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Incorporating Periodic Variability in Hidden Markov Models for Animal Movement

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Abstract

Background: Clustering time-series data into discrete groups can improve prediction and provide insight into the nature of underlying, unobservable states of the system. However, temporal variation in probabilities of group occupancy, or the rates at which individuals move between groups, can obscure such signals. We use finite mixture and hidden Markov models (HMMs), two standard clustering techniques, to model long-term hourly movement data from Florida panthers (*Puma concolor coryi*). Allowing for temporal heterogeneity in transition probabilities, a straightforward but little-used extension of the standard HMM framework, resolves some shortcomings of current models and clarifies the behavioural patterns of panthers.

Results

Simulations and analyses of panther data showed that model misspecification (omitting important sources of variation) can lead to overfitting/overestimating the underlying number of behavioural states. Models incorporating temporal heterogeneity identify fewer underlying states, and can make out-of-sample predictions that capture observed diurnal and autocorrelated movement patterns exhibited by Florida panthers.

Conclusion:

Incorporating temporal heterogeneity improved goodness of fit and predictive capability as well as reducing the selected number of behavioural states to a more biologically interpretable level. Our results suggest that incorporating additional structure in statistical models of movement behaviour can allow more accurate assessment of appropriate model complexity.

Keywords: Hidden Markov Model; Animal Movement; Temporal Autocorrelation; Temporal Heterogeneity; Florida Panther

Background

- 4 Given a sequence of animal movements, movement models aim to find a parsimo-
- 5 nious description that can be used to understand past movements and predict future
- 6 movements. Ecologists have long considered the effects of individual-level covariates
- 7 (sex, age, nutritional status) and environmental covariates (habitat type, location
- s of predators or prey) on movement [1-3]. More recently, modelers have developed
- 9 hidden Markov models (HMMs) [4-6] used in animal ecology under the rubric of

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the "multiphasic movement framework" [7] — that consider the effects of organisms' internal states; in particular, HMMs model animal movement as though individual animals' movement behaviour at particular times is determined by which of a discrete set of unobserved movement states (e.g. "foraging", "traveling", "resting") they currently occupy. Conditional on the state occupied by an individual, HMMs typically assume that animals follow a correlated random walk model [8, 9].

Ever-increasing capabilities of remote sensors are making movement data available
over an ever-wider range of time scales, at both higher resolution (e.g. hourly data
from GPS collars vs. daily or weekly fixes for radio or VHF collars) and longer extent
(e.g. from a few days to months or years). When analyzing such long-term data,
ecologists will more often have to account for temporal variability in movement
behaviour at diurnal and seasonal scales that were previously not captured in the
data.

HMMs have typically been used to model movements over short time scales, where
the probability of transitioning between movement states is approximately constant. Changes in transition probabilities based on the local environment can be
accounted for by incorporating environmental covariates in the HMM [10], or inferred from direct comparisons between inferred states and environmental conditions
[7]. Schliehe-Diecks et al. [11] considered temporal trends in behavioural transitions
over the time scales of a six-hour observation period, but in general ecologists have
turned to other tools to describe behavioural changes over longer (diurnal, seasonal,
or ontogenetic) time scales [12].

For movement behaviours that change on a fast time scale, such that movement
behaviours recorded at successive observations are effectively independent, *finite mixture models* (FMMs) — which can be considered a special case of HMMs where

the probability of state occupancy is independent of the previous state — can

adequately describe movement [13]. When movement varies over long time scales

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(relative to the time between observations) with little short-term persistence or correlation, movement could be well represented by FMMs where the occupancy probabilities change deterministically over time. Thus FMMs and HMMs, with or without temporal variation in the occupancy or transition probabilities, form a useful family of models for capturing changes in movement behaviour over a range of time scales.

Our primary goal in this paper is to introduce the use of HMMs with temporally varying transition probabilities – in particular, transition probabilities that follow a diurnal cycle – for modeling animal movement recorded over long time scales. In addition to simulation-based examples, we also re-analyze data from van de Kerk et al. [14], who used temporally homogeneous hidden semi-Markov models (HSMMs: an extension of HMMs that allow flexible modelling of the distribution of dwell times, the lengths of consecutive occupancy of a behavioural state) to describe the movement and putative underlying behavioural states of Florida panthers (Puma concolor coryi).

van de Kerk et al. [14] found that the best-fitting HSMMs incorporated a surprisingly large number of hidden behavioural states (as many as six for individuals with
a large amount of available data); for reasons of computational practicality and biological interpretability, they restricted their detailed analysis to models with only
three underlying states. In contrast, most studies using HMM have chosen the number of underlying states a priori, typically using either two [6, 7, 11, 15], or three
states [16–18]. In contrast, Dean et al. [16] evaluated models with up to 10 states,
but like van de Kerk et al. they chose to consider only models with three states.

As van de Kerk et al. [14] comment, and as we discuss further below, behavioural
repertoires with more than three distinct states are difficult to interpret — one reason that other authors have not adopted van de Kerk et al.'s model-based approach
to identifying the number of latent states.

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Our second goal, therefore, is to explore whether van de Kerk et al.'s results on optimal model complexity might be driven at least in part by structural problems with their statistical model, i.e. the assumption of temporally homogeneous behaviour. For large data sets, information-theoretic model selection methods will typically choose complex, highly parameterized models. When there is only one way in which models can become more complex (e.g. by increasing the number of latent states), complexity that is present in the data but not accounted for in the model (e.g. spatial or temporal heterogeneity) can be misidentified as other forms of com-71 plexity. We predict that increasing volumes of data will increasingly lead researchers who are accustomed to fitting small models to sparse data into such traps. We ex-73 amine whether allowing for diurnal variation in the Florida panther data allows us to select models with fewer latent states; we also fit models to simulated data 75 with varying numbers of latent states, and with and without temporal heterogeneity, to test our conjecture that heterogeneity can be misidentified as behavioural complexity.

Methods

- 80 Data and previous analyses
- 81 GPS collars were fitted to 18 Florida panthers in 2005-2012 by Florida Fish and
- Wildlife and Conservation Commission staff using trained hounds and houndsmen.
- Of these animals, 13 had sufficient data to be used by van de Kerk et al. [14]. Here
- we focus on the four cats with the most data (all with approximately 10,000-15,000
- observations: see Table 1), in part because our goal is to understand the issues
- that arise when simple models are fitted to large data sets, and in part because
- 87 the general trend in telemetry studies is toward larger data sets. As is typical in
- 88 studies of animal movement, we took first differences of the data by decomposing
- 89 contiguous sequences of hourly GPS coordinates into successive step lengths (in
- meters) and turning angles (in radians) [9, 14].

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van de Kerk et al. [14] used hidden semi-Markov models (HSMM), an extension of HMM that permits explicit modelling of dwell times [6], considering both Poisson and negative binomial distributions for dwell times. As shown by van de Kerk et al. [14] (Figure S3b, top row, middle panel), the estimated shape parameter of the negative binomial dwell time distribution was typically close to $1 \approx 0.4 - 1.6$; confidence intervals were not given), implying that a geometric distribution (i.e., negative binomial with shape=1) might be adequate. In turn, this suggests that we might not lose much accuracy by reverting to a simpler HMM framework, which corresponds to making precisely this assumption.

van de Kerk et al. [14] considered time-homogeneous models with a variety of 100 candidate distributions — log-Normal, Gamma, and Weibull distributions for step 101 lengths and von Mises and wrapped Cauchy distributions for the turning angle 102 concluding on the basis of the Akaike information criterion (AIC) that Weibull 103 step length and wrapped Cauchy turning angle distributions were best. Since our 104 analysis aims for simplicity and qualitative conclusions rather than for picking the 105 very best predictive model, we focus on models that treat each step as a univariate, 106 log-Normally distributed observation, glossing over both the differences in shape 107 between the three candidate step-length distributions and the effects of considering 108 multivariate (i.e., step length plus turning angle) observations. To check that this 109 simplification does not distort our conclusions we do briefly compare log-Normal 110 and Weibull step-length distributions, with and without a von Mises-distributed 111 turning angle included in the model (Figure 2). (Note that most movement analyses, including van de Kerk et al. [14], are only partially multivariate, treating step length 113 and turning angle at a particular time as multivariate observations for the purpose of HMM analysis but neglecting possible correlations between the two measures.) 115

van de Kerk et al. [14] used the Bayesian (Schwarz) information criterion (BIC)
to test the relative penalized goodness of fit for models ranging from 2 to 6 latent

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states. In general, BIC values decreased as the number of states increased from
three to six states, suggesting that the six-state model was favoured statistically;
however, the authors used three-state models in most of their analyses for ease of
biological interpretation. We follow van de Kerk et al. [14] in using BIC-optimality
(i.e., minimum BIC across a family of models) as the criterion for identifying the
best model, because we are interested in explaining the data generation process by
identifying the "true" number of underlying movement states.

Using BIC also simplifies evaluation of model selection procedures; it is easier to 125 test whether our model selection procedure has selected the model used to simulate 126 the data, rather than testing whether it has selected the model with the minimal 127 Kullback-Leibler distance [19]. We recognize that ecologists will often be interested 128 in maximizing predictive accuracy rather than selecting a true model, and that as 129 usual in ecological systems the true model will be far more complicated than any 130 candidate model [20]. We have repeated some of our analyses using AIC rather 131 than BIC (not shown); for our examples, the qualitative conclusions stated here for 132 BIC-optimality carry over to analyses using AIC.

134 Model description

In a HMM, the joint likelihood of *emissions* (i.e., direct observations) $\mathbf{Y} = \mathbf{y}_1, ..., \mathbf{y}_T$ and a hidden state sequence $\mathbf{Z}, z_t \in \{1, ..., n\}, t = 1, ..., T$, given model parameters $\boldsymbol{\theta}$ and covariates $\mathbf{X}_{1:T} = \mathbf{x}_1, ..., \mathbf{x}_T$, can be written as:

$$P(\mathbf{Y}_{1:T}, \mathbf{Z}_{1:T} | \boldsymbol{\theta}, \mathbf{X}_{1:T}) = P(z_1 | \mathbf{x}_1) P(\mathbf{y}_1 | z_1, \mathbf{x}_1) \times \prod_{k=2}^{T} P(z_k | z_{k-1}, \mathbf{x}_k) P(\mathbf{y}_k | z_k, \mathbf{x}_k)$$

$$(1)$$

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The emissions y_i are boldfaced to denote that we may have a vector of observations
    at each time point (e.g., step length and turning angle). The model contains three
139
    distinct components:
140
    Initial probability P(z_1 = i|\mathbf{x}_1)P(\mathbf{y}_1|z_1,\mathbf{x}_1): the probability of state i at time
141
          t=1 given that the covariates are \mathbf{x}_1, times the vector of observations \mathbf{y}_1
142
143
           conditioned on state z_1 and covariates \mathbf{x}_1.
    Transition probability P(z_k = j | z_{k-1} = i, \mathbf{x}_k): the probability of a transition
           from state i at time t = k - 1 to state j at time t = k, given covariates \mathbf{x}_k.
    Emission probability P(\mathbf{y}_k|z_k,\mathbf{x}_k): a vector of observations \mathbf{y}_k given state z_k at
           time t = k and covariates \mathbf{x}_k.
147
      Eq. 1 gives the likelihood of the observed sequence given (conditional on) a partic-
148
    ular hidden sequence. In order to calculate the overall, unconditional (or marginal)
    likelihood of the observed sequence, we need to average over all possible hidden
150
    sequences. There are several efficient algorithms for computing the marginal like-
    lihood and numerically estimating parameters [21]; we used those implemented in
    the depmixS4 package for R [22, 23].
153
      For an n-state HMM, we need to define an n \times n matrix that specifies the proba-
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    bilities \pi_{ij} of being in movement states j at time t+1 given that the individual is
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    in state i. The FMM is a special case of HMM where the probabilities of entering
156
    a given state are identical across all states — i.e., the probability of occupying a
157
    state at the next time step is independent of the current state occupancy. It can be
158
    modelled in the HMM framework by setting the transition probabilities \pi_{ij} = \pi_{i*}.
159
      In any case, the transition matrix \pi_{ij} must respect the constraints that (1) all
160
    probabilities are between 0 and 1 and (2) transition probabilities out of a given state
161
    sum to 1. As is standard for HMMs with covariates [22], we define this multinomial
162
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logistic model in terms of a linear predictor η_{ij} , where η_{i1} is set to 1 without loss

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of generality (i.e. we have only $n \times (n-1)$ distinct parameters; we index j from 2 to n for notational clarity):

$$\pi_{ij} = \exp(\eta_{ij}(t)) / \left(1 + \sum_{j=2}^{n} \exp(\eta_{ij}(t)) \right), \text{ for } j = 2, ..., n$$

$$\pi_{i1} = 1 - \sum_{j=2}^{n} \pi_{ij}$$
(2)

We considered four different transition models for diurnal variation in behaviour, incorporating hour-of-day as a covariate following the general approach of Morales et al. [17] of incorporating covariate dependence in the transition matrix.

Multiple block transition Here we assume piecewise-constant transition probabilities. The transition probability π_{ij} is a function of time (hour of day), where it is assigned to one of M different time blocks:

$$\eta_{ij}(t) = \sum_{m=1}^{M} a_{ijm} \delta_{m=t}$$

where a_{ijm} are parameters, and $\delta_{m=t}$ is a Kronecker delta ($\delta_{m=t} = 1$ for the time block corresponding to time t, and 0 otherwise).

Quadratic transition model We assume the elements of the linear predictor are quadratic functions of hour:

$$\eta_{ij}(t) = b_{ij1} + b_{ij2} \left(\frac{t}{24}\right) + b_{ij3} \left(\frac{t}{24}\right)^2.$$

The quadratic model is not diurnally continuous, i.e. there is no constraint that forces $\eta_{ij}(0) = \eta_{ij}(24)$; imposing a diurnal continuity constraint would collapse the model to a constant.

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Sinusoidal transition model A sinusoidal model with a period of 24 hours is identical in complexity to the quadratic model, but automatically satisfies the diurnal continuity constraint:

$$\eta_{ij}(t) = b_{ij1} + b_{ij2} \cos\left(\frac{2\pi t}{24}\right) + b_{ij3} \sin\left(\frac{2\pi t}{24}\right).$$

Hourly model Lastly, we extended the multi-block approach and assign a different transition matrix for every hour of the day. This model is included for comparative purposes; due to the large number of parameters in the model (more than 24n(n-1) for a HMM with n states), it is not really practical. We only fitted up to four states using the hourly model.

Other periodic functions, such as Fourier series (i.e., the sinusoidal transition model augmented by additional sinusoidal components at higher frequencies) or periodic splines, could also be considered.

Model complexity and the number of parameters increase as the number of latent states increase. For a fixed number of states homogeneous FMMs are simplest, followed by homogeneous HMMs and finally by FMMs and HMMs incorporating temporal heterogeneity. In general, the number of free parameters in an HMM is the 193 sum of the number of free parameters for each of the three model components (initial states, transition probabilities, and emissions). Let n be the number of hidden states 195 and k_i, k_t, k_e be the number of parameters describing the covariate-dependence of 196 the prior distribution, transition function and emission distributions; that is, for a 197 homogeneous model, k = 1, while a single numeric covariate or a categorical predic-198 tor with two levels would give k=2. Then the number of free parameters of an HMM 199 is: [Initial states] $k_i \cdot (n-1) + [Transition probabilities] k_t \cdot n \cdot (n-1) + [Emission]$ 200 parameters $k_e \cdot n$. As the number of states increases, the number of free parameters in (homogeneous or heterogeneous) FMMs and time-homogeneous HMMs increases Li and Bolker Page 10 of 21

linearly, whereas for HMMs with temporal heterogeneity (or covariate-dependent transitions more generally) the number increases quadratically.

205 Model evaluation

We used the depmixS4 package [22] to fit covariate-dependent transition HMMs, simulate states and step lengths using the estimated parameters, and estimate the most likely states with the Viterbi algorithm.

We ran a simulation experiment in which we fitted HMMs with both homogeneous and heterogeneous transition probabilities to simulated data with heterogeneous transition probabilities, to see whether the correct (heterogeneous-transition)
model correctly identified the number of states while the misspecified (homogeneoustransition) model overestimated the number of states. We used 100 realizations of a
two-state HMM with sinusoidally varying transition probabilities and fitted it with
HMMs ranging from 2 to 5 hidden states, with and without temporal heterogeneity
in the transition probabilities.

We used three approaches to assess the fit of both time-homogeneous and time-217 inhomogeneous HMMs with 3 to 6 states to step-length data from the four of the 218 thirteen Florida panthers with the most data (> 9000 observations). (1) BIC was 210 used to compare the goodness of fit of each model type. The model with the lowest 220 BIC was selected to be the optimal-BIC model and all BICs were adjusted to Δ BIC 221 based on the optimal-BIC model ($\Delta BIC = BIC - min(BIC)$). (2) Comparing average 222 step-length by hour of day for the observed data and for data simulated from the 223 models shows how well a particular class of models can capture diurnal variation 224 in behaviour. (3) Comparing temporal autocorrelations for the observed data and 225 for data simulated from the models shows how well a particular class of models can 226 capture serial correlation at both short and long time scales. As a complement, we 227 also fitted FMM and FMM with priors on state occupancy that varied sinusoidally over time to compare the temporal effects in goodness of fit As a reminder, FMMs Li and Bolker Page 11 of 21

assume that the latent state in each time step is *independent* of the latent state
at the previous time step; time-varying FMMs can accurately describe movement
when behaviour can change on a short time scale, but the average propensity for
different behaviours changes over time.

We used simulations to predict expected hourly step lengths and autocorrela-234 tion functions (ACF). While the computation of expected step length and ACF is 235 straightforward for FMMs, and feasible for homogeneous HMMs, the interaction 236 between the geometric dwell time within each state and the temporally varying 237 interaction probabilities makes it infeasible for more complex models. We used this 238 approach to validate our models, comparing our simulated predictions with the 239 observed movements. The more usual approach, generating predictions from the 240 expected step lengths conditional on the most likely state sequence predicted by 241 the Viterbi algorithm or pseudo-residuals [6, 21], is problematic because the pre-242 dictions by these methods rely on the observed data. This approach is useful to 243 predict missing data in the observation sequence, but because it is conditional on the observed values, it can not reliably evaluate goodness of fit for HMM models with different degrees of structural complexity.

Results

Table 1 Frequency of choosing BIC-optimal state on simulated data.

BIC-Optimal States	2	3	4	5	6
Homogeneous Transition	45	21	20	14	0
Heterogeneous Transition	100	0	0	0	0

The simulation experiment supports our hypothesis that homogeneous transition
HMMs can overestimate the number of hidden states when the model is misspecified
(Table 1). Heterogeneous transition models can always predict the correct number
of states (in 100/100 simulations, BIC correctly identifies n=2 as the number of
states), whereas the temporally homogeneous models overestimate the number of

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states (the correct value, n=2, is chosen most often, but in fewer than half of the simulations; values up to n=5 are frequently chosen).

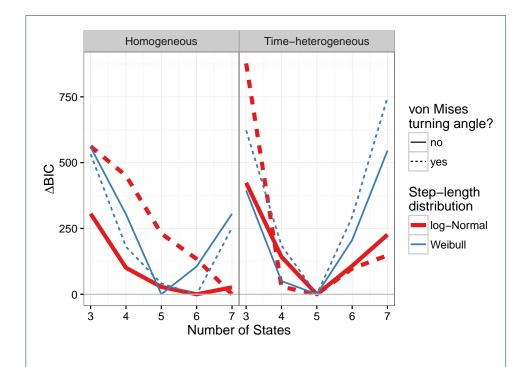


Figure 1 Comparison of BIC-optimal state predictions for homogeneous transition HMMs (left panel) and and heterogeneous transition HMMs (right panel) with different emission complexities on panther data. Solid line represents univariate response/emission HMMs (without turning angles) and dotted line represents multivariate response HMMs (including turning angles with von-Mises distribution). Red lines represents log-normal step-length distribution and blue lines represents Weibull step-length distribution.

The BIC-optimal number of states for time-homogeneous models is consistent with van de Kerk et al.'s [14] results. For time-homogeneous models, the Weibullwrapped-Cauchy [14], Weibull-von Mises, and log Normal without turning angles all identify the same BIC-optimal number of states. While the number of states identified by homogeneous-HMM models varies according to the emissions distributions chosen, ranging from n = 5 for Weibull steps alone to n = 7 for the log Normalvon Mises emissions model, the number of states identified by heterogeneous-HMM models is consistent among emissions models (n = 5: Figure 2).

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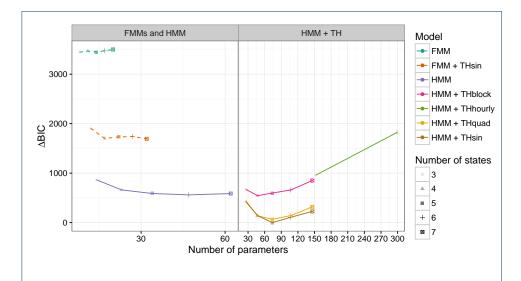


Figure 2 Comparison of adjusted BIC for all HMM transition complexities. The left panel shows homogeneous FMM, heterogeneous FMM (with a sinusoidal prior) and homogeneous HMM. The right panel shows HMMs with different temporal transitions. Dashed lines represents FMMs and solid lines represents HMMs.

Models with temporal heterogeneity provide better fits to the data (lower BIC) than homogeneous models in both FMM and HMM frameworks, but timehomogeneous HMMs are better than FMMs with sinusoidal temporal heterogeneity (Figure 3). Turning to the temporally heterogeneous HMMs (Figure 3, right panel), 266 we see that the model with different transition probabilities for each hour of the day 267 (HMM + THhourly) is overparameterized; it underperforms homogeneous HMM 268 with even 3 states, and gets much worse with 4 states. The multiple-block model 269 gives approximately the same BIC as the homogeneous HMM, although it gives the 270 BIC-optimal number of states as 4, in contrast to 6 for the homogeneous HMM. 271 Finally, the quadratic and sinusoidal models are the best models tested by far; they 272 both give the BIC-optimal number of states as 5, and they have similar goodness 273 of fit. However, the similarity between the quadratic and sinusoidal models may 274 be overstated in Figure 3 due to the very large variation in BIC (over thousands 275 of units) across the full range of models; the best-fit sinusoidal (n = 5) model is 276 approximately 80 BIC units better than the best quadratic model (also n = 5), Li and Bolker Page 14 of 21

which would normally be interpreted as an enormous improvement in goodness of fit (both models have 90 parameters).

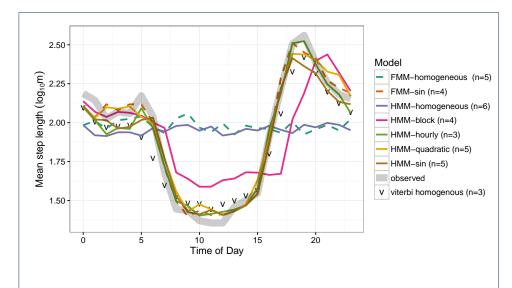


Figure 3 Comparison of average step-length by time of day out of sample predictions for BIC-optimal state FMMs (dashed line) and HMMs (solid lines) of different transition complexities. Gray highlight indicate the observed average step length from panther and "V" points represents Viterbi predictions (within sample) of a three-state homogeneous transition HMM.

The average hourly step lengths from the observed panther data exhibit a clear diurnal pattern (Figure 4). As expected, temporally homogeneous models (whether 281 FMM or HMM) predict the same mean step length regardless of time of day, failing 282 to capture the diurnal activity cycle. All of the models incorporating temporal het-283 erogeneity, including the temporally heterogeneous FMM, can capture the observed 284 patterns. However, the block model does markedly worse than the other tempo-285 ral models (changing the block definitions might help by re-clustering/grouping 286 different hours or increasing the number of blocks), and the (overparameterized) 287 hourly model does better than any other model at capturing the early-evening peak 288 (but worse at capturing the mid-day trough). We also included average hourly step 289 lengths from three-state temporally homogeneous HMM Viter prediction to illus-290 trate within sample predictions can capture the diurnal patterns, but fail to capture 291 out of sample predictions.

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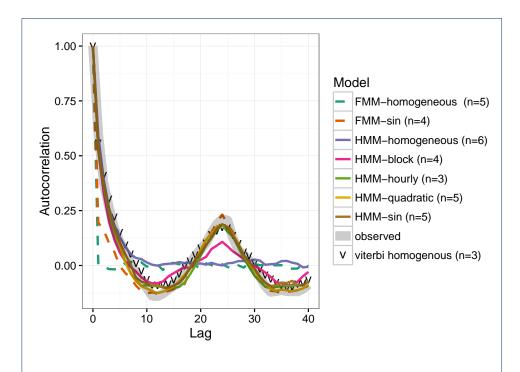


Figure 4 Comparison of out of sample predictions autocorrelations for BIC-optimal state FMMs (dashed line) and HMMs (solid lines) of different transition complexities. Gray highlight indicate the observed average step length from panther and "V" points represents Viterbi predictions (within sample) of a three-state homogeneous transition HMM.

Like the diurnal pattern (Figure 4), the strong autocorrelation of the observed 293 step lengths at a 24-hour lag (Figure 5) shows the need to incorporate temporal 294 heterogeneity in the model — we could have reached this conclusion even without 295 developing any of the temporal-heterogeneity machinery. In contrast to the hourly 296 averages, the autocorrelation (ACF) captures both short- and long-term temporal effects. HMM without temporal heterogeneity captures the short-term autocorrelation, but misses the long-term autocorrelation beyond a 7-hour lag. Temporally 299 homogeneous FMMs, by definition, produce no autocorrelation (neither short- nor long-term autocorrelation). FMMs without temporal heterogeneity, although they 301 capture the diurnal pattern well, underpredict the degree of short-term autocorre-302 lation. 303

The estimated emission parameter values (mean and standard deviation of the step length in each state) are similar, for both homogeneous and heterogeneous Li and Bolker Page 16 of 21

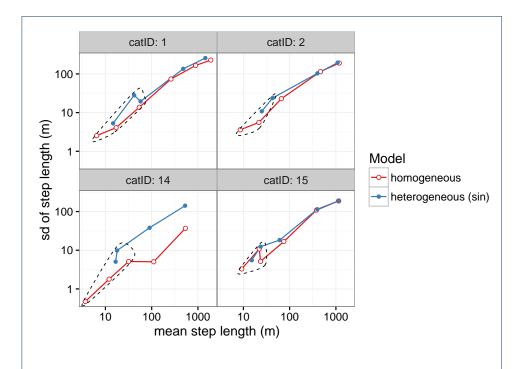


Figure 5 State identification of BIC-optimal HMMs for all panthers. Mean (x-axis) and standard deviation (y-axis) of step length by state $\log_{10}m$ for BIC-optimal homogeneous HMMs (red line) and heterogeneous HMMs with sinusoidal transition (blue line). Short movement states (step-length $< 10^{1.5} \mathrm{m}$) are circled together.

models, across all cats (Figure 6 shows a subset of cats). In general, the states with longer mean step lengths are similar between homogeneous and heterogeneous 307 models. For cats 14 and 15, the states with the longest or next-longest mean step 308 lengths have similar means and standard deviations; for cats 1 and 2, three long-309 step states in the homogeneous HMM appear to divide two long-step states in 310 the heterogeneous HMM. For short-step states, the heterogeneous HMM tends to 311 identify a high-variance state, while the homogeneous HMM picks up states with 312 very short step lengths (questionable in any case because we have not taken any 313 special efforts to account for GPS error). 314

Discussion

HMMs are a widely used and flexible tool for modeling animal movement behaviour; we need to work harder to make sure they are both appropriately comLi and Bolker Page 17 of 21

plex and biologically interpretable. With the increasing volumes of movement data available, ecologists who naively use traditional homogeneous HMMs and standard information-theoretic criteria to estimate the number of behavioural states will generally overfit their data, i.e. they will "discover" large number of states that are difficult to interpret biologically.

As usual, the appropriate approach depends on the goal of the analysis. If ecologists simply want to identify states and associate them with environmental characteristics, it might be sufficient to use a simple (homogeneous) HMM model, prespecifying the number of states to a biologically sensible value, and then match post hoc Viterbi estimates of state occupancy with environmental variation in space and time [7].

On the other hand, if the goal of analysis is to make out-of-sample predictions
about animal behaviour, such as in a management context, it is necessary to fit a
covariate-dependent model that explicitly incorporates the switching process. While
the Viterbi algorithm can be applied to work backward from observed behaviour
to variations in state occupancy with environmental conditions even when using a
homogeneous model, a homogeneous model can never *predict* behaviour that varies
with environmental conditions.

Finally, if our goal is actually to estimate the number of discrete behavioural 336 modes underlying observed behaviour — keeping in mind that these discrete be-337 havioural states are certainly an oversimplified representation of animals' real in-338 ternal states — then, as we have shown above, covariate-dependent models will 339 generally be required to avoid overestimating the number of states. We note that 340 researchers in cluster analysis (of which HMMs are a special case) have shown that 341 the technical conditions required for BIC to apply may be violated [24]; however, 342 BIC can be useful as an approximate *upper* limit on the number of states. Various solutions to this problem have been proposed, including the "integrated classificaLi and Bolker Page 18 of 21

tion likelihood" (ICL) [24, 25], as well as a simpler "knee point" method [26] that looks for the cluster size that corresponds to the largest change in BIC rather than to the smallest overall BIC. Dean *et al.* [16] took a similar approach, but based on the log-likelihood curve rather than the BIC. However, HMMs are a special case even for the various solutions.

Nevertheless, in our simulations the BIC does correctly identify the number of states when appropriate heterogeneity is included in the model; the best practical criterion for identifying numbers of states underlying animal movement data remains an open question.

We have shown the value of incorporating temporal heterogeneity in animal move-354 ment models, but much remains to be done. Our model neglects other predictors — 355 such as sex, habitat type or location with respect to environmental features such as 356 roads — that can potentially improve predictive accuracy and further reduce the 357 estimated number of states. While adding more covariates is in principle straight-358 forward, including even a reasonable range of biological complexity in a HMM with 359 state-dependent transitions rapidly becomes intractable in both computational time 360 and the complexity of model selection. Better diagnostic procedures and tests are needed: these can both test overall goodness-of-fit [27] and, more importantly, localize fitting problems to particular aspects of the data so that models can be constructed without needing to include all possible features of interest. Because there are a huge number of potential complexities that can be added to movement models (e.g. spatial/temporal/among-individual heterogeneity; effects of conspecific 366 attraction or avoidance; memory or cognitive effects), each with associated costs in 367 researcher and computational effort, such diagnostic plots are invaluable. 368

Conclusion

We have presented a relatively simple but little-used extension (time-dependent transitions) that partly resolves the problem. Time-dependent transitions appear to

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offer a simple way to (1) reduce the selected number of states closer to a biologically interpretable level; (2) capture observed diurnal and autocorrelation patterns in a predictive model; (3) improve overall model fit (i.e., lower BIC) and reduce the level of complexity (number of parameters) of the most parsimonious models. Simple simulations where the true number of states is known, and transitions among states vary over time, confirm that using BIC with homogeneous HMMs overestimates the number of behavioural states, while time-dependent HMMs correctly estimate the number.

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385 Ethics approval

386 All data used are secondary, drawn from an existing institutional data repository.

387 Consent for publication

388 Not applicable.

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391 1 Data accessibility

- 392 Hourly step lengths and turning angles of male and female Florida panthers available at
- 393 http://ufdc.ufl.edu//IR00004241/00001.

Authors' contributions

- ML designed analyses and simulations; ran analyses and simulations; and co-wrote the text of the paper. BMB
- $\,$ designed analyses and simulations and co-wrote the text of the paper.

97 Competing interests

398 The authors declare that they have no competing interests.

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469 Tables

Table 2 Cat ID and number of observations; ID numbers are given matching those shown by van de Kerk et al. 2015 and those in the data located at the UF Institutional repository (IR@UF).

IR@UF	Number of Observations	
1	10286	
2	9458	
14	14645	
15	10250	
	1 2 14	