# **RESEARCH**

# Incorporating Periodic Variability in Hidden Markov Models for Animal Movement

Michael Li1\* and Benjamin M. Bolker1,2

\*Correspondence:
lim88@mcmaster.ca

1 Department of Biology,
McMaster University, 1280 Main
St. West, L85 4K1, Hamilton,
Ontario, Canada
Full list of author information is
available at the end of the article

## **Abstract**

Background: Clustering time-series data into discrete groups can improve prediction and provide insight into the nature of underlying, unobservable states of the system. However, temporal variation in probabilities of group occupancy, or the rates at which individuals move between groups, can obscure such signals. We use finite mixture and hidden Markov models (HMMs), two standard clustering techniques, to model long-term hourly movement data from Florida panthers (*Puma concolor coryi*). Allowing for temporal heterogeneity in transition probabilities, a straightforward but little-used extension of the standard HMM framework, resolves some shortcomings of current models and clarifies the behavioural patterns of panthers.

#### Results:

Simulations and analyses of panther data showed that model misspecification (omitting important sources of variation) can lead to overfitting/overestimating the underlying number of behavioural states. Models incorporating temporal heterogeneity identify fewer underlying states, and can make out-of-sample predictions that capture observed diurnal and autocorrelated movement patterns exhibited by Florida panthers.

# **Conclusion:**

Incorporating temporal heterogeneity improved goodness of fit and predictive capability as well as reducing the selected number of behavioural states to a more biologically interpretable level. Our results suggest that incorporating additional structure in statistical models of movement behaviour can allow more accurate assessment of appropriate model complexity.

**Keywords:** Hidden Markov Model; Animal Movement; Temporal Autocorrelation; Temporal Heterogeneity; Florida Panther

**Background** 

- 4 Given a sequence of animal movements, movement models aim to find a parsimo-
- $_{5}$  nious description that can be used to understand past movements and predict future
- 6 movements. Ecologists have long considered the effects of individual-level covariates
- 7 (sex, age, nutritional status) and environmental covariates (habitat type, location
- s of predators or prey) on movement [1-3]. More recently, modelers have developed
- hidden Markov models (HMMs) [4-6] used in animal ecology under the rubric

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of the "multiphasic movement framework" [7] — that consider the effects of organisms' internal states; in particular, HMMs model animal movement as though individual animals' movement behaviour at particular times is determined by which of a discrete set of unobserved movement states (e.g. "foraging", "traveling", "resting") they currently occupy. Conditional on the state occupied by an individual, HMMs typically assume that animals follow a standard correlated random walk model [8, 9].

Ever-increasing capabilities of remote sensors are making movement data available over an ever-wider range of time scales, at both higher resolution (e.g. hourly
data from GPS collars vs. daily or weekly fixes for radio or VHF collars) and longer
extent (e.g. from a few days to significant fractions of a year, or longer). When
analyzing such long-term data, ecologists will more often have to account for temporal variability in movement behaviour at diurnal and seasonal scales that were
previously not captured in the data.

HMMs have typically been used to model movements over short time scales, where
the probability of transitioning between movement states is approximately constant. Changes in transition probabilities based on the local environment can be
accounted for by incorporating environmental covariates in the HMM [10], or inferred from direct comparisons between inferred states and environmental conditions
[7]. Schliehe-Diecks et al. [11] considered temporal trends in behavioural transitions
over the time scales of a six-hour observation period, but in general ecologists have
turned to other tools to describe behavioural changes over longer (diurnal, seasonal,
or ontogenetic) time scales [12].

For movement behaviours that change on a fast time scale, such that movement
behaviours recorded at successive observations are effectively independent, *finite*mixture models (FMMs) — which can be considered a special case of HMMs where
the probability of state occupancy is independent of the previous state — can

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adequately describe movement [13]. When movement varies over long time scales

(relative to the time between observations) with little short-term persistence or

correlation, movement could be well represented by FMMs where the occupancy

probabilities change deterministically over time. Thus FMMs and HMMs, with or

without temporal variation in the occupancy or transition probabilities, form a

useful family of models for capturing changes in movement behaviour over a range

of time scales.

Our primary goal in this paper is to introduce the use of HMMs with temporally varying transition probabilities – in particular, transition probabilities that follow a diurnal cycle – for modeling animal movement recorded over long time scales. In addition to simulation-based examples, we also re-analyze data from van de Kerk et al. [14], who used temporally homogeneous hidden semi-Markov models (HSMMs: an extension of HMMs that allow flexible modelling of the distribution of dwell times, the lengths of consecutive occupancy of a behavioural state) to describe the movement and putative underlying behavioural states of Florida panthers (Puma concolor coryi).

van de Kerk et al. [14] found that the best-fitting HSMMs incorporated a surprisingly large number of hidden behavioural states (as many as six for individuals with
a large amount of available data); for reasons of computational practicality and biological interpretability, they restricted their detailed analysis to models with only
three underlying states. In contrast, most studies using HMM have chosen the number of underlying states a priori, typically using either two [6, 7, 11, 15], or three
states [16–18]. In contrast, Dean et al. [19] evaluated models with up to 10 states,
but like van de Kerk et al. they chose to consider only models with three states.
As van de Kerk et al. [14] comment, and as we discuss further below, behavioural
repertoires with more than three distinct states are difficult to interpret — one rea-

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son that other authors have not adopted van de Kerk et al.'s model-based approach to identifying the number of latent states.

Our second goal, therefore, is to explore whether van de Kerk et al.'s results on optimal model complexity might be driven at least in part by structural problems with
their statistical model, i.e. the assumption of temporally homogeneous behaviour.
For large data sets, information-theoretic model selection methods will typically
choose complex, highly parameterized models; when there is only one way in which
models can become more complex (e.g. by increasing the number of latent states),
complexity that is present in the data but not accounted for in the model (e.g. spatial or temporal heterogeneity) can be misidentified as other forms of complexity.
We predict that increasing volumes of data will increasingly lead researchers who
are accustomed to fitting small models to sparse data into such traps. We examine
whether allowing for diurnal variation in the Florida panther data allows us to select
models with fewer latent states; we also fit models to simulated data with varying
numbers of latent states, and with and without temporal heterogeneity, to test our
conjecture that heterogeneity can be misidentified as behavioural complexity.

# Methods

- 80 Data and previous analyses
- 61 GPS collars were fitted to 18 Florida panthers in 2005-2012 by Florida Fish and
- Wildlife and Conservation Commission staff using trained hounds and houndsmen.
- Of these animals, 13 had sufficient data to be used by van de Kerk et al. [14]. Here
- we focus on the four cats with the most data (all with approximately 10,000-15,000
- observations: see Table 1), in part because our goal is to understand the issues
- that arise when simple models are fitted to large data sets, and in part because
- the general trend in telemetry studies is toward larger data sets. As is typical in
- studies of animal movement, we took first differences of the data by decomposing

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contiguous sequences of hourly GPS coordinates into successive step lengths (in meters) and turning angles (in radians) [9, 14].

van de Kerk et al. [14] used hidden semi-Markov models (HSMM), an extension of HMM that permits explicit modelling of dwell times [6], considering both Poisson and negative binomial distributions for dwell times. As shown by van de Kerk et al. [14] (Figure S3b, top row, middle panel), the estimated shape parameter of the negative binomial dwell time distribution was typically close to  $1 \approx 0.4 - 1.6$ ; confidence intervals were not given), implying that a geometric distribution (i.e., negative binomial with shape=1) might be adequate. In turn, this suggests that we might not lose much accuracy by reverting to a simpler HMM framework, which corresponds to making precisely this assumption.

van de Kerk et al. [14] considered time-homogeneous models with a variety of 100 candidate distributions — log-Normal, Gamma, and Weibull distributions for step 101 lengths and von Mises and wrapped Cauchy distributions for the turning angle — concluding on the basis of the Akaike information criterion (AIC) that Weibull step length and wrapped Cauchy turning angle distributions were best. Since our analysis aims for simplicity and qualitative conclusions rather than for picking the 105 very best predictive model, we focus on models that treat each step as a univariate, 106 log-Normally distributed observation, glossing over both the differences in shape 107 between the three candidate step-length distributions and the effects of consider-108 ing multivariate (i.e., step length plus turning angle) observations. However, we do 109 briefly compare log-Normal and Weibull step-length distributions, with and without 110 a von Mises-distributed turning angle included in the model (Figure 2). (Note that 111 most movement analyses, including van de Kerk et al. [14], are only partially multi-112 variate, treating step length and turning angle at a particular time as multivariate 113 observations for the purpose of HMM analysis but neglecting possible correlations 114 between the two measures.)

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van de Kerk et al. [14] used the Bayesian (Schwarz) information criterion (BIC) to test the relative penalized goodness of fit for models ranging from 2 to 6 latent 117 states. In general, BIC values decreased as the number of states increased from 118 three to six states, suggesting that the six-state model was favoured statistically; 119 however, the authors used three-state models in most of their analyses for ease of 120 biological interpretation. We follow van de Kerk et al. [14] in using BIC-optimality 121 (i.e., minimum BIC across a family of models) as the criterion for identifying the 122 best model, because we are interested in explaining the data generation process by 123 identifying the "true" number of underlying movement states. 124

Using BIC also simplifies evaluation of model selection procedures; it is easier to test whether our model selection procedure has selected the model used to simulate the data, rather than testing whether it has selected the model with the minimal Kullback-Leibler distance [20]. We recognize that ecologists will often be interested in maximizing predictive accuracy rather than selecting a true model, and that as usual in ecological systems the true model will be far more complicated than any candidate model [21]; we believe that the qualitative conclusions stated here for BIC-optimality will carry over to analyses using AIC instead.

# 133 Model description

In a HMM, the joint likelihood of *emissions* (i.e., direct observations)  $\mathbf{Y} = \mathbf{y}_1, ..., \mathbf{y}_T$ and a hidden state sequence  $\mathbf{Z}, z_t \in \{1, ..., n\}, t = 1, ..., T$ , given model parameters  $\boldsymbol{\theta}$  and covariates  $\mathbf{X}_{1:T} = \mathbf{x}_1, ..., \mathbf{x}_T$ , can be written as:

$$P(\mathbf{Y}_{1:T}, \mathbf{Z}_{1:T} | \boldsymbol{\theta}, \mathbf{X}_{1:T}) = P(z_1 \mid \mathbf{x}_1) P(\mathbf{y}_1 | z_1, \mathbf{x}_1) \times \prod_{k=2}^{T} P(z_k | z_{k-1}, \mathbf{x}_k) P(\mathbf{y}_k | z_k, \mathbf{x}_k)$$

$$(1)$$

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The emissions y_i are boldfaced to denote that we may have a vector of observations
    at each time point (e.g., step length and turning angle). The model contains three
138
    distinct components:
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    Initial probability P(z_1 = i|\mathbf{x}_1)P(\mathbf{y}_1|z_1,\mathbf{x}_1): the probability of state i at time
          t=1 given that the covariates are \mathbf{x}_1, times the vector of observations \mathbf{y}_1
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          conditioned on state z_1 and covariates \mathbf{x}_1.
    Transition probability P(z_k = j | z_{k-1} = i, \mathbf{x}_k): the probability of a transition
          from state i at time t = k - 1 to state j at time t = k, given covariates \mathbf{x}_k.
    Emission probability P(\mathbf{y}_k|z_k,\mathbf{x}_k): a vector of observations \mathbf{y}_k given state z_k at
          time t = k and covariates \mathbf{x}_k.
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      Eq. 1 gives the likelihood of the observed sequence given (conditional on) a partic-
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    ular hidden sequence. In order to calculate the overall, unconditional (or marginal)
    likelihood of the observed sequence, we need to average over all possible hidden
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    sequences. There are several efficient algorithms for computing the marginal like-
    lihood and numerically estimating parameters [22]; we used those implemented in
    the depmixS4 package for R [23, 24].
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      For an n-state HMM, we need to define an n \times n matrix that specifies the proba-
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    bilities \pi_{ij} of being in movement states j at time t+1 given that the individual is
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    in state i. The FMM is a special case of HMM where the probabilities of entering
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    a given state are identical across all states — i.e., the probability of occupying a
156
    state at the next time step is independent of the current state occupancy. It can be
157
    modelled in the HMM framework by setting the transition probabilities \pi_{ij} = \pi_{i*}.
158
      In any case, the transition matrix \pi_{ij} must respect the constraints that (1) all
159
    probabilities are between 0 and 1 and (2) transition probabilities out of a given state
160
    sum to 1. As is standard for HMMs with covariates [23], we define this multinomial
161
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logistic model in terms of a linear predictor  $\eta_{ij}$ , where  $\eta_{i1}$  is set to 1 without loss

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of generality (i.e. we have only  $n \times (n-1)$  distinct parameters; we index j from 2 to n for notational clarity):

$$\pi_{ij} = \exp(\eta_{ij}(t)) / \left( 1 + \sum_{j=2}^{n} \exp(\eta_{ij}(t)) \right), \text{ for } j = 2, ..., n$$

$$\pi_{i1} = 1 - \sum_{j=2}^{n} \pi_{ij}$$
(2)

We considered four different transition models for diurnal variation in behaviour, incorporating hour-of-day as a covariate following the general approach of Morales et al. [17] of incorporating covariate dependence in the transition matrix.

Multiple block transition Here we assume piecewise-constant transition probabilities. The transition probability  $\pi_{ij}$  is a function of time (hour of day), where it is assigned to one of M different time blocks:

$$\eta_{ij}(t) = \sum_{m=1}^{M} a_{ijm} \delta_{m=t}$$

where  $a_{ijm}$  are parameters, and  $\delta_{m=t}$  is a Kronecker delta ( $\delta_{m=t} = 1$  for the time block corresponding to time t, and 0 otherwise).

Quadratic transition model We assume the elements of the linear predictor are quadratic functions of hour:

$$\eta_{ij}(t) = b_{ij1} + b_{ij2} \left(\frac{t}{24}\right) + b_{ij3} \left(\frac{t}{24}\right)^2.$$

The quadratic model is not diurnally continuous, i.e. there is no constraint that forces  $\eta_{ij}(0) = \eta_{ij}(24)$ ; imposing a diurnal continuity constraint would collapse the model to a constant.

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Sinusoidal transition model A sinusoidal model with a period of 24 hours is identical in complexity to the quadratic model, but automatically satisfies the diurnal continuity constraint:

$$\eta_{ij}(t) = b_{ij1} + b_{ij2} \cos\left(\frac{2\pi t}{24}\right) + b_{ij3} \sin\left(\frac{2\pi t}{24}\right).$$

Hourly model Lastly, we extended the multi-block approach and assign a different transition matrix for every hour of the day. This model is included for comparative purposes; due to the large number of parameters in the model (more than 24n(n-1) for a HMM with n states), it is not really practical. We only fitted up to four states using the hourly model. Other periodic functions, such as Fourier series (i.e., the sinusoidal transition model augmented by additional sinusoidal components at higher frequencies) or periodic splines, could also be considered.

## 189 Model evaluation

We used the depmixS4 package to fit covariate-dependent transition HMMs, simulate states and step lengths using the estimated parameters, and estimate the most likely states with the Viterbi algorithm.

A simple simulation was conducted to to see whether fitting homogeneous transition probability HMMs to heterogeneous transitions simulated data will over estimate the number of states and estimate the correct number of states using the
heterogeneous transitioning model. We used 100 realizations of a two-state HMM
with sinusoidal temporal transitions and fitted it with 2- to 5-state HMMs with and
without temporal heterogeneity in the transition probabilities.

We used three approaches to assess the fit of both time-homogeneous and timeinhomogeneous HMMs with 3 to 6 states to step-length data from the four of the
thirteen Florida panthers with the most data (> 9000 observations). (1) BIC was

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used to compare the goodness of fit of each model type. The model with the lowest BIC was selected to be the optimal-BIC model and all BICs were adjusted to  $\Delta$ BIC based on the optimal-BIC model ( $\Delta BIC = BIC - min(BIC)$ ). (2) Comparing average step-length by hour of day for the observed data and for data simulated from the models shows how well a particular class of models can capture diurnal variation in behaviour. (3) Comparing temporal autocorrelations for the observed data and 207 for data simulated from the models shows how well a particular class of models can 208 capture serial correlation at both short and long time scales. As a complement, we 209 also fitted FMM and FMM with priors on state occupancy that varied sinusoidally 210 over time to compare the temporal effects in goodness of fit As a reminder, FMMs 211 assume that the latent state in each time step is independent of the latent state 212 at the previous time step; time-varying FMMs can accurately describe movement 213 when behaviour can change on a short time scale, but the average propensity for 214 different behaviours changes over time. 215

Model complexity and the number of parameters increase as the number of latent 216 states increase. For a fixed number of states homogeneous FMMs are simplest, 217 followed by homogeneous HMMs and finally by FMMs and HMMs incorporating 218 temporal heterogeneity. In general, the number of free parameters in an HMM is 219 the sum of the number of free parameters for each of the three model components. 220 Let n be the number of hidden states and  $k_i, k_t, k_e$  be the number of parameters 221 describing the covariate-dependence of the prior distribution, transition function 222 and emission distributions; that is, for a homogeneous model, k = 1, while a single numeric covariate or a categorical predictor with two levels would give k=2. Then 224 the number of free parameters of an HMM is:

Number of Free Parameters = 
$$\underbrace{k_i \cdot (n-1)}_{\text{Initial}} + \underbrace{k_t \cdot n \cdot (n-1)}_{\text{Transition}} + \underbrace{k_e \cdot n}_{\text{Emission}}$$
 (3)

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As the number of states increases, the number of free parameters in (homoge-

neous or heterogenous) FMMs and time-homogeneous HMMs will increase linearly, whereas for HMMs with temporal heterogeneity (or covariate-dependent transitions more generally) the number increases quadratically (Eq. 3). When comparing 220 BICs, it is important to account for the tradeoff between log-likelihood and number 230 of states, but also log-likelihood and number of free parameters. 231 We used simulations to predict expected hourly step lengths and autocorrela-232 tion functions (ACF). While the computation of expected step length and ACF is straightforward for FMMs, and feasible for homogeneous HMMs, the interaction between the geometric dwell time within each state and the temporally varying 235 interaction probabilities makes it infeasible for more complex models. We used this approach to validate our models, comparing our simulated predictions with the 237 observed movements. The more usual approach, generating predictions from the 238 expected step lengths conditional on the most likely state sequence predicted by 230 the Viterbi algorithm or pseduo-residuals [6, 22], is somewhat problematic because 240 the predictions by these methods rely on the observed data. These approach is use-241 ful to predict missing data in the observation sequence, but because it is conditional 242 on the observed values, it can not reliably evaluate goodness of fit for the different 243

# Results

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structural complexities of HMM models.

The simulation agrees with our hypothesis that homogeneous transition HMMs can over estimate the number of hidden states. Heterogeneous transition models can always predict the correct number of states, whereas the temporally homogeneous models overestimate the number of states (based on BIC-optimality: Figure 1). The BIC-optimal number of states for time homogeneous models is consistent with van de Kerk et al.'s [14] results (Weibull wrapped-Cauchy to Weibull von Mises,

and Weibull von Mises to log Normal without turning angles; Figure 2). [BMB:

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Clarify parenthetical clause here. Also, more discussion: in particular,
discuss/clarify the points that the homogeneous-HMM models do vary a
bit among models (log-Normal vs Weibull, with/without turning angles)
in how many states they identify, but the heterogeneous-HMM ones
don't — which is more important for our conclusions here]

Models with temporal heterogeneity are better (lower BIC) than homogeneous models in both FMM and HMM frameworks, but time-homogeneous HMMs are better than FMMs with sinusoidal temporal heterogeneity (Figure 3). Turning to the temporally heterogeneous HMMs (Figure 3, right panel), we see that the model with different transition probabilities for each hour of the day (HMM + THhourly) 262 is overparameterized; it underperforms homogeneous HMM with even 3 states, and gets much worse with 4 states. The multiple-block model gives approximately the 264 same BIC as the homogeneous HMM, although it gives the BIC-optimal number of 265 states as 4, in contrast to 6 for the homogeneous HMM. Finally, the quadratic and 266 sinusoidal models are the best models tested by far; they both give the BIC-optimal 267 number of states as 5, and they have similar goodness of fit. However, this similarity 268 is overstated due to the very large variation in BIC (over thousands of units) across 269 the full range of models; there is a difference of approximately 80 BIC units, which 270 would normally be interpreted as an enormous difference in goodness of fit, between 271 272 the sinusoidal and quadratic models (both of which have 90 parameters).

The average hourly step lengths from the observed panther data exhibit a clear diurnal pattern (Figure 4). As expected, temporally homogeneous models (whether FMM or HMM) predict the same mean step length regardless of time of day, failing to capture the diurnal activity cycle. All of the models incorporating temporal heterogeneity, including the temporally heterogeneous FMM, can capture the observed patterns. However, the block model does markedly worse than the other temporal models (changing the block definitions might help [BMB: clarify?]), and the

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(overparameterized) hourly model does better than any other model at capturing
the early-evening peak (but worse at capturing the mid-day trough). We also included average hourly step lengths from three-state temporally homogeneous HMM
Viterbi prediction (v points [BMB: clarify?]).

Like the diurnal pattern (Figure 4), the strong autocorrelation of the observed 284 step lengths at a 24-hour lag (Figure 5) shows the need to incorporate temporal heterogeneity in the model — we could have reached this conclusion even without developing any of the temporal-heterogeneity machinery. Because there are a huge number of potential complexities that can be added to movement models (e.g. spatial/temporal/among-individual heterogeneity; effects of conspecific attraction 289 or avoidance; memory or cognitive effects), each with associated costs in researcher 290 and computational effort, such diagnostic plots are invaluable. [BMB: move prev 291 sentence to Discussion??] In contrast to the hourly averages, the autocorrelation 292 (ACF) captures both short- and long-term temporal effects. HMM without temporal 293 heterogeneity captures the short-term autocorrelation, but misses the long-term 294 autocorrelation beyond a 7-hour lag. Temporally homogeneous FMMs, by definition, 295 produce no autocorrelation (neither short- nor long-term autocorrelation). FMMs 296 without temporal heterogeneity, although they capture the diurnal pattern well, 297 underpredict the degree of short-term autocorrelation.

[BMB: next para might belong in Discussion?] The hardest problem with
multiple latent states is interpreting them biologically. We have no way of knowing
what panthers are actually thinking (it is certainly more complex than being in one
of a small number of discrete latent states); we don't know the "true" number of
latent states, nor are we able to observe them directly, although incorporating additional direct observations of behaviour (if available) can at least partially address
this problem [7]. Three distinct movement states seem biologically interpretable for
Florida panthers according to van de Kerk et al. [14]: Short step length suggests

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resting states, intermediate step length a foraging state, and long step length a traveling state.

The estimated emission parameter values (mean and standard deviation of the 309 step length in each state) are similar, for both homogeneous and heterogeneous 310 models, across all cats (Figure 7 shows a subset of cats). In general, the states 311 with longer mean step lengths are similar between homogeneous and heterogeneous 312 models. For cats 14 and 15, the states with the longest or next-longest mean step 313 lengths have similar means and standard deviations; for cats 1 and 2, three longstep states in the homogeneous HMM appear to divide two long-step states in 315 the heterogeneous HMM. For short-step states, the heterogeneous HMM tends to 316 identify a high-variance state, while the homogeneous HMM picks up states with 317 very short step lengths (questionable in any case because we have not taken any 318 special efforts to account for GPS error). 319

# 320 Discussion

HMMs are a widely used and flexible tool for modeling animal movement behaviour; we need to work harder to make sure they are both appropriately complex and biologically interpretable. With the increasing volumes of movement data available, ecologists who naively use traditional homogeneous HMMs and standard information-theoretic criteria to estimate the number of behavioural states will generally overfit their data, in the sense of "discovering" large number of states that are difficult to interpret biologically.

On a broad spectrum, it really depends on what kind of question that is being
answered. On one side of the spectrum, if the goal is to identify states, it might
be sufficient to use a simple/traditional HMM model and pre-specify the number
of states and, post hoc, match Viterbi-based states estimates with environmental
variation [7]. On the other side of the spectrum, if the goal of interest is to make
predictions (out of sample), it might be better to fit a covariate-dependent model so

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that we can explicitly model the switching process. In that case, fitting a covariatedependent model is better for out of sample prediction because Viterbi can only estimate state occupancy if observed movements are available (within sample predictions). Finally, if we want to estimate the number of states, BIC is not necessarily 337 good for estimation of number of states [25], but it can be useful as an approximate upper limit estimate. 339 Incorporating temporal heterogeneity in animal movement is one step in the right 340 direction, but much remains to be done. Our model neglects other predictors, such as habitat type or location with respect to environmental features such as roads, that can potentially improve goodness of fit and predictions and further reduce the estimated number of states. While adding more covariates is in principle straightforward using existing frameworks, including all possible biological complexities in 345 a HMM with state-dependent transitions may rapidly become intractable in terms of both computational time and complexity of choosing among possible reduced 347 models and numbers of states. Better diagnostic procedures and tests are needed: 348 these can both test overall goodness-of-fit [26] and, more importantly, localize fit-349 ting problems to particular aspects of the data so that models can be constructed 350 without needing to include all possible features of interest. 351 BMB: where did the BIC stuff (Celeux, finding the "knee point" à la 352 Dean et al., etc.) go? I think we really have to mention this (maybe not 353 until discussion)

# Conclusion

We have presented a relatively simple but little-used extension (time-dependent transitions) that partly resolves the problem. Time-dependent transitions appear to offer a simple way to (1) reduce the selected number of states closer to a biologically interpretable level; (2) capture observed diurnal and autocorrelation patterns in a predictive model; (3) improve overall model fit (i.e., lower BIC) and reduce the level

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of complexity (number of parameters) of the most parsimonious models. Simple

simulations where the true number of states is known, and transitions among states

vary over time, confirm that using BIC with homogeneous HMMs overestimates the

number of behavioural states, while time-dependent HMMs correctly estimate the

365 number.

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- available at the Institutional Repository at the University of Florida (IR@UF).

#### 871 Ethics approval

372 All data used are secondary, drawn from an existing institutional data repository.

#### 373 Consent for publication

374 Not applicable.

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# 77 1 Data accessibility

- 378 Hourly step lengths and turning angles of male and female Florida panthers available at
- 379 http://ufdc.ufl.edu//IR00004241/00001.

## 380 Authors' contributions

- 381 ML designed analyses and simulations; ran analyses and simulations; and co-wrote the text of the paper. BMB
- designed analyses and simulations and co-wrote the text of the paper.

# 383 Competing interests

384 The authors declare that they have no competing interests.

## 385 Author details

- $^{1}$  Department of Biology, McMaster University, 1280 Main St. West, L8S 4K1, Hamilton, Ontario, Canada.  $^{2}$
- Department of Mathematics and Statistics, McMaster University, 1280 Main St. West, L8S 4K1, Hamilton, Ontario,
- 388 Canada.

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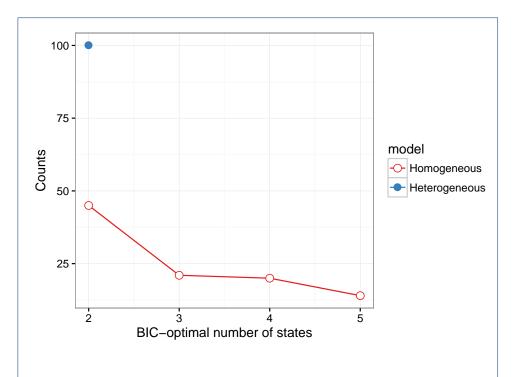
# 454 Tables

Table 1 Cat ID and number of observations; ID numbers are given matching those shown by van de Kerk et al. 2015 and those in the data located at the UF Institutional repository (IR@UF).

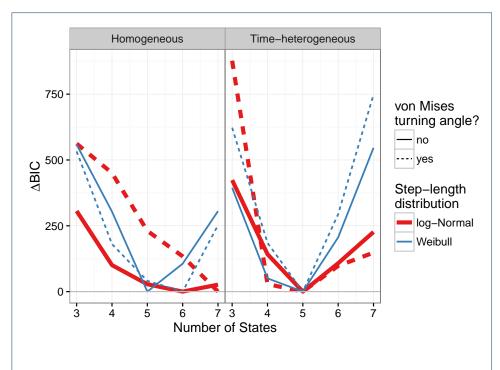
van de Kerk 2015	IR@UF	Number of Observations
130	1	10286
131	2	9458
48	14	14645
94	15	10250

## 455 Figures

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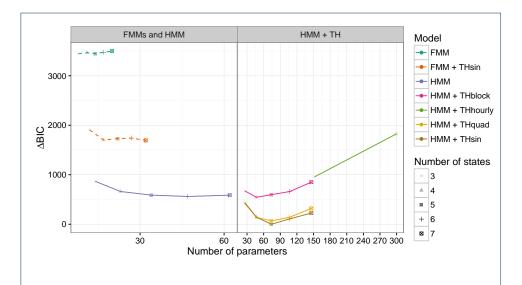


**Figure 1 Simulation Results** BIC-optimal state frequency for 2-6 state HMMs with and without covariate transition on 100 two-state hidden Markov models with covariate transitioning simulations.

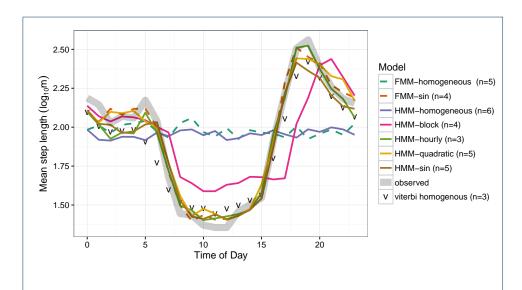


**Figure 2 Adjusted BIC Emission Distribution Comparison** Adjusted Bayesian information criterion values for 3-7 state HMMs with different step-length distributions, with and without temporal transitions and turning angles.

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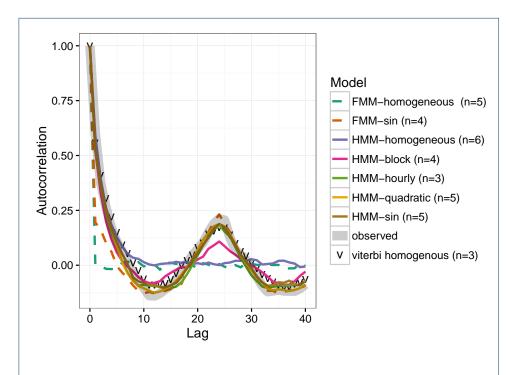


**Figure 3 Adjusted BICs Across All Models** Adjusted BIC by number of free parameters for HMM model types. The left panel shows homogeneous FMM, heterogeneous FMM (with a sinusoidal prior) and homogeneous HMM. The right panel shows HMMs with different temporal transitions.



**Figure 4 Diurnal Step Lengths Plot** Average step length by time of day observed (gray highlight), three-state HMM Viterbi predictions (V points), and all transitions type HMMs predictions (out of sample) with their respective BIC-optimal states.

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**Figure 5 Autocorrelation Plot** Autocorrelation of observed (gray highlight), three-state HMM Viterbi predictions (V points), and all transitions type HMMs predictions (out of sample) with their respective BIC-optimal states.

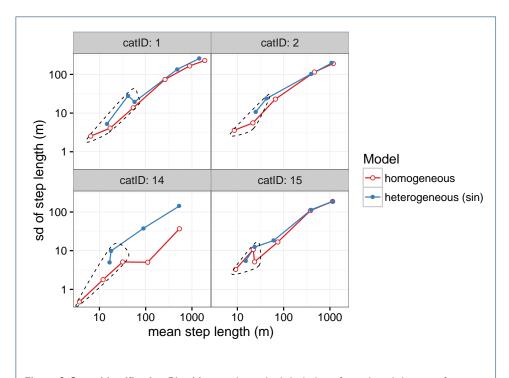


Figure 6 State Identification Plot Mean and standard deviation of step length by state for BIC-optimal HMMs (homogeneous and heterogeneous with sinusoidal transition). [BMB: do I need to explain transformation of LN SD ?]