

# Basic SIR fitting

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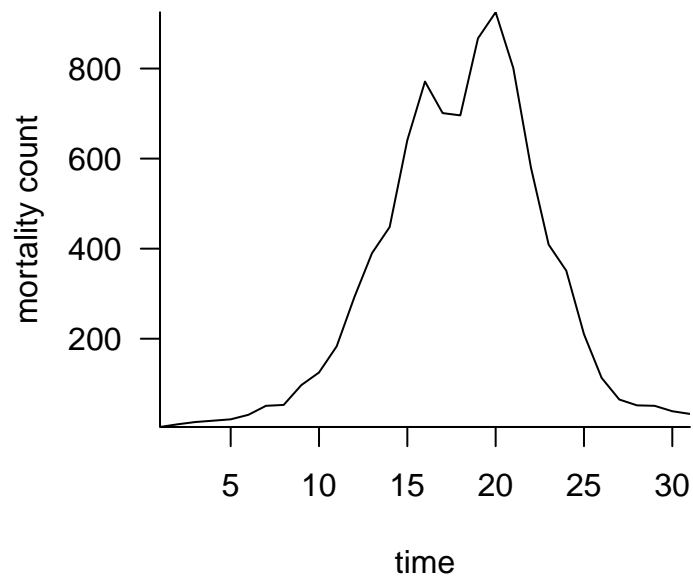
This has been done a million times, but let's try to do it in a reasonably systematic way that could be used in a pedagogical paper.

```
library("fitsir")
library("bbmle") ## need this for now, for coef()
library("plyr")
library("ggplot2"); theme_set(theme_bw())
```

The current version of `fitsir` assumes that time and prevalence are stored as columns `tvec` and `count` within a data frame. Since the `bombay` data set instead has `week` (week of epidemic) and `mort` (mortality), we'll rename it for convenience. (We will for now resolutely ignore issues about fitting weekly mortality counts as prevalences ...)

```
bombay2 <- setNames(bombay, c("tvec", "count"))
```

```
plot(count~tvec, data=bombay2,
      type="l", xaxs="i", yaxs="i",
      xlab="time", ylab="mortality count")
```



## 1 Fit the model to the data

Basic fit:

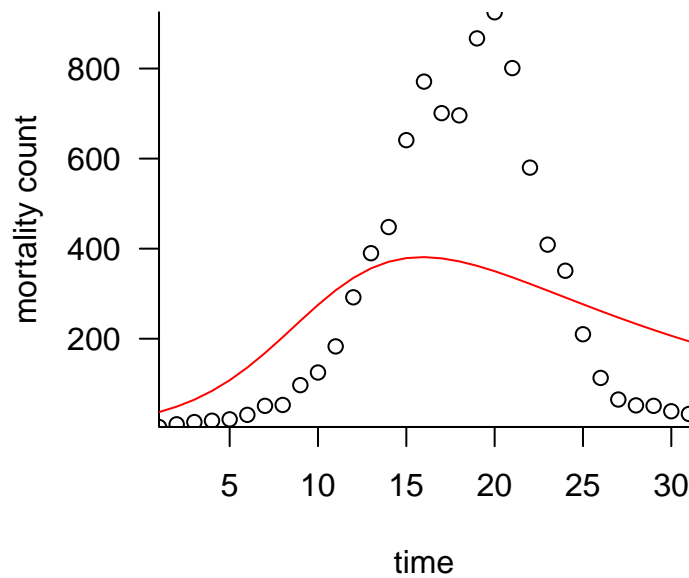
```
m1 <- fitsir(data=bombay2)
```

```
summarize.pars(coef(m1))
```

```
##          R0          r      infper          i0
## 5.13774293 0.28629956 14.45249473 0.05235677
```

Seemingly reasonable answers, but ...

```
ss <- with(bombay2, SIR.detsim(tvec, trans.pars(coef(m1))))
plot(count~tvec, data=bombay2,
      xaxs="i", yaxs="i",
      xlab="time", ylab="mortality count")
lines(bombay2$tvec, ss, col=2)
```



What's going on here? Beta, N, and  $i_0$  might (???) be jointly unidentifiable, ... N enters only as  $\beta/N$  in the gradient function, and only as  $\{N, i_0 N\}$  in the initial conditions ... Except for the fact that  $i_0$  is logit-transformed (constrained to  $0 < i_0 < 1$ ) and  $s_0$  is set to  $N$ , we could set  $N = 1$  without loss of generality?

```
confint(m1,method="quad")

## Warning: NaNs produced

##           2.5 %      97.5 %
## log.beta -1.453650 -0.6148568
## log.gamma -2.748828 -2.5929057
## log.N      NaN      NaN
## logit.i   -4.049810 -1.7419839
```

Suggests *some* sort of unidentifiability ...

What if we try a bunch of starting values?

A crude Latin-hypercube-like strategy: pick evenly spaced values on sensible log scales, then permute to get random (but even) coverage of the space.

```

qlhcfun <- function(n=5,seed=NULL) {
  require("plyr")
  if (!is.null(seed)) set.seed(seed)
  R0vec <- 1+10^seq(-1,1.5,length=n)
  infpervec <- sample(10^seq(-1,2,length=n))
  Nvec <- sample(10^seq(2,5,length=n))
  i0vec <- sample(10^seq(-3,-1,length=n))
  startlist <- alply(cbind(R0=R0vec,infper=infpervec,N=Nvec,i0=i0vec),1,
    function(x) {
      with(as.list(x), {
        beta <- R0/infper
        gamma <- 1/infper
        c(log.beta=log(beta),log.gamma=log(gamma),
          log.N=log(N),logit.i=qlogis(i0))
      })
    })
  return(startlist)
}
startlist <- qlhcfun(n=5,seed=101)

```

```

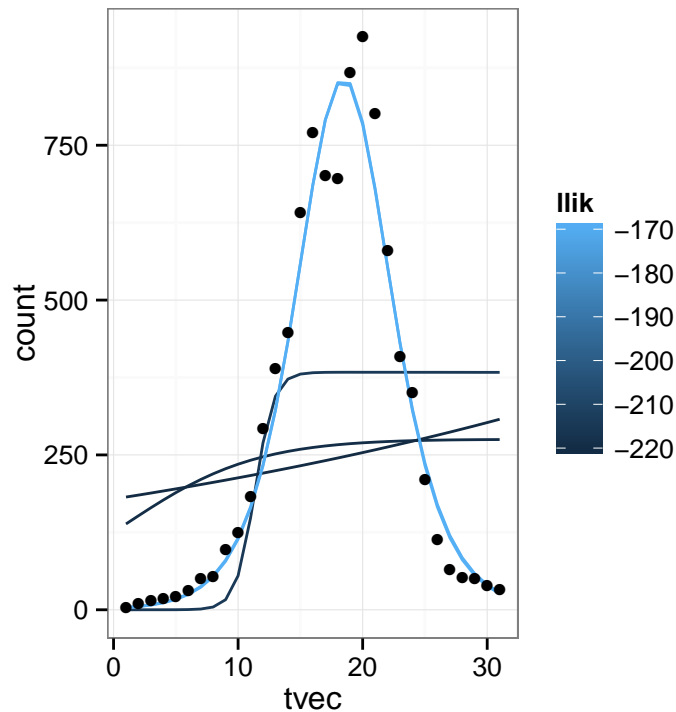
fitlist <- llply(startlist,fitsir,data=bombay2,
  method="Nelder-Mead",control=list(maxit=1e5))

```

```

## extract log-likelihoods
likframe <- data.frame(.id=1:5,llik=unlist(llply(fitlist,logLik)))
## compute trajectories
gettraj <- function(x,tvec=bombay2$tvec) {
  data.frame(tvec=tvec,
    count=SIR.detsim(tvec,trans.pars(coef(x)))
  )
}
fittraj <- ldply(fitlist,gettraj)
fittraj <- merge(fittraj,likframe)
## plot together
ggplot(fittraj,aes(tvec,count,colour=llik,group=.id))+geom_line()+
  geom_point(data=bombay2,colour="black",aes(group=NA))

```



Now try a much larger sample:

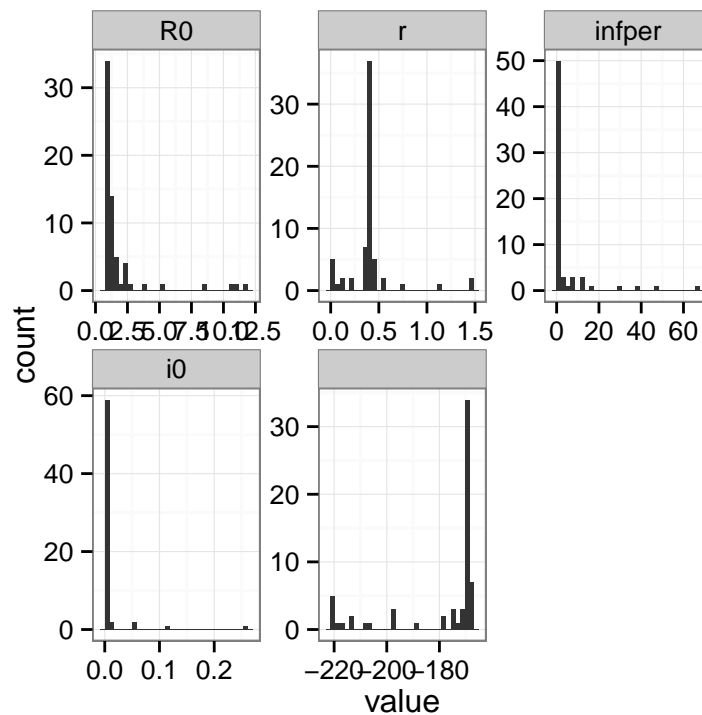
```
startlist100 <- qlhcfun(n=100,seed=101)
fitlist100 <- llply(startlist100,
  function(x) {
    r <- try(fitsir(start=x,data=bombay2),silent=TRUE)
    if (is(r,"try-error")) NULL else r
  })
```

```
testOK <- function(x,max.R0=100,max.r=1000,max.infer=400) {
  if (is.null(x)) return(FALSE)
  ss <- summarize.pars(coef(x))
  return(ss["R0"]<max.R0 & ss["r"]<max.r & ss["infer"] < max.infer)
}
fitlist100.OK <- fitlist100[sapply(fitlist100,testOK)]
length(fitlist100.OK)

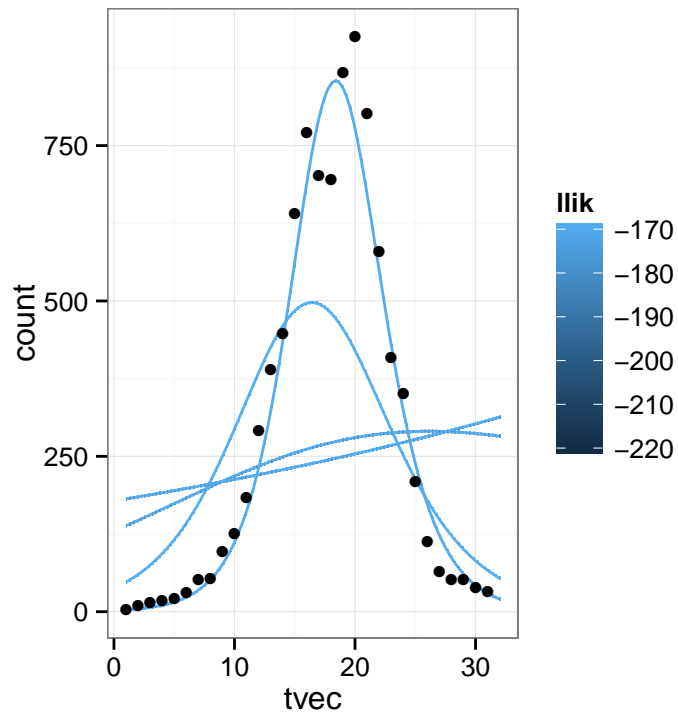
## [1] 65

fittab <- laply(fitlist100.OK,function(x) c(summarize.pars(coef(x)),logLik(x)))
ggplot(melt(fittab),aes(x=value))+geom_histogram()+facet_wrap(~Var2,scale="free")
```

```
## Warning: position.stack requires constant width: output may be
incorrect
```



```
likframe100 <- data.frame(.id=1:5,lik=unlist(llply(fitlist100.OK,logLik)))
fittraj100 <- ldply(fitlist100.OK,gettraj,tvec=seq(1,32,length=101))
fittraj100 <- merge(fittraj100,likframe100)
## plot together
ggplot(fittraj100,aes(tvec,count,colour=lik,group=.id))+geom_line()+
  geom_point(data=bombay2,colour="black",aes(group=NA))
```



Not quite sure what's going on here: there only appear to be 4 trajectories. Is this leftover junk, or do we really have clusters of solutions within the

```
par(las=1,bty="l")
par(mfrow=c(1,2))
LL <- likframe100[,2]
plot(ecdf(LL))
plot(ecdf(LL[LL>(-172)]))
```

