while methods (i), (iii) and (iv) were biased and had lower coverage. For  $\psi_2$ , the parameter corresponding to the confounded but correctly measured exposure, methods (iii)-(vi) all achieved low bias and about nominal coverage, while methods (i) and (ii) performed poorly. For  $\psi_1$ , the parameter corresponding to the mismeasured and confounded exposure, only the methods proposed in this paper (v) and (vi) had approximately 0 bias and nominal coverage. While methods (iii) and (iv) outperformed method (ii) for this exposure, this phenomenon could easily be reversed when the magnitude of measurement error bias is greater than that of the confounding bias.

The second simulation study compared the proposed g-formula and IPW CSME approaches to the proposed DR CSME estimator under various model specifications. In particular, 2000 datasets of  $n = 2000$  individuals were simulated with the following variables: a confounder  $L_1 \sim \text{Bern}(0.5)$ , a second confounder  $L_2 \sim \mathcal{N}(1, 0.5)$ , an exposure  $A \sim \mathcal{N}(2 + 0.2L_1 - 0.3L_2, 0.6)$ , and a binary outcome  $Y \sim \text{Bern}\{\text{logit}^{-1}(-2 + 0.7A - 1.5L_1 - 0.4AL_1 - 0.4L_2 + 0.3AL_2)\}$  such that  $\text{logit}[E\{Y(a)\}] = \psi_0 + \psi_1a = -2 + 0.7a - 0.5 * 0.4a + 1 * 0.3a = -2 + 0.8a$ . The exposure  $A$  was subject to additive measurement error simulated as  $A^* \sim \mathcal{N}(A, 0.3)$ . Then the three approaches were compared in the traditional way of studying DR estimators, namely under scenarios where only the propensity model was correctly specified, only the outcome regression was correctly specified, and where both were correctly specified. The propensity model was mis-specified by not including the confounder  $L_1$  and the outcome regression was mis-specified by leaving out  $L_1$  and the interaction between  $A$  and  $L_1$ . As demonstrated in other applications, the doubly-robust estimator was approximated

by performing a version of the g-formula approach weighted by the inverse probability weights (Hirano and Imbens, 2001).

[Table 2 about here.]

The simulation results are presented in Table 2 and match the theoretical results described in Section 3.5. Namely, when only the propensity score model was specified correctly, the IPW estimator performed well, but the g-formula estimator was subject to substantial bias and undercoverage. Likewise when only the outcome model was specified correctly, the g-formula estimator performed well, but the IPW estimator was biased and had lower than nominal coverage. However, the doubly-robust estimator achieved low bias and approximately nominal coverage when only one of the two models was misspecified, exhibiting its namesake double-robustness property.

## 5. Application

To illustrate the proposed methods, the DR CSME estimator was applied to data from the HVTN 505 vaccine trial. As discussed in the introduction, the candidate HIV vaccine studied in this trial was not effective, but follow-up research described several interesting biomarker correlates of risk. A recent paper, Neidich et al. (2019), investigated potential mechanisms of antibody mediated prevention, finding that antibody-dependent cellular phagocytosis (ADCP) and antigen-specific recruitment of  $\text{Fc}\gamma$  receptors of several HIV-1 specific Env proteins were associated with reduced HIV-1 risk.

In this section, the primary analysis of Neidich et al. (2019) is extended to (i) adjust for measured potential confounders beyond simple inclusion in an outcome regression, and (ii) allow for additive measurement error. In particular, attention is focused on ADCP and recruitment of  $\text{Fc}\gamma\text{RIIa}$  of the H131-Con S gp140 protein, which will be referred to as RII. The primary analysis of Neidich et al. (2019) focused on the effect of the log transform of each

of these exposures individually on HIV-1 acquisition among vaccinees. For each exposure, they fit two logistic regression models and reported (i) odds ratios for the main effect of exposure adjusting for age, BMI, race, and behavior risk, and (ii) odds ratios for the main effect of exposure adjusting for the same covariates as well as CD4 and CD8 polyfunctionality scores (CD4-P and CD8-P).

In this section, the data is analyzed making the same Binomial family distribution assumption for the outcome and using the proposed doubly-robust CSME estimator. To account for the two-phase sampling design used in the HVTN 505 trial, the weights in the doubly-robust estimator are multiplied by inverse probability of sampling weights, following the procedure described in Wang et al. (2009). This version of the proposed estimator is described in more detail and evaluated in a simulation study in Web Appendix B. For the propensity model specification, main effects for baseline covariates age, race, BMI, and behavior risk were included. For the outcome model specification, it's possible that BMI and behavioral risk are colliders on complex and unknown causal pathways connecting the exposures and outcome. Thus, an outcome regression was specified with main effects for the exposure, age, race, CD4-P, and CD8-P and interactions between the exposure of interest with age and race. The same model specifications for both exposures were used separately to match the univariate-style analysis performed in Neidich et al. (2019). Based on the theoretical and empirical results in sections 3 and 4, the model parameter estimates should be consistent if either specification is correct. Finally, each exposure was assumed to follow a classical additive measurement error model where the variances of measurement error were varied from 0 to 0.3 in increments of 0.05 to perform a sensitivity analysis (0.3 is about half of the variance for each variable when restricted to vaccinees with an immune response and acts as a reasonable upper bound for measurement error). Since ADCP and RII are strictly

positive random variables, this setup is equivalent to assuming that their corresponding non-log transformed variables follow multiplicative measurement error models.

[Figure 2 about here.]

The analysis results are plotted in Figure 2. For each exposure and each model, the left-most interval in each panel corresponds to the DR estimator under no measurement error. These results are similar to that found in Neidich et al. (2019) when using outcome regression to adjust for confounding, but slightly further from the null value in general. The results for the ADCP variable seem robust to measurement error, with significant results even under high measurement error variance. The results for RII are somewhat robust to measurement error, with the confidence intervals in the cellular adjustment model including the null value under moderate measurement error and becoming quite wide under high measurement error. The data for HVTN 505 is publicly available at <https://atlas.scharp.org/> and the R code for the simulations and application are provided at <https://github.com/bblette1/causalCSME>.

## 6. Discussion

In this paper, estimators were proposed which adjust for both confounding and measurement error and which are consistent without any supplemental data and without specifying strong distributional or extrapolation assumptions. The proposed methods are semi-parametric in that while parametric assumptions for the errors were made, the true exposures were treated as nuisance parameters and no assumptions were made about their distribution. While the proposed methods were shown to have favorable theoretical and empirical properties, they are not without limitation. In particular, the methods only work without supplemental data if the covariance of measurement error is known or has been previously estimated. As demonstrated in Section 5, if the covariance is unknown then sensitivity analysis can be straightforward and highly informative if the covariance matrix is small or restricted such that it has few



parameters. In addition, in order to perform inference without making strong assumptions on  $\mathbf{A}$ , modeling assumptions on  $\mathbf{A}^*$  and  $Y$  that may be implausible in some settings were necessary. However, additive measurement error models are realistic for many variables and the GLM outcome framework is an extremely common statistical analysis procedure used in many fields.

There are many possible extensions of the methods described in this paper. Methods that accommodate different measurement error model forms and more flexible outcome model specifications would be useful. Generalizations of the conditional score approach to broader semiparametric frameworks such as that described in Tsiatis and Ma (2004) could be adapted to the causal setting to address this and weaken some of the parametric assumptions made in this paper. A version of this idea is proposed by Liu et al. (2017), but the authors take an outcome regression approach to adjusting for confounding, which is often insufficient for causal inference.

Another logical extension would be a g-estimation based estimator that builds off the CSME method to estimate parameters of a structural nested model where at least one exposure is measured with error. In addition, while this paper expands on the conditional score estimation procedure described in Stefanski and Carroll (1987), the corrected score estimation procedure described in Nakamura (1990) also belongs to the score equation family of functional methods, can also correct for measurement error without supplemental data, and has advantages and disadvantages compared to the conditional score approach in various settings. A causal extension of the corrected-score approach would be valuable for many applications. Finally, this paper focuses on point-exposure data, but conditional-score based approaches addressing measurement error and data sparsity for longitudinal and survival data have been described and could be extended to define new causal inference methods in those settings.

This paper adds to a growing literature on addressing measurement error in causal inference problems. No measurement error of any variables is a key assumption in drawing causal inference, but is often left implicit in analyses despite being critical to the identification of causal estimands. Indeed, exposure measurement error is common in observational studies where investigators lack control of the exposure variables - the same conditions in which investigators worry about confounding bias. Methodological contributions at this intersection are needed to facilitate simultaneous adjustment for these prevalent issues.

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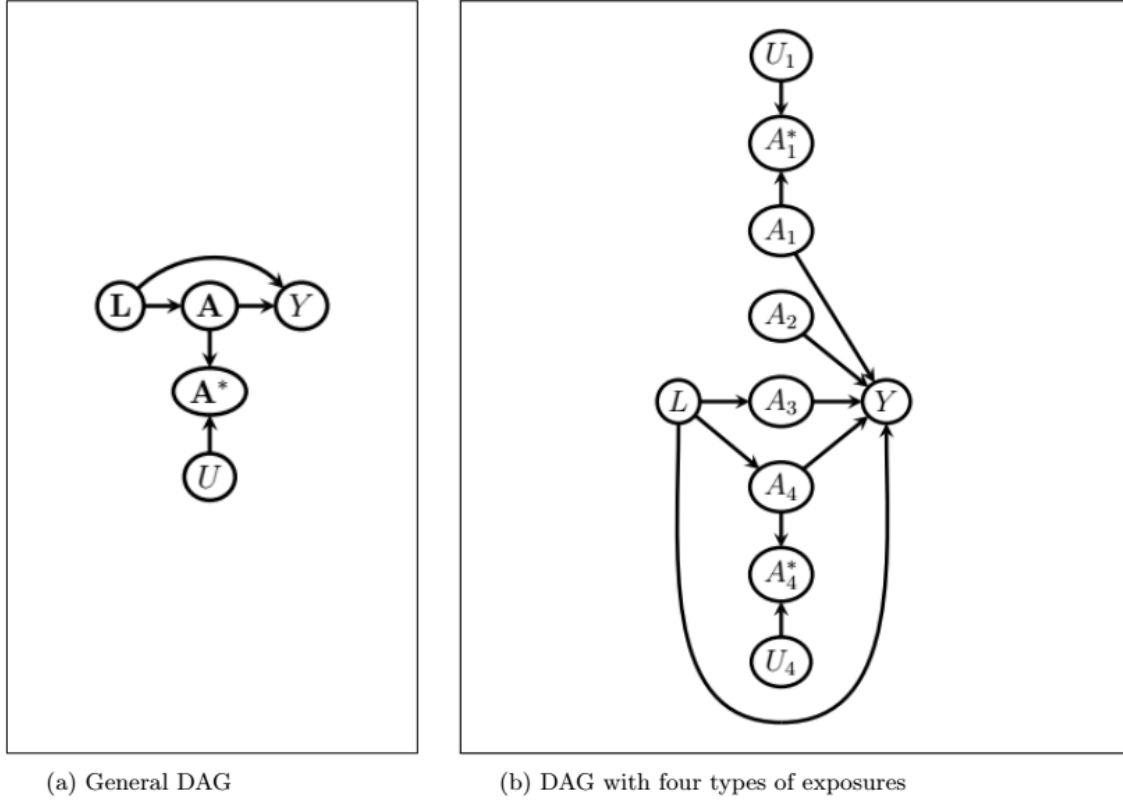
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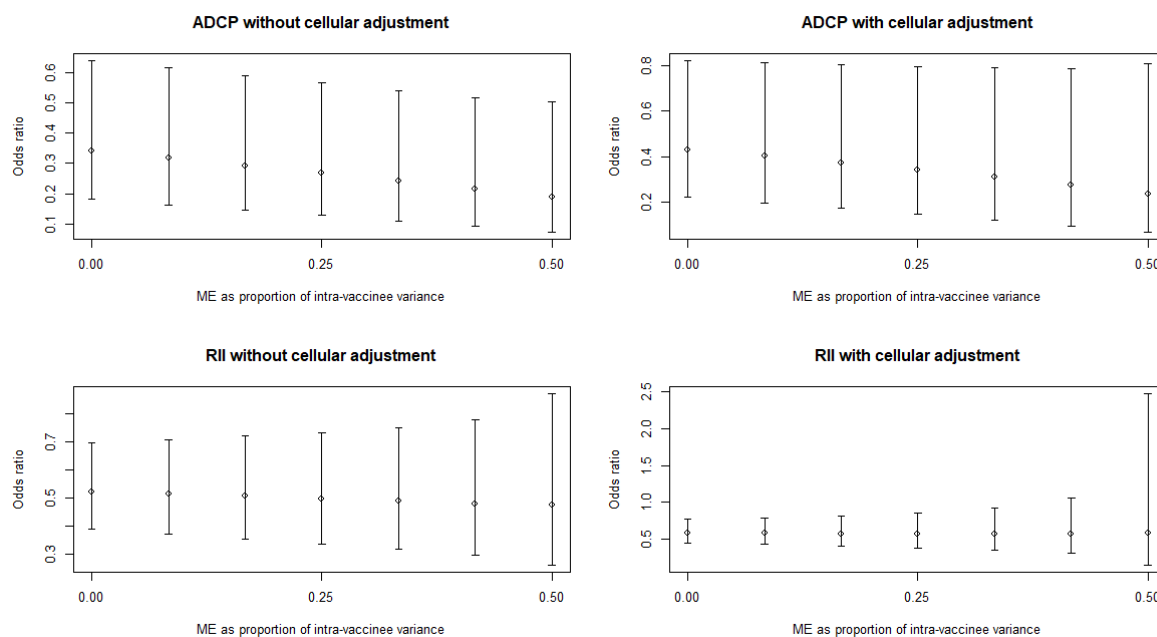
## SUPPLEMENTARY MATERIALS

The Web Appendix is available with this paper at the Biometrics website on Wiley Online Library.



**Figure 1.** Assumed directed acyclic graph (DAG) structure with variables defined in section 2 and  $U$  corresponding to measurement error. (a) A general DAG where  $\mathbf{A}$  is a vector of exposures, some of which may be mismeasured (indicated by the arrow to  $\mathbf{A}^*$ ) and some of which may be subject to confounding bias (indicated by the arrows from  $\mathbf{L}$  to  $\mathbf{A}$  and  $Y$ ). (b) A DAG for a specific exposure vector with four different types of exposures: mismeasured and unconfounded ( $A_1$ ), correctly measured and unconfounded ( $A_2$ ), correctly measured and confounded ( $A_3$ ), and mismeasured and confounded ( $A_4$ ). Each of these four types of exposures can be handled by the proposed methods.





**Figure 2.** HVTN 505 results. Each panel shows the DR estimate and 95% confidence interval for the main effect of ADCP or RII in their respective models. The horizontal axis reflects increasing user-specified variance of measurement error for the exposures as a proportion of the observed exposure variance within vaccinated individuals.

**Table 1**

Results from the first simulation study. Bias: 100 times the average bias across simulated data sets for each method; ASE: 100 times the average of estimated standard errors; ESE: 100 times the standard deviation of parameter estimates; Cov: Empirical coverage of 95% confidence intervals for each method, rounded to the nearest integer.

Estimator	Bias	$\gamma_1$			Bias	$\gamma_2$			Bias	$\gamma_3$		
		ASE	ESE	Cov		ASE	ESE	Cov		ASE	ESE	Cov
Regression	5.0	2.4	2.4	45%	7.1	4.3	4.4	68%	1.6	2.1	2.1	89%
CSME	7.6	2.6	2.7	17%	7.1	4.3	4.4	67%	-0.2	3.1	3.2	96%
G-formula	-1.8	1.7	1.7	83%	0.0	3.7	3.6	94%	1.6	2.1	2.1	89%
IPW	-1.8	2.7	3.0	92%	-0.3	5.9	6.2	96%	1.6	3.2	3.2	91%
G-formula CSME	0.1	1.9	1.9	95%	0.0	3.7	3.6	94%	-0.2	3.1	3.2	96%
IPW CSME	0.1	3.0	3.2	96%	-0.3	5.8	6.2	96%	-0.2	4.9	4.8	94%

**Table 2**

*Results from the second simulation study. Bias, ASE, ESE, and Coverage defined as in Table 1; PS: Propensity score model; OR: Outcome regression model.*

Estimator	Correct Specifications	Bias	ASE	ESE	Coverage
G-formula CSME	PS	-16.3	6.4	6.3	28%
IPW CSME	PS	-2.8	7.1	7.1	93%
DR CSME	PS	-2.4	7.1	7.2	94%
G-formula CSME	OR	0.0	7.1	7.1	95%
IPW CSME	OR	-16.4	6.7	6.7	32%
DR CSME	OR	0.2	7.5	7.5	95%
G-formula CSME	PS and OR	0.0	7.1	7.1	95%
IPW CSME	PS and OR	-2.8	7.1	7.2	93%
DR CSME	PS and OR	0.4	7.8	7.7	95%